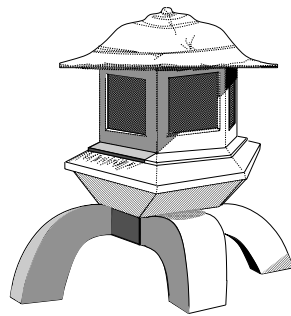


The HOL System REFERENCE



Preface

This volume is the reference manual for the HOL system. It is one of four documents making up the documentation for HOL:

- (i) *LOGIC*: a formal description of the higher order logic implemented by the HOL system.
- (ii) *TUTORIAL*: a tutorial introduction to HOL, with case studies.
- (iii) *DESCRIPTION*: a detailed user's guide for the HOL system;
- (iv) *REFERENCE*: the reference manual for HOL.

These four documents will be referred to by the short names (in small slanted capitals) given above.

This document, *REFERENCE*, provides documentation on all the pre-defined ML variable bindings in the HOL system. These include: general-purpose functions, such as ML functions for list processing, arithmetic, input/output, and interface configuration; functions for processing the types and terms of the HOL logic, for setting up theories, and for using the subgoal package; primitive and derived forward inference rules; tactics and tacticals; and pre-proved built-in theorems.

The manual entries for these ML identifiers are divided into two chapters. The first chapter is an alphabetical sequence of manual entries for all ML identifiers in the system except those identifiers that are bound to theorems. The theorems are listed in the second chapter, roughly grouped into sections based on subject matter.

The *REFERENCE* volume is purely for reference and browsing. It is generated from the same database that is used by the help system. For an introduction to the HOL system, see *TUTORIAL*; for a systematic presentation, see *DESCRIPTION* and *LOGIC*.

Acknowledgements

The bulk of HOL is based on code written by—in alphabetical order—Hasan Amjad, Richard Boulton, Anthony Fox, Mike Gordon, Elsa Gunter, John Harrison, Peter Homeier, Gérard Huet (and others at INRIA), Joe Hurd, Ramana Kumar, Ken Friis Larsen, Tom Melham, Robin Milner, Lockwood Morris, Magnus Myreen, Malcolm Newey, Michael Norrish, Larry Paulson, Konrad Slind, Don Syme, Thomas Türk, Chris Wadsworth, and Tjark Weber. Many others have supplied parts of the system, bug fixes, etc.

Current edition

The current edition of all four volumes (*LOGIC*, *TUTORIAL*, *DESCRIPTION* and *REFERENCE*) has been prepared by Michael Norrish and Konrad Slind. Further contributions to these volumes came from: Hasan Amjad, who developed a model checking library and wrote sections describing its use; Jens Brandt, who developed and documented a library for the rational numbers; Anthony Fox, who formalized and documented new word theories and the associated libraries; Mike Gordon, who documented the libraries for BDDs and SAT; Peter Homeier, who implemented and documented the quotient library; Joe Hurd, who added material on first order proof search; and Tjark Weber, who wrote libraries for Satisfiability Modulo Theories (SMT) and Quantified Boolean Formulae (QBF).

The material in the third edition constitutes a thorough re-working and extension of previous editions. The only essentially unaltered piece is the semantics by Andy Pitts (in *LOGIC*), reflecting the fact that, although the HOL system has undergone continual development and improvement, the HOL logic is unchanged since the first edition (1988).

Second edition

The second edition of *REFERENCE* was a joint effort by the Cambridge HOL group.

First edition

The three volumes *TUTORIAL*, *DESCRIPTION* and *REFERENCE* were produced at the Cambridge Research Center of SRI International with the support of DSTO Australia.

The HOL documentation project was managed by Mike Gordon, who also wrote parts of *DESCRIPTION* and *TUTORIAL* using material based on an early paper describing the HOL system¹ and *The ML Handbook*². Other contributors to *DESCRIPTION* include Avra Cohn, who contributed material on theorems, rules, conversions and tactics, and also composed the index (which was typeset by Juanito Camilleri); Tom Melham, who wrote the sections describing type definitions, the concrete type package and the ‘resolution’ tactics; and Andy Pitts, who devised the set-theoretic semantics of the HOL logic and wrote the material describing it.

The original document design used \LaTeX macros supplied by Elsa Gunter, Tom Melham and Larry Paulson. The typesetting of all three volumes was managed by Tom Melham. The cover design is by Arnold Smith, who used a photograph of a ‘snow watching lantern’ taken by Avra Cohn (in whose garden the original object resides). John Van Tassel composed the \LaTeX picture of the lantern.

Many people other than those listed above have contributed to the HOL documentation effort, either by providing material, or by sending lists of errors in the first edition. Thanks to everyone who helped, and thanks to DSTO and SRI for their generous support.

¹M.J.C. Gordon, ‘HOL: a Proof Generating System for Higher Order Logic’, in: *VLSI Specification, Verification and Synthesis*, edited by G. Birtwistle and P.A. Subrahmanyam, (Kluwer Academic Publishers, 1988), pp. 73–128.

²*The ML Handbook*, unpublished report from Inria by Guy Cousineau, Mike Gordon, Gérard Huet, Robin Milner, Larry Paulson and Chris Wadsworth.

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Chapter 1

Entries

This chapter provides manual entries for pre-defined ML identifiers in the HOL system. These include: general-purpose functions, such as functions for list processing, arithmetic, input/output, and interface configuration; functions for processing the types and terms of the HOL logic, for setting up theories, and for using the subgoal package; primitive and derived forward inference rules; and tactics and tacticals. The arrangement is alphabetical. If an entry's title box includes a parenthesised word to the right, this identifies the ML structure where that identifier is bound. The interactive system starts with some structures already present, others will need to be load-ed first.

##	(Lib)
-----------	-------

```
op ## : ('a -> 'b) * ('c -> 'd) -> 'a * 'c -> 'b * 'd
```

Synopsis

Infix combinator for applying two functions to the two projections of a pair.

Description

An application $(f \ ## \ g) \ (x,y)$ is equal to $(f \ x, \ g \ y)$.

Failure

If $f \ x$ or $g \ y$ fails.

Example

```
- (I ## dest_imp) (strip_forall (Term '!x y z. x /\ y ==> z /\ p'));  
> val it = (['x', 'y', 'z'], ('x /\ y', 'z /\ p'))
```

Comments

The ## combinator can be thought of as a map operation for pairs. It is declared as a right associative infix.

See also

Lib.pair.

&&**(BasicProvers)**

```
op && : simpset * thm list -> simpset
```

Synopsis

Infix operator for adding theorems into a simpset.

Description

BasicProvers.&& is identical to bossLib.&&.

See also

bossLib.&&.

&&**(bossLib)**

```
op && : simpset * thm list -> simpset
```

Synopsis

Infix operator for adding theorems into a simpset.

Description

It is occasionally necessary to extend an existing simpset *ss* with a collection *rwlist* of new rewrite rules. To achieve this, one applies the `&&` function via `ss && rwlist`.

Failure

Never fails.

Example

```
- open bossLib;
... <output elided> ...
- val ss = boolSimps.bool_ss && pairTheory.pair_rws;
> val ss = <simpset> : simpset
```

Comments

Of limited applicability since most of the tactics for rewriting already include this functionality. However, applications of ZAP_TAC can benefit.

See also

`simpLib.++`, `simpLib.SIMP_CONV`, `bossLib.RW_TAC`.

++

(simpLib)

```
op ++ : simpset * ssfrag -> simpset
```

Synopsis

Infix operator for adding an `ssfrag` item into a `simpset`.

Description

`bossLib.++` is identical to `simpLib.++`.

See also

`bossLib.++`.

--

(Parse)

```
-- : term quotation -> 'a -> term
```

Synopsis

Parses a quotation into a term value

Description

An invocation `-- ' ... ' --` is identical to `Term ' ... ' .`

Failure

As for `Parse.Term`.

Uses

Turns strings into terms.

See also

Parse.Term, Parse.==.

<div style="display: flex; justify-content: space-between; align-items: center;"> --> (Type) </div>
--

op --> : hol_type * hol_type -> hol_type

Synopsis

Right associative infix operator for building a function type.

Description

If `ty1` and `ty2` are HOL types, then `ty1 --> ty2` builds the HOL type `ty1 -> ty2`.

Failure

Never fails.

Example

```
- bool --> alpha;
> val it = ':bool -> 'a' : hol_type
```

Comments

This operator associates to the right, that is, `ty1 --> ty2 --> ty3` is identical to `ty1 --> (ty2 --> ty3)`.

See also

Type.dom_rng, Type.mk_type, Type.mk_thy_type.

<div style="display: flex; justify-content: space-between; align-items: center;"> == (Parse) </div>

== : hol_type quotation -> 'a -> hol_type

Synopsis

Parses a quotation into a HOL type.

Description

An invocation `== ' ... '==` is identical to `Type ' ... '.`

Failure

As for `Parse.Type`.

Uses

Turns strings into types.

See also

`Parse.Term`, `Parse.--`.

A

(Lib)

```
A : ('a -> 'b) -> 'a -> 'b
```

Synopsis

Combinator for function application

Description

The application `A f x` equals `f x`.

Failure

`A f` never fails. `A f x` fails if `f x` fails.

Example

```
- map2 A [I, K 3, fn x => x + 1] [1,2,3];
```

```
> val it = [1, 3, 4] : int list
```

See also

`Lib`, `Lib.##`, `Lib.B`, `Lib.C`, `Lib.I`, `Lib.K`, `Lib.S`, `Lib.W`.

Abbr

(BasicProvers)

```
BasicProvers.Abbr : term quotation -> thm
```

Synopsis

Signals to simplification tactics that an abbreviation should be used.

Description

The `Abbr` function is used to signal to various simplification tactics that an abbreviation in the current goal should be eliminated before simplification proceeds. Each theorem created by `Abbr` is removed from the tactic's theorem-list argument, and causes a call to `Q.UNABBREV_TAC` with that `Abbr` theorem's argument. Finally, the simplification tactic continues, with the rest of the theorem-list as its argument. Thus,

```
tac [..., Abbr'v', ..., Abbr'u', ...]
```

has the same effect as

```
Q.UNABBREV_TAC 'v' THEN Q.UNABBREV_TAC 'u' THEN
tac [..., ..., ...]
```

Every theorem created by `Abbr` in the argument list is treated in this way. The tactics that understand `Abbr` arguments are `SIMP_TAC`, `ASM_SIMP_TAC`, `FULL_SIMP_TAC`, `RW_TAC` and `SRW_TAC`.

Failure

`Abbr` itself never fails, but the tactic it is used in may do, particularly if the induced calls to `UNABBREV_TAC` fail.

Comments

This function is a notational convenience that allows the effect of multiple tactics to be packaged into just one.

See also

`Q.ABBREV_TAC`, `simpLib.SIMP_TAC`, `Q.UNABBREV_TAC`.

ABBREV_TAC	(Q)
-------------------	------------

`Q.ABBREV_TAC` : term quotation -> tactic

Synopsis

Introduces an abbreviation into a goal.

Description

The tactic `Q.ABBREV_TAC q` parses the quotation `q` in the context of the goal to which it is applied. The result must be a term of the form `v = e` with `v` a variable. The effect of the tactic is to replace the term `e` wherever it occurs in the goal by `v` (or a primed variant of

v if v already occurs in the goal), and to add the assumption $\text{Abbrev}(v = e)$ to the goal's assumptions. Again, if v already occurs free in the goal, then the new assumption will be $\text{Abbrev}(v' = e)$, with v' a suitably primed version of v .

It is not an error if the expression e does not occur anywhere within the goal. In this situation, the effect of the tactic is simply to add the assumption $\text{Abbrev}(v = e)$.

The `Abbrev` constant is defined in `markerTheory` to be the identity function over boolean values. It is used solely as a tag, so that abbreviations can be found by other tools, and so that simplification tactics such as `RW_TAC` will not eliminate them. When it sees them as part of its context, the simplifier treats terms of the form $\text{Abbrev}(v = e)$ as assumptions $e = v$. In this way, the simplifier can use abbreviations to create further sharing, after an abbreviation's creation.

Failure

Fails if the quotation is ill-typed. This may happen because variables in the quotation that also appear in the goal are given the same type in the quotation as they have in the goal. Also fails if the variable of the equation appears in the expression that it is supposed to be abbreviating.

Example

Substitution in the goal:

```
- Q.ABBREV_TAC 'n = 10' ([], '10 < 9 * 10');
> val it = ([(['Abbrev(n = 10)', 'n < 9 * n'], fn) :
  (term list * term) list * (thm list -> thm)
```

and the assumptions:

```
- Q.ABBREV_TAC 'm = n + 2' (['f (n + 2) < 6', 'n < 7'];
> val it = ([(['Abbrev(m = n + 2)', 'f m < 6', 'n < 7'], fn) :
  (term list * term) list * (thm list -> thm)
```

and both

```
- Q.ABBREV_TAC 'u = x ** 32' (['x ** 32 = f z',
                               'g (x ** 32 + 6) - 10 < 65'];
> val it =
  ([(['Abbrev(u = x ** 32)', 'u = f z', 'g (u + 6) - 10 < 65'],
    fn) :
  (term list * term) list * (thm list -> thm)
```

Comments

Though it is possible to abbreviate functions, using quotations such as `'f = \n. n + 3'`, in this case `ABBREV_TAC` will not do anything more than replace exact copies of the abstraction. Following `ABBREV_TAC` with

```
POP_ASSUM (ASSUME_TAC o GSYM o
          SIMP_RULE bool_ss [FUN_EQ_THM, markerTheory.Abbrev_def])
```

will turn the assumption ‘Abbrev($f = (\lambda n. n + 3)$)’ into ‘ $\lambda n. n + 3 = f\ n$ ’ which may find more instances of the desired pattern.

See also

BasicProvers.Abbbr, Q.HO_MATCH_ABBREV_TAC, Q.MATCH_ABBREV_TAC, Q.UNABBREV_TAC.

<h1 style="margin: 0;">ABS</h1>	<h1 style="margin: 0;">(Thm)</h1>
---------------------------------	-----------------------------------

ABS : term -> thm -> thm

Synopsis

Abstracts both sides of an equation.

Description

$$\frac{A \mid- t1 = t2}{A \mid- (\lambda x. t1) = (\lambda x. t2)} \quad \text{ABS } x \quad [\text{Where } x \text{ is not free in } A]$$

Failure

If the theorem is not an equation, or if the variable x is free in the assumptions A .

Example

```
- let val m = Term 'm:bool'
  in
    ABS m (REFL m)
  end;

> val it = |- (\m. m) = (\m. m) : thm
```

See also

Drule.ETA_CONV, Drule.EXT, Drule.MK_ABS.

ABS_CONV

(Conv)

ABS_CONV : conv -> conv

Synopsis

Applies a conversion to the body of an abstraction.

Description

If c is a conversion that maps a term tm to the theorem $\vdash tm = tm'$, then the conversion $ABS_CONV\ c$ maps abstractions of the form $\lambda x. tm$ to theorems of the form:

$$\vdash (\lambda x. tm) = (\lambda x. tm')$$

That is, $ABS_CONV\ c\ (\lambda x. t)$ applies c to the body of the abstraction $\lambda x. t$.

Failure

$ABS_CONV\ c\ tm$ fails if tm is not an abstraction or if tm has the form $\lambda x. t$ but the conversion c fails when applied to the term t . The function returned by $ABS_CONV\ c$ may also fail if the ML function $c : term \rightarrow thm$ is not, in fact, a conversion (i.e. a function that maps a term M to a theorem $\vdash M = N$).

Example

```
- ABS_CONV SYM_CONV (Term '\x. 1 = x')
> val it = \vdash (\lambda x. 1 = x) = (\lambda x. x = 1) : thm
```

See also

Conv.RAND_CONV, Conv.RATOR_CONV, Conv.SUB_CONV, Conv.BINDER_CONV,
Conv.QUANT_CONV, Conv.STRIP_BINDER_CONV, Conv.STRIP_QUANT_CONV.

ABS_TAC

(Tactic)

ABS_TAC : tactic

Synopsis

Strips lambda abstraction on both sides of an equation.

Description

When applied to a goal of the form $A \vdash (\lambda x. f\ x) = (\lambda y. g\ u)$, the tactic ABS_TAC strips away the lambda abstractions:

$$\frac{A \text{ ?- } (\lambda x. f x) = (\lambda y. g y)}{\text{===== ABS_TAC}} A \text{ ?- } f x = g x$$
Failure

Fails unless the goal has the above form, namely an equation both sides of which consist of a lambda abstraction.

See also

Tactic.AP_TERM_TAC, Tactic.AP_THM_TAC.

Absyn

(Parse)

Absyn : term quotation -> Absyn.absyn

Synopsis

Implements the first phase of term parsing; the removal of special syntax.

Description

Absyn takes a quotation and parses it into an abstract syntax tree of type `absyn`, using the current term and type grammars. This phase of parsing is unconcerned with types, and will happily parse meaningless expressions that are syntactically valid.

Example

Absyn will parse the expression ‘let x = e1 in e2’ into

```
APP(APP(IDENT "LET", LAM(VIDENT "x", IDENT "e2")), IDENT "e1")
```

The record syntax ‘rec.fld1’ is converted into something of the form

```
APP(IDENT "...fld1", IDENT "rec")
```

where the dots will actually be equal to the value of `GrammarSpecials.recsel_special` (a string).

Failure

Fails if the quotation has a syntax error.

Uses

Absyn is not often used, but may be handy for implementing some weird and wonderful concrete syntax that surpasses the functionality of the HOL parser.

See also

Parse.Term, Parse.term_grammar.

AC	(simpLib)
----	-----------

AC : thm -> thm -> thm

Synopsis

Packages associativity and commutativity theorems for use in the simplifier.

Description

The AC function combines an associativity and commutativity theorem. The resulting theorem can be passed to the simplifier as if a rewrite, but will rather be used by the simplifier as the basis for performing AC-normalisation.

The theorems can be combined in either order, can be partly generalised, and need not express associativity in any particular direction from left to right.

Failure

AC never fails, but if applied to theorems that are not of the required form, the simplifier will raise an exception when it attempts to use the result.

Example

```
- SIMP_CONV bool_ss [AC ADD_COMM ADD_ASSOC] ``3 + x + y + 1``;
> val it = |- 3 + x + y + 1 = x + (y + (1 + 3)) : thm
```

```
- SIMP_CONV bool_ss [AC (GSYM ADD_ASSOC) ADD_COMM] ``x + 1 + y + 3``;
> val it = |- x + 1 + y + 3 = x + (y + (1 + 3)) : thm
```

See also

simpLib.SSFRAG.

AC_CONV	(Conv)
---------	--------

AC_CONV : (thm * thm) -> conv

Synopsis

Proves equality of terms using associative and commutative laws.

Description

Suppose `_` is a function, which is assumed to be infix in the following syntax, and `ath` and `cth` are theorems expressing its associativity and commutativity; they must be of the following form, except that any free variables may have arbitrary names and may be universally quantified:

$$\begin{aligned} \text{ath} &= |- m _ (n _ p) = (m _ n) _ p \\ \text{cth} &= |- m _ n = n _ m \end{aligned}$$

Then the conversion `AC_CONV(ath,cth)` will prove equations whose left and right sides can be made identical using these associative and commutative laws.

Failure

Fails if the associative or commutative law has an invalid form, or if the term is not an equation between AC-equivalent terms.

Example

Consider the terms `x + SUC t + ((3 + y) + z)` and `3 + SUC t + x + y + z`. `AC_CONV` proves them equal.

```
- AC_CONV(ADD_ASSOC,ADD_SYM)
  (Term 'x + (SUC t) + ((3 + y) + z) = 3 + (SUC t) + x + y + z');

> val it =
  |- (x + ((SUC t) + ((3 + y) + z))) = 3 + ((SUC t) + (x + (y + z))) = T
```

Comments

Note that the preproved associative and commutative laws for the operators `+`, `*`, `/\` and `\/` are already in the right form to give to `AC_CONV`.

See also

`Conv.SYM_CONV`.

ACCEPT_TAC	(Tactic)
------------	----------

ACCEPT_TAC : thm_tactic

Synopsis

Solves a goal if supplied with the desired theorem (up to alpha-conversion).

Description

ACCEPT_TAC maps a given theorem `th` to a tactic that solves any goal whose conclusion is alpha-convertible to the conclusion of `th`.

Failure

ACCEPT_TAC `th` `(A,g)` fails if the term `g` is not alpha-convertible to the conclusion of the supplied theorem `th`.

Example

ACCEPT_TAC applied to the axiom

```
BOOL_CASES_AX = |- !t. (t = T) \\/ (t = F)
```

will solve the goal

```
?- !x. (x = T) \\/ (x = F)
```

but will fail on the goal

```
?- !x. (x = F) \\/ (x = T)
```

Uses

Used for completing proofs by supplying an existing theorem, such as an axiom, or a lemma already proved.

See also

Tactic.MATCH_ACCEPT_TAC.

`aconv`

(Term)

```
aconv : term -> term -> bool
```

Synopsis

Tests for alpha-convertibility of terms.

Description

When applied to two terms, `aconv` returns `true` if they are alpha-convertible, and `false` otherwise. Two terms are alpha-convertible if they differ only in the way that names have been given to bound variables.

Failure

Never fails.

Example

```
- aconv (Term '?x y. x /\ y') (Term '?y x. y /\ x')
> val it = true : bool
```

See also

Thm.ALPHA, Drule.ALPHA_CONV.

ADD_ASSUM	(Drule)
------------------	----------------

ADD_ASSUM : term -> thm -> thm

Synopsis

Adds an assumption to a theorem.

Description

When applied to a boolean term s and a theorem $A \vdash t$, the inference rule ADD_ASSUM returns the theorem $A \cup \{s\} \vdash t$.

$$\frac{A \vdash t}{A \cup \{s\} \vdash t} \text{ ADD_ASSUM } s$$
Failure

Fails unless the given term has type bool.

See also

Thm.ASSUME, Drule.UNDISCH.

add_bare_numeral_form	(Parse)
------------------------------	----------------

add_bare_numeral_form : (char * string option) -> unit

Synopsis

Adds support for annotated numerals to the parser/pretty-printer.

Description

The function `add_bare_numeral_form` allows the user to give special meaning to strings of digits that are suffixed with single characters. A call to this function with pair argument (c, s) adds c as a possible suffix. Subsequently, if a sequence of digits is parsed, and it has the character c directly after the digits, then the natural number corresponding to these digits is made the argument of the “map function” corresponding to s .

This map function is computed as follows: if the s option value is `NONE`, then the function is considered to be the identity and never really appears; the digits denote a natural number. If the value of s is `SOME s'`, then the parser translates the string to an application of s' to the natural number denoted by the digits.

Failure

Fails if the suffix character is not a letter.

Example

The following function, `binary_of`, defined with equations:

```
val bthm =
  |- binary_of n = if n = 0 then 0
                  else n MOD 10 + 2 * binary_of (n DIV 10) : thm
```

can be used to convert numbers whose decimal notation is x , to numbers whose binary notation is x (as long as x only involves zeroes and ones).

The following call to `add_bare_numeral_form` then sets up a numeral form that could be used by users wanting to deal with binary numbers:

```
- add_bare_numeral_form("#b", SOME "binary_of");
> val it = () : unit

- Term'1011b';
> val it = '1011b' : term

- dest_comb it;
> val it = ('binary_of', '1011') : term * term
```

Comments

It is highly recommended that users avoid using suffixes that might be interpreted as hexadecimal digits A to F, in either upper or lower case. Further, HOL convention has it that suffix character should be lower case.

Uses

If one has a range of values that are usefully indexed by natural numbers, the function `add_bare_numeral_form` provides a syntactically convenient way of reading and writing these values. If there are other functions in the range type such that the mapping function is a homomorphism from the natural numbers, then `add_numeral_form` could be used, and the appropriate operators (+, * etc) overloaded.

See also

`Parse.add_numeral_form`.

<code>ADD_CONV</code>	<code>(reduceLib)</code>
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`ADD_CONV` : `conv`

Synopsis

Calculates by inference the sum of two numerals.

Description

If `m` and `n` are numerals (e.g. 0, 1, 2, 3,...), then `ADD_CONV "m + n"` returns the theorem:

$$\vdash m + n = s$$

where `s` is the numeral that denotes the sum of the natural numbers denoted by `m` and `n`.

Failure

`ADD_CONV tm` fails unless `tm` is of the form "`m + n`", where `m` and `n` are numerals.

Example

```
#ADD_CONV "75 + 25";;
|- 75 + 25 = 100
```

<code>add_implicit_rewrites</code>	<code>(Rewrite)</code>
------------------------------------	------------------------

`Rewrite.add_implicit_rewrites`: `thm list -> unit`

Synopsis

Augments the built-in database of simplifications automatically included in rewriting.

Uses

Used to build up the power of the built-in simplification set.

See also

`Rewrite.set_implicit_rewrites.`

<code>add_infix</code>

(Parse)

```
add_infix : string * int * HOLgrammars.associativity -> unit
```

Synopsis

Adds a string as an infix with the given precedence and associativity to the term grammar.

Description

This function adds the given string to the global term grammar such that the string

```
<str1> s <str2>
```

will be parsed as

```
s <t1> <t2>
```

where `<str1>` and `<str2>` have been parsed to two terms `<t1>` and `<t2>`. The parsing process does not pay any attention to whether or not `s` corresponds to a constant or not. This resolution happens later in the parse, and will result in either a constant or a variable with name `s`. In fact, if this name is overloaded, the eventual term generated may have a constant of quite a different name again; the resolution of overloading comes as a separate phase (see the entry for `overload_on`).

Failure

`add_infix` fails if the precedence level chosen for the new infix is the same as a different type of grammar rule (e.g., suffix or binder), or if the specified precedence level has infixes already but of a different associativity.

It is also possible that the choice of string `s` will result in an ambiguous grammar. This will be marked with a warning. The parser may behave in strange ways if it encounters ambiguous phrases, but will work normally otherwise.

Example

Though we may not have `+` defined as a constant, we can still define it as an infix for the purposes of printing and parsing:

```
- add_infix ("+", 500, HOLgrammars.LEFT);
> val it = () : unit

- val t = Term 'x + y';
<<HOL message: inventing new type variable names: 'a, 'b, 'c.>>
> val t = 'x + y' : term
```

We can confirm that this new infix has indeed been parsed that way by taking the resulting term apart:

```
- dest_comb t;
> val it = ('$+ x', 'y') : term * term
```

With its new status, `+` has to be “quoted” with a dollar-sign if we wish to use it in a position where it is not an infix, as in the binding list of an abstraction:

```
- Term '\$+. x + y';
<<HOL message: inventing new type variable names: 'a, 'b, 'c.>>
> val it = '\$+. x + y' : term
- dest_abs it;
> val it = ('$+', 'x + y') : term * term
```

The generation of three new type variables in the examples above emphasises the fact that the terms in the first example and the body of the second are really no different from `f x y` (where `f` is a variable), and don't have anything to do with the constant for addition from `arithmeticTheory`. The new `+` infix is left associative:

```
- Term 'x + y + z';
<<HOL message: inventing new type variable names: 'a, 'b.>>
> val it = 'x + y + z' : term

- dest_comb it;
> val it = ('$+ (x + y)', 'z') : term * term
```

It is also more tightly binding than `/\` (which has precedence 400 by default):

```
- Term 'p /\ q + r';
<<HOL message: inventing new type variable names: 'a, 'b.>>
> val it = 'p /\ q + r' : term

- dest_comb it;
> val it = ('$/\ p', 'q + r') : term * term
```

An attempt to define a right associative operator at the same level fails:

```
Lib.try add_infix("-", 500, HOLgrammars.RIGHT);
```

```
Exception raised at Parse.add_infix:
```

```
Grammar Error: Attempt to have differently associated infixes
                (RIGHT and LEFT) at same level
```

Similarly we can't define an infix at level 900, because this is where the (true prefix) rule for logical negation (\sim) is.

```
- Lib.try add_infix("-", 900, HOLgrammars.RIGHT);
```

```
Exception raised at Parse.add_infix:
```

```
Grammar Error: Attempt to have different forms at same level
```

Finally, an attempt to have a second + infix at a different precedence level causes grief when we later attempt to use the parser:

```
- add_infix("+", 400, HOLgrammars.RIGHT);
```

```
> val it = () : unit
```

```
- Term'p + q';
```

```
<<HOL warning: Parse.Term: Grammar ambiguous on token pair + and +,
                and probably others too>>
```

```
<<HOL message: inventing new type variable names: 'a, 'b, 'c>>
```

```
> val it = 'p + q' : term
```

In this situation, the behaviour of the parser will become quite unpredictable whenever the + token is encountered. In particular, + may parse with either fixity.

Uses

Most use of infixes will want to have them associated with a particular constant in which case the definitional principles (`new_infix1_definition` etc) are more likely to be appropriate. However, a development of a theory of abstract algebra may well want to have infix variables such as + above.

Comments

As with other functions in the `Parse` structure, there is a companion `temp_add_infix` function, which has the same effect on the global grammar, but which does not cause this effect to persist when the current theory is exported.

See also

`Parse.add_rule`, `Parse.add_listform`, `Parse.Term`.

<div data-bbox="236 349 644 405" data-label="Text"><code>add_infix_type</code></div>	<div data-bbox="1203 349 1412 400" data-label="Text"><code>(Parse)</code></div>
--	---

```
add_infix_type : {Assoc : associativity,
                  Name : string,
                  ParseName : string option,
                  Prec : int} ->
unit
```

Synopsis

Adds a type infix.

Description

A call to `add_infix_type` adds an infix type symbol to the type grammar. The argument is a record of four values providing information about the infix.

The `Assoc` field specifies the associativity of the symbol (possible values: `LEFT`, `RIGHT` and `NONASSOC`). The standard HOL type infixes (`+`, `#`, `->` and `|->`) are all right-associative. The `Name` field specifies the name of the binary type operator that is being mapped to. If the name of the type is not the same as the concrete syntax (as in all the standard HOL examples above), the concrete syntax can be provided in the `ParseName` field. The `Prec` field specifies the binding precedence of the infix. This should be a number less than 100, and probably greater than or equal to 50, where the function `->` symbol lies. The greater the number, the more tightly the symbol attempts to “grab” its arguments.

Failure

Fails if the desired precedence level contains an existing infix with a different associativity.

Example

```
- Hol_datatype 'atree = Nd of 'v => ('k # atree) list';
<<HOL message: Defined type: "atree">>
> val it = () : unit

- add_infix_type { Assoc = LEFT, Name = "atree",
                  ParseName = SOME ">->", Prec = 65 };
> val it = () : unit

- type_of 'Nd';
<<HOL message: inventing new type variable names: 'a, 'b>>
> val it = '': 'a -> ('b # ('b >-> 'a)) list -> 'b >-> 'a' : hol_type
```

add_listform

(Parse)

```
add_listform :
  {separator : pp_element list, leftdelim : pp_element list,
   rightdelim : pp_element list, cons : string, nilstr : string,
   block_info : term_grammar.block_info } ->
  unit
```

Synopsis

Adds a “list-form” to the built-in grammar, allowing the parsing of strings such as [a; b; c] and {}.

Description

The `add_listform` function allows the user to augment the HOL parser with rules so that it can turn a string of the form

```
<ld> str1 <sep> str2 <sep> ... strn <rd>
```

into the term

```
<cons> t1 (<cons> t2 ... (<cons> tn <nilstr>))
```

where `<ld>` is the left delimiter string, `<rd>` the right delimiter, and `<sep>` is the separator string from the fields of the record argument to the function. The various `stri` are strings representing the `ti` terms. Further, the grammar will also parse `<ld> <rd>` into `<nilstr>`.

The `pp_element` lists passed to this function for the `separator`, `leftdelim` and `rightdelim` fields are interpreted as by the `add_rule` function. These lists must have exactly one `TOK` element (this provides the string that will be printed), and other formatting elements such as `BreakSpace`.

The `block_info` field is a pair consisting of a “consistency” (`PP.CONSISTENT`, or `PP.INCONSISTENT`), and an indentation depth (an integer). The standard value for this field is `(PP.INCONSISTENT, 0)`, which will cause lists too long to fit in a single line to print with as many elements on the first line as will fit, and for subsequent elements to appear unindented on subsequent lines. Changing the “consistency” to `PP.CONSISTENT` would cause lists too long for a single line to print with one element per line. The indentation level number specifies the number of extra spaces to be inserted when a line-break occurs.

In common with the `add_rule` function, there is no requirement that the `cons` and `nilstr` fields be the names of constants; the parser/grammar combination will generate variables with these names if there are no corresponding constants.

The HOL pretty-printer is simultaneously aware of the new rule, and terms of the forms above will print appropriately.

Failure

Fails if any of the `pp_element` lists are ill-formed: if they include `TM`, `BeginFinalBlock`, or `EndInitialBlock` elements, or if do not include exactly one `TOK` element. Subsequent calls to the term parser may also fail or behave unpredictably if the strings chosen for the various fields above introduce precedence conflicts. For example, it will almost always be impossible to use left and right delimiters that are already present in the grammar, unless they are there as the left and right parts of a `closefix`.

Example

The definition of the “list-form” for lists in the HOL distribution is:

```
add_listform {separator = [TOK ";", BreakSpace(1,0)],
              leftdelim = [TOK "["], rightdelim = [TOK "]"],
              cons = "CONS", nilstr = "NIL",
              block_info = (PP.INCONSISTENT, 0)};
```

while the set syntax is defined similarly:

```
add_listform {leftdelim = [TOK "{"], rightdelim = TOK ["}"],
              separator = [";", BreakSpace(1,0)],
              cons = "INSERT", nilstr = "EMPTY",
              block_info = (PP.INCONSISTENT, 0)};
```

Uses

Used to make sequential term structures print and parse more pleasingly.

Comments

As with other parsing functions, there is a `temp_add_listform` version of this function, which has the same effect on the global grammar, but which does not cause this effect to persist when the current theory is exported.

See also

`Parse.add_rule`.

<div data-bbox="161 349 627 400" data-label="Text"> <pre>add_numeral_form</pre> </div>	<div data-bbox="1125 347 1331 398" data-label="Text"> <pre>(Parse)</pre> </div>
--	---

```
Parse.add_numeral_form : (char * string option) -> unit
```

Synopsis

Adds support for numerals of differing types to the parser/pretty-printer.

Description

This function allows the user to extend HOL's parser and pretty-printer so that they recognise and print numerals. A numeral in this context is a string of digits. Each such string corresponds to a natural number (i.e., the HOL type `num`) but `add_numeral_form` allows for numerals to stand for values in other types as well.

A call to `add_numeral_form(c,s)` augments the global term grammar in two ways. Firstly, in common with the function `add_bare_numeral_form` (q.v.), it allows the user to write a single letter suffix after a numeral (the argument `c`). The presence of this character specifies `s` as the “injection function” which is to be applied to the natural number denoted by the preceding digits.

Secondly, the constant denoted by the `s` argument is overloaded to be one of the possible resolutions of an internal, overloaded operator, which is invisibly wrapped around all numerals that appear without a character suffix. After applying `add_numeral_form`, the function denoted by the argument `s` is now a possible resolution of this overloading, so numerals can now be seen as members of the range of the type of `s`.

Finally, if `s` is not `NONE`, the constant denoted by `s` is overloaded to be one of the possible resolutions of the string `&`. This operator is thus the standard way of writing the injection function from `:num` into other numeric types.

The injection function specified by argument `s` is either the constant with name `s0`, if `s` is of the form `SOME s0`, or the identity function if `s` is `NONE`. Using `add_numeral_form` with `NONE` for this parameter is done in the development of `arithmeticTheory`, and should not be done subsequently.

Failure

Fails if `arithmeticTheory` is not loaded, as this is where the basic constants implementing natural number numerals are defined. Also fails if there is no constant with the given name, or if it doesn't have type `:num -> 'a` for some `'a`. Fails if `add_bare_numeral_form` would also fail on this input.

Example

The natural numbers are given numeral forms as follows:

```
val _ = add_numeral_form ("n", NONE);
```

This is done in `arithmeticTheory` so that after it is loaded, one can write numerals and have them parse (and print) as natural numbers. However, later in the development, in `integerTheory`, numeral forms for integers are also introduced:

```
val _ = add_numeral_form("i", SOME "int_of_num");
```

Here `int_of_num` is the name of the function which injects natural numbers into integers. After this call is made, numeral strings can be treated as integers or natural numbers, depending on the context.

```
- load "integerTheory";
> val it = () : unit
- Term'3';
<<HOL message: more than one resolution of overloading was possible.>>
> val it = '3' : term
- type_of it;
> val it = ':int' : hol_type
```

The parser has chosen to give the string “3” integer type (it will prefer the most recently specified possibility, in common with overloading in general). However, numerals can appear with natural number type in appropriate contexts:

```
- Term'(SUC 3, 4 + ~x)';
> val it = '(SUC 3,4 + ~x)' : term
- type_of it;
> val it = ':num # int' : hol_type
```

Moreover, one can always use the character suffixes to absolutely specify the type of the numeral form:

```
- Term'f 3 /\ p';
<<HOL message: more than one resolution of overloading was possible.>>
> val it = 'f 3 /\ p' : term

- Term'f 3n /\ p';
> val it = 'f 3 /\ p' : term
```

Comments

Overloading on too many numeral forms is a sure recipe for confusion.

See also

`Parse.add_bare_numeral_form`, `Parse.overload_on`, `Parse.show_numeral_types`.

add_rewrites

(Rewrite)

```
add_rewrites : rewrites -> thm list -> rewrites
```

Synopsis

Add theorems to a collection of rewrite rules.

Description

The function `add_rewrites` processes each element in a list of theorems and adds the resulting rewrite rules to a value of type `rewrites`.

Failure

Never fails.

Example

```
- load "pairTheory"; open pairTheory;
  add_rewrites empty_rewrites (PAIR_MAP_THM::pair_rws);

> val it =
  |- (f ## g) (x,y) = (f x,g y);
  |- (FST x,SND x) = x;
  |- FST (x,y) = x;
  |- SND (x,y) = y
  Number of rewrite rules = 4
  : rewrites
```

Uses

For building bespoke rewrite rule sets.

See also

`Rewrite.bool_rewrites`, `Rewrite.empty_rewrites`, `Rewrite.implicit_rewrites`,
`Rewrite.GEN_REWRITE_CONV`, `Rewrite.GEN_REWRITE_RULE`, `Rewrite.GEN_REWRITE_TAC`.

<code>add_rule</code>	<code>(Parse)</code>
-----------------------	----------------------

```
add_rule :
  {term_name : string, fixity : fixity,
   pp_elements: term_grammar.pp_element list,
   paren_style : term_grammar.ParenStyle,
   block_style : term_grammar.PhraseBlockStyle *
                term_grammar.block_info} -> unit
```

Synopsis

Adds a parsing/printing rule to the global grammar.

Description

The function `add_rule` is a fundamental method for adding parsing (and thus printing) rules to the global term grammar that sits behind the functions `Term` and `--`, and the pretty-printer installed for terms. It is used for everything except the addition of list-forms, for which refer to the entry for `add_listform`.

There are five components in the record argument to `add_rule`. The `term_name` component is the name of the term (whether a constant or a variable) that will be generated at the head of the function application. Thus, the `term_name` component when specifying parsing for conditional expressions is `COND`.

The following values (all in structure `Parse`) are useful for constructing fixity values:

```
val LEFT      : HOLgrammars.associativity
val RIGHT     : HOLgrammars.associativity
val NONASSOC  : HOLgrammars.associativity

val Binder    : fixity
val Closefix  : fixity
val Infixl    : int -> fixity
val Infixr    : int -> fixity
val Infix     : HOLgrammars.associativity * int -> fixity
val Prefix    : int -> fixity
val Suffix    : int -> fixity
```

The `Binder` fixity is for binders such as universal and existential quantifiers (`!` and `?`). Binders can actually be seen as (true) prefixes (should `!x. p /\ q` be parsed as `(!x. p) /\ q` or as `!x. (p /\ q)?`), but the `add_rule` interface only allows binders to be added at the one level (the weakest in the grammar). Further, when binders

are added using this interface, all elements of the record apart from the `term_name` are ignored, so the name of the binder must be the same as the string that is parsed and printed (but see also restricted quantifiers: `associate_restriction`).

The remaining fixities all cause `add_rule` to pay due heed to the `pp_elements` (“parsing/printing elements”) component of the record. As far as parsing is concerned, the only important elements are `TOK` and `TM` values, of the following types:

```
val TM : term_grammar.pp_element
val TOK : string -> term_grammar.pp_element
```

The `TM` value corresponds to a “hole” where a sub-term is possible. The `TOK` value corresponds to a piece of concrete syntax, a string that is required when parsing, and which will appear when printing. The sequence of `pp_elements` specified in the record passed to `add_rule` specifies the “kernel” syntax of an operator in the grammar. The “kernel” of a rule is extended (or not) by additional sub-terms depending on the fixity type, thus:

```
Closefix   :      [Kernel]      (* no external arguments *)
Prefix     :      [Kernel] _    (* an argument to the right *)
Suffix     :      _ [Kernel]    (* an argument to the left *)
Infix      :      _ [Kernel] _  (* arguments on both sides *)
```

Thus simple infixes, suffixes and prefixes would have singleton `pp_element` lists, consisting of just the symbol desired. More complicated mix-fix syntax can be constructed by identifying whether or not sub-term arguments exist beyond the kernel of concrete syntax. For example, syntax for the evaluation relation of an operational semantics (`_ |- _ --> _`) is an infix with a kernel delimited by `|-` and `-->` tokens. Syntax for denotation brackets [`| _ |`] is a closefix with one internal argument in the kernel.

The remaining sorts of possible `pp_element` values are concerned with pretty-printing. (The basic scheme is implemented on top of a standard Open-style pretty-printing package.) They are

```
(* where
   type term_grammar.block_info = PP.break_style * int
*)
val BreakSpace : (int * int) -> term_grammar.pp_element
val HardSpace  : int -> term_grammar.pp_element

val BeginFinalBlock : term_grammar.block_info -> term_grammar.pp_element
val EndInitialBlock : term_grammar.block_info -> term_grammar.pp_element
val PPBlock : term_grammar.pp_element list * term_grammar.block_info
             -> term_grammar.pp_element
```

```

val OnlyIfNecessary : term_grammar.ParenStyle
val ParoundName     : term_grammar.ParenStyle
val ParoundPrec     : term_grammar.ParenStyle
val Always          : term_grammar.ParenStyle

val AroundEachPhrase : term_grammar.PhraseBlockStyle
val AroundSamePrec   : term_grammar.PhraseBlockStyle
val AroundSameName   : term_grammar.PhraseBlockStyle
val NoPhrasing       : term_grammar.PhraseBlockStyle

```

The two spacing values provide ways of specifying white-space should be added when terms are printed. Use of `HardSpace n` results in `n` spaces being added to the term whatever the context. On the other hand, `BreakSpace(m,n)` results in a break of width `m` spaces unless this makes the current line too wide, in which case a line-break will occur, and the next line will be indented an extra `n` spaces.

For example, the `add_infix` function (q.v.) is implemented in terms of `add_rule` in such a way that a single token infix `s`, has a `pp_element` list of

```
[HardSpace 1, TOK s, BreakSpace(1,0)]
```

This results in chains of infixes (such as those that occur with conjunctions) that break so as to leave the infix on the right hand side of the line. Under this constraint, printing can't break so as to put the infix symbol on the start of a line, because that would imply that the `HardSpace` had in fact been broken. (Consequently, if a change to this behaviour is desired, there is no global way of effecting it, but one can do it on an infix-by-infix basis by deleting the given rule (see, for example, `remove_termtok`) and then “putting it back” with different pretty-printing constraints.)

The `PPBlock` function allows the specification of nested blocks (blocks in the Open pretty-printing sense) within the list of `pp_elements`. Because there are sub-terms in all but the `Closefix` fixities that occur beyond the scope of the `pp_element` list, the `BeginFinalBlock` and `EndInitialBlock` functions can also be used to indicate the boundary of blocks whose outer extent is the term beyond the kernel represented by the `pp_element` list. There is an example of this below.

The possible `ParenStyle` values describe when parentheses should be added to terms. The `OnlyIfNecessary` value will cause parentheses to be added only when required to disambiguate syntax. The `ParoundName` will cause parentheses to be added if necessary, or where the head symbol has the given `term_name` and where this term is not the argument of a function with the same head name. This style of parenthesisation is used with tuples, for example. The `ParoundPrec` value is similar, but causes parentheses to be added when the term is the argument to a function with a different precedence level. Finally, the `Always` value causes parentheses always to be added.


```

        TOK "then"], (PP.CONSISTENT, 0)),
    BreakSpace(1,2), TM, BreakSpace(1,0),
    BeginFinalBlock(PP.CONSISTENT, 2),
    TOK "else", BreakSpace(1,0)],
    paren_style = OnlyIfNecessary,
    block_style = (AroundEachPhrase,
        (PP.INCONSISTENT, 0))});

```

Note that the above form is not that actually used in the system. As written, it allows for pretty-printing some expressions as:

```

if P then
    <very long term> else Q

```

because the `block_style` is `INCONSISTENT`.

The pretty-printer prefers later rules over earlier rules by default (though this choice can be changed with `prefer_form_with_tok` (q.v.)), so conditional expressions print using the `if-then-else` syntax rather than the `_ => _ | _` syntax.

Uses

For making pretty concrete syntax possible.

Comments

Because adding new rules to the grammar may result in precedence conflicts in the operator-precedence matrix, it is as well with interactive use to test the `Term` parser immediately after adding a new rule, as it is only with this call that the precedence matrix is built.

As with other functions in the `Parse` structure, there is a companion `temp_add_rule` function, which has the same effect on the global grammar, but which does not cause this effect to persist when the current theory is exported.

An Isabelle-style concrete syntax for specifying rules would probably be desirable as it would conceal the complexity of the above from most users.

See also

`Parse.add_listform`, `Parse.add_infix`, `Parse.prefer_form_with_tok`,
`Parse.remove_rules_for_term`.

<code>add_tag</code>	<code>(Thm)</code>
----------------------	--------------------

`add_tag : tag * thm -> thm`

Synopsis

Adds oracle tags to a theorem.

Description

A call to `add_tag(tg,th)` returns a `th'` such that calling `Thm.tag(th')` returns the tag that is the merge of the tag associated with `th` (if any) and `tg`.

Failure

Never fails.

Comments

If an oracle implementation wishes to record additional information about the oracle mechanisms that have contributed to the ‘proof’ of a theorem (perhaps the use of existing HOL theorems that will have their own tags), then this function can be used to add that record.

See also

`Thm.mk_oracle_thm`.

`add_user_printer`

(Parse)

```
add_user_printer : (string * term * userprinter) -> unit
```

Synopsis

Adds a user specified pretty-printer for a specified type.

Description

The function `add_user_printer` is used to add a special purpose term pretty-printer to the interactive system. The pretty-printer is called whenever the term to be printed matches (with `match_term`) the term provided as the second parameter of the triple. If multiple calls to `add_user_printer` are made with the same string parameter, the older functions are replaced entirely. If multiple printers match, the more specific match will be chosen. If two matches are equally specific, the match chosen is unspecified.

The user-supplied function may choose not to print anything for the given term and hand back control to the standard printer by raising the exception `term_pp_types.UserPP_Failed`. All other exceptions will propagate to the top-level. If the system printer receives the `UserPP_Failed` exception, it prints out the term using its standard algorithm, but will again attempt to call the user function on any sub-terms that match the pattern.

The type `userprinter` is an abbreviation defined in `term_grammar` to be

```

type userprinter =
  type_grammar.grammar * term_grammar.grammar ->
  PPBackend.t ->
  sysprinter ->
  term_pp_types.ppstream_funs ->
  (grav * grav * grav) -> int ->
  term -> uprinter

```

where the type `grav` (from `term_pp_types`) is

```

datatype grav = Top | RealTop | Prec of (int * string)

```

The type `uprinter` (standing for "unit printer") is a special monadic printing type based on the `smp` module (explained further in the example below). The type `sysprinter` is another abbreviation

```

type sysprinter = (grav * grav * grav) -> int -> term -> uprinter

```

Thus, when the user's printing function is called, it is passed ten parameters, including three "gravity" values in a triple, and two grammars. The fourth parameter is the system's own printer. The fifth parameter is a record of functions to call for adding a string to the output, adding a break, adding new lines, defining some styles for printing like the color, etc. The availability of the system's printer allows the user function to use the default printer on sub-terms that it is not interested in. The user function must not call the `sysprinter` on the term that it is handed initially as the `sysprinter` will immediately call the user printing function all over again. If the user printer wants to give the whole term back to the system printer, then it must use the `UserPP_Failed` exception described above.

Though there are existing functions `add_string`, `add_break` etc. that can be used to manipulate pretty-printing streams, users should prefer instead to use the functions that are provided in the triple with the `sysprinter`. This then gives them access to functions that can prevent inadvertent symbol merges.

The `grav` type is used to let pretty-printers know a little about the context in which a term is to be printed out. The triple of gravities is given in the order "parent", "left" and "right". The left and right gravities specify the precedence of any operator that might be attempting to "grab" arguments from the left and right. For example, the term

```

(p /\ (if q then r else s)) ==> t

```

should be pretty-printed as

```

p /\ (if q then r else s) ==> t

```


The system figures this out when it comes to print the conditional expression because it knows both that the operator to the left has the appropriate precedence for conjunction but also that there is an operator with implication's precedence to the right. The issue arises because conjunction is tighter than implication in precedence, leading the printer to decide that parentheses aren't necessary around the conjunction. Similarly, considered on its own, the conjunction doesn't require parentheses around the conditional expression because there is no competition between them for arguments.

The `grav` constructors `Top` and `RealTop` indicate a context analogous to the top of the term, where there is no binding competition. The constructor `RealTop` is reserved for situations where the term really is the top of the tree; `Top` is used for analogous situations such when the term is enclosed in parentheses. (In the conditional expression above, the printing of `q` will have `Top` gravities to the left and right.)

The `Prec` constructor for gravity values takes both a number indicating precedence level and a string corresponding to the token that has this precedence level. This string parameter is of most importance in the parent gravity (the first component of the triple) where it can be useful in deciding whether or not to print parentheses and whether or not to begin fresh pretty-printing blocks. For example, tuples in the logic look better if they have parentheses around the topmost instance of the comma-operator, regardless of whether or not this is required according to precedence considerations. By examining the parent gravity, a printer can determine more about the term's context. (Note that the parent gravity will also be one or other of the left and right gravities; but it is not possible to tell which.)

The integer parameter to both the system printing function and the user printing function is the depth of the term. The system printer will stop printing a term if the depth ever reaches exactly zero. Each time it calls itself recursively, the depth parameter is reduced by one. It starts out at the value stored in `Globals.max_print_depth`. Setting the latter to `~1` will ensure that all of a term is always printed.

Finally, the string parameter to the `add_user_printer` function is a string corresponding to the ML function. Best practice is probably to define the printing function in an independent structure and to then have the string be of the form `"module.fname"`. This parameter is not present in the accompanying `temp_add_user_printer`, as this latter function does not affect the grammar exported to disk with `export_theory`.

Failure

Will not fail directly, but if the function parameter fails to print all terms of the registered type in any other way than raising the `UserPP_Failed` exception, then the pretty-printer will also fail. If the string parameter does not correspond to valid ML code, then the theory file generated by `export_theory` will not compile.

Example

This example uses the system printer to print sub-terms, and concerns itself only with

printing conjunctions. Note how the actions that make up the pretty-printer (combinations of `add_string` and `add_break` are combined with the infix `>>` operator (from the `smpp` module).

```
- fun myprint Gs B sys (ppfns:term_pp_types.ppstream_funs) gravs d t =
  let
    open Portable term_pp_types smpp
    val (str,brk) = (#add_string ppfns, #add_break ppfns);
    val (l,r) = dest_conj t
  in
    str "CONJ:" >>
    brk (1,0) >>
    sys (Top, Top, Top) (d - 1) l >>
    brk (1,0) >> str "and then" >> brk(1,0) >>
    sys (Top, Top, Top) (d - 1) r >>
    str "ENDCONJ"
  end handle HOL_ERR _ => raise term_pp_types.UserPP_Failed;
> val myprint = fn :
  'a -> 'b ->
  (grav * grav * grav -> int -> term -> (term_pp_types.printing_info,'c)smpp.t
  term_pp_types.ppstream_funs -> 'd -> int -> term ->
  (term_pp_types.printing_info,unit)smpp.t

- temp_add_user_printer ("myprint", ``p /\ q``, myprint);
> val it = () : unit

- ``p ==> q /\ r``;
> val it = ``p ==> CONJ: q and then r ENDCONJ`` : term
```

The variables `p`, `q` and `r` as well as the implication are all of boolean type, but are handled by the system printer. The user printer handles just the special form of the conjunction. Note that this example actually falls within the scope of the `add_rule` functionality.

The next approach to printing conjunctions is not possible with `add_rule`. This example uses the styling and blocking functions to create part of its effect. These functions (`ustyle` and `ublock` respectively) are higher-order functions that take printers as arguments and cause the arguments to be printed with a particular governing style (`ustyle`), or indented to reveal block structure (`ublock`).

```
- fun myprint2 Gs B sys (ppfns:term_pp_types.ppstream_funs) (pg,lg,rg) d t = let
  open Portable term_pp_types PPBackEnd smpp
```

```

val {add_string,add_break,ublock,ustyle,...} = ppfns
val (l,r) = dest_conj t
fun delim wrap body =
  case pg of
    Prec(_, "CONJ") => body
  | _ => wrap body
in
  delim (fn bod => ublock CONSISTENT 0
          (ustyle [Bold] (add_string "CONJ") >>
           add_break (1,2) >>
           ublock INCONSISTENT 0 bod >>
           add_break (1,0) >>
           ustyle [Bold] (add_string "ENDCONJ")))
    (sys (Prec(0, "CONJ"), Top, Top) (d - 1) l >>
     add_string "," >> add_break (1,0) >>
     sys (Prec(0, "CONJ"), Top, Top) (d - 1) r)
end handle HOL_ERR _ => raise term_pp_types.UserPP_Failed;

- temp_add_user_printer ("myprint2", ‘‘p /\ q‘‘, myprint2);

- ‘‘p /\ q /\ r /\ s /\ t /\ u /\ p /\ p /\ p /\ p /\ p /\ p /\
  p /\ p /\ p /\ p /\ p /\ p /\ q /\ r /\ s /\ t /\ u /\ v /\
  (w /\ x) /\ (p \/ q) /\ r‘‘;

> val it =
  ‘‘CONJ
    p, q, r, s, t, u, p, p, p, p, p, p, p, p, p, p, p, q,
    r, s, t, u, v, w, x, p \/ q, r
  ENDCONJ‘‘ : term

```

This example also demonstrates using parent gravities to print out a big term. The function passed as an argument to `delim` is only called when the parent gravity is not "CONJ". This ensures that the special delimiters only get printed when the first conjunction is encountered. Subsequent, internal conjunctions get passed the "CONJ" gravity in the calls to `sys`.

A better approach (and certainly a more direct one) would probably be to call `strip_conj` and print all of the conjuncts in one fell swoop. Additionally, this example demonstrates how easy it is to conceal genuine syntactic structure with a pretty-printer. Finally, it shows how styles can be used.

Uses

For extending the pretty-printer in ways not possible to encompass with the built-in grammar rules for concrete syntax.

See also

`Parse.add_rule`, `Term.match_term`, `Parse.remove_user_printer`.

<code>adjoin_to_theory</code>	<code>(Theory)</code>
-------------------------------	-----------------------

```
adjoin_to_theory : thy_addon -> unit
```

Synopsis

Include arbitrary ML in exported theory.

Description

It often happens that algorithms and flag settings accompany a logical theory (call it `thy`). One would want to simply load the `thyTheory` module and have the appropriate proof support, etc. loaded automatically as well.

There are several ways to support this. One simple way would be to define another ML structure, `thySupport` say, that depended on `thyTheory`. The algorithms, etc, could be placed in `thySupport` and the interested user would know that by loading `thySupport`, its contents, and those of `thyTheory`, would become available. This approach, and extensions of it are accomodated already in the notion of a HOL library.

However, it is sometimes more appropriate to actually include the support code directly in `thyTheory`. The function `adjoin_to_theory` performs this operation.

A call `adjoin_to_theory {sig_ps, struct_ps}` adds a signature prettyprinter `sig_ps` and a structure prettyprinter `struct_ps` to an internal queue of prettyprinters. When `export_theory ()` is eventually called two things happen: (a) the signature file `thyTheory.sig` is written, and (b) the structure file `thyTheory.sml` is written. When `thyTheory.sig` is written, each signature prettyprinter in the queue is called, in the order that they were added to the queue. This printing activity happens after the rest of the signature (coming from the declarations in the theory) has been written. Similarly, when `thyTheory.sml` is written, the structure prettyprinters are invoked in queue order, after the bindings of the theory have been written.

If `sig_ps` is `NONE`, then no signature additions are made. Likewise, if `struct_ps` is `NONE`, then no structure additions are made. (This latter possibility doesn't seem to be useful.)

Failure

It is up to the writer of a prettyprinter to ensure that it generates valid ML. If a prettyprinter added by a call to `adjoin_to_theory` fails, `thyTheory.sig` or `thyTheory.sml` could be malformed, and therefore not properly exported, or compiled.

Example

The following excerpt from the script for the theory of pairs is a fairly typical use of `adjoin_to_theory`. It adds the declaration of an ML variable `pair_rws` to the structure `pairTheory`.

```
val _ = adjoin_to_theory
{sig_ps =
  SOME(fn ppstrm => PP.add_string ppstrm "val pair_rws:thm list"),
  struct_ps =
    SOME(fn ppstrm => PP.add_string ppstrm
          "val pair_rws = [PAIR, FST, SND];")
}
```

Comments

The PP structure is documented in the MoscowML library documentation.

See also

`Theory.after_new_theory`, `Theory.thy_addon`, `BasicProvers.export_rewrites`.

after_new_theory

(Theory)

```
after_new_theory : (string * string -> unit) -> unit
```

Synopsis

Initialize package once a theory is declared.

Description

Some HOL infrastructure depends on certain packages being informed each time a new theory is created. The function `after_new_theory` supports this. An invocation `after_new_theory f` adds the function `f` to an internal queue of ‘initializers’. All subsequent calls to `new_theory` will cause each initializer to be run, in queue order. Each initializer will be given the names of the theory segments from before and after the call to `new_theory` as its argument..

Failure

It can be that an initializer fails for some reason when it is executed. Any exceptions will be caught, and an attempt will be made to print out a message. Then execution of the remaining initializers will continue.

Example

```
- fun every8 s (a::b::c::d::e::f::g::h::rst) =
      a::b::c::d::e::f::g::h::s::every8 s rst
  | every8 s otherwise = otherwise;
> val 'a every8 = fn : 'a -> 'a list -> 'a list

- after_new_theory (fn (old,s) =>
  (print ("Ancestors of "^s^":\n ");
   print (String.concat (every8 "\n " (commafy (ancestry s))));
   print ".\n"));
> val it = () : unit

- new_theory"foo";
<<HOL message: Created theory "foo">>
Ancestors of foo:
  one, option, pair, sum,
  combin, relation, min, bool,
  num, prim_rec, arithmetic, numeral,
  ind_type, list.
> val it = () : unit

- new_theory"bar";
Exporting theory "foo" ... done.
<<HOL message: Created theory "bar">>
Ancestors of bar:
  one, option, pair, sum,
  combin, relation, min, bool,
  num, prim_rec, arithmetic, numeral,
  ind_type, list, foo.
> val it = () : unit
```

Comments

Perhaps there should be a `before_export_theory` call as well?

Uses

Fairly low level system support tasks.

See also

Theory.adjoin_to_theory.

all**(Lib)**

```
all : ('a -> bool) -> 'a list -> bool
```

Synopsis

Tests whether a predicate holds throughout a list.

Description

`all P [x1,...,xn]` equals `P x1 andalso andalso P xn`. `all P []` yields true.

Failure

If `P x0, ..., P x(j-1)` all evaluate to true and `P xj` raises an exception `e`, then `all P [x0, ..., x(j-1), xj, ...]` raises `e`.

Example

```
- all (equal 3) [3,3,3];
> val it = true : bool

- all (equal 3) [];
> val it = true : bool

- all (fn _ => raise Fail "") [];
> val it = true : bool

- all (fn _ => raise Fail "") [1];
! Uncaught exception:
! Fail ""
```

See also

Lib.all2, Lib.exists, Lib.first.

all2**(Lib)**

```
all2 : ('a -> 'b -> bool) -> 'a list -> 'b list -> bool
```

Synopsis

Tests whether a predicate holds pairwise throughout two lists.

Description

An invocation

```
all2 P [x1,...,xn] [y1,...,yn]
```

equals

```
P x1 y1 andalso .... andalso P xn yn
```

Also, `all2 P [] []` yields `true`.

Failure

If `P x0, ..., P x(j-1)` all evaluate to `true` and `P xj` raises an exception `e`, then

```
all2 P [x0,...,x(j-1),xj,...,xn]
```

raises `e`. An invocation `all2 P l1 l2` will also raise an exception if the length of `l1` is not equal to the length of `l2`.

Example

```
- all2 equal [1,2,3] [1,2,3];
```

```
> val it = true : bool
```

```
- all2 equal [1,2,3] [1,2,3,4] handle e => Raise e;
```

```
Exception raised at Lib.all2:
```

```
different length lists
```

```
! Uncaught exception:
```

```
! HOL_ERR
```

```
- all2 (fn _ => fn _ => raise Fail "") [] [];
```

```
> val it = true : bool
```

```
- all2 (fn _ => fn _ => raise Fail "") [1] [1];
```

```
! Uncaught exception:
```

```
! Fail ""
```

See also

`Lib.all`.

all_consts	(Term)
------------	--------

```
all_consts : unit -> term list
```

Synopsis

All known constants in the current theory.

Description

An invocation `all_consts` returns a list of all declared constants in the current theory, i.e., all constants in the current theory segment and in its ancestry.

Failure

Never fails.

Example

```
- all_consts();
> val it =
  ['transitive', 'CONS', 'RES_ABSTRACT', 'COND', 'OPTION_MAP', 'FCONS',
   'FACT', '&', 'RPROD', 'mk_list', 'ZIP', 'IS_NUM_REP', 'ABS_sum', 'SUM',
   'SUC', 'OPTION_JOIN', 'REP_sum', 'RTC', 'SND', 'RES_SELECT', 'THE',
   'APPEND', 'option_REP', 'PRE', 'ABS_num', 'PRIM_REC', 'EXISTS', 'REP_num',
   'approx', 'case', 'CONSTR', '[]', '$MOD', 'ODD', 'MIN', 'case', 'MEM',
   'ISR', 'MAX', '$LEX', 'ISO', 'case_arrow_magic', 'ISL', 'LET', 'MAP',
   'INR', 'INL', '$EXP', 'FST', 'case', 'mk_rec', 'IS_SOME', '$DIV', 'ARB',
   'option_ABS', 'wellfounded', 'iiSUC', 'SIMP_REC_REL', 'RES_FORALL',
   '$==>', 'MK_PAIR', 'ZBOT', 'IS_NONE', 'TYPE_DEFINITION', 'case',
   'dest_rec', 'IS_PAIR', 'ONE_ONE', 'case', 'RES_EXISTS_UNIQUE', 'NUMRIGHT',
   'NUMPAIR', 'FILTER', 'BOTTOM', 'SOME', 'reflexive', 'EMPTY_REL',
   'REVERSE', 'ABS_prod', 'NUMERAL_BIT2', 'NUMERAL_BIT1', 'FRONT', 'OUTR',
   'OUTL', 'SIMP_REC', 'measure', 'NUMLEFT', 'REP_prod', 'list1', 'list0',
   'NULL', 'ONTO', 'EVERY', 'inv_image', 'list_size', 'NONE', 'ALT_ZERO',
   'case_magic', 'UNCURRY', 'UNZIP', 'FOLDR', 'FOLDL', 'iBIT_cases',
   'NUMERAL', 'ZRECSpace', 'iZ', 'case', 'iSUB', 'iSQR', 'ZCONSTR', 'WFREC',
   'WF', '$\/', 'TL', 'TC', 'RC', 'case_split_magic', '$IN', 'NUMSUM', 'HD',
   'EL', 'MAP2', 'CURRY', 'RES_EXISTS', 'LAST', 'NUMSND', '()', '$>=', '$<=',
   'INJP', 'INJN', 'INJF', '$?!', 'INJA', '$/\', 'IS_SUM_REP', 'RESTRICT',
   'iDUB', '$##', 'FUNPOW', 'NUMFST', 'EVEN', 'SUC_REP', '$~', 'dest_list',
   '$o', 'FNIL', 'W', 'the_fun', 'T', 'S', 'LENGTH', 'PRIM_REC_FUN', 'K',
```

```
'I', 'F', 'combin$C', '$@', '$?', '$>', '$=', '$<', 'ZERO_REP', '0', '$-',
'$,', 'FLAT', '$+', '$*', '$!'] : term list
```

See also

Parse.term_grammar.

ALL_CONV	(Conv)
----------	--------

ALL_CONV : conv

Synopsis

Conversion that always succeeds, raising the UNCHANGED exception.

Description

When applied to a term t , the conversion ALL_CONV raises the special UNCHANGED exception.

Failure

Never fails.

Uses

Identity element for THENC.

See also

Conv.NO_CONV, Thm.REFL.

ALL_EL_CONV	(listLib)
-------------	-----------

ALL_EL_CONV : conv -> conv

Synopsis

Computes by inference the result of applying a predicate to elements of a list.

Description

ALL_EL_CONV takes a conversion $conv$ and a term tm in the following form:

```
ALL_EL P [x0;...xn]
```

It returns the theorem

```
|- ALL_EL P [x0;...xn] = T
```

if for every x_i occurring in the list, `conv (--'P xi'--)` returns a theorem `|- P xi = T`, otherwise, if for at least one x_i , evaluating `conv (--'P xi'--)` returns the theorem `|- P xi = F`, then it returns the theorem

```
|- ALL_EL P [x0;...xn] = F
```

Failure

`ALL_EL_CONV conv tm` fails if `tm` is not of the form described above, or failure occurs when evaluating `conv (--'P xi'--)` for some x_i .

Example

Evaluating

```
ALL_EL_CONV bool_EQ_CONV (--'ALL_EL ($= T) [T;F;T]'--);
```

returns the following theorem:

```
|- ALL_EL($= T) [T;F;T] = F
```

In general, if the predicate P is an explicit lambda abstraction $(\lambda x. P x)$, the conversion should be in the form

```
(BETA_CONV THENC conv')
```

See also

`listLib.SOME_EL_CONV`, `listLib.IS_EL_CONV`, `listLib.FOLDL_CONV`,
`listLib.FOLDR_CONV`, `listLib.list_FOLD_CONV`.

ALL_TAC	(Tactical)
----------------	-------------------

`ALL_TAC` : tactic

Synopsis

Passes on a goal unchanged.

Description

ALL_TAC applied to a goal g simply produces the subgoal list $[g]$. It is the identity for the THEN tactical.

Failure

Never fails.

Example

The tactic

```
INDUCT_THEN numTheory.INDUCTION THENL [ALL_TAC, tac]
```

applied to a goal g , applies INDUCT_THEN numTheory.INDUCTION to g to give a basis and step subgoal; it then returns the basis unchanged, along with the subgoals produced by applying tac to the step.

Uses

Used to write tacticals such as REPEAT. Also, it is often used as a place-holder in building compound tactics using tacticals such as THENL.

See also

Prim_rec.INDUCT_THEN, Tactical.NO_TAC, Tactical.REPEAT, Tactical.THENL.

<div data-bbox="236 1314 474 1364" data-label="Text"> <p>ALL_THEN</p> </div>	<div data-bbox="1114 1314 1412 1364" data-label="Text"> <p>(Thm_cont)</p> </div>
--	--

ALL_THEN : thm_tactical

Synopsis

Passes a theorem unchanged to a theorem-tactic.

Description

For any theorem-tactic $ttac$ and theorem th , the application ALL_THEN $ttac$ th results simply in $ttac$ th , that is, the theorem is passed unchanged to the theorem-tactic. ALL_THEN is the identity theorem-tactical.

Failure

The application of ALL_THEN to a theorem-tactic never fails. The resulting theorem-tactic fails under exactly the same conditions as the original one.

Uses

Writing compound tactics or tacticals, e.g. terminating list iterations of theorem-tacticals.

See also

Tactical.ALL_TAC, Tactical.FAIL_TAC, Tactical.NO_TAC, Thm_cont.NO_THEN, Thm_cont.THEN_TCL, Thm_cont.ORELSE_TCL.

all_thys	(DB)
----------	------

```
all_thys : unit -> data list
```

Synopsis

All theorems, axioms, and definitions in the currently loaded theory segments.

Description

An invocation `all_thys()` returns everything that has been stored in all theory segments currently loaded.

Example

```
- length (all_thys());
> val it = 736 : int
```

See also

DB.thy, DB.theorems, DB.definitions, DB.axioms, DB.find, DB.match.

all_vars	(Term)
----------	--------

```
all_vars : term -> term list
```

Synopsis

Returns the set of all variables in a term.

Description

An invocation `all_vars tm` returns a list representing the set of all bound and free term variables occurring in `tm`.

Failure

Never fails.

Example

```
- all_vars (Term '!x y. x /\ y /\ y ==> z');
> val it = ['z', 'y', 'x'] : term list
```

Comments

Code should not depend on how elements are arranged in the result of `all_vars`.

See also

`Term.free_vars`, `Term.all_varsl`.

<code>all_varsl</code>	<code>(Term)</code>
------------------------	---------------------

```
all_varsl : term list -> term list
```

Synopsis

Returns the set of all variables in a list of terms.

Description

An invocation `all_varsl [t1, ..., tn]` returns a list representing the set of all term variables occurring in `t1, ..., tn`.

Failure

Never fails.

Example

```
- all_varsl [Term 'x /\ y /\ y ==> x',
            Term '!a. a ==> p ==> y'];
> val it = ['x', 'y', 'p', 'a'] : term list
```

Comments

Code should not depend on how elements are arranged in the result of `all_varsl`.

See also

`Term.FVL`, `Term.free_vars_lr`, `Term.free_vars`, `Term.free_varsl`, `Term.empty_varset`, `Type.type_vars`.

allowed_term_constant	(Lexis)
-----------------------	---------

```
Lexis.allowed_term_constant : string -> bool
```

Synopsis

Tests if a string has a permissible name for a term constant.

Description

When applied to a string, `allowed_term_constant` returns `true` if the string is a permissible constant name for a term, that is, if it is an identifier (see the `DESCRIPTION` for more details), and `false` otherwise.

Failure

Never fails.

Example

The following gives a sample of some allowed and disallowed constant names:

```
- map Lexis.allowed_term_constant ["pi", "@", "a name", "+++++", "10"];  
> val it = [true, true, false, true, false] : bool list
```

Comments

Note that this function only performs a lexical test; it does not check whether there is already a constant of that name in the current theory.

See also

`Theory.constants`, `Lexis.allowed_type_constant`.

allowed_type_constant	(Lexis)
-----------------------	---------

```
allowed_type_constant : string -> bool
```

Synopsis

Tests if a string has a permissible name for a type constant.

Description

When applied to a string, `allowed_type_constant` returns `true` if the string is a permissible constant name for a type operator, and `false` otherwise.

Failure

Never fails.

Example

The following gives a sample of some allowed and disallowed names for type operators:

```
- map Lexis.allowed_type_constant ["list", "'a", "fun", "->", "#", "fun2"];
> val it = [true, false, true, false, false, true] : bool list
```

Comments

Note that this function only performs a lexical test; it does not check whether there is already a type operator of that name in the current theory.

This function is not currently enforced by the system, as it was found that more flexibility in naming was preferable.

See also

`Lexis.allowed_term_constant`.

ALPHA	(Thm)
--------------	--------------

`ALPHA : term -> term -> thm`

Synopsis

Proves equality of alpha-equivalent terms.

Description

When applied to a pair of terms t_1 and t_1' which are alpha-equivalent, `ALPHA` returns the theorem $\vdash t_1 = t_1'$.

```
----- ALPHA t1 t1'
|- t1 = t1'
```

Failure

Fails unless the terms provided are alpha-equivalent.

See also

`Term.aconv`, `Drule.ALPHA_CONV`, `Drule.GEN_ALPHA_CONV`.

alpha

(Type)

alpha : hol_type

Synopsis

Common type variable.

DescriptionThe ML variable `Type.alpha` is bound to the type variable 'a.**See also**`Type.beta`, `Type.gamma`, `Type.delta`, `Type.bool`.

ALPHA_CONV

(Drule)

ALPHA_CONV : term -> conv

Synopsis

Renames the bound variable of a lambda-abstraction.

DescriptionIf x is a variable of type ty and M is an abstraction (with bound variable y of type ty and body t), then `ALPHA_CONV x M` returns the theorem:

$$\vdash (\lambda y. t) = (\lambda x'. t[x'/y])$$

where the variable $x' : ty$ is a primed variant of x chosen so as not to be free in $\lambda y. t$.**Failure**`ALPHA_CONV x tm` fails if x is not a variable, if tm is not an abstraction, or if x is a variable v and tm is a lambda abstraction $\lambda y. t$ but the types of v and y differ.**See also**`Thm.ALPHA`, `Drule.GEN_ALPHA_CONV`.

ancestry

(Theory)

```
ancestry : string -> string list
```

Synopsis

Returns the (proper) ancestry of a theory in a list.

Description

A call to `ancestry thy` returns a list of all the proper ancestors (i.e. parents, parents of parents, etc.) of the theory `thy`. The shorthand `"-"` may be used to denote the name of the current theory segment.

Failure

Fails if `thy` is not an ancestor of the current theory.

Example

```
- load "bossLib";
> val it = () : unit

- current_theory();
> val it = "scratch" : string

- ancestry "-";
> val it =
    ["one", "option", "pair", "sum", "combin", "relation", "min", "bool",
     "num", "prim_rec", "arithmetic", "numeral", "ind_type", "list"] :
    string list
```

See also

`Theory.parents`.

AND_CONV

(reduceLib)

```
AND_CONV : conv
```

Synopsis

Simplifies certain boolean conjunction expressions.

Description

If tm corresponds to one of the forms given below, where t is an arbitrary term of type `bool`, then `AND_CONV tm` returns the corresponding theorem. Note that in the last case the conjuncts need only be alpha-equivalent rather than strictly identical.

```

AND_CONV "T /\ t" = |- T /\ t = t
AND_CONV "t /\ T" = |- t /\ T = t
AND_CONV "F /\ t" = |- F /\ t = F
AND_CONV "t /\ F" = |- t /\ F = F
AND_CONV "t /\ t" = |- t /\ t = t

```

Failure

`AND_CONV tm` fails unless tm has one of the forms indicated above.

Example

```

#AND_CONV "(x = T) /\ F";;
|- (x = T) /\ F = F

#AND_CONV "T /\ (x = T)";;
|- T /\ (x = T) = (x = T)

#AND_CONV "(?x. x=T) /\ (?y. y=T)";;
|- (?x. x = T) /\ (?y. y = T) = (?x. x = T)

```

AND_EL_CONV	(listLib)
--------------------	------------------

`AND_EL_CONV` : `conv`

Synopsis

Computes by inference the result of taking the conjunction of the elements of a boolean list.

Description

For any object language list of the form `-- '[x1;x2;...;xn]' --`, where x_1, x_2, \dots, x_n are boolean expressions, the result of evaluating

AND_EL_CONV (--'AND_EL [x1;x2;...;xn]'--)

is the theorem

$|-\text{ AND_EL } [x_1;x_2;\dots;x_n] = b$

where b is either the boolean constant that denotes the conjunction of the elements of the list, or a conjunction of those x_i that are not boolean constants.

Example

- AND_EL_CONV (--'AND_EL [T;F;F;T]'--);
| - AND_EL [T;F;F;T] = F

- AND_EL_CONV (--'AND_EL [T;T;T]'--);
| - AND_EL [T;T;T] = T

- AND_EL_CONV (--'AND_EL [T;x;y]'--);
| - AND_EL [T; x; y] = x /\ y

- AND_EL_CONV (--'AND_EL [x;F;y]'--);
| - AND_EL [x; F; y] = F

Failure

AND_EL_CONV t_m fails if t_m is not of the form described above.

AND_EXISTS_CONV

(Conv)

AND_EXISTS_CONV : conv

Synopsis

Moves an existential quantification outwards through a conjunction.

Description

When applied to a term of the form $(?x.P) /\ (?x.Q)$, where x is free in neither P nor Q , AND_EXISTS_CONV returns the theorem:

$|-\ (?x. P) /\ (?x. Q) = (?x. P /\ Q)$

Failure

AND_EXISTS_CONV fails if it is applied to a term not of the form $(?x.P) \wedge (?x.Q)$, or if it is applied to a term $(?x.P) \wedge (?x.Q)$ in which the variable x is free in either P or Q .

Comments

It may be easier to use higher order rewriting with some of BOTH_EXISTS_AND_THM, LEFT_EXISTS_AND_THM, and RIGHT_EXISTS_AND_THM.

See also

Conv.EXISTS_AND_CONV, Conv.LEFT_AND_EXISTS_CONV, Conv.RIGHT_AND_EXISTS_CONV.

AND_FORALL_CONV	(Conv)
-----------------	--------

AND_FORALL_CONV : conv

Synopsis

Moves a universal quantification outwards through a conjunction.

Description

When applied to a term of the form $(!x.P) \wedge (!x.Q)$, the conversion AND_FORALL_CONV returns the theorem:

$$\vdash (!x.P) \wedge (!x.Q) = (!x. P \wedge Q)$$

Failure

Fails if applied to a term not of the form $(!x.P) \wedge (!x.Q)$.

Comments

It may be easier to use higher order rewriting with FORALL_AND_THM.

See also

Conv.FORALL_AND_CONV, Conv.LEFT_AND_FORALL_CONV, Conv.RIGHT_AND_FORALL_CONV.

AND_PEXISTS_CONV	(PairRules)
------------------	-------------

AND_PEXISTS_CONV : conv

Synopsis

Moves a paired existential quantification outwards through a conjunction.

Description

When applied to a term of the form $(?p. t) \wedge (?p. u)$, where no variables in p are free in either t or u , `AND_PEXISTS_CONV` returns the theorem:

$$\vdash (?p. t) \wedge (?p. u) = (?p. t \wedge u)$$

Failure

`AND_PEXISTS_CONV` fails if it is applied to a term not of the form $(?p. t) \wedge (?p. u)$, or if it is applied to a term $(?p. t) \wedge (?p. u)$ in which variables from p are free in either t or u .

See also

`Conv.AND_EXISTS_CONV`, `PairRules.PEXISTS_AND_CONV`,
`PairRules.LEFT_AND_PEXISTS_CONV`, `PairRules.RIGHT_AND_PEXISTS_CONV`.

AND_PFORALL_CONV	(PairRules)
-------------------------	--------------------

`AND_PFORALL_CONV` : `conv`

Synopsis

Moves a paired universal quantification outwards through a conjunction.

Description

When applied to a term of the form $(!p. t) \wedge (!p. u)$, the conversion `AND_PFORALL_CONV` returns the theorem:

$$\vdash (!p. t) \wedge (!p. u) = (!p. t \wedge u)$$

Failure

Fails if applied to a term not of the form $(!p. t) \wedge (!p. u)$.

See also

`Conv.AND_FORALL_CONV`, `PairRules.PFORALL_AND_CONV`,
`PairRules.LEFT_AND_PFORALL_CONV`, `PairRules.RIGHT_AND_PFORALL_CONV`.

ANTE_CONJ_CONV

(Conv)

ANTE_CONJ_CONV : conv

Synopsis

Eliminates a conjunctive antecedent in favour of implication.

Description

When applied to a term of the form $(t1 \wedge t2) ==> t$, the conversion ANTE_CONJ_CONV returns the theorem:

$$\vdash (t1 \wedge t2 ==> t) = (t1 ==> t2 ==> t)$$

Failure

Fails if applied to a term not of the form " $(t1 \wedge t2) ==> t$ ".

Uses

Somewhat ad-hoc, but can be used (with CONV_TAC) to transform a goal of the form $?- (P \wedge Q) ==> R$ into the subgoal $?- P ==> (Q ==> R)$, so that only the antecedent P is moved into the assumptions by DISCH_TAC.

See also

Tactic.CONV_TAC, Tactic.DISCH_TAC.

ANTE_RES_THEN

(Thm_cont)

ANTE_RES_THEN : thm_tactical

Synopsis

Resolves implicative assumptions with an antecedent.

Description

Given a theorem-tactic $ttac$ and a theorem $A \vdash t$, the function ANTE_RES_THEN produces a tactic that attempts to match t to the antecedent of each implication

$$A_i \vdash !x_1 \dots x_n. u_i ==> v_i$$

(where A_i is just $!x_1 \dots x_n. u_i \implies v_i$) that occurs among the assumptions of a goal. If the antecedent u_i of any implication matches t , then an instance of $A_i \cup A \vdash v_i$ is obtained by specialization of the variables x_1, \dots, x_n and type instantiation, followed by an application of modus ponens. Because all implicative assumptions are tried, this may result in several modus-ponens consequences of the supplied theorem and the assumptions. Tactics are produced using `ttac` from all these theorems, and these tactics are applied in sequence to the goal. That is,

```
ANTE_RES_THEN ttac (A |- t) g
```

has the effect of:

```
MAP EVERY ttac [A1 u A |- v1, ..., Am u A |- vm] g
```

where the theorems $A_i \cup A \vdash v_i$ are all the consequences that can be drawn by a (single) matching modus-ponens inference from the implications that occur among the assumptions of the goal g and the supplied theorem $A \vdash t$. Any negation $\sim v$ that appears among the assumptions of the goal is treated as an implication $v \implies F$. The sequence in which the theorems $A_i \cup A \vdash v_i$ are generated and the corresponding tactics applied is unspecified.

Failure

`ANTE_RES_THEN ttac (A |- t)` fails when applied to a goal g if any of the tactics produced by `ttac (A_i u A |- v_i)`, where $A_i \cup A \vdash v_i$ is the i th resolvent obtained from the theorem $A \vdash t$ and the assumptions of g , fails when applied in sequence to g .

Uses

Painfully detailed proof hacking.

See also

`Tactic.IMP_RES_TAC`, `Thm.cont.IMP_RES_THEN`, `Drule.MATCH_MP`, `Tactic.RES_TAC`, `Thm.cont.RES_THEN`.

<div data-bbox="237 1572 446 1621" data-label="Text"> <p>AP_TERM</p> </div>	<div data-bbox="1260 1568 1410 1621" data-label="Text"> <p>(Thm)</p> </div>
--	--

`AP_TERM : term -> thm -> thm`

Synopsis

Applies a function to both sides of an equational theorem.

Description

When applied to a term f and a theorem $A \vdash x = y$, the inference rule `AP_TERM` returns the theorem $A \vdash f x = f y$.

$$\frac{A \vdash x = y}{A \vdash f x = f y} \quad \text{AP_TERM } f$$
Failure

Fails unless the theorem is equational and the supplied term is a function whose domain type is the same as the type of both sides of the equation.

See also

Tactic.AP_TERM_TAC, Thm.AP_THM, Tactic.AP_THM_TAC, Thm.MK_COMB.

<div data-bbox="159 819 485 873" data-label="Text"> <p style="font-size: 24pt; margin: 0;">AP_TERM_TAC</p> </div>	<div data-bbox="1096 819 1331 873" data-label="Text"> <p style="font-size: 24pt; margin: 0;">(Tactic)</p> </div>
---	--

AP_TERM_TAC : tactic

Synopsis

Strips a function application from both sides of an equational goal.

Description

AP_TERM_TAC reduces a goal of the form $A \text{ ?- } f x = f y$ by stripping away the function applications, giving the new goal $A \text{ ?- } x = y$.

$$\frac{A \text{ ?- } f x = f y}{A \text{ ?- } x = y} \quad \text{AP_TERM_TAC}$$
Failure

Fails unless the goal is equational, with both sides being applications of the same function.

See also

Thm.AP_TERM, Thm.AP_THM, Tactic.AP_THM_TAC, Tactic.ABS_TAC.

<div data-bbox="159 1816 343 1872" data-label="Text"> <p style="font-size: 24pt; margin: 0;">AP_THM</p> </div>	<div data-bbox="1182 1816 1331 1872" data-label="Text"> <p style="font-size: 24pt; margin: 0;">(Thm)</p> </div>
--	---

AP_THM : thm -> term -> thm

Synopsis

Proves equality of equal functions applied to a term.

Description

When applied to a theorem $A \vdash f = g$ and a term x , the inference rule `AP_THM` returns the theorem $A \vdash f\ x = g\ x$.

$$\frac{A \vdash f = g}{A \vdash f\ x = g\ x} \quad \text{AP_THM } (A \vdash f = g)\ x$$

Failure

Fails unless the conclusion of the theorem is an equation, both sides of which are functions whose domain type is the same as that of the supplied term.

See also

`Tactic.AP_THM_TAC`, `Thm.AP_TERM`, `Drule.ETA_CONV`, `Drule.EXT`, `Conv.FUN_EQ_CONV`, `Thm.MK_COMB`.

<code>AP_THM_TAC</code>	<code>(Tactic)</code>
-------------------------	-----------------------

`AP_THM_TAC` : `tactic`

Synopsis

Strips identical operands from functions on both sides of an equation.

Description

When applied to a goal of the form $A \text{ ?- } f\ x = g\ x$, the tactic `AP_THM_TAC` strips away the operands of the function application:

$$\frac{A \text{ ?- } f\ x = g\ x}{A \text{ ?- } f = g} \quad \text{AP_THM_TAC}$$

Failure

Fails unless the goal has the above form, namely an equation both sides of which consist of function applications to the same arguments.

See also

`Thm.AP_TERM`, `Tactic.AP_TERM_TAC`, `Thm.AP_THM`, `Tactic.ABS_TAC`, `Drule.EXT`.

append

(Lib)

```
append : 'a list -> 'a list -> 'a list
```

Synopsis

Curried form of list append

Description

The function `append` is a curried form of the standard operation for appending two ML lists.

Failure

Never fails.

Example

```
- append [1] [2,3] = [1] @ [2,3];
> val it = true : bool
```

APPEND_CONV

(listLib)

```
APPEND_CONV : conv
```

Synopsis

Computes by inference the result of appending two object-language lists.

Description

For any pair of object language lists of the form `-- '[x1; ...; xn] '--` and `-- '[y1; ...; ym] '--`, the result of evaluating

```
APPEND_CONV (--'APPEND [x1;...;xn] [y1;...;ym] '--)
```

is the theorem

```
|- APPEND [x1;...;xn] [y1;...;ym] = [x1;...;xn;y1;...;ym]
```

The length of either list (or both) may be 0.

Failure

APPEND_CONV tm fails if tm is not of the form `--'APPEND l1 l2'--`, where $l1$ and $l2$ are (possibly empty) object-language lists of the forms `--'[x1;...;xn]'--` and `--'[y1;...;ym]'--`.

<div data-bbox="236 672 387 728" data-label="Text"> <p>apply</p> </div>	<div data-bbox="1203 667 1412 721" data-label="Text"> <p>(Count)</p> </div>
---	---

`apply : ('a -> 'b) -> 'a -> 'b`

Synopsis

Counts primitive inferences performed when a function is applied.

Description

The `apply` function provides a way of counting the primitive inferences that are performed when a function is applied to its argument. The reporting of the count is done when the function terminates (normally, or with an exception). The reporting also includes timing information about the function call.

Example

```
- Count.apply (CONJUNCTS o SPEC_ALL) AND_CLAUSES;
runtime: 0.000s,    gctime: 0.000s,    systime: 0.000s.
Axioms asserted: 0.
Definitions made: 0.
Oracle invocations: 0.
Theorems loaded from disk: 0.
HOL primitive inference steps: 9.
Total: 9.
> val it =
  [|- T /\ t = t, |- t /\ T = t, |- F /\ t = F, |- t /\ F = F,
   |- t /\ t = t] : thm list
```

Failure

The call to `apply f x` will raise an exception if `f x` would. It will still report elapsed time and inference counts up to the point of the exception being raised.

See also

Count.thm_count.

apropos

(DB)

apropos : term -> data list

Synopsis

Attempt to find matching theorems in the currently loaded theories.

Description

An invocation `DB.apropos M` collects all theorems, definitions, and axioms of the currently loaded theories that have a subterm that matches `M`. If there are no matches, the empty list is returned.

Failure

Never fails.

Example

```
- DB.apropos (Term '(!x y. P x y) ==> Q');
<<HOL message: inventing new type variable names: 'a, 'b>>
> val it =
  [(("ind_type", "INJ_INVERSE2"),
    (|- !P.
      (!x1 y1 x2 y2. (P x1 y1 = P x2 y2) = (x1 = x2) /\ (y1 = y2)) ==>
      ?X Y. !x y. (X (P x y) = x) /\ (Y (P x y) = y), Thm)),
   ("pair", "pair_induction"),
   (|- (!p_1 p_2. P (p_1,p_2)) ==> !p. P p, Thm))] :
  ((string * string) * (thm * class)) list
```

Comments

The notion of matching is a restricted version of higher-order matching.

For finer control over the theories searched, use `DB.match`.

See also

DB.match, DB.find.

arb

(boolSyntax)

arb : term

Synopsis

Constant denoting arbitrary items.

DescriptionThe ML variable `boolSyntax.arb` is bound to the term `bool$ARB`.**See also**

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`, `boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.bool_case`.

ARITH_CONV

(numLib)

ARITH_CONV : conv

Synopsis

Partial decision procedure for a subset of linear natural number arithmetic.

Description

ARITH_CONV is a partial decision procedure for Presburger natural arithmetic. Presburger natural arithmetic is the subset of arithmetic formulae made up from natural number constants, numeric variables, addition, multiplication by a constant, the relations $<$, $<=$, $=$, $>=$, $>$ and the logical connectives \sim , \wedge , \vee , \implies , $=$ (if-and-only-if), $!$ ('forall') and $?$ ('there exists'). Products of two expressions which both contain variables are not included in the subset, but the functions `SUC` and `PRE` which are not normally included in a specification of Presburger arithmetic are allowed in this HOL implementation.

ARITH_CONV further restricts the subset as follows: when the formula has been put in prenex normal form it must contain only one kind of quantifier, that is the quantifiers must either all be universal ('forall') or all existential. Variables may appear free (unquantified) provided any quantifiers that do appear in the prenex normal form are universal; free variables are taken as being implicitly universally quantified so mixing them with existential quantifiers would violate the above restriction.

Given a formula in the permitted subset, ARITH_CONV attempts to prove that it is equal to T (true). For universally quantified formulae the procedure only works if the formula would also be true of the non-negative rationals; it cannot prove formulae whose truth depends on the integral properties of the natural numbers. The procedure is also incomplete for existentially quantified formulae, but in this case there is no rule-of-thumb for determining whether the procedure will work.

The function features a number of preprocessors which extend the coverage beyond the subset specified above. In particular, natural number subtraction and conditional statements are allowed. Another permits substitution instances of universally quantified formulae to be accepted. Note that Boolean-valued variables are not allowed.

Failure

The function can fail in two ways. It fails if the argument term is not a formula in the specified subset, and it also fails if it is unable to prove the formula. The failure strings are different in each case. However, the function may announce that it is unable to prove a formula that one would expect it to reject as being outside the subset. This is due to it looking for substitution instances; it has generalised the formula so that the new formula is in the subset but is not valid.

Example

A simple example containing a free variable:

```
- ARITH_CONV ‘‘m < SUC m’’;
> val it = |- m < (SUC m) = T : thm
```

A more complex example with subtraction and universal quantifiers, and which is not initially in prenex normal form:

```
#ARITH_CONV
# "!m p. p < m ==> !q r. (m < (p + q) + r) ==> ((m - p) < q + r)";;
|- (!m p. p < m ==> (!q r. m < ((p + q) + r) ==> (m - p) < (q + r))) = T
```

Two examples with existential quantifiers:

```
#ARITH_CONV "?m n. m < n";;
|- (?m n. m < n) = T

#ARITH_CONV "?m n. (2 * m) + (3 * n) = 10";;
|- (?m n. (2 * m) + (3 * n) = 10) = T
```

An instance of a universally quantified formula involving a conditional statement and subtraction:

```
#ARITH_CONV
# " $((p + 3) \leq n) \implies (!m. ((m \text{ EXP } 2 = 0) \implies (n - 1) \mid (n - 2)) > p)$ ";;
|-  $(p + 3) \leq n \implies (!m. ((m \text{ EXP } 2 = 0) \implies n - 1 \mid n - 2) > p) = T$ 
```

Failure due to mixing quantifiers:

```
#ARITH_CONV "!m. ?n. m < n";;
evaluation failed      ARITH_CONV -- formula not in the allowed subset
```

Failure because the truth of the formula relies on the fact that the variables cannot have fractional values:

```
#ARITH_CONV "!m n. ~(SUC (2 * m) = 2 * n)";;
evaluation failed      ARITH_CONV -- cannot prove formula
```

See also

Arith.NEGATE_CONV, Arith.EXISTS_ARITH_CONV, Arith.FORALL_ARITH_CONV,
Arith.INSTANCE_T_CONV, Arith.PRENEX_CONV, Arith.SUB_AND_COND_ELIM_CONV.

ARITH_FORM_NORM_CONV	(Arith)
-----------------------------	----------------

ARITH_FORM_NORM_CONV : conv

Synopsis

Normalises an unquantified formula of linear natural number arithmetic.

Description

ARITH_FORM_NORM_CONV converts a formula of natural number arithmetic into a disjunction of conjunctions of less-than-or-equal-to inequalities. The arithmetic expressions are only allowed to contain natural number constants, numeric variables, addition, the SUC function, and multiplication by a constant. The formula must not contain quantifiers, but may have disjunction, conjunction, negation, implication, equality on Booleans (if-and-only-if), and the natural number relations: $<$, \leq , $=$, \geq , $>$. The formula must not contain products of two expressions which both contain variables.

The inequalities in the result are normalised so that each variable appears on only one side of the inequality, and each side is a linear sum in which any constant appears first followed by products of a constant and a variable. The variables are ordered lexicographically, and if the coefficient of the variable is 1, the product of 1 and the variable appears in the term rather than the variable on its own.

Failure

The function fails if the argument term is not a formula in the specified subset.

Example

```
#ARITH_FORM_NORM_CONV "m < n";;
|- m < n = (1 + (1 * m)) <= (1 * n)

#ARITH_FORM_NORM_CONV
# "(n < 4) ==> ((n = 0) \\/ (n = 1) \\/ (n = 2) \\/ (n = 3))";;
|- n < 4 ==> (n = 0) \\/ (n = 1) \\/ (n = 2) \\/ (n = 3) =
  4 <= (1 * n) \\/
  (1 * n) <= 0 /\ 0 <= (1 * n) \\/
  (1 * n) <= 1 /\ 1 <= (1 * n) \\/
  (1 * n) <= 2 /\ 2 <= (1 * n) \\/
  (1 * n) <= 3 /\ 3 <= (1 * n)
```

Uses

Useful in constructing decision procedures for linear arithmetic.

arith_ss**(bossLib)**

arith_ss : simpset

Synopsis

Simplification set for arithmetic.

Description

The simplification set `arith_ss` is a version of `std_ss` enhanced for arithmetic. It includes many arithmetic rewrites, an evaluation mechanism for ground arithmetic terms, and a decision procedure for linear arithmetic. It also incorporates a cache of successfully solved conditions proved when conditional rewrite rules are successfully applied.

The following rewrites are currently used to augment those already present from `std_ss`:

```
|- !m n. (m * n = 0) = (m = 0) \\/ (n = 0)
|- !m n. (0 = m * n) = (m = 0) \\/ (n = 0)
|- !m n. (m + n = 0) = (m = 0) /\ (n = 0)
```

```

|- !m n. (0 = m + n) = (m = 0) /\ (n = 0)
|- !x y. (x * y = 1) = (x = 1) /\ (y = 1)
|- !x y. (1 = x * y) = (x = 1) /\ (y = 1)
|- !m. m * 0 = 0
|- !m. 0 * m = 0
|- !x y. (x * y = SUC 0) = (x = SUC 0) /\ (y = SUC 0)
|- !x y. (SUC 0 = x * y) = (x = SUC 0) /\ (y = SUC 0)
|- !m. m * 1 = m
|- !m. 1 * m = m
|- !x. ((SUC x = 1) = (x = 0)) /\ ((1 = SUC x) = (x = 0))
|- !x. ((SUC x = 2) = (x = 1)) /\ ((2 = SUC x) = (x = 1))
|- !m n. (m + n = m) = (n = 0)
|- !m n. (n + m = m) = (n = 0)
|- !c. c - c = 0
|- !m. SUC m - 1 = m
|- !m. (0 - m = 0) /\ (m - 0 = m)
|- !a c. a + c - c = a
|- !m n. (m - n = 0) = m <= n
|- !m n. (0 = m - n) = m <= n
|- !n m. n - m <= n
|- !n m. SUC n - SUC m = n - m
|- !m n p. m - n > p = m > n + p
|- !m n p. m - n < p = m < n + p /\ 0 < p
|- !m n p. m - n >= p = m >= n + p \/ 0 >= p
|- !m n p. m - n <= p = m <= n + p
|- !n. n <= 0 = (n = 0)
|- !m n p. m + p < n + p = m < n
|- !m n p. p + m < p + n = m < n
|- !m n p. m + n <= m + p = n <= p
|- !m n p. n + m <= p + m = n <= p
|- !m n p. (m + p = n + p) = (m = n)
|- !m n p. (p + m = p + n) = (m = n)
|- !x y w. x + y < w + x = y < w
|- !x y w. y + x < x + w = y < w
|- !m n. (SUC m = SUC n) = (m = n)
|- !m n. SUC m < SUC n = m < n
|- !n m. SUC n <= SUC m = n <= m
|- !m i n. SUC n * m < SUC n * i = m < i
|- !p m n. (n * SUC p = m * SUC p) = (n = m)
|- !m i n. (SUC n * m = SUC n * i) = (m = i)

```

```

|- !n m. ~(SUC n <= m) = m <= n
|- !p q n m. (n * SUC q ** p = m * SUC q ** p) = (n = m)
|- !m n. ~(SUC n ** m = 0)
|- !n m. ~(SUC (n + n) = m + m)
|- !m n. ~(SUC (m + n) <= m)
|- !n. ~(SUC n <= 0)
|- !n. ~(n < 0)
|- !n. (MIN n 0 = 0) /\ (MIN 0 n = 0)
|- !n. (MAX n 0 = n) /\ (MAX 0 n = n)
|- !n. MIN n n = n
|- !n. MAX n n = n
|- !n m. MIN m n <= m /\ MIN m n <= n
|- !n m. m <= MAX m n /\ n <= MAX m n
|- !n m. (MIN m n < m = ~(m = n) /\ (MIN m n = n)) /\
          (MIN m n < n = ~(m = n) /\ (MIN m n = m)) /\
          (m < MIN m n = F) /\ (n < MIN m n = F)
|- !n m. (m < MAX m n = ~(m = n) /\ (MAX m n = n)) /\
          (n < MAX m n = ~(m = n) /\ (MAX m n = m)) /\
          (MAX m n < m = F) /\ (MAX m n < n = F)
|- !m n. (MIN m n = MAX m n) = (m = n)
|- !m n. MIN m n < MAX m n = ~(m = n)

```

The decision procedure proves valid purely universal formulas constructed using variables and the operators `SUC`, `PRE`, `+`, `-`, `<`, `>`, `<=`, `>=`. Multiplication by constants is accommodated by translation to repeated addition. An attempt is made to generalize subformulas of type `num` not fitting into this syntax.

Comments

The philosophy behind this simpset is fairly conservative. For example, some potential rewrite rules, e.g., the recursive clauses for addition and multiplication, are not included, since it was felt that their incorporation too often resulted in formulas becoming more complex rather than simpler. Also, transitivity theorems are avoided because they tend to make simplification diverge.

See also

`BasicProvers.RW_TAC`, `BasicProvers.SRW_TAC`, `simpLib.SIMP_TAC`, `simpLib.SIMP_CONV`, `simpLib.SIMP_RULE`, `BasicProvers.bool_ss`, `bossLib.std_ss`, `bossLib.list_ss`.

ASM_CASES_TAC	(Tactic)
----------------------	-----------------

ASM_CASES_TAC : term -> tactic

Synopsis

Given a term, produces a case split based on whether or not that term is true.

Description

Given a term u , ASM_CASES_TAC applied to a goal produces two subgoals, one with u as an assumption and one with $\sim u$:

$$\frac{A \text{ ?- } t}{\text{===== ASM_CASES_TAC } u} A \text{ u } \{u\} \text{ ?- } t \quad A \text{ u } \{\sim u\} \text{ ?- } t$$

ASM_CASES_TAC u is implemented by DISJ_CASES_TAC(SPEC u EXCLUDED_MIDDLE), where EXCLUDED_MIDDLE is the axiom $\vdash !u. u \ \backslash / \ \sim u$.

Failure

By virtue of the implementation (see above), the decomposition fails if EXCLUDED_MIDDLE cannot be instantiated to u , e.g. if u does not have boolean type.

Example

The tactic ASM_CASES_TAC u can be used to produce a case analysis on u :

```
- let val u = Term 'u:bool'
      val g = Term '(P:bool -> bool) u'
  in
    ASM_CASES_TAC u ([],g)
  end;

  ([[ ['u'], 'P u'],
    [['~u'], 'P u']], fn) : tactic_result
```

Uses

Performing a case analysis according to whether a given term is true or false.

See also

Tactic.BOOL_CASES_TAC, Tactic.COND_CASES_TAC, Tactic.DISJ_CASES_TAC, Thm.SPEC, Tactic.STRUCT_CASES_TAC, BasicProvers.Cases, bossLib.Cases_on.

ASM_MESON_TAC	(mesonLib)
----------------------	-------------------

ASM_MESON_TAC : thm list -> tactic

Synopsis

Performs first order proof search to prove the goal, using the assumptions and the theorems given.

Description

ASM_MESON_TAC is identical in behaviour to MESON_TAC except that it uses the assumptions of a goal as well as the provided theorems.

Failure

ASM_MESON_TAC fails if it can not find a proof of the goal with depth less than or equal to the mesonLib.max_depth value.

See also

mesonLib.GEN_MESON_TAC, mesonLib.MESON_TAC.

ASM_REWRITE_RULE	(Rewrite)
-------------------------	------------------

ASM_REWRITE_RULE : thm list -> thm -> thm

Synopsis

Rewrites a theorem including built-in rewrites and the theorem's assumptions.

Description

ASM_REWRITE_RULE rewrites using the tautologies in basic_rewrites, the given list of theorems, and the set of hypotheses of the theorem. All hypotheses are used. No ordering is specified among applicable rewrites. Matching subterms are searched for recursively, starting with the entire term of the conclusion and stopping when no rewritable expressions remain. For more details about the rewriting process, see GEN_REWRITE_RULE. To avoid using the set of basic tautologies, see PURE_ASM_REWRITE_RULE.

Failure

ASM_REWRITE_RULE does not fail, but may result in divergence. To prevent divergence where it would occur, ONCE_ASM_REWRITE_RULE can be used.

See also

Rewrite.GEN_REWRITE_RULE, Rewrite.ONCE_ASM_REWRITE_RULE,
 Rewrite.PURE_ASM_REWRITE_RULE, Rewrite.PURE_ONCE_ASM_REWRITE_RULE,
 Rewrite.REWRITE_RULE.

ASM_REWRITE_TAC	(Rewrite)
------------------------	------------------

```
ASM_REWRITE_TAC : thm list -> tactic
```

Synopsis

Rewrites a goal using built-in rewrites and the goal's assumptions.

Description

ASM_REWRITE_TAC generates rewrites with the tautologies in `basic_rewrites`, the set of assumptions, and a list of theorems supplied by the user. These are applied top-down and recursively on the goal, until no more matches are found. The order in which the set of rewrite equations is applied is an implementation matter and the user should not depend on any ordering. Rewriting strategies are described in more detail under `GEN_REWRITE_TAC`. For omitting the common tautologies, see the tactic `PURE_ASM_REWRITE_TAC`. To rewrite with only a subset of the assumptions use `FILTER_ASM_REWRITE_TAC`.

Failure

ASM_REWRITE_TAC does not fail, but it can diverge in certain situations. For rewriting to a limited depth, see `ONCE_ASM_REWRITE_TAC`. The resulting tactic may not be valid if the applicable replacement introduces new assumptions into the theorem eventually proved.

Example

The use of assumptions in rewriting, specially when they are not in an obvious equational form, is illustrated below:

```
- let val asm = [Term 'P x']
      val goal = Term 'P x = Q x'
      in
      ASM_REWRITE_TAC[] (asm, goal)
      end;

val it = ([[('P x'), ('Q x')], fn) : tactic_result
```

```

- let val asm = [Term '~P x']
      val goal = Term 'P x = Q x'
      in
      ASM_REWRITE_TAC[] (asm, goal)
      end;

val it = ([[('~P x'], '~Q x')], fn) : tactic_result

```

See also

Rewrite.FILTER_ASM_REWRITE_TAC, Rewrite.FILTER_ONCE_ASM_REWRITE_TAC,
 Rewrite.GEN_REWRITE_TAC, Rewrite.ONCE_ASM_REWRITE_TAC, Rewrite.ONCE_REWRITE_TAC,
 Rewrite.PURE_ASM_REWRITE_TAC, Rewrite.PURE_ONCE_ASM_REWRITE_TAC,
 Rewrite.PURE_REWRITE_TAC, Rewrite.REWRITE_TAC, Tactic.SUBST_TAC.

ASM_SIMP_RULE	(simpLib)
----------------------	------------------

ASM_SIMP_RULE : simpset -> thm list -> thm -> thm

Synopsis

Simplifies a theorem, using the theorem's assumptions as rewrites in addition to the provided rewrite theorems and simpset.

Failure

Never fails, but may diverge.

Example

```

- ASM_SIMP_RULE bool_ss [] (ASSUME (Term 'x = 3'))
> val it = [...] |- T : thm

```

Uses

The assumptions can be used to simplify the conclusion of the theorem. For example, if the conclusion of a theorem is an implication, the antecedent together with the hypotheses may help simplify the conclusion.

See also

simpLib.SIMP_CONV, simpLib.SIMP_RULE.

ASM_SIMP_TAC	(bossLib)
---------------------	------------------

```
ASM_SIMP_TAC : simpset -> thm list -> tactic
```

Synopsis

Simplifies a goal using the simpset, the provided theorems, and the goal's assumptions.

Description

ASM_SIMP_TAC does a simplification of the goal, adding both the assumptions and the provided theorem to the given simpset as rewrites. This simpset is then applied to the goal in the manner explained in the entry for SIMP_CONV.

ASM_SIMP_TAC is to SIMP_TAC, as ASM_REWRITE_TAC is to REWRITE_TAC.

Failure

ASM_SIMP_TAC never fails, though it may diverge.

Example

The simple goal $x < y \text{ ?- } x + y < y + y$ can be proved by using `bossLib.arith_ss` and the assumption by

```
ASM_SIMP_TAC bossLib.arith_ss []
```

See also

`bossLib.++`, `bossLib.bool_ss`, `bossLib.FULL_SIMP_TAC`, `simpLib.mk_simpset`, `bossLib.SIMP_CONV`, `bossLib.SIMP_TAC`.

ASM_SIMP_TAC	(simpLib)
---------------------	------------------

```
ASM_SIMP_TAC : simpset -> thm list -> tactic
```

Synopsis

Simplify a term with the given simpset and theorems.

Description

`bossLib.ASM_SIMP_TAC` is identical to `simpLib.ASM_SIMP_TAC`.

See also`bossLib.ASM_SIMP_TAC.`**assert****(Lib)**`assert : ('a -> bool) -> 'a -> 'a`**Synopsis**

Checks that a value satisfies a predicate.

Description

`assert p x` returns `x` if the application `p x` yields `true`. Otherwise, `assert p x` fails.

Failure

`assert p x` fails with exception `HOL_ERR` if the predicate `p` yields `false` when applied to the value `x`. If the application `p x` raises an exception `e`, then `assert p x` raises `e`.

Example

```
- null [];  
> val it = true : bool  
  
- assert null ([]:int list);  
> val it = [] : int list  
  
- null [1];  
> false : bool  
  
- assert null [1];  
! Uncaught exception:  
! HOL_ERR <poly>
```

See also`Lib.can`, `Lib.assert_exn`.**assert_exn****(Lib)**`assert_exn : ('a -> bool) -> 'a -> exn -> 'a`

Synopsis

Checks that a value satisfies a predicate.

Description

`assert_exn p x e` returns `x` if the application `p x` evaluates to `true`. Otherwise, `assert_exn p x e` raises `e`

Failure

`assert_exn p x e` fails with exception `e` if the predicate `p` yields `false` when applied to the value `x`. If the application `p x` raises an exception `ex`, then `assert_exn p x e` raises `ex`.

Example

```

- null [];
> val it = true : bool

- assert_exn null ([]:int list) (Fail "non-empty list");
> val it = [] : int list

- null [1];
> false : bool

- assert_exn null [1] (Fail "non-empty list");;
! Uncaught exception:
! Fail "non-empty list"

```

See also

`Lib.can`, `Lib.assert`.

`assoc`

(`hol88Lib`)

```
assoc : 'a -> ('a * 'b) list -> 'a * 'b
```

Synopsis

Searches a list of pairs for a pair whose first component equals a specified value.

Description

`assoc x [(x1,y1), ..., (xn,yn)]` returns the first (x_i, y_i) in the list such that x_i equals x . The lookup is done on an eqtype, i.e., the SML implementation must be able to decide equality for the type of x .

Failure

Fails if no matching pair is found. This will always be the case if the list is empty.

Example

```
- assoc 2 [(1,4), (3,2), (2,5), (2,6)];  
(2, 5) : (int * int)
```

Comments

Superseded by `Lib.assoc` and `Lib.assoc1`.

See also

`hol88Lib.rev_assoc`, `Lib.assoc`, `Lib.assoc1`.

<code>assoc</code>	<code>(Lib)</code>
--------------------	--------------------

```
assoc : 'a -> ('a * 'b) list -> 'b
```

Synopsis

Searches a list of pairs for a pair whose first component equals a specified value, then returns the second component of the pair.

Description

`assoc x [(x1,y1), ..., (xn,yn)]` locates the first (x_i, y_i) in a left-to-right scan of the list such that x_i equals x . Then y_i is returned. The lookup is done on an eqtype, i.e., the SML implementation must be able to decide equality for the type of x .

Failure

Fails if no matching pair is found. This will always be the case if the list is empty.

Example

```
- assoc 2 [(1,4), (3,2), (2,5), (2,6)];  
> val it = 5 : int
```

See also

Lib.assoc1, Lib.assoc2, Lib.rev_assoc, Lib.mem, Lib.tryfind, Lib.exists,
Lib.all.

assoc1	(Lib)
--------	-------

```
assoc1 : 'a -> ('a * 'b) list -> ('a * 'b)option
```

Synopsis

Searches a list of pairs for a pair whose first component equals a specified value.

Description

assoc1 x [(x1,y1), ..., (xn,yn)] returns SOME (xi,yi) for the first pair (xi,yi) in the list such that xi equals x. Otherwise, NONE is returned. The lookup is done on an eqtype, i.e., the SML implementation must be able to decide equality for the type of x.

Failure

Never fails.

Example

```
- assoc1 2 [(1,4), (3,2), (2,5), (2,6)];
> val it = SOME (2, 5) : (int * int)option
```

See also

Lib.assoc, Lib.assoc2, Lib.rev_assoc, Lib.mem, Lib.tryfind, Lib.exists,
Lib.all.

assoc2	(Lib)
--------	-------

```
assoc2 : 'a -> ('b * 'a) list -> ('b * 'a)option
```

Synopsis

Searches a list of pairs for a pair whose second component equals a specified value.

Description

An invocation `assoc2 y [(x1,y1),..., (xn,yn)]` returns `SOME (xi,yi)` for the first `(xi,yi)` in the list such that `yi` equals `y`. Otherwise, `NONE` is returned. The lookup is done on an `eqtype`, i.e., the SML implementation must be able to decide equality for the type of `y`.

Failure

Never fails.

Example

```
- assoc2 2 [(1,4), (3,2), (2,5), (2,6)];
> val it = SOME (3, 2) : (int * int) option
```

See also

`Lib.assoc`, `Lib.assoc1`, `Lib.rev_assoc`, `Lib.mem`, `Lib.tryfind`, `Lib.exists`, `Lib.all`.

associate_restriction

(Parse)

```
associate_restriction : (string * string) -> unit
```

Synopsis

Associates a restriction semantics with a binder.

Description

If `B` is a binder and `RES_B` a constant then

```
associate_restriction("B", "RES_B")
```

will cause the parser and pretty-printer to support:

```

          ----- parse ----->
Bv::P. B                               RES_B P (\v. B)
<----- print -----
```

Anything can be written between the binder and `::` that could be written between the binder and `.` in the old notation. See the examples below.

The following associations are predefined:

```

\ v :: P. B    <----> RES_ABSTRACT P (\ v. B)
! v :: P. B    <----> RES_FORALL   P (\ v. B)
? v :: P. B    <----> RES_EXISTS   P (\ v. B)
@ v :: P. B    <----> RES_SELECT   P (\ v. B)

```

Where the constants RES_FORALL, RES_EXISTS and RES_SELECT are defined in the theory `bool`, such that :

```

|- RES_FORALL P B    = !x:'a. P x ==> B x

|- RES_EXISTS P B    = ?x:'a. P x /\ B x

|- RES_SELECT P B    = @x:'a. P x /\ B x

```

The constant RES_ABSTRACT has the following characterisation

```

|- (!p m x. x IN p ==> (RES_ABSTRACT p m x = m x)) /\
  !p m1 m2.
  (!x. x IN p ==> (m1 x = m2 x)) ==>
  (RES_ABSTRACT p m1 = RES_ABSTRACT p m2)

```

Failure

Never fails.

Example

```

- new_binder_definition("DURING", ``DURING(p:num#num->bool) = $!p``);
> val it = |- !p. $DURING p = $! p : thm

- ``DURING x::(m,n). p x``;
<<HOL warning: parse_term.parse_term: on line 2, characters 4-23:
parse_term: No restricted quantifier associated with DURING>>

[...]

- new_definition("RES_DURING",
  ``RES_DURING(m,n)p = !x. m<=x /\ x<=n ==> p x``);
> val it = |- !m n p. RES_DURING (m,n) p = !x. m <= x /\ x <= n ==> p x : thm

- associate_restriction("DURING","RES_DURING");
> val it = () : unit

```

```

- ‘‘DURING x::(m,n). p x‘‘;
> val it = ‘‘DURING x::(m,n). p x‘‘ : term

- dest_comb it;
> val it = (‘‘RES_DURING (m,n)‘‘, ‘‘\x. p x‘‘) : term * term

```

ASSUM_LIST	(Tactical)
-------------------	-------------------

```
ASSUM_LIST : (thm list -> tactic) -> tactic
```

Synopsis

Applies a tactic generated from the goal's assumption list.

Description

When applied to a function of type `thm list -> tactic` and a goal, `ASSUM_LIST` constructs a tactic by applying `f` to a list of `ASSUMED` assumptions of the goal, then applies that tactic to the goal.

$$\text{ASSUM_LIST } f \text{ } (\{A_1, \dots, A_n\} \text{ ?- } t)$$

$$= f [A_1 \text{ |- } A_1, \dots, A_n \text{ |- } A_n] (\{A_1, \dots, A_n\} \text{ ?- } t)$$

Failure

Fails if the function fails when applied to the list of `ASSUMED` assumptions, or if the resulting tactic fails when applied to the goal.

Comments

There is nothing magical about `ASSUM_LIST`: the same effect can usually be achieved just as conveniently by using `ASSUME a` wherever the assumption `a` is needed. If `ASSUM_LIST` is used, it is extremely unwise to use a function which selects elements from its argument list by number, since the ordering of assumptions should not be relied on.

Example

The tactic:

```
ASSUM_LIST SUBST_TAC
```

makes a single parallel substitution using all the assumptions, which can be useful if the rewriting tactics are too blunt for the required task.

Uses

Making more careful use of the assumption list than simply rewriting or using resolution.

See also

Rewrite.ASM_REWRITE_TAC, Tactical.EVERY_ASSUM, Tactic.IMP_RES_TAC, Tactical.POP_ASSUM, Tactical.POP_ASSUM_LIST, Rewrite.REWRITE_TAC.

<div data-bbox="236 792 418 842" data-label="Text"> <h2 style="margin: 0;">ASSUME</h2> </div>	<div data-bbox="1260 792 1414 844" data-label="Text"> (Thm) </div>
---	---

ASSUME : term -> thm

Synopsis

Introduces an assumption.

Description

When applied to a term t , which must have type `bool`, the inference rule `ASSUME` returns the theorem $t \mid\!-\! t$.

$$\frac{}{t \mid\!-\! t} \text{ ASSUME } t$$

Failure

Fails unless the term t has type `bool`.

See also

Drule.ADD_ASSUM, Thm.REFL.

<div data-bbox="236 1706 531 1758" data-label="Text"> <h2 style="margin: 0;">ASSUME_TAC</h2> </div>	<div data-bbox="1173 1706 1414 1758" data-label="Text"> (Tactic) </div>
---	--

ASSUME_TAC : thm_tactic

Synopsis

Adds an assumption to a goal.

Description

Given a theorem th of the form $A' \vdash u$, and a goal, `ASSUME_TAC th` adds u to the assumptions of the goal.

$$\begin{array}{l} A \text{ ?- } t \\ \hline \text{ASSUME_TAC } (A' \text{ } \vdash \text{ } u) \\ A \text{ } u \{u\} \text{ ?- } t \end{array}$$

Note that unless A' is a subset of A , this tactic is invalid.

Failure

Never fails.

Example

Given a goal g of the form $\{x = y, y = z\} \text{ ?- } P$, where x, y and z have type $: 'a$, the theorem $x = y, y = z \vdash x = z$ can, first, be inferred by forward proof

```
let val eq1 = Term '(x:'a) = y'
    val eq2 = Term '(y:'a) = z'
in
TRANS (ASSUME eq1) (ASSUME eq2)
end;
```

and then added to the assumptions. This process requires the explicit text of the assumptions, as well as invocation of the rule `ASSUME`:

```
let val eq1 = Term '(x:'a) = y'
    val eq2 = Term '(y:'a) = z'
    val goal = ([eq1,eq2],Parse.Term 'P:bool')
in
ASSUME_TAC (TRANS (ASSUME eq1) (ASSUME eq2)) goal
end;
```

```
val it = ([[('x = z', 'x = y', 'y = z'], 'P')], fn) : tactic_result
```

This is the naive way of manipulating assumptions; there are more advanced proof styles (more elegant and less transparent) that achieve the same effect, but this is a perfectly correct technique in itself.

Alternatively, the axiom `EQ_TRANS` could be added to the assumptions of g :

```
let val eq1 = Term '(x:'a) = y'
    val eq2 = Term '(y:'a) = z'
    val goal = ([eq1,eq2], Term 'P:bool')
```

```

in
ASSUME_TAC EQ_TRANS goal
end;

val it =
  ([[(!x y z. (x = y) /\ (y = z) ==> (x = z)’,
    ‘x = y’, ‘y = z’], ‘P’)], fn) : tactic_result

```

A subsequent resolution (see RES_TAC) would then be able to add the assumption $x = z$ to the subgoal shown above. (Aside from purposes of example, it would be more usual to use IMP_RES_TAC than ASSUME_TAC followed by RES_TAC in this context.)

Uses

ASSUME_TAC is the naive way of manipulating assumptions (i.e. without recourse to advanced tacticals); and it is useful for enriching the assumption list with lemmas as a prelude to resolution (RES_TAC, IMP_RES_TAC), rewriting with assumptions (ASM_REWRITE_TAC and so on), and other operations involving assumptions.

See also

Tactic.ACCEPT_TAC, Tactic.IMP_RES_TAC, Tactic.RES_TAC, Tactic.STRIP_ASSUME_TAC.

<div style="display: flex; justify-content: space-between;"> augment_srw_ss (BasicProvers) </div>

```
augment_srw_ss : ssfrag list -> unit
```

Synopsis

Augments the "stateful" simpset used by SRW_TAC with a list of simpset fragments.

Description

bossLib.augment_srw_ss is identical to BasicProvers.augment_srw_ss

See also

bossLib.augment_srw_ss, BasicProvers.diminish_srw_ss.

<div style="display: flex; justify-content: space-between;"> augment_srw_ss (bossLib) </div>
--

```
bossLib.augment_srw_ss : simplib.ssfrag list -> unit
```

Synopsis

Augments the “stateful rewriter” with a list of `simpset` fragments.

Description

A call to `augment_srw_ss slist` causes each element of `slist` to be merged into the `simpset` value that the system maintains “behind” `srw_ss()`.

Failure

Never fails.

Comments

The change to the `srw_ss()` `simpset` brought about with `augment_srw_ss` is not exported with a theory, so it is not “permanent”. But see `export_rewrites` for a simple way to achieve a sort of permanence.

See also

`BasicProvers.export_rewrites`, `bossLib.srw_ss`, `bossLib.SRW_TAC`.

<div data-bbox="161 1039 339 1084" data-label="Text"> <p>axioms</p> </div>	<div data-bbox="1212 1034 1331 1086" data-label="Text"> <p>(DB)</p> </div>
--	--

```
axioms : string -> (string * thm) list
```

Synopsis

All the axioms stored in the named theory.

Description

An invocation `axioms thy`, where `thy` is the name of a currently loaded theory segment, will return a list of the axioms stored in that theory. Each theorem is paired with its name in the result. The string “-” may be used to denote the current theory segment.

Failure

Never fails. If `thy` is not the name of a currently loaded theory segment, the empty list is returned.

Example

```
- axioms "bool";
> val it =
  [("INFINITY_AX", |- ?f. ONE_ONE f /\ ~ONTO f),
   ("SELECT_AX", |- !P x. P x ==> P ($@ P)),
   ("ETA_AX", |- !t. (\x. t x) = t),
   ("BOOL_CASES_AX", |- !t. (t = T) \\/ (t = F))] : (string * thm) list
```

See also

DB.thy, DB.fetch, DB.thms, DB.theorems, DB.definitions, DB.listDB.

<div data-bbox="236 517 416 564" data-label="Text"> <p>axioms</p> </div>	<div data-bbox="1173 512 1414 571" data-label="Text"> <p>(Theory)</p> </div>
--	--

```
axioms : unit -> (string * thm) list
```

Synopsis

Returns the axioms of the current theory.

Description

A call `axioms ()` returns the axioms of the current theory segment together with their names. The names are those given to the axioms by the user when they were originally added to the theory segment (by a call to `new_axiom`).

Failure

Never fails.

See also

Theory.axiom, Theory.definitions, Theory.theorems, Theory.new_axiom.

<div data-bbox="236 1438 276 1482" data-label="Text"> <p>B</p> </div>	<div data-bbox="1260 1433 1414 1487" data-label="Text"> <p>(Lib)</p> </div>
---	---

```
B : ('a -> 'b) -> ('c -> 'a) -> 'c -> 'b
```

Synopsis

Performs curried function-composition: $B\ f\ g\ x = f\ (g\ x)$.

Failure

Never fails.

See also

Lib, Lib.##, Lib.A, Lib.C, Lib.I, Lib.K, Lib.S, Lib.W.

b

(proofManagerLib)

```
b : unit -> proof
```

Synopsis

Restores the proof state undoing the effects of a previous expansion.

Description

The function `b` is part of the subgoal package. It is an abbreviation for the function `backup`. For a description of the subgoal package, see `set_goal`.

Failure

As for `backup`.

Uses

Back tracking in a goal-directed proof to undo errors or try different tactics.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`, `proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`, `proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`, `proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

backup

(proofManagerLib)

```
backup : unit -> proof
```

Synopsis

Restores the proof state, undoing the effects of a previous expansion.

Description

The function `backup` is part of the subgoal package. It may be abbreviated by the function `b`. It allows backing up from the last state change (caused by calls to `expand`, `rotate` and similar functions). The package maintains a backup list of previous proof states. A call to `backup` restores the state to the previous state (which was on top of the backup list). The current state and the state on top of the backup list are discarded. The maximum number of proof states saved on the backup list can be set using `set_backup`. It

defaults to 15. Adding new proof states after the maximum is reached causes the earliest proof state on the list to be discarded. The user may backup repeatedly until the list is exhausted. The state restored includes all unproven subgoals or, if a goal had been proved in the previous state, the corresponding theorem. For a description of the subgoal package, see `set_goal`.

Failure

The function `backup` will fail if the backup list is empty.

Example

```
- g '(HD[1;2;3] = 1) /\ (TL[1;2;3] = [2;3])';
> val it =
  Proof manager status: 1 proof.
  1. Incomplete:
      Initial goal:
      (HD [1; 2; 3] = 1) /\ (TL [1; 2; 3] = [2; 3])

      : proofs

- e CONJ_TAC;
OK..
2 subgoals:
> val it =
  TL [1; 2; 3] = [2; 3]

  HD [1; 2; 3] = 1

  : proof

- backup();
> val it =
  Initial goal:

  (HD [1; 2; 3] = 1) /\ (TL [1; 2; 3] = [2; 3])

  : proof

- e (REWRITE_TAC[listTheory.HD, listTheory.TL]);
OK..
```

```
> val it =
  Initial goal proved.
  |- (HD [1; 2; 3] = 1) /\ (TL [1; 2; 3] = [2; 3]) : proof
```

Uses

Back tracking in a goal-directed proof to undo errors or try different tactics.

See also

proofManagerLib.set_goal, proofManagerLib.restart, proofManagerLib.backup, proofManagerLib.restore, proofManagerLib.save, proofManagerLib.set_backup, proofManagerLib.expand, proofManagerLib.expandf, proofManagerLib.p, proofManagerLib.top_thm, proofManagerLib.top_goal.

<div data-bbox="161 911 481 963" data-label="Text"> <p>BBLAST_CONV</p> </div>	<div data-bbox="1038 911 1331 963" data-label="Text"> <p>(blastLib)</p> </div>
--	--

BBLAST_CONV : conv

Synopsis

Bit-blasting conversion for words.

Description

This conversion expands bit-vector terms into Boolean propositions. It goes beyond the functionality of wordsLib.WORD_BIT_EQ_CONV by handling addition, subtraction and orderings. Consequently, this conversion can automatically handle small, but tricky, bit-vector goals that wordsLib.WORD_DECIDE cannot handle. Obviously bit-blasting is a brute force approach, so this conversion should be used with care. It will only work well for smallish word sizes and when there is only a handful of additions around. It is also "eager" – additions are expanded out even when not strictly necessary. For example, in

$$(a + b) <+ c \wedge c <+ d \implies (a + b) <+ d : \text{word32}$$

the sum $a + b$ is expanded. Users may be able to achieve speed-ups by first introducing abbreviations and then proving general forms, e.g.

$$x <+ c \wedge c <+ d \implies x <+ d : \text{word32}$$

The conversion handles most operators, however, the following are not covered / interpreted:

- Type variables for word lengths, i.e. terms of type `'a word`.

- General multiplication, i.e. $w1 * w2$. Multiplication by a literal is okay, although this may introduce many additions.
- Bit-field selections with non-literal bounds, e.g. $(expr1 \text{ -- } expr2) w$.
- Shifting by non-literal amounts, e.g. $w \ll expr$.
- $n2w \text{ expr}$ and $w2n w$. Also $w2s$, $s2w$, $w2l$ and $l2w$.
- `word_div`, `word_sdiv`, `word_mod` and `word_log2`.

Example

Word orderings are handled:

```
- blastLib.BBLAST_CONV “!a b. ~word_msb a /\ ~word_msb b ==> (a <+ b = a < b:word3
val it =
  |- (!a b. ~word_msb a /\ ~word_msb b ==> (a <+ b <=> a < b)) <=> T
  : thm
```

In some cases the result will be a proposition over bit values:

```
- blastLib.BBLAST_CONV “!a. (a + 1w:word8) ’ 1“;
val it =
  |- (!a. (a + 1w) ’ 1) <=> !a. a ’ 1 <=> ~a ’ 0
  : thm
```

This conversion is especially useful where "logical" and "arithmetic" bit-vector operations are combined:

```
- blastLib.BBLAST_CONV “!a. ((((((a:word8) * 16w) + 0x10w)) && 0xF0w) >>> 4) = (3
val it =
  |- (!a. (a * 16w + 16w && 240w) >>> 4 = (3 -- 0) (a + 1w)) <=> T
  : thm
```

See also

`wordsLib.WORD_ss`, `wordsLib.WORD_ARITH_CONV`, `wordsLib.WORD_LOGIC_CONV`,
`wordsLib.WORD_MUL_LSL_CONV`, `wordsLib.WORD_BIT_EQ_CONV`, `wordsLib.WORD_EVAL_CONV`,
`wordsLib.WORD_CONV`.

BEQ_CONV

(reduceLib)

`BEQ_CONV` : conv

Synopsis

Simplifies certain expressions involving boolean equality.

Description

If tm corresponds to one of the forms given below, where t is an arbitrary term of type `bool`, then `BEQ_CONV tm` returns the corresponding theorem. Note that in the last case the left-hand and right-hand sides need only be alpha-equivalent rather than strictly identical.

```
BEQ_CONV "T = t" = |- T = t = t
BEQ_CONV "t = T" = |- t = T = t
BEQ_CONV "F = t" = |- F = t = ~t
BEQ_CONV "t = F" = |- t = F = ~t
BEQ_CONV "t = t" = |- t = t = T
```

Failure

`BEQ_CONV tm` fails unless tm has one of the forms indicated above.

Example

```
#BEQ_CONV "T = T";;
|- (T = T) = T
```

```
#BEQ_CONV "F = T";;
|- (F = T) = F
```

```
#BEQ_CONV "(!x:***. x = (FST x,SND x)) = (!y:***. y = (FST y,SND y))";;
|- ((!x. x = FST x,SND x) = (!y. y = FST y,SND y)) = T
```

Beta	(Thm)
------	-------

```
Beta : thm -> thm
```

Synopsis

Perform one step of beta-reduction on the right hand side of an equational theorem.

Description

Beta performs a single beta-reduction step on the right-hand side of an equational theorem.

$$\frac{A \vdash t = ((\lambda x.M) N)}{\text{Beta}} \\ A \vdash t = M [N/x]$$

Failure

If the theorem is not an equation, or if the right hand side of the equation is not a beta-redex.

Example

```
val th = REFL (Term '(K:'a ->'b->'a) x');
> val th = |- K x = K x : thm

- SUBS_OCCS [[2], combinTheory.K_DEF] th;
> val it = |- K x = (\x y. x) x : thm

- Beta it;
> val it = |- K x = (\y. x) : thm
```

Comments

Beta is equivalent to RIGHT_BETA but faster.

See also

Drule.RIGHT_BETA, Drule.ETA_CONV.

beta	(Type)
------	--------

beta : hol_type

Synopsis

Common type variable.

Description

The ML variable Type.beta is bound to the type variable 'b.

See also

Type.alpha, Type.gamma, Type.delta, Type.bool.

beta_conv

(Term)

beta_conv : term -> term

Synopsis

Performs one step of beta-reduction.

Description

Beta-reduction is one of the primitive operations in the lambda calculus. A step of beta-reduction may be performed by `beta_conv M`, where `M` is the application of a lambda abstraction to an argument, i.e., has the form $(\lambda v.N) P$. The beta-reduction occurs by systematically replacing every free occurrence of `v` in `N` by `P`.

Care is taken so that no free variable of `P` becomes captured in this process.

Failure

If `M` is not the application of an abstraction to an argument.

Example

```
- beta_conv (mk_comb (Term '(x:'a) (y:'b). x', Term '(P:bool -> 'a) Q'));
> val it = '\y. P Q' : term
```

```
- beta_conv (mk_comb (Term '(x:'a) (y:'b) (y':'b). x', Term 'y:'a'));
> val it = '\y'. y' : term
```

Comments

More complex strategies for coding up full beta-reduction can be coded up in ML. The conversions of Larry Paulson support this activity as inference steps.

Uses

For programming derived rules of inference.

See also

`Thm.BETA_CONV`, `Drule.RIGHT_BETA`, `Drule.LIST_BETA_CONV`, `Drule.RIGHT_LIST_BETA`, `Conv.DEPTH_CONV`, `Conv.TOP_DEPTH_CONV`, `Conv.REDEPTH_CONV`.

BETA_CONV

(Thm)

BETA_CONV : conv

Synopsis

Performs a single step of beta-conversion.

Description

The conversion `BETA_CONV` maps a beta-redex " $(\lambda x. u)v$ " to the theorem

$$\vdash (\lambda x. u)v = u[v/x]$$

where $u[v/x]$ denotes the result of substituting v for all free occurrences of x in u , after renaming sufficient bound variables to avoid variable capture. This conversion is one of the primitive inference rules of the HOL system.

Failure

`BETA_CONV tm` fails if `tm` is not a beta-redex.

Example

```

- BETA_CONV (Term '(λx.x+1)y');
> val it = ⊢ (λx. x + 1)y = y + 1 : thm

- BETA_CONV (Term '(λx y. x+y)y');
> val it = ⊢ (λx y. x + y)y = (λy'. y + y') : thm

```

See also

`Conv.BETA_RULE`, `Tactic.BETA_TAC`, `Drule.LIST_BETA_CONV`, `PairedLambda.PAIRED_BETA_CONV`, `Drule.RIGHT_BETA`, `Drule.RIGHT_LIST_BETA`.

BETA_RULE**(Conv)**

`BETA_RULE` : (thm -> thm)

Synopsis

Beta-reduces all the beta-redexes in the conclusion of a theorem.

Description

When applied to a theorem $A \vdash \tau$, the inference rule `BETA_RULE` beta-reduces all beta-redexes, at any depth, in the conclusion τ . Variables are renamed where necessary to avoid free variable capture.

$$\frac{A \vdash \dots((\lambda x. s1) s2)\dots}{A \vdash \dots(s1[s2/x])\dots} \text{ BETA_RULE}$$

Failure

Never fails, but will have no effect if there are no beta-redexes.

Example

The following example is a simple reduction which illustrates variable renaming:

```
- Globals.show_assums := true;
val it = () : unit

- local val tm = Parse.Term 'f = ((\x y. x + y) y)'
  in
  val x = ASSUME tm
  end;
val x = [f = (\x y. x + y)y] |- f = (\x y. x + y)y : thm

- BETA_RULE x;
val it = [f = (\x y. x + y)y] |- f = (\y'. y + y') : thm
```

See also

Thm.BETA_CONV, Tactic.BETA_TAC, PairedLambda.PAIRED_BETA_CONV, Drule.RIGHT_BETA.

BETA_TAC	(Tactic)
----------	----------

BETA_TAC : tactic

Synopsis

Beta-reduces all the beta-redexes in the conclusion of a goal.

Description

When applied to a goal $A \text{ ?- } \tau$, the tactic BETA_TAC produces a new goal which results from beta-reducing all beta-redexes, at any depth, in τ . Variables are renamed where necessary to avoid free variable capture.

$$\frac{A \text{ ?- } \dots((\lambda x. s1) s2)\dots}{\text{===== BETA_TAC}} A \text{ ?- } \dots(s1[s2/x])\dots$$
Failure

Never fails, but will have no effect if there are no beta-redexes.

See also

Thm.BETA_CONV, Tactic.BETA_TAC, PairedLambda.PAIRED_BETA_CONV.

BINDER_CONV**(Conv)**

BINDER_CONV : conv -> conv

Synopsis

Applies a conversion underneath a binder.

Description

If conv N returns A |- N = P, then BINDER_CONV conv (M (\v.N)) returns A |- M (\v.N) = M (\v.P) and BINDER_CONV conv (\v.N) returns A |- (\v.N) = (\v.P)

Failure

If conv N fails, or if v is free in A.

Example

```
- BINDER_CONV SYM_CONV (Term '\x. x + 0 = x');
> val it = |- (\x. x + 0 = x) = \x. x = x + 0 : thm
```

Comments

For deeply nested quantifiers, STRIP_BINDER_CONV and STRIP_QUANT_CONV are more efficient than iterated application of BINDER_CONV, BINDER_CONV, or ABS_CONV.

See also

Conv.QUANT_CONV, Conv.STRIP_QUANT_CONV, Conv.STRIP_BINDER_CONV, Conv.ABS_CONV.

BINOP_CONV**(Conv)**

BINOP_CONV : conv -> conv

Synopsis

Applies a conversion to both arguments of a binary operator.

Description

If c is a conversion that when applied to t_1 returns the theorem $\vdash t_1 = t_1'$ and when applied to t_2 returns the theorem $\vdash t_2 = t_2'$, then `BINOP_CONV c (Term 'f t1 t2')` will return the theorem

$$\vdash f\ t_1\ t_2 = f\ t_1'\ t_2'$$

Failure

`BINOP_CONV c t` will fail if t is not of the general form $f\ t_1\ t_2$, or if c fails when applied to either t_1 or t_2 , or if c fails to return theorems of the form $\vdash t_1 = t_1'$ and $\vdash t_2 = t_2'$ when applied to those arguments. (The latter case would imply that c wasn't a conversion at all.)

Example

```
- BINOP_CONV REDUCE_CONV (Term '3 * 4 + 6 * 7');
> val it =  $\vdash 3 * 4 + 6 * 7 = 12 + 42$  : thm
```

See also

`Conv.FORK_CONV`, `Conv.LAND_CONV`, `Conv.RAND_CONV`, `Conv.RATOR_CONV`, `numLib.REDUCE_CONV`.

<div data-bbox="159 1469 341 1520" data-label="Text"> <p><code>BIT_ss</code></p> </div>	<div data-bbox="1038 1467 1331 1520" data-label="Text"> <p><code>(wordsLib)</code></p> </div>
---	---

`BIT_ss` : `ssfrag`

Synopsis

Simplification fragment for words.

Description

The fragment `BIT_ss` rewrites the term '`BIT i n`' for ground n .

Example

```

- SIMP_CONV (std_ss++BIT_ss) [] ‘‘BIT i 33’’;
> val it = |- BIT i 33 = i IN {0; 5} : thm

- SIMP_CONV (std_ss++BIT_ss) [] ‘‘BIT 5 33’’;
> val it = |- BIT 5 33 = T : thm

```

See also

wordsLib.WORD_CONV, fcpLib.FCP_ss, wordsLib.SIZES_ss, wordsLib.WORD_ARITH_ss, wordsLib.WORD_LOGIC_ss, wordsLib.WORD_SHIFT_ss, wordsLib.WORD_ARITH_EQ_ss, wordsLib.WORD_BIT_EQ_ss, wordsLib.WORD_EXTRACT_ss, wordsLib.WORD_MUL_LSL_ss, wordsLib.WORD_ss.

body**(Term)**

body : term -> term

Synopsis

Returns the body of an abstraction.

Description

If M is a lambda abstraction, i.e, has the form $\lambda v. t$, then `body M` returns t .

Failure

Fails unless M is an abstraction.

See also

Term.bvar, Term.dest_abs.

BODY_CONJUNCTS**(Drule)**

BODY_CONJUNCTS : (thm -> thm list)

Synopsis

Splits up conjuncts recursively, stripping away universal quantifiers.

Description

When applied to a theorem, `BODY_CONJUNCTS` recursively strips off universal quantifiers by specialization, and breaks conjuncts into a list of conjuncts.

$$A \vdash !x_1 \dots x_n. t_1 \wedge (!y_1 \dots y_m. t_2 \wedge t_3) \wedge \dots$$

BODY_CONJUNCTS

$$[A \vdash t_1, A \vdash t_2, A \vdash t_3, \dots]$$

Failure

Never fails, but has no effect if there are no top-level universal quantifiers or conjuncts.

Example

The following illustrates how a typical term will be split:

```
- local val tm = Parser.term_parser
      ' !x:bool. A /\ (B \/ (C /\ D)) /\ ((!y:bool. E) /\ F) '
  in
  val x = ASSUME tm
  end;

  val x = . |- !x. A /\ (B \/ C /\ D) /\ (!y. E) /\ F : thm

- BODY_CONJUNCTS x;
val it = [. |- A, . |- B \/ C /\ D, . |- E, . |- F] : thm list
```

See also

Thm.CONJ, Thm.CONJUNCT1, Thm.CONJUNCT2, Drule.CONJUNCTS, Tactic.CONJ_TAC.

<div data-bbox="159 1438 284 1487" data-label="Text">bool</div>	<div data-bbox="1155 1435 1331 1496" data-label="Text">(Type)</div>
---	---

bool : hol_type

Synopsis

Basic type constant.

Description

The ML variable `Type.bool` is bound to the type constant `bool`.

See also

alpha, Type.beta, Type.gamma, Type.delta.

`bool_case``(boolSyntax)``bool_case : term`

Synopsis

Constant denoting case expressions for `bool`.

Description

The ML variable `boolSyntax.bool_case` is bound to the term `bool$bool_case`.

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`, `boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.let_tm`, `boolSyntax.arb`.

`BOOL_CASES_TAC``(Tactic)``BOOL_CASES_TAC : (term -> tactic)`

Synopsis

Performs boolean case analysis on a (free) term in the goal.

Description

When applied to a term `x` (which must be of type `bool` but need not be simply a variable), and a goal `A ?- t`, the tactic `BOOL_CASES_TAC` generates the two subgoals corresponding to `A ?- t` but with any free instances of `x` replaced by `F` and `T` respectively.

$$\begin{array}{c}
 A \text{ ?- } t \\
 \hline
 \text{====} \quad \text{BOOL_CASES_TAC "x"} \\
 A \text{ ?- } t[F/x] \quad A \text{ ?- } t[T/x]
 \end{array}$$

The term given does not have to be free in the goal, but if it isn't, `BOOL_CASES_TAC` will merely duplicate the original goal twice.

Failure

Fails unless the term `x` has type `bool`.

Example

The goal:

```
?- (b ==> ~b) ==> (b ==> a)
```

can be completely solved by using `BOOL_CASES_TAC` on the variable `b`, then simply rewriting the two subgoals using only the inbuilt tautologies, i.e. by applying the following tactic:

```
BOOL_CASES_TAC (Parse.Term 'b:bool') THEN REWRITE_TAC[]
```

Uses

Avoiding fiddly logical proofs by brute-force case analysis, possibly only over a key term as in the above example, possibly over all free boolean variables.

See also

`Tactic.ASM_CASES_TAC`, `Tactic.COND_CASES_TAC`, `Tactic.DISJ_CASES_TAC`,
`Tactic.STRUCT_CASES_TAC`.

<code>bool_compset</code>	<code>(computeLib)</code>
---------------------------	---------------------------

```
bool_compset : unit -> compset
```

Synopsis

Creates a new simplification set to use with `CBV_CONV` for basic computations.

Description

This function creates a new simplification set to use with the `compute` library performing computations about operations on primitive booleans and other basic constants, such as `LET`, conditional, implication, conjunction, disjunction, and negation.

Example

```
- CBV_CONV (bool_compset()) (Term 'F ==> (T \\/ F)');
> val it = |- F ==> (T \\/ F) = T : thm
```

See also

`computeLib.CBV_CONV`.

<code>bool_EQ_CONV</code>	<code>(Conv)</code>
---------------------------	---------------------

```
bool_EQ_CONV : conv
```

Synopsis

Simplifies expressions involving boolean equality.

Description

The conversion `bool_EQ_CONV` simplifies equations of the form $t_1 = t_2$, where t_1 and t_2 are of type `bool`. When applied to a term of the form $t = t$, the conversion `bool_EQ_CONV` returns the theorem

$$\vdash (t = t) = T$$

When applied to a term of the form $t = T$, the conversion returns

$$\vdash (t = T) = t$$

And when applied to a term of the form $T = t$, it returns

$$\vdash (T = t) = t$$

Failure

Fails unless applied to a term of the form $t_1 = t_2$, where t_1 and t_2 are boolean, and either t_1 and t_2 are syntactically identical terms or one of t_1 and t_2 is the constant `T`.

Example

```
- bool_EQ_CONV (Parse.Term 'T = F');
val it =  $\vdash (T = F) = F$  : thm

- bool_EQ_CONV (Parse.Term '(0 < n) = T');
val it =  $\vdash (0 < n = T) = 0 < n$  : thm
```

<code>bool_rewrites</code>	<code>(Rewrite)</code>
----------------------------	------------------------

`bool_rewrites: rewrites`

Synopsis

Contains a number of basic equalities useful in rewriting.

Description

The variable `bool_rewrites` is a basic collection of rewrite rules useful in expression simplification. The current collection is

```

- bool_rewrites;

> val it =
  |- (x = x) = T;  |- (T = t) = t;  |- (t = T) = t;  |- (F = t) = ~t;
  |- (t = F) = ~t;  |- ~~t = t;  |- ~T = F;  |- ~F = T;  |- T /\ t = t;
  |- t /\ T = t;  |- F /\ t = F;  |- t /\ F = F;  |- t /\ t = t;
  |- T \/ t = T;  |- t \/ T = T;  |- F \/ t = t;  |- t \/ F = t;
  |- t \/ t = t;  |- T ==> t = t;  |- t ==> T = T;  |- F ==> t = T;
  |- t ==> t = T;  |- t ==> F = ~t;  |- (if T then t1 else t2) = t1;
  |- (if F then t1 else t2) = t2;  |- (!x. t) = t;  |- (?x. t) = t;
  |- (\x. t1) t2 = t1
Number of rewrite rules = 28
: rewrites

```

Uses

The contents of `bool_rewrites` provide a standard basis upon which to build bespoke rewrite rule sets for use by the functions in `Rewrite`.

See also

`Rewrite.GEN_REWRITE_CONV`, `Rewrite.GEN_REWRITE_RULE`, `Rewrite.GEN_REWRITE_TAC`,
`Rewrite.REWRITE_RULE`, `Rewrite.REWRITE_TAC`, `Rewrite.add_rewrites`,
`Rewrite.add_implicit_rewrites`, `Rewrite.empty_rewrites`,
`Rewrite.implicit_rewrites`, `Rewrite.set_implicit_rewrites`.

<div data-bbox="159 1402 368 1453" data-label="Text"> <p><code>bool_ss</code></p> </div>	<div data-bbox="927 1397 1331 1451" data-label="Text"> <p>(BasicProvers)</p> </div>
--	---

`bool_ss` : simpset

Synopsis

Basic simpset containing standard propositional and first order logic simplifications, plus beta and eta conversion.

Description

`BasicProvers.bool_ss` is identical to `boolSimps.bool_ss`.

See also

`boolSimps.bool_ss`.

`bool_ss``(boolSimps)``bool_ss : simpset`

Synopsis

Basic simpset containing standard propositional and first order logic simplifications, plus beta-conversion.

Description

`bossLib.bool_ss` is identical to `boolSimps.bool_ss`.

See also

`bossLib.bool_ss`.

`bool_ss``(bossLib)``bool_ss : simpset`

Synopsis

Basic simpset containing standard propositional and first order logic simplifications, plus beta conversion.

Description

The `bool_ss` simpset is almost at the base of the system-provided simpset hierarchy. Though not very powerful, it does include the following ad hoc collection of rewrite rules for propositions and first order terms:

```

|- !A B. ~(A ==> B) = A /\ ~B
|- !A B. ~(A /\ B) = ~A \/\ ~B /\
      (~A \/\ B) = ~A /\ ~B
|- !P. ~(!x. P x) = ?x. ~P x
|- !P. ~(?x. P x) = !x. ~P x
|- (~p = ~q) = (p = q)
|- !x. (x = x) = T
|- !t. ((T = t) = t) /\
      ((t = T) = t) /\

```

```

      ((F = t) = ~t) /\
      ((t = F) = ~t)
|- (!t. ~~t = t) /\ (~T = F) /\ (~F = T)
|- !t. (T /\ t = t) /\
      (t /\ T = t) /\
      (F /\ t = F) /\
      (t /\ F = F) /\
      (t /\ t = t)
|- !t. (T \/ t = T) /\
      (t \/ T = T) /\
      (F \/ t = t) /\
      (t \/ F = t) /\
      (t \/ t = t)
|- !t. (T ==> t = t) /\
      (t ==> T = T) /\
      (F ==> t = T) /\
      (t ==> t = T) /\
      (t ==> F = ~t)
|- !t1 t2. ((if T then t1 else t2) = t1) /\
      ((if F then t1 else t2) = t2)
|- !t. (!x. t) = t
|- !t. (?x. t) = t
|- !b t. (if b then t else t) = t
|- !a. ?x. x = a
|- !a. ?x. a = x
|- !a. ?!x. x = a,
|- !a. ?!x. a = x,
|- (!b e. (if b then T else e) = b \/ e) /\
      (!b t. (if b then t else T) = b ==> t) /\
      (!b e. (if b then F else e) = ~b /\ e) /\
      (!b t. (if b then t else F) = b /\ t)
|- !t. t \/ ~t
|- !t. ~t \/ t
|- !t. ~(t /\ ~t)
|- !x. (@y. y = x) = x
|- !x. (@y. x = y) = x
|- !f v. (!x. (x = v) ==> f x) = f v
|- !f v. (!x. (v = x) ==> f x) = f v
|- !P a. (?x. (x = a) /\ P x) = P a
|- !P a. (?x. (a = x) /\ P x) = P a

```

Also included in `bool_ss` is a conversion to perform beta reduction, as well as the following congruence rules, which allow the simplifier to glean additional contextual information as it descends through implications and conditionals.

```
|- !x x' y y'.
    (x = x') ==>
    (x' ==> (y = y')) ==> (x ==> y = x' ==> y')

|- !P Q x x' y y'.
    (P = Q) ==>
    (Q ==> (x = x')) ==>
    (~Q ==> (y = y')) ==> ((if P then x else y) = (if Q then x' else y'))
```

Failure

Can't fail, as it is not a functional value.

Uses

The `bool_ss` simpset is an appropriate simpset from which to build new user-defined simpsets. It is also useful in its own right, for example when a delicate simplification is desired, where other more powerful simpsets might cause undue disruption to a goal. If even less system rewriting is desired, the `pure_ss` value can be used.

See also

`pureSimps.pure_ss`, `bossLib.std_ss`, `bossLib.arith_ss`, `bossLib.list_ss`,
`bossLib.SIMP_CONV`, `bossLib.SIMP_TAC`, `bossLib.RW_TAC`.

BUTFIRSTN_CONV

(listLib)

`BUTFIRSTN_CONV` : `conv`

Synopsis

Computes by inference the result of dropping the initial `n` elements of a list.

Description

For any object language list of the form `--'[x0;...x(n-k);...;x(n-1)]'--`, the result of evaluating

```
BUTFIRSTN_CONV (--'BUTFIRSTN k [x0;...x(n-k);...;x(n-1)]'--)
```

is the theorem

$$\vdash \text{BUTFIRSTN } k \ [x_0; \dots; x_{(n-k)}; \dots; x_{(n-1)}] = [x_{(n-k)}; \dots; x_{(n-1)}]$$

Failure

`BUTFIRSTN_CONV tm` fails if `tm` is not of the form described above, or `k` is greater than the length of the list.

<div data-bbox="161 636 368 685" data-label="Text"> <p><code>butlast</code></p> </div>	<div data-bbox="1182 633 1331 687" data-label="Text"> <p>(Lib)</p> </div>
--	---

`butlast : 'a list -> 'a list`

Synopsis

Computes the sub-list of a list consisting of all but the last element.

Description

`butlast [x1, ..., xn]` returns `[x1, ..., x(n-1)]`.

Failure

Fails if the list is empty.

See also

`Lib.last`, `Lib.el`, `Lib.front_last`.

<div data-bbox="161 1384 512 1438" data-label="Text"> <p><code>BUTLAST_CONV</code></p> </div>	<div data-bbox="1067 1382 1331 1438" data-label="Text"> <p>(listLib)</p> </div>
---	---

`BUTLAST_CONV : conv`

Synopsis

Computes by inference the result of stripping the last element of a list.

Description

For any object language list of the form `--'[x0; ... x(n-1)]'--`, the result of evaluating

$$\text{BUTLAST_CONV } (--'\text{BUTLAST } [x_0; \dots; x_{(n-1)}]'\text{--})$$

is the theorem

$$\vdash \text{BUTLAST } [x_0; \dots; x_{(n-1)}] = [x_0; \dots; x_{(n-2)}]$$

Failure

BUTLAST_CONV t_m fails if t_m is an empty list.

BUTLASTN_CONV	(listLib)
---------------	-----------

BUTLASTN_CONV : conv

Synopsis

Computes by inference the result of dropping the last n elements of a list.

Description

For any object language list of the form $--'[x_0; \dots x_{(n-k)}; \dots; x_{(n-1)}]'$, the result of evaluating

$$\text{BUTLASTN_CONV } (--'\text{BUTLASTN } k [x_0; \dots x_{(n-k)}; \dots; x_{(n-1)}]'$$

is the theorem

$$|- \text{BUTLASTN } k [x_0; \dots; x_{(n-k)}; \dots; x_{(n-1)}] = [x_0; \dots; x_{(n-k-1)}]$$
Failure

BUTLASTN_CONV t_m fails if t_m is not of the form described above, or k is greater than the length of the list.

bvar	(Term)
------	--------

bvar : term -> term

Synopsis

Returns the bound variable of an abstraction.

Description

If M is a lambda abstraction, i.e, has the form $\lambda v. t$, then $\text{bvar } M$ returns v .

Failure

Fails unless M is an abstraction.

See also

Term.body, Term.dest_abs.

bvk_find_term**(HolKernel)**

```
bvk_find_term : (term list * term -> bool) -> (term -> 'a) -> term -> 'a option
```

Synopsis

Finds a sub-term satisfying predicate argument; applies a continuation.

Description

A call to `bvk_find_term P k tm` searches `tm` for a sub-term satisfying `P` and calls the continuation `k` on the first that it finds. If `k` succeeds on this sub-term, the result is wrapped in `SOME` and returned to the caller. If `k` raises a `HOL_ERR` exception on the sub-term, control returns to `bvk_find_term`, which continues to look for a sub-term satisfying `P`. Other exceptions are returned to the caller. If there is no sub-term that both satisfies `P` and on which `k` operates successfully, the result is `NONE`.

The search order is top-down, left-to-right (i.e., raters of combs are examined before rands).

As with `find_term`, `P` should be total. In addition, `P` is given not just the sub-term of interest, but also the stack of bound variables that have scope over the sub-term, with the innermost bound variables appearing earlier in the list.

Failure

Fails if the predicate argument fails (i.e., raises an exception; returning false is acceptable) on a sub-term, or if the continuation argument raises a non-`HOL_ERR` exception on a sub-term on which the predicate has returned true.

Example

The `RED_CONV` function from `reduceLib` reduces a ground arithmetic term over the natural numbers, failing if the term is not of the right shape.

```
- val find = bvk_find_term (equal ``:num`` o type_of o #2)
                        reduceLib.RED_CONV;
> val find = fn : term -> thm option

- find ``SUC n``;
> val it = NONE : thm option
```

```

- find ‘‘2 * 3 + SUC n‘‘;
> val it = SOME |- 2 * 3 = 6 : thm option

- find ‘‘SUC n + 2 * 3‘‘;
> val it = SOME |- 2 * 3 = 6 : thm option

- find ‘‘2 + 1 + SUC n + 2 * 3‘‘;
> val it = SOME |- 2 + 1 = 3 : thm option

```

See also

`HolKernel.find_term`, `HolKernel.find_terms`.

by

(bossLib)

op by : term quotation * tactic -> tactic

Synopsis

Prove and place a theorem on the assumptions of the goal.

Description

An invocation `tm by tac`, when applied to goal $A \text{ ?- } g$, applies `tac` to goal $A \text{ ?- } tm$. If `tm` is thereby proved, it is added to A , yielding the new goal $A, tm \text{ ?- } g$. If `tm` is not proved by `tac`, then any remaining subgoals generated are added to $A, tm \text{ ?- } g$.

When `tm` is added to the existing assumptions A , it is "stripped", i.e., broken apart by eliminating existentials, conjunctions, and disjunctions. This can lead to case splitting.

Failure

Fails if `tac` fails when applied to $A \text{ ?- } tm$.

Example

Given the goal $\{x \leq y, w < x\} \text{ ?- } P$, suppose that the fact $\text{?n. } y = n + w$ would help in eventually proving P . Invoking

```
‘?n. y = n + w’ by (EXISTS_TAC ‘‘y-w‘‘ THEN DECIDE_TAC)
```

yields the goal $\{y = n + w, x \leq y, w < x\} \text{ ?- } P$ in which the proved fact has been added to the assumptions after its existential quantifier is eliminated. Note the parentheses around the tactic: this is needed for the example because `by` binds more tightly than `THEN`.

Since the tactic supplied need not solve the generated subgoal, `by` gives a useful way of generating proof obligations while pursuing a particular line of reasoning. For example, the above goal could also be attacked by

```
'?n. y = n + w' by ALL_TAC
```

with the result being the goal $\{x \leq y, w < x\} \text{ ?- } ?n. y = n + w$ and the augmented original $\{y = n + w, x \leq y, w < x\} \text{ ?- } P$. Now either may be attempted.

Comments

Use of `by` can be more convenient than `IMP_RES_TAC` and `RES_TAC` when they would generate many useless assumptions.

See also

`Tactical.SUBGOAL_THEN`, `Tactic.IMP_RES_TAC`, `Tactic.RES_TAC`,
`Tactic.STRIP_ASSUME_TAC`.

C

(Lib)

```
C : ('a -> 'b -> 'c) -> 'b -> 'a -> 'c
```

Synopsis

Permutates first two arguments to curried function: `C f x y` equals `f y x`.

Failure

`C f` never fails and `C f x` never fails, but `C f x y` fails if `f y x` fails.

Example

```
- map (C cons []) [1,2,3];
> val it = [[1], [2], [3]] : int list list
```

See also

`Lib.##`, `Lib.A`, `Lib.B`, `Lib.I`, `Lib.K`, `Lib.S`, `Lib.W`.

can

(Lib)

```
can : ('a -> 'b) -> 'a -> bool
```

Synopsis

Tests for failure.

Description

`can f x` evaluates to `true` if the application of `f` to `x` succeeds. It evaluates to `false` if the application fails.

Failure

Only fails if `f x` raises the `Interrupt` exception.

Example

```
- hd [];
! Uncaught exception:
! Empty

- can hd [];
> val it = false : bool

- can (fn _ => raise Interrupt) 3;
> Interrupted.
```

See also

`Lib.assert`, `Lib.trye`, `Lib.partial`, `Lib.total`, `Lib.assert_exn`.

CASE_TAC

(BasicProvers)

`CASE_TAC` : tactic

Synopsis

Case splits on a term `t` that features in the goal as `case t of ...`, and then performs some simplification.

Description

`BasicProvers.CASE_TAC` first calls `BasicProvers.PURE_CASE_TAC`, which searches the goal for an instance of `case t of ...` and performs a `BasicProvers.Cases_on 't'`. If this succeeds, it then simplifies the goal using definitions of `case` constants, plus distinctness and injectivity theorems for datatypes.

Comments

When there are multiple case constants in the goal, it can be very convenient to execute the tactic `REPEAT CASE_TAC. bossLib.CASE_TAC` is the same as `BasicProvers.CASE_TAC`.

Failure

`BasicProvers.CASE_TAC` fails precisely when `BasicProvers.PURE_CASE_TAC` fails.

See also

`BasicProvers.PURE_CASE_TAC`.

Cases

(BasicProvers)

Cases : tactic

Synopsis

Case split on leading universally quantified variable in a goal.

Description

`bossLib.Cases` is identical to `BasicProof.Cases`.

See also

`bossLib.Cases`.

Cases

(bossLib)

Cases : tactic

Synopsis

Performs case analysis on the variable of the leading universally quantified variable of the goal.

Description

When applied to a universally quantified goal $\forall u. G$, `Cases` performs a case-split, based on the cases theorem for the type of `u` stored in the global `TypeBase` database.

The cases theorem for a type `ty` will be of the form:

$$\begin{aligned} &|- !v:ty. (?x11\dots x1n1. v = C1\ x11\ \dots\ x1n1) \ \vee\ \dots\ \vee \\ &\quad (?xm1\dots xnm. v = Cm\ xm1\ \dots\ xnm) \end{aligned}$$

where there is no requirement for there to be more than one disjunct, nor for there to be any particular number of existentially quantified variables in any disjunct. For example, the cases theorem for natural numbers initially in the `TypeBase` is:

$$|- !n. (n = 0) \ \vee\ (?m. n = \text{SUC } m)$$

Case-splitting consists of specialising the cases theorem with the variable from the goal and then generating as many sub-goals as there are disjuncts in the cases theorem, where in each sub-goal (including the assumptions) the variable has been replaced by an expression involving the given ‘constructor’ (the C_i ’s above) applied to as many fresh variables as appropriate.

Failure

Fails if the goal is not universally quantified, or if the type of the universally quantified variable does not have a case theorem in the `TypeBase`, as will happen, for example, with variable types.

Example

If we have defined the following type:

```
- Hol_datatype 'foo = Bar of num | Baz of bool';
> val it = () : unit
```

and the following function:

```
- val foofn_def = Define '(foofn (Bar n) = n + 10) /\
                          (foofn (Baz x) = 10)';
> val foofn_def =
  |- (!n. foofn (Bar n) = n + 10) /\
     !x. foofn (Baz x) = 10 : thm
```

then it is possible to make progress with the goal `!x. foofn x >= 10` by applying the tactic `Cases`, thus:

```

          ?- !x. foofn x >= 10
===== Cases
?- foofn (Bar n) >= 10      ?- foofn (Baz b) >= 10
```

producing two new goals, one for each constructor of the type.

See also

`bossLib.Cases.on`, `bossLib.Induct`, `Tactic.STRUCT_CASES_TAC`.

Cases_on**(BasicProvers)**`Cases_on : term -> tactic`

Synopsis

Case split on type of supplied term.

Description

`bossLib.Cases_on` is identical to `BasicProvers.Cases_on`.

See also

`bossLib.Cases_on`, `bossLib.Cases`.

Cases_on**(bossLib)**`Cases_on : term -> tactic`

Synopsis

Performs case analysis on the type of a given term.

Description

An application `Cases_on M` performs a case-split based on the type `ty` of `M`, using the cases theorem for `ty` from the global `TypeBase` database.

`Cases_on` can be used to specify variables that are buried in the quantifier prefix. `Cases_on` can also be used to perform case splits on non-variable terms. If `M` is a non-variable term that does not occur bound in the goal, then the cases theorem is instantiated with `M` and used to generate as many sub-goals as there are disjuncts in the cases theorem.

Failure

Fails if `ty` does not have a case theorem in the `TypeBase`.

Example

None yet.

See also

`bossLib.Cases`, `bossLib.Induct`, `bossLib.Induct_on`, `Tactic.STRUCT_CASES_TAC`.

CASES_THENL	(Thm_cont)
--------------------	-------------------

`CASES_THENL : (thm_tactic list -> thm_tactic)`

Synopsis

Applies the theorem-tactics in a list to corresponding disjuncts in a theorem.

Description

When given a list of theorem-tactics `[ttac1;...;ttacn]` and a theorem whose conclusion is a top-level disjunction of n terms, `CASES_THENL` splits a goal into n subgoals resulting from applying to the original goal the result of applying the i 'th theorem-tactic to the i 'th disjunct. This can be represented as follows, where the number of existentially quantified variables in a disjunct may be zero. If the theorem `th` has the form:

$$A' \mid- ?x11..x1m. t1 \vee \dots \vee ?xn1..xnp. tn$$

where the number of existential quantifiers may be zero, and for all i from 1 to n :

$$\begin{array}{l} A \text{ ?- } s \\ \text{===== } ttaci \text{ (}\mid- ti[xi1'/xi1]..[xim'/xim]\text{)} \\ Ai \text{ ?- } si \end{array}$$

where the primed variables have the same type as their unprimed counterparts, then:

$$\begin{array}{l} A \text{ ?- } s \\ \text{===== } CASES_THENL \text{ [ttac1;...;ttacn] th} \\ A1 \text{ ?- } s1 \quad \dots \quad An \text{ ?- } sn \end{array}$$

Unless A' is a subset of A , this is an invalid tactic.

Failure

Fails if the given theorem does not, at the top level, have the same number of (possibly multiply existentially quantified) disjuncts as the length of the theorem-tactic list (this includes the case where the theorem-tactic list is empty), or if any of the tactics generated as specified above fail when applied to the goal.

Uses

Performing very general disjunctive case splits.

See also

`Thm_cont.DISJ_CASES_THENL`, `Thm_cont.X_CASES_THENL`.

CBV_CONV

(computeLib)

CBV_CONV : compset -> conv

Synopsis

Call by value rewriting.

Description

The conversion `CBV_CONV` expects an simplification set and a term. Its term argument is rewritten using the equations added in the simplification set. The strategy used is somewhat similar to ML's, that is call-by-value (arguments of constants are completely reduced before the rewrites associated to the constant are applied) with weak reduction (no reduction of the function body before the function is applied). The main differences are that beta-redexes are reduced with a call-by-name strategy (the argument is not reduced), and reduction under binders is done when it occurs in a position where it cannot be substituted.

The simplification sets are mutable objects, this means they are extended by side-effect. The function `new_compset` will create a new set containing reflexivity (`REFL_CLAUSE`), plus the supplied rewrites. Theorems can be added to an existing compset with the function `add_thms`.

It is also possible to add conversions to a simplification set with `add_conv`. The only restriction is that a constant (`c`) and an arity (`n`) must be provided. The conversion will be called only on terms in which `c` is applied to `n` arguments.

Two theorem “preprocessors” are provided to control the strictness of the arguments of a constant. `lazyfy_thm` has pattern variables on the left hand side turned into abstractions on the right hand side. This transformation is applied on every conjunct, and removes prenex universal quantifications. A typical example is `COND_CLAUSES`:

$$(\text{COND } T \ a \ b = a) \ /\ \ (\text{COND } F \ a \ b = b)$$

Using these equations is very inefficient because both `a` and `b` are evaluated, regardless of the value of the boolean expression. It is better to use `COND_CLAUSES` with the form above

$$(\text{COND } T = \ \lambda a \ b. \ a) \ /\ \ (\text{COND } F = \ \lambda a \ b. \ b)$$

The call-by-name evaluation of beta redexes avoids computing the unused branch of the conditional.

Conversely, `strictify_thm` does the reverse transformation. This is particularly relevant for `LET_DEF`:

```
LET = \f x. f x  -->  LET f x = f x
```

This forces the evaluation of the argument before reducing the beta-redex. Hence the usual behaviour of LET.

It is necessary to provide rules for all the constants appearing in the expression to reduce (all also for those that appear in the right hand side of a rule), unless the given constant is considered as a constructor of the representation chosen. As an example, `reduceLib.num_compset` creates a new simplification set with all the rules needed for basic boolean and arithmetical calculations built in.

Example

```
- val rws = new_compset [lazyfy_thm COND_CLAUSES];
> val rws = <compset> : compset

- CBV_CONV rws (--'(\x.x) ((\x.x) if T then 0+0 else 10)'--);
> val it = |- (\x. x) ((\x. x) (if T then 0 + 0 else 10)) = 0 + 0 : thm

- CBV_CONV (reduceLib.num_compset())
          (--'if 100 - 5 * 5 < 80 then 2 EXP 16 else 3'--);
> val it = |- (if 100 - 5 * 5 < 80 then 2 ** 16 else 3) = 65536 : thm
```

Failing to give enough rules may make `CBV_CONV` build a huge result, or even loop. The same may occur if the initial term to reduce contains free variables.

```
val eqn = bossLib.Define 'exp n p = if p=0 then 1 else n * (exp n (p-1))';
val _ = add_thms [eqn] computeLib.the_compset;

- CBV_CONV rws (--'exp 2 n'--);
> Interrupted.

- set_skip rws "COND" (SOME 1);
> val it = () : unit

- CBV_CONV rws (--'exp 2 n'--);
> val it = |- exp 2 n = (if n = 0 then 1 else 2 * exp 2 (n - 1)) : thm
```

The first invocation of `CBV_CONV` loops since the exponent never reduces to 0. Below the first steps are computed:

```
exp 2 n
if n = 0 then 1 else 2 * exp 2 (n-1)
```

```
if n = 0 then 1 else 2 * if (n-1) = 0 then 1 else 2 * exp 2 (n-1-1)
...
```

The call to `set_skip` means that if the constants `COND` appears applied to one argument and does not create a redex (in the example, if the condition does not reduce to `T` or `F`), then the forthcoming arguments (the two branches of the conditional) are not reduced at all.

Failure

Should never fail. Nonetheless, using rewrites with assumptions may cause problems when rewriting under abstractions. The following example illustrates that issue.

```
- val th = ASSUME (--'0 = x'--);
- val tm = Term\'(x:num). x = 0\';
- val rws = from_list [th];
- CBV_CONV rws tm;
```

This fails because the `0` is replaced by `x`, making the assumption `0 = x`. Then, the abstraction cannot be rebuilt since `x` appears free in the assumptions.

See also

`numLib.REDUCE_CONV`, `computeLib.bool_compset`, `bossLib.EVAL`.

CCONTR	(Thm)
--------	-------

`CCONTR : term -> thm -> thm`

Synopsis

Implements the classical contradiction rule.

Description

When applied to a term `t` and a theorem `A |- F`, the inference rule `CCONTR` returns the theorem `A - {~t} |- t`.

$$\frac{A \mid\!-\! F}{A - \{\sim t\} \mid\!-\! t} \text{ CCONTR } t$$

Failure

Fails unless the term has type `bool` and the theorem has `F` as its conclusion.

Comments

The usual use will be when $\sim t$ exists in the assumption list; in this case, `CCONTR` corresponds to the classical contradiction rule: if $\sim t$ leads to a contradiction, then `t` must be true.

See also

`Drule.CONTR`, `Drule.CONTRAPOS`, `Tactic.CONTR_TAC`, `Thm.NOT_ELIM`.

<code>CCONTR_TAC</code>	<code>(Tactic)</code>
-------------------------	-----------------------

`CCONTR_TAC` : `tactic`

Synopsis

Prepares for a proof by Classical contradiction.

Description

`CCONTR_TAC` takes a theorem `A' |- F` and completely solves the goal. This is an invalid tactic unless `A'` is a subset of `A`.

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \text{ CCONTR_TAC } (A' \text{ |- } F) \end{array}$$
Failure

Fails unless the theorem is contradictory, i.e. has `F` as its conclusion.

See also

`Tactic.CHECK_ASSUME_TAC`, `Thm.CCONTR`, `Drule.CONTRAPOS`, `Thm.NOT_ELIM`.

<code>CHANGED_CONSEQ_CONV</code>	<code>(ConseqConv)</code>
----------------------------------	---------------------------

`CHANGED_CONSEQ_CONV` : `(conseq_conv -> conseq_conv)`

Synopsis

Makes a consequence conversion fail if applying it leaves a term unchanged.

Description

If c is a consequence conversion that maps a term ‘ t ’ to a theorem $\vdash t = t'$, $\vdash t' \implies t$ or $\vdash t \implies t'$, where t' is alpha-equivalent to t , or if c raises the `UNCHANGED` exception when applied to ‘ t ’, then `CHANGED_CONSEQ_CONV c` fails when applied to the term ‘ t ’. Otherwise, `CHANGED_CONSEQ_CONV c` behaves like c .

See also

`Conv.CHANGED_CONV`, `ConseqConv.QCHANGED_CONSEQ_CONV`.

CHANGED_CONV

(Conv)

`CHANGED_CONV : (conv -> conv)`

Synopsis

Makes a conversion fail if applying it leaves a term unchanged.

Description

If c is a conversion that maps a term ‘ t ’ to a theorem $\vdash t = t'$, where t' is alpha-equivalent to t , or if c raises the `UNCHANGED` exception when applied to ‘ t ’, then `CHANGED_CONV c` is a conversion that fails when applied to the term ‘ t ’. If c maps ‘ t ’ to $\vdash t = t'$, where t' is not alpha-equivalent to t , then `CHANGED_CONV c` also maps ‘ t ’ to $\vdash t = t'$. That is, `CHANGED_CONV c` is the conversion that behaves exactly like c , except that it fails whenever the conversion c would leave its input term unchanged (up to alpha-equivalence).

Failure

`CHANGED_CONV c` ‘ t ’ fails if c maps ‘ t ’ to $\vdash t = t'$, where t' is alpha-equivalent to t , or if c raises the `UNCHANGED` exception when applied to ‘ t ’, or if c fails when applied to ‘ t ’. The function returned by `CHANGED_CONV c` may also fail if the ML function $c : \text{term} \rightarrow \text{thm}$ is not, in fact, a conversion (i.e. a function that maps a term t to a theorem $\vdash t = t'$).

Uses

`CHANGED_CONV` is used to transform a conversion that may leave terms unchanged, and therefore may cause a nonterminating computation if repeated, into one that can safely be repeated until application of it fails to substantially modify its input term.

CHANGED_TAC

(Tactical)

CHANGED_TAC : (tactic -> tactic)

Synopsis

Makes a tactic fail if it has no effect.

Description

When applied to a tactic T , the tactical CHANGED_TAC gives a new tactic which is the same as T if that has any effect, and otherwise fails.

Failure

The application of CHANGED_TAC to a tactic never fails. The resulting tactic fails if the basic tactic either fails or has no effect.

See also

Tactical.TRY, Tactical.VALID.

CHECK_ASSUME_TAC

(Tactic)

CHECK_ASSUME_TAC : thm_tactic

Synopsis

Adds a theorem to the assumption list of goal, unless it solves the goal.

Description

When applied to a theorem $A' \vdash s$ and a goal $A \text{ ?- } t$, the tactic CHECK_ASSUME_TAC checks whether the theorem will solve the goal (this includes the possibility that the theorem is just $A' \vdash F$). If so, the goal is duly solved. If not, the theorem is added to the assumptions of the goal, unless it is already there.

```

      A ?- t
===== CHECK_ASSUME_TAC (A' |- F)   [special case 1]

```

```

      A ?- t
===== CHECK_ASSUME_TAC (A' |- t)   [special case 2]

```


$$\frac{A \text{ ?- } t}{\text{===== CHECK_ASSUME_TAC (A' |- s) [general case] A u \{s\} \text{ ?- } t}}$$

Unless A' is a subset of A, the tactic will be invalid, although it will not fail.

Failure

Never fails.

See also

Tactic.ACCEPT_TAC, Tactic.ASSUME_TAC, Tactic.CONTR_TAC, Tactic.DISCARD_TAC, Tactic.MATCH_ACCEPT_TAC.

CHOOSE (Thm)

CHOOSE : term * thm -> thm -> thm

Synopsis

Eliminates existential quantification using deduction from a particular witness.

Description

When applied to a term-theorem pair (v,A1 |- ?x. s) and a second theorem of the form A2 u {s[v/x]} |- t, the inference rule CHOOSE produces the theorem A1 u A2 |- t.

$$\frac{A1 \text{ |- } ?x. s \quad A2 \text{ u } \{s[v/x]\} \text{ |- } t}{\text{----- CHOOSE (v, (A1 \text{ |- } ?x. s))} A1 \text{ u } A2 \text{ |- } t}$$

Where v is not free in A1, A2 or t.

Failure

Fails unless the terms and theorems correspond as indicated above; in particular v must have the same type as the variable existentially quantified over, and must not be free in A1, A2 or t.

See also

Tactic.CHOOSE_TAC, Thm.EXISTS, Tactic.EXISTS_TAC, Drule.SELECT_ELIM.

CHOOSE_TAC	(Tactic)
-------------------	-----------------

CHOOSE_TAC : thm_tactic

Synopsis

Adds the body of an existentially quantified theorem to the assumptions of a goal.

Description

When applied to a theorem $A' \vdash ?x. t$ and a goal, CHOOSE_TAC adds $t[x'/x]$ to the assumptions of the goal, where x' is a variant of x which is not free in the assumption list; normally x' is just x .

$$\frac{A \quad ?- \quad u}{\text{CHOOSE_TAC } (A' \vdash ?x. t) \quad A \quad u \quad \{t[x'/x]\} \quad ?- \quad u}$$

Unless A' is a subset of A , this is not a valid tactic.

Failure

Fails unless the given theorem is existentially quantified.

Example

Suppose we have a goal asserting that the output of an electrical circuit (represented as a boolean-valued function) will become high at some time:

$?- \ ?t. \text{output}(t)$

and we have the following theorems available:

$t1 = \vdash \ ?t. \text{input}(t)$
 $t2 = !t. \text{input}(t) \implies \text{output}(t+1)$

Then the goal can be solved by the application of:

```
CHOOSE_TAC th1
  THEN EXISTS_TAC (Term 't+1')
  THEN UNDISCH_TAC (Term 'input (t:num) :bool')
  THEN MATCH_ACCEPT_TAC th2
```

See also

Thm.cont.CHOOSE_THEN, Tactic.X.CHOOSE_TAC.

CHOOSE_THEN

(Thm_cont)

CHOOSE_THEN : thm_tactical

Synopsis

Applies a tactic generated from the body of existentially quantified theorem.

Description

When applied to a theorem-tactic `ttac`, an existentially quantified theorem $A' \vdash \exists x. t$, and a goal, `CHOOSE_THEN` applies the tactic `ttac (t[x'/x] |- t[x'/x])` to the goal, where x' is a variant of x chosen not to be free in the assumption list of the goal. Thus if:

```
A ?- s1
===== ttac (t[x'/x] |- t[x'/x])
B ?- s2
```

then

```
A ?- s1
===== CHOOSE_THEN ttac (A' |- ?x. t)
B ?- s2
```

This is invalid unless A' is a subset of A .

Failure

Fails unless the given theorem is existentially quantified, or if the resulting tactic fails when applied to the goal.

Example

This theorem-tactical and its relatives are very useful for using existentially quantified theorems. For example one might use the inbuilt theorem

```
LESS_ADD_1 = |- !m n. n < m ==> (?p. m = n + (p + 1))
```

to help solve the goal

```
?- x < y ==> 0 < y * y
```

by starting with the following tactic

```
DISCH_THEN (CHOOSE_THEN SUBST1_TAC o MATCH_MP LESS_ADD_1)
```

which reduces the goal to

```
?- 0 < ((x + (p + 1)) * (x + (p + 1)))
```

which can then be finished off quite easily, by, for example:

```
REWRITE_TAC[ADD_ASSOC, SYM (SPEC_ALL ADD1),
            MULT_CLAUSES, ADD_CLAUSES, LESS_0]
```

See also

Tactic.CHOOSE_TAC, Thm_cont.X.CHOOSE_THEN.

<code>class</code>	(DB)
--------------------	------

datatype class

Synopsis

Datatype for classifying theory elements.

Description

Many of the functions in the DB structure return answers that involve the `class` type, which is declared as

```
datatype class = Thm | Axiom | Def
```

When occurring with `th`, an ML value of type `thm`, `Axiom` means that `th` has been asserted as an axiom; `Def` means that `th` is a constant definition; and `Thm` means that `th` is a plain old theorem, i.e., not an axiom or a definition.

See also

DB.data.

<code>clear_overloads_on</code>	(Parse)
---------------------------------	---------

Parse.clear_overloads_on : string -> unit

Synopsis

Clears all overloading on the specified operator.

Description

This function removes all overloading associated with the given string, except those "overloads" that map the string to constants of the same name. These additional overloads (there may be more than one constant of the same name, as long as each such is part of a different theory) may be removed with `remove_ovl_mapping`, or by using `hide`.

Failure

Never fails. If a string is not overloaded, this function simply has no effect.

Example

```
- load "realTheory";
> val it = () : unit
- realTheory.REAL_INV_LT1;
> val it = |- !x. 0 < x /\ x < 1 ==> 1 < inv x : thm
- clear_overloads_on "<";
> val it = () : unit
- realTheory.REAL_INV_LT1;
> val it = |- !x. 0 real_lt x /\ x real_lt 1 ==> 1 real_lt inv x : thm
- clear_overloads_on "&";
> val it = () : unit
- realTheory.REAL_INV_LT1;
> val it = |- !x. 0r real_lt x /\ x real_lt 1r ==> 1r real_lt inv x : thm
```

Uses

If overloading gets too confusing, this function should help to clear away one layer of supposedly helpful obfuscation.

Comments

As with other parsing functions, there is a sister function, `temp_clear_overloads_on` that does the same thing, but whose effect is not saved to a theory file.

See also

`Parse.overload_on`, `Parse.remove_ovl_mapping`.

CNF_CONV	(normalForms)
----------	---------------

CNF_CONV : conv

Synopsis

Converts a formula into Conjunctive Normal Form (CNF).

Description

Given a formula consisting of truths, falsities, conjunctions, disjunctions, negations, equivalences, conditionals, and universal and existential quantifiers, `CNF_CONV` will convert it to the canonical form:

$$\begin{aligned} & ?a_1 \dots a_k. \\ & (\!v_1 \dots v_{m1}. P_1 \ \backslash / \dots \ \backslash / P_{n1}) \ / \ \wedge \\ & \dots \ / \ \wedge \\ & (\!v_1 \dots v_{mp}. P_1 \ \backslash / \dots \ \backslash / P_{np}) \end{aligned}$$

The P_{ij} are literals: possibly-negated atoms. In first-order logic an atom is a formula consisting of a top-level relation symbol applied to first-order terms: function symbols and variables. In higher-order logic there is no distinction between formulas and terms, so the concept of atom is not well-formed. Note also that the a_i existentially bound variables may be functions, as a result of Skolemization.

Failure

`CNF_CONV` should never fail.

Example

```
- CNF_CONV ‘‘!x. P x ==> ?y z. Q y \\/ ~?z. P z /\ Q z’’;
> val it =
  |- (!x. P x ==> ?y z. Q y \\/ ~?z. P z /\ Q z) =
    ?y. !x x'. Q (y x) \\/ ~P x' \\/ ~Q x' \\/ ~P x : thm
```

Example

```
- CNF_CONV ‘‘~(~(x = y) = z) = ~(x = ~(y = z))’’;
> val it = |- (~(~(x = y) = z) = ~(x = ~(y = z))) = T : thm
```

COMB_CONV	(Conv)
------------------	---------------

`COMB_CONV` : `conv -> conv`

Synopsis

Applies a conversion to both immediate sub-terms of an application.

Description

If t is an application term of the form $f\ x$, and c is a conversion, such that c maps f to $|- f = f'$ and x to $|- x = x'$, then `COMB_CONV c` maps t to $|- f\ x = f'\ x'$.

Failure

`COMB_CONV c t` fails if t is not an application term, or if c fails when applied to the rator and rand of t , or if c is not in fact a conversion (i.e., a function which maps terms t to a theorem $|- t = t'$).

See also

`Conv.ABS_CONV`, `Conv.SUB_CONV`.

combine	(Lib)
---------	-------

```
combine : 'a list * 'b list -> ('a * 'b) list
```

Synopsis

Transforms a pair of lists into a list of pairs.

Description

`combine ([x1, ..., xn], [y1, ..., yn])` returns `[(x1, y1), ..., (xn, yn)]`.

Failure

Fails if the two lists are of different lengths.

Comments

Has much the same effect as the SML Basis function `ListPair.zip` except that it fails if the arguments are not of equal length. Also note that `zip` is a curried version of `combine`

See also

`Lib.zip`, `Lib.unzip`, `Lib.split`.

commafy	(Lib)
---------	-------

```
commafy : string list -> string list
```

Synopsis

Add commas into a list of strings.

Description

An application `commafy [s1,...,sn]` yields `[s1, ", ", ..., ", ", sn]`.

Failure

Never fails.

Example

```
- commafy ["donkey", "mule", "horse", "camel", "llama"];
> val it =
    ["donkey", ", ", "mule", ", ", "horse", ", ", "camel", ", ", "llama"] :
    string list

- print (String.concat it ^ "\n");
donkey, mule, horse, camel, llama
> val it = () : unit

- commafy ["foo"];
> val it = ["foo"] : string list
```

<div data-bbox="236 1308 445 1361" data-label="Text"><code>compare</code></div>	<div data-bbox="1228 1301 1412 1357" data-label="Text"><code>(Term)</code></div>
---	--

`Term.compare : term * term -> order`

Synopsis

Ordering on terms.

Description

An invocation `compare (M,N)` will return one of `{LESS, EQUAL, GREATER}`, according to an ordering on terms. The ordering is transitive and total, and equates alpha-convertible terms.

Failure

Never fails.

Example


```
- compare (T,F);
> val it = GREATER : order

- compare (Term `x y. x /\ y`, Term `y z. y /\ z`);
> val it = EQUAL : order
```

Comments

Used to build high performance datastructures for dealing with sets having many terms.

See also

`Term.empty_tmset`, `Term.var_compare`.

<div data-bbox="161 887 368 940" data-label="Text"> <p><code>compare</code></p> </div>	<div data-bbox="1155 882 1331 940" data-label="Text"> <p>(Type)</p> </div>
--	--

`Type.compare` : `hol_type * hol_type -> order`

Synopsis

An ordering on HOL types.

Description

An invocation `compare (ty1,ty2)` returns one of `{LESS, EQUAL, GREATER}`. This is a total and transitive order.

Failure

Never fails.

Example

```
- Type.compare (bool, alpha --> alpha);
> val it = LESS : order
```

Comments

One use of `compare` is to build efficient set or dictionary datastructures involving HOL types in the keys.

There is also a `Term.compare`.

See also

`Term.compare`.

<code>completeInduct_on</code>	<code>(bossLib)</code>
--------------------------------	------------------------

```
completeInduct_on : term quotation -> tactic
```

Synopsis

Perform complete induction

Description

If q parses into a well-typed term M , an invocation `completeInduct_on q` begins a proof by complete (also known as ‘course-of-values’) induction on M . The term M should occur free in the current goal.

Failure

If M does not parse into a term or does not occur free in the current goal.

Example

Suppose we wish to prove that every number not equal to one has a prime factor:

$$!n. \sim(n = 1) \implies ?p. \text{prime } p \wedge p \text{ divides } n$$

A natural way to prove this is by complete induction. Invoking `completeInduct_on 'n'` yields the goal

$$\begin{aligned} &\{ !m. m < n \implies \sim(m = 1) \implies ?p. \text{prime } p \wedge p \text{ divides } m \} \\ &?- \\ &\sim(n = 1) \implies ?p. \text{prime } p \wedge p \text{ divides } n \end{aligned}$$

See also

`bossLib.measureInduct_on`, `bossLib.Induct`, `bossLib.Induct_on`.

<code>concl</code>	<code>(Thm)</code>
--------------------	--------------------

```
concl : thm -> term
```

Synopsis

Returns the conclusion of a theorem.

Description

When applied to a theorem $A \vdash t$, the function `concl` returns t .

Failure

Never fails.

See also

`Thm.dest_thm`, `Thm.hyp`.

COND_CASES_TAC

(Tactic)

`COND_CASES_TAC : tactic`

Synopsis

Induces a case split on a conditional expression in the goal.

Description

`COND_CASES_TAC` searches for a conditional sub-term in the term of a goal, i.e. a sub-term of the form $p \Rightarrow u \mid v$, choosing one by its own criteria if there is more than one. It then induces a case split over p as follows:

$$\frac{A \quad ?- \quad t}{\text{COND_CASES_TAC} \quad A \quad u \quad \{p\} \quad ?- \quad t[u/(p \Rightarrow u \mid v)] \quad A \quad u \quad \{\sim p\} \quad ?- \quad t[v/(p \Rightarrow u \mid v)]}$$

where p is not a constant, and the term $p \Rightarrow u \mid v$ is free in t . Note that it both enriches the assumptions and inserts the assumed value into the conditional.

Failure

`COND_CASES_TAC` fails if there is no conditional sub-term as described above.

Example

For "x", "y", "z1" and "z2" of type ":", and "P: *->bool",

```
COND_CASES_TAC ([], "x = (P y => z1 | z2)");;
([(["P y"], "x = z1"); (["~P y"], "x = z2")], -) : subgoals
```

but it fails, for example, if "y" is not free in the term part of the goal:

```
COND_CASES_TAC ([], "!y. x = (P y => z1 | z2)");;
evaluation failed      COND_CASES_TAC
```

In contrast, `ASM_CASES_TAC` does not perform the replacement:

```
ASM_CASES_TAC "P y" ([], "x = (P y => z1 | z2)");;
  ([(["P y"], "x = (P y => z1 | z2)"); (["~P y"], "x = (P y => z1 | z2)"),
   -)
  : subgoals
```

Uses

Useful for case analysis and replacement in one step, when there is a conditional sub-term in the term part of the goal. When there is more than one such sub-term and one in particular is to be analyzed, `COND_CASES_TAC` cannot be depended on to choose the ‘desired’ one. It can, however, be used repeatedly to analyze all conditional sub-terms of a goal.

See also

`Tactic.ASM_CASES_TAC`, `Tactic.DISJ_CASES_TAC`, `Tactic.STRUCT_CASES_TAC`.

<code>COND_CONV</code>	<code>(Conv)</code>
------------------------	---------------------

`COND_CONV` : conv

Synopsis

Simplifies conditional terms.

Description

The conversion `COND_CONV` simplifies a conditional term " $c \Rightarrow u \mid v$ " if the condition c is either the constant `T` or the constant `F` or if the two terms u and v are equivalent up to alpha-conversion. The theorems returned in these three cases have the forms:

$$\vdash (T \Rightarrow u \mid v) = u$$

$$\vdash (F \Rightarrow u \mid v) = u$$

$$\vdash (c \Rightarrow u \mid u) = u$$

Failure

`COND_CONV` tm fails if tm is not a conditional " $c \Rightarrow u \mid v$ ", where c is `T` or `F`, or u and v are alpha-equivalent.

COND_CONV

(reduceLib)

COND_CONV : conv

Synopsis

Simplifies certain conditional expressions.

Description

If t_m corresponds to one of the forms given below, where b has type `bool` and t_1 and t_2 have the same type, then `COND_CONV t_m` returns the corresponding theorem. Note that in the last case the arms need only be alpha-equivalent rather than strictly identical.

```
COND_CONV "F => t1 | t2" = |- (T => t1 | t2) = t2
COND_CONV "T => t1 | t2" = |- (T => t1 | t2) = t1
COND_CONV "b => t | t    " = |- (b => t | t) = t
```

Failure

`COND_CONV t_m` fails unless t_m has one of the forms indicated above.

Example

```
#COND_CONV "F => F | T";;
|- (F => F | T) = T
```

```
#COND_CONV "T => F | T";;
|- (T => F | T) = F
```

```
#COND_CONV "b => (\x. SUC x) | (\p. SUC p)";;
|- (b => (\x. SUC x) | (\p. SUC p)) = (\x. SUC x)
```

COND_ELIM_CONV

(Arith)

COND_ELIM_CONV : conv

Synopsis

Eliminates conditional statements from a formula.

Description

This function moves conditional statements up through a term and if at any point the branches of the conditional become Boolean-valued the conditional is eliminated. If the term is a formula, only an abstraction can prevent a conditional being moved up far enough to be eliminated.

Failure

Never fails.

Example

```
#COND_ELIM_CONV "!f n. f ((SUC n = 0) => 0 | (SUC n - 1)) < (f n) + 1";;
|- (!f n. (f((SUC n = 0) => 0 | (SUC n) - 1)) < ((f n) + 1)) =
  (!f n.
    (~(SUC n = 0) \\/ (f 0) < ((f n) + 1)) /\
    ((SUC n = 0) \\/ (f((SUC n) - 1)) < ((f n) + 1)))

#COND_ELIM_CONV "!f n. (\m. f ((m = 0) => 0 | (m - 1))) (SUC n) < (f n) + 1";;
|- (!f n. ((\m. f((m = 0) => 0 | m - 1))(SUC n)) < ((f n) + 1)) =
  (!f n. ((\m. ((m = 0) => f 0 | f(m - 1)))(SUC n)) < ((f n) + 1))
```

Uses

Useful as a preprocessor to decision procedures which do not allow conditional statements in their argument formula.

See also

Arith.SUB_AND_COND_ELIM_CONV.

COND_REWR_CANON	(Cond_rewrite)
-----------------	----------------

COND_REWR_CANON : thm -> thm

Synopsis

Transform a theorem into a form accepted by COND_REWR_TAC.

Description

COND_REWR_CANON transforms a theorem into a form accepted by COND_REWR_TAC. The input theorem should be an implication of the following form

$$\begin{aligned} & !x_1 \dots x_n. P_1[x_i] \implies \dots \implies !y_1 \dots y_m. Pr[x_i, y_i] \implies \\ & (!z_1 \dots z_k. u[x_i, y_i, z_i] = v[x_i, y_i, z_i]) \end{aligned}$$

where each antecedent P_i itself may be a conjunction or disjunction. The output theorem will have all universal quantifications moved to the outer most level with possible renaming to prevent variable capture, and have all antecedents which are a conjunction transformed to implications. The output theorem will be in the following form

$$\begin{aligned} & !x_1 \dots x_n y_1 \dots y_m z_1 \dots z_k. \\ & P_{11}[x_i] \implies \dots \implies P_{1p}[x_i] \implies \dots \implies \\ & Pr_1[x_i, y_i] \implies \dots \implies Pr_q[x_1, y_i] \implies (u[x_i, y_i, z_i] = v[x_i, y_i, z_i]) \end{aligned}$$

Failure

This function fails if the input theorem is not in the correct form.

Example

COND_REWR_CANON transforms the built-in theorem CANCEL_SUB into the form for conditional rewriting:

```
#COND_REWR_CANON CANCEL_SUB;;
Theorem CANCEL_SUB autoloading from theory 'arithmetic' ...
CANCEL_SUB = |- !p n m. p <= n /\ p <= m ==> ((n - p = m - p) = (n = m))

|- !p n m. p <= n ==> p <= m ==> ((n - p = m - p) = (n = m))
```

See also

Cond_rewrite.COND_REWRITE1_TAC, Cond_rewrite.COND_REWR_TAC,
Cond_rewrite.COND_REWRITE1_CONV, Cond_rewrite.COND_REWR_CONV,
Cond_rewrite.search_top_down.

COND_REWR_CONV

(Cond_rewrite)

```
COND_REWR_CONV : ((term -> term ->
  ((term # term) list # (type # type) list) list) -> thm -> conv)
```

Synopsis

A lower level conversion implementing simple conditional rewriting.

Description

`COND_REWR_CONV` is one of the basic building blocks for the implementation of the simple conditional rewriting conversions in the HOL system. In particular, the conditional term replacement or rewriting done by all the conditional rewriting conversions in this library is ultimately done by applications of `COND_REWR_CONV`. The description given here for `COND_REWR_CONV` may therefore be taken as a specification of the atomic action of replacing equals by equals in a term under certain conditions that are used in all these higher level conditional rewriting conversions.

The first argument to `COND_REWR_CONV` is expected to be a function which returns a list of matches. Each of these matches is in the form of the value returned by the built-in function `match`. It is used to search the input term for instances which may be rewritten.

The second argument to `COND_REWR_CONV` is expected to be an implicative theorem in the following form:

$$A \mid - !x_1 \dots x_n. P_1 ==> \dots P_m ==> (Q[x_1, \dots, x_n] = R[x_1, \dots, x_n])$$

where x_1, \dots, x_n are all the variables that occur free in the left hand side of the conclusion of the theorem but do not occur free in the assumptions.

The last argument to `COND_REWR_CONV` is the term to be rewritten.

If fn is a function and th is an implicative theorem of the kind shown above, then `COND_REWR_CONV fn th` will be a conversion. When applying to a term tm , it will return a theorem

$$P_1', \dots, P_m' \mid - tm = tm[R'/Q']$$

if evaluating $fn \ Q[x_1, \dots, x_n] \ tm$ returns a non-empty list of matches. The assumptions of the resulting theorem are instances of the antecedents of the input theorem th . The right hand side of the equation is obtained by rewriting the input term tm with instances of the conclusion of the input theorem.

Failure

`COND_REWR_CONV fn th` fails if th is not an implication of the form described above. If th is such an equation, but the function fn returns a null list of matches, or the function fn returns a non-empty list of matches, but the term or type instantiation fails.

Example

The following example illustrates a straightforward use of `COND_REWR_CONV`. We use the built-in theorem `LESS_MOD` as the input theorem, and the function `search_top_down` as the search function.

```
#LESS_MOD;;
Theorem LESS_MOD autoloading from theory 'arithmetic' ...
LESS_MOD = |- !n k. k < n ==> (k MOD n = k)
```



```

|- !n k. k < n ==> (k MOD n = k)

#search_top_down;;
- : (term -> term -> ((term # term) list # (type # type) list) list)

#COND_REWR_CONV search_top_down LESS_MOD "2 MOD 3";;
2 < 3 |- 2 MOD 3 = 2

```

See also

Cond_rewrite.COND_REWR_TAC, Cond_rewrite.COND_REWRITE1_TAC,
 Cond_rewrite.COND_REWRITE1_CONV, Cond_rewrite.COND_REWR_CANON,
 Cond_rewrite.search_top_down.

COND_REWR_TAC	(Cond_rewrite)
---------------	----------------

```

COND_REWR_TAC :
  (term -> term -> ((term * term) list * (type * type) list) list) ->
  thm_tactic

```

Synopsis

A lower level tactic used to implement simple conditional rewriting tactic.

Description

COND_REWR_TAC is one of the basic building blocks for the implementation of conditional rewriting in the HOL system. In particular, the conditional term replacement or rewriting done by all the built-in conditional rewriting tactics is ultimately done by applications of COND_REWR_TAC. The description given here for COND_REWR_TAC may therefore be taken as a specification of the atomic action of replacing equals by equals in the goal under certain conditions that are used in all these higher level conditional rewriting tactics.

The first argument to COND_REWR_TAC is expected to be a function which returns a list of matches. Each of these matches is in the form of the value returned by the built-in function `match`. It is used to search the goal for instances which may be rewritten.

The second argument to COND_REWR_TAC is expected to be an implicative theorem in the following form:

$$A \text{ |- } !x_1 \dots x_n. P_1 \implies \dots P_m \implies (Q[x_1, \dots, x_n] = R[x_1, \dots, x_n])$$

where x_1, \dots, x_n are all the variables that occur free in the left-hand side of the conclusion of the theorem but do not occur free in the assumptions.

If fn is a function and th is an implicative theorem of the kind shown above, then `COND_REWR_TAC fn th` will be a tactic which returns a list of subgoals if evaluating

$$fn \ Q[x_1, \dots, x_n] \ g1$$

returns a non-empty list of matches when applied to a goal $(asm, g1)$.

Let $m1$ be the match list returned by evaluating $fn \ Q[x_1, \dots, x_n] \ g1$. Each element in this list is in the form of

$$([(e_1, x_1); \dots; (e_p, x_p)], [(ty_1, vty_1); \dots; (ty_q, vty_q)])$$

which specifies the term and type instantiations of the input theorem th . Either the term pair list or the type pair list may be empty. In the case that both lists are empty, an exact match is found, i.e., no instantiation is required. If $m1$ is an empty list, no match has been found and the tactic will fail.

For each match in $m1$, `COND_REWR_TAC` will perform the following: 1) instantiate the input theorem th to get

$$th' = A \ |- \ P_1' \ ==> \ \dots \ ==> \ P_m' \ ==> \ (Q' = R')$$

where the primed subterms are instances of the corresponding unprimed subterms obtained by applying `INST_TYPE` with $[(ty_1, vty_1); \dots; (ty_q, vty_q)]$ and then `INST` with $[(e_1, x_1); \dots; (e_p, x_p)]$; 2) search the assumption list asm for occurrences of any antecedents P_1', \dots, P_m' ; 3) if all antecedents appear in asm , the goal $g1$ is reduced to $g1'$ by substituting R' for each free occurrence of Q' , otherwise, in addition to the substitution, all antecedents which do not appear in asm are added to it and new subgoals corresponding to these antecedents are created. For example, if P_k', \dots, P_m' do not appear in asm , the following subgoals are returned:

$$asm \ ?- \ P_k' \ \dots \ asm \ ?- \ P_m' \ \ \{\{asm, P_k', \dots, P_m'\}\} \ ?- \ g1'$$

If `COND_REWR_TAC` is given a theorem th :

$$A \ |- \ !x_1 \ \dots \ x_n \ y_1 \ \dots \ y_k. \ P_1 \ ==> \ \dots \ ==> \ P_m \ ==> \ (Q = R)$$

where the variables y_1, \dots, y_m do not occur free in the left-hand side of the conclusion Q but they do occur free in the antecedents, then, when carrying out Step 2 described above, `COND_REWR_TAC` will attempt to find instantiations for these variables from the assumption asm . For example, if x_1 and y_1 occur free in P_1 , and a match is found in which e_1 is an instantiation of x_1 , then P_1' will become $P_1[e_1/x_1, y_1]$. If a term $P_1'' = P_1[e_1, e_1'/x_1, y_1]$ appears in asm , th' is instantiated with (e_1', y_1) to get

$$th'' = A \ |- \ P_1'' \ ==> \ \dots \ ==> \ P_m'' \ ==> \ (Q' = R'')$$

then R' is substituted into g_1 for all free occurrences of Q' . If no consistent instantiation is found, then P_1' which contains the uninstantiated variable y_1 will become one of the new subgoals. In such a case, the user has no control over the choice of the variable y_i .

Failure

COND_REWR_TAC fn th fails if th is not an implication of the form described above. If th is such an equation, but the function fn returns a null list of matches, or the function fn returns a non-empty list of matches, but the term or type instantiation fails.

Example

The following example illustrates a straightforward use of COND_REWR_TAC. We use the built-in theorem LESS_MOD as the input theorem, and the function search_top_down as the search function.

```
#LESS_MOD;;
Theorem LESS_MOD autoloading from theory 'arithmetic' ...
LESS_MOD = |- !n k. k < n ==> (k MOD n = k)

|- !n k. k < n ==> (k MOD n = k)

#search_top_down;;
- : (term -> term -> ((term # term) list # (type # type) list) list)
```

We set up a goal

```
#g"2 MOD 3 = 2";;
"2 MOD 3 = 2"

() : void
```

and then apply the tactic

```
#e(COND_REWR_TAC search_top_down LESS_MOD);;
OK..
2 subgoals
"2 = 2"
  [ "2 < 3" ]

"2 < 3"

() : void
```

See also

Cond_rewrite.COND_REWRITE1_TAC, Cond_rewrite.COND_REWRITE1_CONV,
 Cond_rewrite.COND_REWR_CONV, Cond_rewrite.COND_REWR_CANON,
 Cond_rewrite.search_top_down.

COND_REWRITE1_CONV	(Cond_rewrite)
--------------------	----------------

COND_REWRITE1_CONV : thm list -> thm -> conv

Synopsis

A simple conditional rewriting conversion.

Description

COND_REWRITE1_CONV is a front end of the conditional rewriting conversion COND_REWR_CONV. The input theorem should be in the following form

$$A \mid - !x_1 \dots . P_1 ==> \dots !x_m \dots . P_m ==> (!x \dots . Q = R)$$

where each antecedent P_i itself may be a conjunction or disjunction. This theorem is transformed to a standard form expected by COND_REWR_CONV which carries out the actual rewriting. The transformation is performed by COND_REWR_CANON. The search function passed to COND_REWR_CONV is search_top_down. The effect of applying the conversion COND_REWRITE1_CONV ths th to a term tm is to derive a theorem

$$A' \mid - tm = tm[R'/Q']$$

where the right hand side of the equation is obtained by rewriting the input term tm with an instance of the conclusion of the input theorem. The theorems in the list ths are used to discharge the assumptions generated from the antecedents of the input theorem.

Failure

COND_REWRITE1_CONV ths th fails if th cannot be transformed into the required form by COND_REWR_CANON. Otherwise, it fails if no match is found or the theorem cannot be instantiated.

Example

The following example illustrates a straightforward use of COND_REWRITE1_CONV. We use the built-in theorem LESS_MOD as the input theorem.

```

#LESS_MOD;;
Theorem LESS_MOD autoloading from theory 'arithmetic' ...
LESS_MOD = |- !n k. k < n ==> (k MOD n = k)

|- !n k. k < n ==> (k MOD n = k)

#COND_REWRITE1_CONV [] LESS_MOD "2 MOD 3";;
2 < 3 |- 2 MOD 3 = 2

#let less_2_3 = REWRITE_RULE[LESS_MONO_EQ;LESS_0]
#(REDEPTH_CONV num_CONV "2 < 3");;
less_2_3 = |- 2 < 3

#COND_REWRITE1_CONV [less_2_3] LESS_MOD "2 MOD 3";;
|- 2 MOD 3 = 2

```

In the first example, an empty theorem list is supplied to `COND_REWRITE1_CONV` so the resulting theorem has an assumption `2 < 3`. In the second example, a list containing a theorem `|- 2 < 3` is supplied, the resulting theorem has no assumptions.

See also

`Cond_rewrite.COND_REWR_TAC`, `Cond_rewrite.COND_REWRITE1_TAC`,
`Cond_rewrite.COND_REWR_CONV`, `Cond_rewrite.COND_REWR_CANON`,
`Cond_rewrite.search_top_down`.

COND_REWRITE1_TAC	(Cond_rewrite)
-------------------	----------------

`COND_REWRITE1_TAC` : `thm_tactic`

Synopsis

A simple conditional rewriting tactic.

Description

`COND_REWRITE1_TAC` is a front end of the conditional rewriting tactic `COND_REWR_TAC`. The input theorem should be in the following form

$$A \text{ |- } !x_1 \dots . P_1 \implies \dots !x_m \dots . P_m \implies (!x \dots . Q = R)$$

where each antecedent P_i itself may be a conjunction or disjunction. This theorem is transformed to a standard form expected by `COND_REWR_TAC` which carries out the actual rewriting. The transformation is performed by `COND_REWR_CANON`. The search function passed to `COND_REWR_TAC` is `search_top_down`. The effect of applying this tactic is to substitute into the goal instances of the right hand side of the conclusion of the input theorem R_i' for the corresponding instances of the left hand side. The search is top-down left-to-right. All matches found by the search function are substituted. New subgoals corresponding to the instances of the antecedents which do not appear in the assumption of the original goal are created. See manual page of `COND_REWR_TAC` for details of how the instantiation and substitution are done.

Failure

`COND_REWRITE1_TAC th` fails if `th` cannot be transformed into the required form by the function `COND_REWR_CANON`. Otherwise, it fails if no match is found or the theorem cannot be instantiated.

Example

The following example illustrates a straightforward use of `COND_REWRITE1_TAC`. We use the built-in theorem `LESS_MOD` as the input theorem.

```
#LESS_MOD;;
Theorem LESS_MOD autoloading from theory 'arithmetic' ...
LESS_MOD = |- !n k. k < n ==> (k MOD n = k)

|- !n k. k < n ==> (k MOD n = k)
```

We set up a goal

```
#g"2 MOD 3 = 2";;
"2 MOD 3 = 2"
```

```
() : void
```

and then apply the tactic

```
#e(COND_REWRITE1_TAC LESS_MOD);;
OK..
2 subgoals
"2 = 2"
  [ "2 < 3" ]

"2 < 3"

() : void
```

See also

Cond_rewrite.COND_REWR_TAC, Cond_rewrite.COND_REWRITE1_CONV,
 Cond_rewrite.COND_REWR_CONV, Cond_rewrite.COND_REWR_CANON,
 Cond_rewrite.search_top_down.

conditional

(boolSyntax)

conditional : term

Synopsis

Constant denoting conditional expressions.

Description

The ML variable `boolSyntax.conditional` is bound to the term `bool$COND`.

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`,
`boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`,
`boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.bool_case`,
`boolSyntax.let_tm`, `boolSyntax.arb`.

Cong

(simpLib)

Cong : thm -> thm

Synopsis

Marks a theorem as a congruence rule for the simplifier.

Description

The `Cong` function marks (or "tags") a theorem so that when passed to the simplifier, it is not used as a rewrite, but rather as a congruence rule. This is a simpler way of adding a congruence rule to the simplifier than using the underlying `SSFRAG` function.

Failure

Never fails. On the other hand, `Cong` does not check that the theorem passed as an argument is a valid congruence rule, and invalid congruence rules may have unpredictable effects on the behaviour of the simplifier.

Example

```

- SIMP_CONV pure_ss [] ‘‘!x::P. x IN P /\ Q x’’;
<<HOL message: inventing new type variable names: 'a>>
! Uncaught exception:
! UNCHANGED
- RES_FORALL_CONG;
> val it =
  |- (P = Q) ==>
    (!x. x IN Q ==> (f x = g x)) ==>
      (RES_FORALL P f = RES_FORALL Q g) : thm
- SIMP_CONV pure_ss [Cong RES_FORALL_CONG] ‘‘!x::P. x IN P’’;
<<HOL message: inventing new type variable names: 'a>>
> val it = |- (!x::P. x IN P /\ Q x) = !x::P. T /\ Q x : thm

```

(Note that RES_FORALL_CONG is already included in bool_ss and all simpsets built on it.)

See also

simpLib.SSFRAG.

CONJ	(Thm)
------	-------

CONJ : thm -> thm -> thm

Synopsis

Introduces a conjunction.

Description

$$\begin{array}{l}
 A1 \text{ |- } t1 \qquad A2 \text{ |- } t2 \\
 \hline
 A1 \text{ u } A2 \text{ |- } t1 \text{ /\ } t2
 \end{array}
 \quad \text{CONJ}$$

Failure

Never fails.

Comments

The theorem AND_INTRO_THM can be instantiated to similar effect.

See also

Drule.BODY_CONJUNCTS, Thm.CONJUNCT1, Thm.CONJUNCT2, Drule.CONJ_PAIR, Drule.LIST_CONJ, Drule.CONJ_LIST, Drule.CONJUNCTS.

CONJ_DISCH

(Drule)

CONJ_DISCH : (term -> thm -> thm)

Synopsis

Discharges an assumption and conjoins it to both sides of an equation.

Description

Given an term t and a theorem $A \vdash t_1 = t_2$, which is an equation between boolean terms, CONJ_DISCH returns $A - \{t\} \vdash (t \wedge t_1) = (t \wedge t_2)$, i.e. conjoins t to both sides of the equation, removing t from the assumptions if it was there.

$$\frac{A \vdash t_1 = t_2}{A - \{t\} \vdash t \wedge t_1 = t \wedge t_2} \quad \text{CONJ_DISCH "t"}$$

Failure

Fails unless the theorem is an equation, both sides of which, and the term provided are of type `bool`.

See also

`Drule.CONJ_DISCHL`.

CONJ_DISCHL

(Drule)

CONJ_DISCHL : (term list -> thm -> thm)

Synopsis

Conjoins multiple assumptions to both sides of an equation.

Description

Given a term list $[t_1; \dots; t_n]$ and a theorem whose conclusion is an equation between boolean terms, CONJ_DISCHL conjoins all the terms in the list to both sides of the equation, and removes any of the terms which were in the assumption list.

$$\frac{A \vdash s = t}{A - \{t_1, \dots, t_n\} \vdash (t_1 \wedge \dots \wedge t_n \wedge s) = (t_1 \wedge \dots \wedge t_n \wedge t)} \quad \text{CONJ_DISCHL [t1, \dots, tn]}$$

Failure

Fails unless the theorem is an equation, both sides of which, and all the terms provided, are of type `bool`.

See also

`Drule.CONJ_DISCH`.

CONJ_FORALL_CONV	(unwindLib)
-------------------------	--------------------

`CONJ_FORALL_CONV : conv`

Synopsis

Moves universal quantifiers up through a tree of conjunctions.

Description

`CONJ_FORALL_CONV "(!x1 ... xm. t1) /\ ... /\ (!x1 ... xm. tn)"` returns the following theorem:

$$\begin{array}{l} |- (!x1 \dots xm. t1) /\ \dots /\ (!x1 \dots xm. tn) = \\ \quad !x1 \dots xm. t1 /\ \dots /\ tn \end{array}$$

where the original term can be an arbitrary tree of conjunctions. The structure of the tree is retained in both sides of the equation.

Failure

Never fails.

Example

```
#CONJ_FORALL_CONV "((!(x:*) (y:*) (z:*) . a) /\ (!(x:*) (y:*) (z:*) . b)) /\
#
                    (!(x:*) (y:*) (z:*) . c)";;
|- ((!x y z . a) /\ (!x y z . b)) /\ (!x y z . c) = (!x y z . (a /\ b) /\ c)
```

```
#CONJ_FORALL_CONV "T";;
|- T = T
```

```
#CONJ_FORALL_CONV "((!(x:*) (y:*) (z:*) . a) /\ (!(x:*) (w:*) (z:*) . b)) /\
#
                    (!(x:*) (y:*) (z:*) . c)";;
|- ((!x y z . a) /\ (!x w z . b)) /\ (!x y z . c) =
    (!x . ((!y z . a) /\ (!w z . b)) /\ (!y z . c))
```

See also

unwindLib.FORALL_CONJ_CONV, unwindLib.CONJ_FORALL_ONCE_CONV,
 unwindLib.FORALL_CONJ_ONCE_CONV, unwindLib.CONJ_FORALL_RIGHT_RULE,
 unwindLib.FORALL_CONJ_RIGHT_RULE.

<div data-bbox="161 564 767 613" data-label="Text"> <p>CONJ_FORALL_ONCE_CONV</p> </div>	<div data-bbox="1011 564 1331 613" data-label="Text"> <p>(unwindLib)</p> </div>
---	---

CONJ_FORALL_ONCE_CONV : conv

Synopsis

Moves a single universal quantifier up through a tree of conjunctions.

Description

CONJ_FORALL_ONCE_CONV "(!x. t1) /\ ... /\ (!x. tn)" returns the theorem:

$$\vdash (!x. t1) /\ \dots /\ (!x. tn) = !x. t1 /\ \dots /\ tn$$

where the original term can be an arbitrary tree of conjunctions. The structure of the tree is retained in both sides of the equation.

Failure

Fails if the argument term is not of the required form. The term need not be a conjunction, but if it is every conjunct must be universally quantified with the same variable.

Example

```
#CONJ_FORALL_ONCE_CONV "((!x. x \\/ a) /\ (!x. x \\/ b)) /\ (!x. x \\/ c)";;
|- ((!x. x \\/ a) /\ (!x. x \\/ b)) /\ (!x. x \\/ c) =
  (!x. ((x \\/ a) /\ (x \\/ b)) /\ (x \\/ c))
```

```
#CONJ_FORALL_ONCE_CONV "!x. x \\/ a";;
|- (!x. x \\/ a) = (!x. x \\/ a)
```

```
#CONJ_FORALL_ONCE_CONV "((!x. x \\/ a) /\ (!y. y \\/ b)) /\ (!x. x \\/ c)";;
evaluation failed      CONJ_FORALL_ONCE_CONV
```

See also

unwindLib.FORALL_CONJ_ONCE_CONV, unwindLib.CONJ_FORALL_CONV,
 unwindLib.FORALL_CONJ_CONV, unwindLib.CONJ_FORALL_RIGHT_RULE,
 unwindLib.FORALL_CONJ_RIGHT_RULE.

CONJ_FORALL_RIGHT_RULE	(unwindLib)
------------------------	-------------

```
CONJ_FORALL_RIGHT_RULE : (thm -> thm)
```

Synopsis

Moves universal quantifiers up through a tree of conjunctions.

Description

$$\frac{A \mid- !z1 \dots zr. \quad t = ?y1 \dots yp. (!x1 \dots xm. t1) \wedge \dots \wedge (!x1 \dots xm. tn)}{A \mid- !z1 \dots zr. t = ?y1 \dots yp. !x1 \dots xm. t1 \wedge \dots \wedge tn}$$

Failure

Fails if the argument theorem is not of the required form, though either or both of r and p may be zero.

See also

unwindLib.FORALL_CONJ_RIGHT_RULE, unwindLib.CONJ_FORALL_CONV,
unwindLib.FORALL_CONJ_CONV, unwindLib.CONJ_FORALL_ONCE_CONV,
unwindLib.FORALL_CONJ_ONCE_CONV.

CONJ_LIST	(Drule)
-----------	---------

```
CONJ_LIST : (int -> thm -> thm list)
```

Synopsis

Extracts a list of conjuncts from a theorem (non-flattening version).

Description

CONJ_LIST is the proper inverse of LIST_CONJ. Unlike CONJUNCTS which recursively splits as many conjunctions as possible both to the left and to the right, CONJ_LIST splits the top-level conjunction and then splits (recursively) only the right conjunct. The integer argument is required because the term tn may itself be a conjunction. A list of n theorems is returned.

$$\frac{A \vdash t_1 \wedge (t_2 \wedge (\dots \wedge t_n) \dots)}{A \vdash t_1 \quad A \vdash t_2 \quad \dots \quad A \vdash t_n} \text{CONJ_LIST } n \ (A \vdash t_1 \wedge \dots \wedge t_n)$$

Failure

Fails if the integer argument (n) is less than one, or if the input theorem has less than n conjuncts.

Example

Suppose the identifier `th` is bound to the theorem:

$$A \vdash (x \wedge y) \wedge z \wedge w$$

Here are some applications of `CONJ_LIST` to `th`:

```
- CONJ_LIST 0 th;
! Uncaught exception:
! HOL_ERR

- CONJ_LIST 1 th;
> val it = [[A] |- (x /\ y) /\ z /\ w] : thm list

- CONJ_LIST 2 th;
> val it = [ [A] |- x /\ y, [A] |- z /\ w ] : thm list

- CONJ_LIST 3 th;
> val it = [ [A] |- x /\ y, [A] |- z, [A] |- w ] : thm list

- CONJ_LIST 4 th;
! Uncaught exception:
! HOL_ERR
```

See also

`Drule.BODY_CONJUNCTS`, `Drule.LIST_CONJ`, `Drule.CONJUNCTS`, `Thm.CONJ`, `Thm.CONJUNCT1`, `Thm.CONJUNCT2`, `Drule.CONJ_PAIR`.

CONJ_PAIR	(Drule)
------------------	----------------

`CONJ_PAIR` : `thm -> thm * thm`

Synopsis

Extracts both conjuncts of a conjunction.

Description

$$\frac{A \mid\text{- } t1 \wedge t2}{A \mid\text{- } t1 \quad A \mid\text{- } t2} \text{ CONJ_PAIR}$$

The two resultant theorems are returned as a pair.

Failure

Fails if the input theorem is not a conjunction.

See also

Drule.BODY_CONJUNCTS, Thm.CONJUNCT1, Thm.CONJUNCT2, Thm.CONJ, Drule.LIST_CONJ, Drule.CONJ_LIST, Drule.CONJUNCTS.

<div data-bbox="236 1097 474 1149" data-label="Text">CONJ_TAC</div>	<div data-bbox="1171 1097 1414 1149" data-label="Text">(Tactic)</div>
--	--

CONJ_TAC : tactic

Synopsis

Reduces a conjunctive goal to two separate subgoals.

Description

When applied to a goal $A \text{ ?- } t1 \wedge t2$, the tactic CONJ_TAC reduces it to the two subgoals corresponding to each conjunct separately.

$$\frac{A \text{ ?- } t1 \wedge t2}{A \text{ ?- } t1 \quad A \text{ ?- } t2} \text{ CONJ_TAC}$$

Failure

Fails unless the conclusion of the goal is a conjunction.

See also

Tactic.STRIP_TAC.

CONJUNCT1

(Thm)

CONJUNCT1 : thm -> thm

Synopsis

Extracts left conjunct of theorem.

Description

$$\frac{A \vdash t1 \wedge t2}{A \vdash t1} \text{ CONJUNCT1}$$
Failure

Fails unless the input theorem is a conjunction.

Comments

The theorem AND1_THM can be instantiated to similar effect.

See also

Drule.BODY_CONJUNCTS, Thm.CONJUNCT2, Drule.CONJ_PAIR, Thm.CONJ, Drule.LIST_CONJ, Drule.CONJ_LIST, Drule.CONJUNCTS.

CONJUNCT2

(Thm)

CONJUNCT2 : thm -> thm

Synopsis

Extracts right conjunct of theorem.

Description

$$\frac{A \vdash t1 \wedge t2}{A \vdash t2} \text{ CONJUNCT2}$$

Failure

Fails unless the input theorem is a conjunction.

Comments

The theorem `AND2_THM` can be instantiated to similar effect.

See also

`Drule.BODY_CONJUNCTS`, `Thm.CONJUNCT1`, `Drule.CONJ_PAIR`, `Thm.CONJ`, `Drule.LIST_CONJ`, `Drule.CONJ_LIST`, `Drule.CONJUNCTS`.

<code>conjunction</code>	<code>(boolSyntax)</code>
--------------------------	---------------------------

`conjunction` : term

Synopsis

Constant denoting logical conjunction.

Description

The ML variable `boolSyntax.conjunction` is bound to the term `bool$/\`.

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`, `boolSyntax.disjunction`, `boolSyntax.negation`, `boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let_tm`, `boolSyntax.arb`.

<code>CONJUNCTS</code>	<code>(Drule)</code>
------------------------	----------------------

`CONJUNCTS` : (thm -> thm list)

Synopsis

Recursively splits conjunctions into a list of conjuncts.

Description

Flattens out all conjuncts, regardless of grouping. Returns a singleton list if the input theorem is not a conjunction.

$$\frac{A \vdash t_1 \wedge t_2 \wedge \dots \wedge t_n}{A \vdash t_1 \quad A \vdash t_2 \quad \dots \quad A \vdash t_n} \text{ CONJUNCTS}$$
Failure

Never fails.

Example

Suppose the identifier `th` is bound to the theorem:

$$A \vdash (x \wedge y) \wedge z \wedge w$$

Application of `CONJUNCTS` to `th` returns the following list of theorems:

$$[A \vdash x; A \vdash y; A \vdash z; A \vdash w] : \text{thm list}$$
See also

`Drule.BODY_CONJUNCTS`, `Drule.CONJ_LIST`, `Drule.LIST_CONJ`, `Thm.CONJ`, `Thm.CONJUNCT1`, `Thm.CONJUNCT2`, `Drule.CONJ_PAIR`.

CONJUNCTS_AC	(Drule)
---------------------	----------------

`CONJUNCTS_AC : term * term -> thm`

Synopsis

Prove equivalence under idempotence, symmetry and associativity of conjunction.

Description

`CONJUNCTS_AC` takes a pair of terms (`t1`, `t2`) and proves `|- t1 = t2` if `t1` and `t2` are equivalent up to idempotence, symmetry and associativity of conjunction. That is, if `t1` and `t2` are two (different) arbitrarily-nested conjunctions of the same set of terms, then `CONJUNCTS_AC (t1,t2)` returns `|- t1 = t2`. Otherwise, it fails.

Failure

Fails if `t1` and `t2` are not equivalent, as described above.

Example

```
- CONJUNCTS_AC (Term '(P /\ Q) /\ R', Term 'R /\ (Q /\ R) /\ P');
> val it = |- (P /\ Q) /\ R = R /\ (Q /\ R) /\ P : thm
```

Uses

Used to reorder a conjunction. First sort the conjuncts in a term t_1 into the desired order (e.g., lexicographic order, for normalization) to get a new term t_2 , then call `CONJUNCTS_AC(t1,t2)`.

See also

`Drule.DISJUNCTS_AC`.

CONJUNCTS_THEN	(Thm_cont)
-----------------------	-------------------

`CONJUNCTS_THEN : thm_tactical`

Synopsis

Applies a theorem-tactic to each conjunct of a theorem.

Description

`CONJUNCTS_THEN` takes a theorem-tactic f , and a theorem t whose conclusion must be a conjunction. `CONJUNCTS_THEN` breaks t into two new theorems, t_1 and t_2 which are `CONJUNCT1` and `CONJUNCT2` of t respectively, and then returns a new tactic: $f \ t_1 \ \text{THEN} \ f \ t_2$. That is,

$$\text{CONJUNCTS_THEN } f \ (A \ |- \ l \ /\ \ r) = f \ (A \ |- \ l) \ \text{THEN} \ f \ (A \ |- \ r)$$

so if

$\begin{array}{l} A1 \ ?- \ t1 \\ \text{=====} \\ f \ (A \ - \ l) \\ A2 \ ?- \ t2 \end{array}$	$\begin{array}{l} A2 \ ?- \ t2 \\ \text{=====} \\ f \ (A \ - \ r) \\ A3 \ ?- \ t3 \end{array}$
---	---

then

$$\begin{array}{l} A1 \ ?- \ t1 \\ \text{=====} \\ \text{CONJUNCTS_THEN } f \ (A \ |- \ l \ /\ \ r) \\ A3 \ ?- \ t3 \end{array}$$
Failure

`CONJUNCTS_THEN f` will fail if applied to a theorem whose conclusion is not a conjunction.

Comments

`CONJUNCTS_THEN f (A |- u1 /\ ... /\ un)` results in the tactic:

```
f (A |- u1) THEN f (A |- u2 /\ ... /\ un)
```

Unfortunately, it is more likely that the user had wanted the tactic:

```
f (A |- u1) THEN ... THEN f(A |- un)
```

Such a tactic could be defined as follows:

```
let CONJUNCTS_THENL (f:thm_tactic) thm =
  itlist $THEN (map f (CONJUNCTS thm)) ALL_TAC;;
```

or by using REPEAT_TCL.

See also

Thm.CONJUNCT1, Thm.CONJUNCT2, Drule.CONJUNCTS, Tactic.CONJ_TAC,
Thm.cont.CONJUNCTS_THEN2, Thm.cont.STRIP_THM_THEN.

CONJUNCTS_THEN2	(Thm_cont)
-----------------	------------

```
CONJUNCTS_THEN2 : (thm_tactic -> thm_tactic -> thm_tactic)
```

Synopsis

Applies two theorem-tactics to the corresponding conjuncts of a theorem.

Description

CONJUNCTS_THEN2 takes two theorem-tactics, f_1 and f_2 , and a theorem t whose conclusion must be a conjunction. CONJUNCTS_THEN2 breaks t into two new theorems, t_1 and t_2 which are CONJUNCT1 and CONJUNCT2 of t respectively, and then returns the tactic $f_1 t_1$ THEN $f_2 t_2$. Thus

```
CONJUNCTS_THEN2 f1 f2 (A |- l /\ r) = f1 (A |- l) THEN f2 (A |- r)
```

so if

<pre>A1 ?- t1 ===== f1 (A - l)</pre>	<pre>A2 ?- t2 ===== f2 (A - r)</pre>
<pre>A2 ?- t2</pre>	<pre>A3 ?- t3</pre>

then

```
A1 ?- t1
===== CONJUNCTS_THEN2 f1 f2 (A |- l /\ r)
A3 ?- t3
```

Failure

CONJUNCTS_THEN *f* will fail if applied to a theorem whose conclusion is not a conjunction.

Comments

The system shows the type as (thm_tactic -> thm_tactical).

Uses

The construction of complex tacticals like CONJUNCTS_THEN.

See also

Thm.CONJUNCT1, Thm.CONJUNCT2, Drule.CONJUNCTS, Tactic.CONJ_TAC,
Thm.cont.CONJUNCTS_THEN2, Thm.cont.STRIP_THM_THEN.

<code>cons</code>	<code>(Lib)</code>
-------------------	--------------------

```
cons : 'a -> 'a list -> 'a list
```

Synopsis

Curried form of list cons operation

Description

In some programming situations it is handy to use the "cons" operation in a curried form. Although it is easy to code up on demand, the `cons` function is provided for convenience.

Failure

Never fails.

Example

```
- map (cons 1) [[],[2],[2,3]];
> val it = [[1], [1, 2], [1, 2, 3]] : int list list
```

<code>conseq_conv</code>	<code>(ConseqConv)</code>
--------------------------	---------------------------

```
type conseq_conv
```

Synopsis

A type for functions that given a term produce a theorem with an implication at the top level.

Description

Classical conversions (see `Conv`) convert a given term t to a term eqt that is equal to t . For a boolean term t , it is however sometimes useful not to preserve equivalence, but to either strengthen t to st or to weaken it to wt . The type `conseq_conv` is used for ML functions that perform these operations. These ML Functions are called *consequence conversions* in the following.

Given a consequence conversion `CONSEQ_CONV` and a term t , then `CONSEQ_CONV` can either fail with an `HOL_ERR`-exception, raise an `UNCHANGED`-exception or produce a theorem of one of the following forms:

1. $st \implies t$
2. $t \implies wt$
3. $t = eqt$

Example

Examples of simple consequence conversion are `TRUE_CONSEQ_CONV` and `FALSE_CONSEQ_CONV`.

See also

`ConseqConv.directed_conseq_conv`, `ConseqConv.TRUE_FALSE_REFL_CONSEQ_CONV`.

<div data-bbox="161 1319 769 1370" data-label="Text"> <p><code>CONSEQ_CONV_direction</code></p> </div>	<div data-bbox="984 1319 1331 1375" data-label="Text"> <p><code>(ConseqConv)</code></p> </div>
--	--

```
type CONSEQ_CONV_direction
```

Synopsis

A type used to tell directed consequence conversions what the desired result should look like.

Description

This type is used to instruct a directed consequence conversion how to behave. Given a direction `dir` and a boolean term t the result of a directed consequence conversion `DCONSEQ_CONV` should be of the form

- $st \implies t$ for `dir = CONSEQ_CONV_STRENGTHEN_direction`
- $t \implies wt$ for `dir = CONSEQ_CONV_WEAKEN_direction`
- $st \implies t$, $t \implies wt$ or $t = eqt$ for `dir = CONSEQ_CONV_UNKNOWN_direction`

See also

`ConseqConv.directed_conseq_conv`, `ConseqConv.TRUE_FALSE_REFL_CONSEQ_CONV`.

CONSEQ_CONV_TAC	(ConseqConv)
------------------------	---------------------

`CONSEQ_CONV_TAC` : `directed_conseq_conv` -> `tactic`

Synopsis

Reduces the goal using a consequence conversion.

Description

`CONSEQ_CONV_TAC` *c* tries to strengthen a goal *P* using *c* to a new goal *P'*. It then remains to show that *P'* holds.

See also

`Tactic.MATCH_MP_TAC`.

CONSEQ_REWRITE_CONV	(ConseqConv)
----------------------------	---------------------

`CONSEQ_REWRITE_CONV` : `(thm list * thm list * thm list)` -> `directed_conseq_conv`

Synopsis

Applies `CONSEQ_TOP_REWRITE_CONV` repeatedly at subterms.

Description

This directed consequence conversion is a combination of `CONSEQ_TOP_REWRITE_CONV` and `DEPTH_CONSEQ_CONV`. Given lists of theorems, these theorems are preprocessed to extract implications. Then these implications are used to either weaken or strengthen an input term.

Example

Reconsider the example for `DEPTH_CONSEQ_CONV`. Let `rewrite_every_thm` be the following theorem:

```
val rewrite_every_thm =
  |- FEVERY P FEMPTY /\
    (FEVERY P f /\ P (x,y) ==> FEVERY P (f |+ (x,y)));
```

Then the following call of `CONSEQ_REWRITE_CONV`

```
CONSEQ_REWRITE_CONV ([], [rewrite_every_thm], []) CONSEQ_CONV_STRENGTHEN_direction
  ‘‘!y2. FEVERY P (f |+ (x1, y1) |+ (x2,y2)) /\ Q z’’
```

results in

```
|- (!y2. ((FEVERY P f /\ P (x1, y1)) /\ P (x2,y2)) /\ Q z) ==>
  (!y2. FEVERY P (f |+ (x1, y1) |+ (x2,y2)) /\ Q z)
```

More examples can be found at the end of `ConseqConv.sml`.

See also

`Drule.MATCH_MP`, `ConseqConv.CONSEQ_TOP_REWRITE_CONV`,
`ConseqConv.DEPTH_CONSEQ_CONV`, `ConseqConv.EXT_CONSEQ_REWRITE_CONV`.

CONSEQ_TOP_REWRITE_CONV

(ConseqConv)

```
CONSEQ_TOP_REWRITE_CONV : (thm list * thm list * thm list) -> directed_conseq_conv
```

Synopsis

An extended version of `MATCH_MP`.

Description

This consequence conversion gets 3 lists of theorems as parameters: `both_thmL`, `strengthen_thmL` and `weaken_thmL`. The theorems in these lists are used to strengthen or weaken a given boolean term at toplevel. If using them for strengthening this consequence conversion behaves similar to `MATCH_MP`. As the names suggest, the theorems in `strengthen_thmL` are used for strengthening, the ones in `weaken_thmL` for weakening and the ones in `both_thmL` for both.

Before trying to apply the conversion, the theorem lists are preprocessed. The theorems are split along conjunctions and allquantification is removed. Then theorems with toplevel negation $\neg P$ are rewritten to $\neg P = F$. Afterwards every theorem $\neg P$ that is not an implication or an boolean equation is replaced by $\neg P = T$. Finally, boolean equations $\neg P = Q$ are splitted into two theorems $\neg P \implies Q$ and $\neg Q \implies P$. One ends up with a list of implications.

Given a term t the conversion tries to find a theorem $\neg P \implies Q$ and - depending on to the direction - strengthen t by matching it with Q or weaken it by matching it with P .

Example

This directed consequence conversion is intended to be used together with `DEPTH_CONSEQ_CONV`. The combination of both is called `CONSEQ_REWRITE_CONV`. Please have a look there for an example.

See also

`Drule.MATCH_MP`, `ConseqConv.CONSEQ_REWRITE_CONV`, `ConseqConv.DEPTH_CONSEQ_CONV`.

<div data-bbox="237 723 501 770" data-label="Text"> <p><code>constants</code></p> </div>	<div data-bbox="1173 719 1414 777" data-label="Text"> <p><code>(Theory)</code></p> </div>
--	---

```
constants : string -> term list
```

Synopsis

Returns a list of the constants defined in a named theory.

Description

The call

```
constants thy
```

where `thy` is an ancestor theory (the special string `"-"` means the current theory), returns a list of all the constants in that theory.

Failure

Fails if the named theory does not exist, or is not an ancestor of the current theory.

Example

```
- load "combinTheory";
> val it = () : unit

- constants "combin";
> val it = ['$o', 'W', 'S', 'K', 'I', 'combin$C'] : term list
```

See also

`Theory.types`, `Theory.current_axioms`, `Theory.current_definitions`, `Theory.current_theorems`.

CONTR

(Drule)

```
CONTR : term -> thm -> thm
```

Synopsis

Implements the intuitionistic contradiction rule.

Description

When applied to a term t and a theorem $A \vdash F$, the inference rule `CONTR` returns the theorem $A \vdash t$.

$$\begin{array}{l} A \vdash F \\ \text{-----} \quad \text{CONTR } t \\ A \vdash t \end{array}$$

Failure

Fails unless the term has type `bool` and the theorem has F as its conclusion.

See also

`Thm.CCONTR`, `Drule.CONTRAPOS`, `Tactic.CONTR_TAC`, `Thm.NOT_ELIM`.

CONTR_TAC

(Tactic)

```
CONTR_TAC : thm_tactic
```

Synopsis

Solves any goal from contradictory theorem.

Description

When applied to a contradictory theorem $A' \vdash F$, and a goal $A \text{ ?- } t$, the tactic `CONTR_TAC` completely solves the goal. This is an invalid tactic unless A' is a subset of A .

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \quad \text{CONTR_TAC } (A' \vdash F) \end{array}$$

Failure

Fails unless the theorem is contradictory, i.e. has F as its conclusion.

See also

Tactic.CHECK_ASSUME_TAC, Drule.CONTR, Thm.CCONTR, Drule.CONTRAPOS, Thm.NOT_ELIM.

<div data-bbox="236 600 501 647" data-label="Text"> <p style="font-size: 24pt; margin: 0;">CONTRAPOS</p> </div>	<div data-bbox="1203 600 1414 649" data-label="Text"> <p style="font-size: 24pt; margin: 0;">(Drule)</p> </div>
---	---

CONTRAPOS : (thm -> thm)

Synopsis

Deduces the contrapositive of an implication.

Description

When applied to a theorem $A \mid- s \implies t$, the inference rule CONTRAPOS returns its contrapositive, $A \mid- \sim t \implies \sim s$.

$$\frac{A \mid- s \implies t}{A \mid- \sim t \implies \sim s} \text{ CONTRAPOS}$$

Failure

Fails unless the theorem is an implication.

See also

Thm.CCONTR, Drule.CONTR, Conv.CONTRAPOS_CONV, Thm.NOT_ELIM.

<div data-bbox="236 1552 644 1603" data-label="Text"> <p style="font-size: 24pt; margin: 0;">CONTRAPOS_CONV</p> </div>	<div data-bbox="1230 1552 1414 1603" data-label="Text"> <p style="font-size: 24pt; margin: 0;">(Conv)</p> </div>
--	--

CONTRAPOS_CONV : conv

Synopsis

Proves the equivalence of an implication and its contrapositive.

Description

When applied to an implication $P \implies Q$, the conversion CONTRAPOS_CONV returns the theorem:

$\vdash (P \implies Q) = (\sim Q \implies \sim P)$

Failure

Fails if applied to a term that is not an implication.

See also

`Drule.CONTRAPOS`.

CONV_RULE	(Conv)
-----------	--------

`CONV_RULE : (conv -> thm -> thm)`

Synopsis

Makes an inference rule from a conversion.

Description

If `c` is a conversion, then `CONV_RULE c` is an inference rule that applies `c` to the conclusion of a theorem. That is, if `c` maps a term "`t`" to the theorem $\vdash t = t'$, then the rule `CONV_RULE c` infers $\vdash t'$ from the theorem $\vdash t$. More precisely, if `c "t"` returns `A' $\vdash t = t'$` , then:

$$\frac{A \vdash t}{A \cup A' \vdash t'} \text{ CONV_RULE } c$$

Note that if the conversion `c` returns a theorem with assumptions, then the resulting inference rule adds these to the assumptions of the theorem it returns.

Failure

`CONV_RULE c th` fails if `c` fails when applied to the conclusion of `th`. The function returned by `CONV_RULE c` will also fail if the ML function `c:term->thm` is not, in fact, a conversion (i.e. a function that maps a term `t` to a theorem $\vdash t = t'$).

See also

`Tactic.CONV_TAC`, `Conv.RIGHT_CONV_RULE`.

CONV_TAC	(Tactic)
----------	----------

`CONV_TAC : (conv -> tactic)`

Synopsis

Makes a tactic from a conversion.

Description

If c is a conversion, then `CONV_TAC c` is a tactic that applies c to the goal. That is, if c maps a term "g" to the theorem $\vdash g = g'$, then the tactic `CONV_TAC c` reduces a goal g to the subgoal g' . More precisely, if c "g" returns $A' \vdash g = g'$, then:

$$\frac{A \vdash g}{\text{===== CONV_TAC } c} A \vdash g'$$

Note that the conversion c should return a theorem whose assumptions are also among the assumptions of the goal (normally, the conversion will return a theorem with no assumptions). `CONV_TAC` does not fail if this is not the case, but the resulting tactic will be invalid, so the theorem ultimately proved using this tactic will have more assumptions than those of the original goal.

Failure

`CONV_TAC c` applied to a goal $A \vdash g$ fails if c fails when applied to the term g . The function returned by `CONV_TAC c` will also fail if the ML function $c : \text{term} \rightarrow \text{thm}$ is not, in fact, a conversion (i.e. a function that maps a term t to a theorem $\vdash t = t'$).

Uses

`CONV_TAC` is used to apply simplifications that can't be expressed as equations (rewrite rules). For example, a goal can be simplified by beta-reduction, which is not expressible as a single equation, using the tactic

```
CONV_TAC(DEPTH_CONV BETA_CONV)
```

The conversion `BETA_CONV` maps a beta-redex " $(\lambda x. u)v$ " to the theorem

$$\vdash (\lambda x. u)v = u[v/x]$$

and the ML expression `(DEPTH_CONV BETA_CONV)` evaluates to a conversion that maps a term "t" to the theorem $\vdash t=t'$ where t' is obtained from t by beta-reducing all beta-redexes in t . Thus `CONV_TAC(DEPTH_CONV BETA_CONV)` is a tactic which reduces beta-redexes anywhere in a goal.

See also

`Conv.CONV_RULE`.

`current_axioms``(Theory)`

```
current_axioms : unit -> (string * thm) list
```

Synopsis

Return the axioms in the current theory segment.

Description

An invocation `current_axioms()` returns a list of the axioms asserted in the current theory segment.

Failure

Never fails. If no axioms have been asserted, the empty list is returned.

See also

`Theory.current_theory`, `Theory.new_theory`, `Theory.current_definitions`,
`Theory.current_theorems`, `Theory.constants`, `Theory.types`, `Theory.parents`.

`current_definitions``(Theory)`

```
current_definitions : unit -> (string * thm) list
```

Synopsis

Return the definitions in the current theory segment.

Description

An invocation `current_definitions()` returns the list of definitions stored in the current theory segment. Every definition is automatically stored in the current segment by the primitive definition principles.

Advanced definition principles are built in terms of the primitives, so they also store their results in the current segment. However, the definitions may be quite far removed from the user input, and they may also store some consequences of the definition as theorems.

Failure

Never fails. If no definitions have been made, the empty list is returned.

See also

Theory.current_theory, Theory.new_theory, Theory.current_axioms,
 Theory.current_theorems, Theory.constants, Theory.types, Theory.parents,
 Definition.new_definition, Definition.new_specification,
 Definition.new_type_definition, TotalDefn.Define, IndDefLib.Hol_reln.

current_defs	(Theory)
--------------	----------

```
current_defs : unit -> (string * thm) list
```

Synopsis

Return the definitions in the current theory segment.

Description

An invocation `current_defs ()` returns a list of the definitions made in the current theory segment.

Failure

Never fails. If no definitions have been made, the empty list is returned.

See also

Theory.current_theory, Theory.new_theory, Theory.current_axioms,
 Theory.current_thms, Theory.constants, Theory.types, Theory.parents.

current_theorems	(Theory)
------------------	----------

```
current_theorems : unit -> (string * thm) list
```

Synopsis

Return the theorems stored in the current theory segment.

Description

An invocation `current_theorems ()` returns the list of theorems stored in the current theory segment.

Failure

Never fails. If no theorems have been stored, the empty list is returned.

See also

`Theory.current_theory`, `Theory.new_theory`, `Theory.current_definitions`,
`Theory.current_theorems`, `Theory.constants`, `Theory.types`, `Theory.parents`.

`current_theory``(Theory)`

```
current_theory : unit -> string
```

Synopsis

Returns the name of the current theory segment.

Description

A HOL session has a notion of ‘current theory’. There are two senses to this phrase. First, the current theory denotes the totality of all loaded theories plus whatever definitions, axioms, and theorems have been stored in the current session. In this sense, the current theory is the full logical context being used at the moment. This logical context can be extended in two ways: (a) by loading in prebuilt theories residing on disk; and (b) by making a definition, asserting an axiom, or storing a theorem. Therefore, the current theory consists of a body of prebuilt theories that have been loaded from disk (a collection of static components) plus whatever has been stored in the current session.

This latter component — what has been stored in the current session — embodies the second sense of ‘current theory’. It is more properly known as the ‘current theory segment’. The current segment is dynamic in nature, for its contents can be augmented and overwritten. It functions as a kind of scratchpad used to help build a static theory segment.

In a HOL session, there is always a single current theory segment. Its name is given by calling `current_theory()`. On startup, the current theory segment is called "scratch", which is just a default name. If one is just experimenting, or hacking about, then this segment can be used.

On the other hand, if one intends to build a static theory segment, one usually creates a new theory segment named `thy` by calling `new_theory thy`. This changes the value of `current_theory` to `thy`. Once such a theory segment has been built (which may take many sessions), one calls `export_theory`, which exports the stored elements to disk.

Example

```
- current_theory();  
> val it = "scratch" : string
```

```

- new_theory "foo";
<<HOL message: Created theory "foo">>
> val it = () : unit

- current_theory();
> val it = "foo" : string

```

Failure

Never fails.

See also

`Theory.new_theory`, `Theory.export_theory`.

<code>current_thms</code>	<code>(Theory)</code>
---------------------------	-----------------------

```
current_thms : unit -> (string * thm) list
```

Synopsis

Return the theorems stored in the current theory segment.

Description

An invocation `current_thms ()` returns a list of the theorems that have been stored in the current theory segment.

Failure

Never fails. If no theorems have been stored, the empty list is returned.

See also

`Theory.current_theory`, `Theory.new_theory`, `Theory.current_defs`,
`Theory.current_thms`, `Theory.constants`, `Theory.types`, `Theory.parents`.

<code>current_trace</code>	<code>(Feedback)</code>
----------------------------	-------------------------

```
current_trace : string -> int
```


Synopsis

Returns the current value of the tracing variable specified.

Failure

Fails if the name given is not associated with a registered tracing variable.

See also

`Feedback.register_trace`, `Feedback.reset_trace`, `Feedback.reset_traces`,
`Feedback.trace`, `Feedback.traces`.

curry**(Lib)**

```
curry : ('a * 'b -> 'c) -> 'a -> 'b -> 'c
```

Synopsis

Converts a function on a pair to a corresponding curried function.

Description

The application `curry f` returns `fn x => fn y => f(x,y)`, so that

$$\text{curry } f \ x \ y = f(x,y)$$
Failure

A call `curry f` never fails; however, `curry f x y` fails if `f (x,y)` fails.

Example

```
- val increment = curry op+ 1;
> val it = increment = fn : int -> int
```

```
- increment 6;
> val it = 7 : int
```

See also

`Lib`, `Lib.uncurry`.

CURRY_CONV**(PairRules)**

```
CURRY_CONV : conv
```

Synopsis

Currys an application of a paired abstraction.

Example

```
- CURRY_CONV (Term '(λ(x,y). x + y) (1,2)');
> val it = |- (λ(x,y). x + y) (1,2) = (λx y. x + y) 1 2 : thm

- CURRY_CONV (Term '(λ(x,y). x + y) z');
> val it = |- (λ(x,y). x + y) z = (λx y. x + y) (FST z) (SND z) : thm
```

Failure

CURRY_CONV *tm* fails if *tm* is not an application of a paired abstraction.

See also

PairRules.UNCURRY_CONV.

<div data-bbox="234 1039 729 1090" data-label="Text"> <p>CURRY_EXISTS_CONV</p> </div>	<div data-bbox="1086 1039 1412 1090" data-label="Text"> <p>(PairRules)</p> </div>
---	---

CURRY_EXISTS_CONV : conv

Synopsis

Currys paired existential quantifications into consecutive existential quantifications.

Example

```
- CURRY_EXISTS_CONV (Term '?(x,y). x + y = y + x');
> val it = |- (?(x,y). x + y = y + x) = ?x y. x + y = y + x : thm

- CURRY_EXISTS_CONV (Term '?((w,x),(y,z)). w+x+y+z = z+y+x+w');
> val it =
  |- (?((w,x),y,z). w + x + y + z = z + y + x + w) =
    ?(w,x) (y,z). w + x + y + z = z + y + x + w : thm
```

Failure

CURRY_EXISTS_CONV *tm* fails if *tm* is not a paired existential quantification.

See also

PairRules.CURRY_CONV, PairRules.UNCURRY_CONV, PairRules.UNCURRY_EXISTS_CONV,
PairRules.CURRY_FORALL_CONV, PairRules.UNCURRY_FORALL_CONV.

CURRY_FORALL_CONV	(PairRules)
-------------------	-------------

```
CURRY_FORALL_CONV : conv
```

Synopsis

Currys paired universal quantifications into consecutive universal quantifications.

Example

```
- CURRY_FORALL_CONV (Term '(x,y). x + y = y + x');
> val it = |- (!x,y). x + y = y + x) = !x y. x + y = y + x : thm

- CURRY_FORALL_CONV (Term '((w,x),(y,z)). w+x+y+z = z+y+x+w');
> val it =
  |- (!((w,x),y,z). w + x + y + z = z + y + x + w) =
    !w,x (y,z). w + x + y + z = z + y + x + w : thm
```

Failure

CURRY_FORALL_CONV tm fails if tm is not a paired universal quantification.

See also

PairRules.CURRY_CONV, PairRules.UNCURRY_CONV, PairRules.UNCURRY_FORALL_CONV, PairRules.CURRY_EXISTS_CONV, PairRules.UNCURRY_EXISTS_CONV.

data	(DB)
------	------

```
type data
```

Synopsis

Type abbreviation used in DB structure.

Description

When functions from the DB structure are used to query the current theory, answer are often phrased in terms of the data type, which is a type abbreviation declared as

```
type data = (string * string) * (thm * class)
```

An element $((thy, name), (th, cl))$ means that th is a theorem with classification $class$, stored in theory segment thy under $name$.

Example

```
- DB.find "BOOL_CASES_AX";
> val it = [(("bool", "BOOL_CASES_AX"),
             (|- !t. (t = T) \/\ (t = F), Axm))]
           : ((string * string) * (thm * class)) list
```

See also

DB.class, DB.thy, DB.find, DB.match, DB.apropos, DB.listDB.

datatype_theorems	(EmitTeX)
-------------------	-----------

```
datatype_theorems : string -> (string * thm) list
```

Synopsis

All the datatype theorems stored in the named theory.

Description

An invocation `datatype_theorems thy`, where thy is the name of a currently loaded theory segment, will return a list of the datatype theorems stored in that theory. Each theorem is paired with the name of the datatype in the result. The string `"-"` may be used to denote the current theory segment.

Failure

Never fails. If thy is not the name of a currently loaded theory segment, the empty list is returned.

Example

```
- new_theory "example";
<<HOL message: Created theory "example">>
> val it = () : unit
- val _ = Hol_datatype 'example = First | Second';
<<HOL message: Defined type: "example">>
- EmitTeX.datatype_theorems "example";
> val it = [("example", |- DATATYPE (example First Second))] :
           (string * thm) list
```

See also

DB.theorems, bossLib.Hol_datatype.

<div data-bbox="161 504 798 560" data-label="Text"> <p>datatype_thm_to_string</p> </div>	<div data-bbox="1069 504 1331 553" data-label="Text"> <p>(EmitTeX)</p> </div>
--	---

datatype_thm_to_string : thm -> string

Synopsis

Converts a datatype theorem to a string.

Description

An invocation of `datatype_thm_to_string thm`, where `thm` is a datatype theorem produced by `Hol_datatype`, will return a string that corresponds with the original datatype declaration.

Failure

Will fail if the supplied theorem is not a datatype theorem, as created by `Hol_datatype`.

Example

```
- new_theory "example";
<<HOL message: Created theory "example">>
> val it = () : unit
- val _ = Hol_datatype 'example = First | Second';
<<HOL message: Defined type: "example">>
- EmitTeX.datatype_thm_to_string (theorem "datatype_example");
> val it = "example = First | Second" : string
```

See also

bossLib.Hol_datatype.

<div data-bbox="161 1812 343 1861" data-label="Text"> <p>DECIDE</p> </div>	<div data-bbox="1069 1812 1331 1863" data-label="Text"> <p>(bossLib)</p> </div>
--	---

DECIDE : term -> thm

Synopsis

Invoke decision procedure(s).

Description

An application `DECIDE M`, where `M` is a boolean term, attempts to prove `M` using a propositional tautology checker and a linear arithmetic decision procedure.

Failure

The invocation fails if `M` is not of boolean type. It also fails if `M` is not a tautology or an instance of a theorem of linear arithmetic.

Example

```
- DECIDE (Term 'p /\ p /\ r ==> r');
> val it = |- p /\ p /\ r ==> r : thm

- DECIDE (Term 'x < 17 /\ y < 26 ==> x + y < 17 + 26');
> val it = |- x < 17 /\ y < 26 ==> x + y < 17 + 26 : thm
```

Comments

`DECIDE` is currently somewhat underpowered. Formerly it was implemented by a cooperating decision procedure mechanism. However, most proofs seemed to go somewhat smoother with simplification using the `arith_ss` simpset, so we have adopted a simpler implementation. That should not be taken as final, since cooperating decision procedures are an important component in highly automated proof systems.

See also

`bossLib.RW_TAC`, `bossLib.arith_ss`.

DECIDE_TAC	(bossLib)
-------------------	------------------

`DECIDE_TAC` : tactic

Synopsis

Invoke decision procedure(s).

Description

`DECIDE_TAC` is the tactical version of `DECIDE`.

Failure

As for DECIDE

See also

bossLib.DECIDE.

`declare_ring``(ringLib)`

```

declare_ring :
  { Name : string, Theory : thm, Const : term->bool, Rewrites : thm list } ->
  { NormConv : conv, EqConv : conv,
    Reify : term list -> {Metamap : term, Poly : term list} }

```

Synopsis

Simplification and conversion in an arbitrary ring or semi-ring theory.

Description

Given a record gathering information about a ring structure, `declare_ring` returns two conversions `NormConv` and `EqConv`. The former does simplifications on any ring expression. Ring expressions are HOL terms built on the ring operations and the constants (or values) of that ring. Other subterms are abstracted and considered as variables.

The simplification of the expression (that can be seen as a polynomial) consists in developing, reordering monomials and grouping terms of same degree. `EqConv` solves an equality by simplifying both sides, and then using reflexivity. This cannot exactly be achieved by applying `NormConv` on both hand sides, since the variable ordering is not necessarily the same for both sides, and then applying reflexivity may not be enough.

The input structure contains various information about the ring: field `Name` is a prefix that will be used when declaring new constants for internal use of the conversions. `Theory` is a proof that a given structure is a ring or a semi-ring. `Const` is a predicate on HOL terms that defines the constants of the ring. `Rewrites` is a bunch of rewrites that should allow to compute the ring operations and also decide equality upon constants. If $(\text{Const } c1)$ and $(\text{Const } c2)$ then $(c1 + c2)$ and $(c1 * c2)$ should simplify to terms c and c' such that $(\text{Const } c)$ and $(\text{Const } c')$, and also $(c1 = c2)$ should simplify to either T or F.

Example

Assuming we have proved that the integers form a ring, and gathered all required information in `int_ring_infos`, we can build the conversions and simplify or solve symbolic equations on integers:

```

- val {EqConv=INT_RING_CONV, NormConv=INT_NORM_CONV,...} =
  ringLib.declare_ring int_ring_infos
> val INT_RING_CONV = fn : Term.term -> Thm.thm
  val INT_NORM_CONV = fn : Term.term -> Thm.thm
- INT_NORM_CONV (--'(a+b)*(a+b):int'--);
> val it = |- (a + b) * (a + b) = a * a + (2 * (a * b) + b * b) : Thm.thm
- INT_RING_CONV (--'(a+b)*(a+b) = (b+a)*(b+a):int'--);
> val it = |- ((a + b) * (a + b) = (b + a) * (b + a)) = T : Thm.thm

```

These conversions can also be used like `reduceLib`, but will evaluate only sums, products and unary negation:

```

- INT_NORM_CONV (--' ~(3 * (9 + ~7)) '--);
> val it = |- ~(3 * (9 + ~7)) = ~6 : Thm.thm
- INT_NORM_CONV (--' ~(3 * (10 - 1 + ~7)) '--);
> val it = |- ~(3 * (10 - 1 + ~7)) = 21 + ~3 * (10 - 1) : Thm.thm

```

Failure

If the Theory theorem is not of the form `— is_ring r` or `— is_semi_ring r` or if `Name` is not allowed to start a constant identifier.

The returned conversions fail on terms that do not belong to the type of the ring, but does not fail if no rewrite has been done.

<code>decls</code>	<code>(Term)</code>
--------------------	---------------------

`decls : string -> term list`

Synopsis

Returns a list of constants having the same name.

Description

An invocation `Term.decls s` returns a list of constants found in the current theory having the name `s`. If there are no constants with name `s`, then the empty list is returned.

Failure

Never fails.

Example


```
- decls "+";
> val it = ['$+'] : term list

- map dest_thy_const it;
> val it = [{Name = "+", Thy = "arithmetic", Ty = ':num -> num -> num'}] : ...
```

Comments

Useful for untangling confusion arising from overloading and also the possibility to declare two different constants with the same name in different theories.

See also

`Type.decls`, `Term.dest_thy_const`.

decls

(Type)

```
decls : string -> {Thy : string, Tyop : string} list
```

Synopsis

Lists all theories a named type operator is declared in.

Description

An invocation `Type.decls s` finds all theories in the ancestry of the current theory with a type constant having the given name.

Failure

Never fails.

Example

```
- Type.decls "prod";
> val it = [{Thy = "pair", Tyop = "prod"}] : {Thy:string, Tyop:string} list
```

Comments

There is also a function `Term.decls` that performs a similar operation on term constants.

See also

`Theory.ancestry`, `Term.decls`, `Theory.constants`.

Define

(bossLib)

```
Define : term quotation -> thm
```

Synopsis

General-purpose function definition facility.

Description

`Define` takes a high-level specification of an HOL function, and attempts to define the function in the logic. If this attempt is successful, the specification is derived from the definition. The derived specification is returned to the user, and also stored in the current theory. `Define` may be used to define abbreviations, recursive functions, and mutually recursive functions. An induction theorem may be stored in the current theory as a by-product of `Define`'s activity. This induction theorem follows the recursion structure of the function, and may be useful when proving properties of the function.

`Define` takes as input a quotation representing a conjunction of equations. The specified function(s) may be phrased using ML-style pattern-matching. A call `Define <spec>` should conform with the following grammar:

```
spec ::= <eqn>
      | (<eqn>) /\ <spec>

eqn ::= <alphanumeric> <pat> ... <pat> = <term>

pat ::= <variable>
      | <wildcard>
      | <cname> (* 0-ary constructor *)
      | (<cname>_n <pat>_1 ... <pat>_n) (* constructor appl. *)

cname ::= <alphanumeric> | <symbolic>

wildcard ::= _
          | _<wildcard>
```

When processing the specification of a recursive function, `Define` must perform a termination proof. It automatically constructs termination conditions for the function, and invokes a termination prover in an attempt to prove the termination conditions.

If the function is primitive recursive, in the sense that it exactly follows the recursion pattern of a previously declared HOL datatype, then this proof always succeeds, and `Define` stores the derived equations in the current theory segment. Otherwise, the function is not an instance of primitive recursion, and the termination prover may succeed or fail.

If it succeeds, then `Define` stores the specified equations in the current theory segment. An induction theorem customized for the defined function is also stored in the current segment. Note, however, that an induction theorem is not stored for primitive recursive functions, since that theorem would be identical to the induction theorem resulting from the declaration of the datatype.

If the termination proof fails, then `Define` fails.

In general, `Define` attempts to derive exactly the specified conjunction of equations. However, the rich syntax of patterns allows some ambiguity. For example, the input

```
Define '(f 0 _ = 1)
      /\ (f _ 0 = 2)'
```

is ambiguous at `f 0 0`: should the result be 1 or 2? The system attempts to resolve this ambiguity in the same way as compilers and interpreters for functional languages. Namely, a conjunction of equations is treated as being processed left-conjunct first, followed by processing the right conjunct. Therefore, in the example above, the right-hand side of the first clause is taken as the value of `f 0 0`. In the implementation, ambiguities arising from such overlapping patterns are systematically translated away in a pre-processing step.

Another case of vagueness in patterns is shown above: the specification is ‘incomplete’ since it does not tell us how `f` should behave when applied to two non-zero arguments: e.g., `f (SUC m) (SUC n)`. In the implementation, such missing clauses are filled in, and have the value `ARB`. This ‘pattern-completion’ step is a way of turning descriptions of partial functions into total functions suitable for HOL. However, since the user has not completely specified the function, the system takes that as a hint that the user is not interested in using the function at the missing-but-filled-in clauses, and so such clauses are dropped from the final theorem.

In summary, `Define` will derive the unambiguous and complete equations

```
|- (f 0 (SUC v4) = 1) /\
   (f 0 0 = 1) /\
   (f (SUC v2) 0 = 2)
   (f (SUC v2) (SUC v4) = ARB)
```

from the above ambiguous and incomplete equations. The odd-looking variable names are due to the pre-processing steps described above. The above result is only an intermediate value: in the final result returned by `Define`, the last equation is dropped:

```
|- (f 0 (SUC v4) = 1) /\
    (f 0 0 = 1) /\
    (f (SUC v2) 0 = 2)
```

`Define` automatically generates names with which to store the definition and, (if it exists) the associated induction theorem, in the current theory. The name for storing the definition is built by concatenating the name of the function with the value of the reference variable `Defn.def_suffix`. The name for storing the induction theorem is built by concatenating the name of the function with the value of the reference variable `Defn.ind_suffix`. For mutually recursive functions, where there is a choice of names, the name of the function in the first clause is taken.

Since the names used to store elements in the current theory segment are transformed into ML bindings after the theory is exported, it is required that every invocation of `Define` generates names that will be valid ML identifiers. For this reason, `Define` requires alphanumeric function names. If one wishes to define symbolic identifiers, the ML function `xDefine` should be used.

Failure

`Define` fails if its input fails to parse and typecheck.

`Define` fails if the name of the function being defined is not alphanumeric.

`Define` fails if there are more free variables on the right hand sides of the recursion equations than the left.

`Define` fails if it cannot prove the termination of the specified recursive function. In that case, one has to embark on the following multi-step process in order to get the same effect as if `Define` had succeeded: (1) construct the function and synthesize its termination conditions with `Hol_defn`; (2) set up a goal to prove the termination conditions with `tgoal`; (3) interactively prove the termination conditions, starting with an invocation of `WF_REL_TAC`; and (4) package everything up with an invocation of `tDefine`.

Example

We will give a number of examples that display the range of functions that may be defined with `Define`. First, we have a recursive function that uses "destructors" in the recursive call. Since `fact` is not primitive recursive, an induction theorem for `fact` is generated and stored in the current theory.

```
Define 'fact x = if x = 0 then 1 else x * fact(x-1)';
```

```
Equations stored under "fact_def".
```

```
Induction stored under "fact_ind".
```

```
> val it = |- fact x = (if x = 0 then 1 else x * fact (x - 1)) : thm
```

```
- DB.fetch "-" "fact_ind";
```

```
> val it =
  |- !P. (!x. (~(x = 0) ==> P (x - 1)) ==> P x) ==> !v. P v : thm
```

Next we have a recursive function with relatively complex pattern-matching. We omit to examine the generated induction theorem.

```
Define '(flatten [] = [])
  /\ (flatten ([]::rst) = flatten rst)
  /\ (flatten ((h::t)::rst) = h::flatten(t::rst))'
```

```
<<HOL message: inventing new type variable names: 'a>>
```

```
Equations stored under "flatten_def".
```

```
Induction stored under "flatten_ind".
```

```
> val it =
  |- (flatten [] = []) /\
     (flatten ([]::rst) = flatten rst) /\
     (flatten ((h::t)::rst) = h::flatten (t::rst)) : thm
```

Next we define a curried recursive function, which uses wildcard expansion and pattern-matching pre-processing.

```
Define '(min (SUC x) (SUC y) = min x y + 1)
  /\ (min _ _ = 0)';
```

```
Equations stored under "min_def".
```

```
Induction stored under "min_ind".
```

```
> val it =
  |- (min (SUC x) (SUC y) = min x y + 1) /\
     (min (SUC v2) 0 = 0) /\
     (min 0 v1 = 0) : thm
```

Next we make a primitive recursive definition. Note that no induction theorem is generated in this case.

```
Define '(filter P [] = [])
  /\ (filter P (h::t) = if P h then h::filter P t else filter P t)';
```

```
<<HOL message: inventing new type variable names: 'a>>
```

Definition has been stored under "filter_def".

```
> val it =
  |- (!P. filter P [] = []) /\
    !P h t. filter P (h::t) =
      (if P h then h::filter P t else filter P t) : thm
```

Define may also be used to define mutually recursive functions. For example, we can define a datatype of propositions and a function for putting a proposition into negation normal form as follows. First we define a datatype for boolean formulae (prop):

```
- Hol_datatype
  'prop = VAR of 'a
        | NOT of prop
        | AND of prop => prop
        | OR  of prop => prop';
```

```
> val it = () : unit
```

Then two mutually recursive functions `nnfpos` and `nnfneg` are defined:

```
- Define
  '(nnfpos (VAR x)   = VAR x)
  /\ (nnfpos (NOT p)  = nnfneg p)
  /\ (nnfpos (AND p q) = AND (nnfpos p) (nnfpos q))
  /\ (nnfpos (OR p q)  = OR  (nnfpos p) (nnfpos q))

  /\ (nnfneg (VAR x)   = NOT (VAR x))
  /\ (nnfneg (NOT p)   = nnfpos p)
  /\ (nnfneg (AND p q) = OR  (nnfneg p) (nnfneg q))
  /\ (nnfneg (OR p q)  = AND (nnfneg p) (nnfneg q))';
```

The system returns:

```
<<HOL message: inventing new type variable names: 'a>>
```

```
Equations stored under "nnfpos_def".
```

```
Induction stored under "nnfpos_ind".
```

```
> val it =
  |- (nnfpos (VAR x) = VAR x) /\
    (nnfpos (NOT p) = nnfneg p) /\
    (nnfpos (AND p q) = AND (nnfpos p) (nnfpos q)) /\
```

```

(nnfpos (OR p q) = OR (nnfpos p) (nnfpos q)) /\
(nfneg (VAR x) = NOT (VAR x)) /\
(nfneg (NOT p) = nnfpos p) /\
(nfneg (AND p q) = OR (nfneg p) (nfneg q)) /\
(nfneg (OR p q) = AND (nfneg p) (nfneg q)) : thm

```

Define may also be used to define non-recursive functions.

```
Define 'f x (y,z) = (x + 1 = y DIV z)';
```

Definition has been stored under "f_def".

```
> val it = |- !x y z. f x (y,z) = (x + 1 = y DIV z) : thm
```

Define may also be used to define non-recursive functions with complex pattern-matching. The pattern-matching pre-processing of Define can be convenient for this purpose, but can also generate a large number of equations. For example:

```

Define '(g (0,_,_,_,_) = 1) /\
      (g (_,0,_,_,_) = 2) /\
      (g (_,_,0,_,_) = 3) /\
      (g (_,_,_,0,_) = 4) /\
      (g (_,_,_,_,0) = 5)

```

yields a definition with thirty-one clauses.

Comments

In an eqn, no variable can occur more than once on the left hand side of the equation.

In HOL, constructors are curried functions, unlike in ML. When used in a pattern, a constructor must be fully applied to its arguments.

Also unlike ML, a pattern variable in a clause of a definition is not distinct from occurrences of that variable in other clauses.

Define translates a wildcard into a new variable, which is named to be different from any other variable in the function definition. As in ML, wildcards are not allowed to occur on the right hand side of any clause in the definition.

An induction theorem generated in the course of processing an invocation of Define can be applied by `recInduct`.

Invoking Define on a conjunction of non-recursive clauses having complex pattern-matching will result in an induction theorem being stored. This theorem may be useful for case analysis, and can be applied by `recInduct`.

Define takes a 'quotation' as an argument. Some might think that the input to Define should instead be a term. However, some important pre-processing happens in Define that would not be possible if the input was a term.

Define is a mechanization of a well-founded recursion theorem (`relationTheory.WFREC_COROLLARY`).

Define currently has a rather weak termination prover. For example, it always fails to prove the termination of nested recursive functions.

`bossLib.Define` is most commonly used. `TotalDefn.Define` is identical to `bossLib.Define`, except that the `TotalDefn` structure comes with less baggage—it depends only on `numLib` and `pairLib`.

Define automatically adds the definition it makes into the hidden ‘compset’ accessed by `EVAL` and `EVAL_TAC`.

See also

`bossLib.tDefine`, `bossLib.xDefine`, `TotalDefn.DefineSchema`, `bossLib.Hol.defn`, `Defn.tgoal`, `Defn.tprove`, `bossLib.WF_REL_TAC`, `bossLib.recInduct`, `bossLib.EVAL`, `bossLib.EVAL_TAC`.

Define	(TotalDefn)
--------	-------------

Define : term quotation -> thm

Synopsis

General purpose function definition facility.

Description

`bossLib.Define` is identical to `TotalDefn.Define`.

See also

`bossLib.Define`.

Define_mk_ptree	(patriciaLib)
-----------------	---------------

Define_mk_ptree : string -> term_ptree -> thm

Synopsis

Define a new Patricia tree constant.

Description

A call to `Define_mk_ptree c t` builds a HOL Patricia tree from the ML tree `t` and uses this to define a new constant `c`. This provides an efficient mechanism to define

large patricia trees in HOL: the trees can be quickly built in ML and then imported into HOL via `patriciaLib.mk_ptree`. Provided the tree is not too large, a side-effect of `Define_mk_ptree` is to prove the theorem `|- IS_PTREE c`. This is controlled by the reference `is_ptree_term_size_limit`.

To avoid producing large terms, a call to `EVAL` will not expand out the definition of the new constant `c`. However, it will efficiently evaluate operations performed on `c`, e.g. `PEEK c n` for ground `n`.

Failure

`Define_mk_ptree` will fail when `patriciaLib.mk_ptree` fails.

Example

The following session shows the construction of Patricia trees in ML, which are then imported into HOL.

```
open patriciaLib;
...
> val ptree = Define_mk_ptree "ptree" (int_ptree_of_list [(1, '1'), (2, '2')]);
<<HOL message: Saved IS_PTREE theorem for new constant "ptree">>
val ptree = |- ptree = Branch 0 0 (Leaf 1 1) (Leaf 2 2): thm
> DB.theorem "ptree_is_ptree_thm";
val it = |- IS_PTREE ptree: thm

> val _ = Globals.max_print_depth := 7;
> let
  fun pp _ _ (_: term_ptree) = PolyML.PrettyString "<ptree>"
in
  PolyML.addPrettyPrinter pp
end;
val it = (): unit

> val random_ptree =
  real_time patriciaLib.ptree_of_ints
    (Random.rangelist (0,100000) (10000,Random.newgenseed 1.0));
realtime: 0.091s
val random_ptree = <ptree>: term_ptree

> val random = real_time (patriciaLib.Define_mk_ptree "random") random_ptree;
<<HOL warning: patriciaLib.Define_ptree: Failed to prove IS_PTREE (is_ptree_term_size_li
realtime: 0.196s
val random =
```

```

|- random =
Branch 0 0
  (... ... 1 (... ... (... ... ))
    (... ... (... ... ) (... ... (... ... )))
  (Branch 0 1 (... ... (... ... ) (... ... (... ... )))
    (... ... 2 (... ... (... ... ))
      (... ... (... ... ) (... ... (... ... ))))):
thm

> patriciaLib.size random_ptree;
val it = 9517: int
> real_time EVAL "SIZE random";
realtime: 3.531s
val it = |- SIZE random = 9517: thm

> int_peek random_ptree 3;
val it = SOME "(): term option
> real_time EVAL "random ' 3";
realtime: 0.004s
val it = |- random ' 3 = SOME (): thm

> int_peek random_ptree 100;
val it = NONE: term option
> real_time EVAL "random ' 100";
realtime: 0.004s
val it = |- random ' 100 = NONE: thm

```

See also

patriciaLib.mk_ptree, patriciaLib.PTREE_CONV, patriciaLib.PTREE_DEFN_CONV.

<div data-bbox="234 1637 986 1695" data-label="Text"> <pre>define_new_type_bijections</pre> </div>	<div data-bbox="1201 1637 1414 1691" data-label="Text"> <pre>(Drule)</pre> </div>
--	---

```

define_new_type_bijections :
  {name:string, ABS:string, REP:string, tyax:thm} -> thm

```

Synopsis

Introduces abstraction and representation functions for a defined type.

Description

The result of making a type definition using `new_type_definition` is a theorem of the following form:

$$\vdash \ ?rep:nty \rightarrow ty. \text{TYPE_DEFINITION } P \text{ rep}$$

which asserts only the existence of a bijection from the type it defines (in this case, `nty`) to the corresponding subset of an existing type (here, `ty`) whose characteristic function is specified by `P`. To automatically introduce constants that in fact denote this bijection and its inverse, the ML function `define_new_type_bijections` is provided.

`name` is the name under which the constant definition (a constant specification, in fact) made by `define_new_type_bijections` will be stored in the current theory segment. `tyax` must be a definitional axiom of the form returned by `new_type_definition`. `ABS` and `REP` are the user-specified names for the two constants that are to be defined. These constants are defined so as to denote mutually inverse bijections between the defined type, whose definition is given by `tyax`, and the representing type of this defined type.

If `th` is a theorem of the form returned by `new_type_definition`:

$$\vdash \ ?rep:newty \rightarrow ty. \text{TYPE_DEFINITION } P \text{ rep}$$

then evaluating:

`define_new_type_bijections{name="name",ABS="abs",REP="rep",tyax=th} th`
 automatically defines two new constants `abs:ty→newty` and `rep:newty→ty` such that:

$$\vdash \ (!a. \text{abs}(\text{rep } a) = a) \wedge (!r. P \ r = (\text{rep}(\text{abs } r) = r))$$

This theorem, which is the defining property for the constants `abs` and `rep`, is stored under the name `name` in the current theory segment. It is also the value returned by `define_new_type_bijections`. The theorem states that `abs` is the left inverse of `rep` and, for values satisfying `P`, that `rep` is the left inverse of `abs`.

Failure

A call `define_new_type_bijections{name,ABS,REP,tyax}` fails if `tyax` is not a theorem of the form returned by `new_type_definition`.

See also

`Definition.new_type_definition`, `Prim_rec.prove_abs_fn_one_one`,
`Prim_rec.prove_abs_fn_onto`, `Drule.prove_rep_fn_one_one`, `Drule.prove_rep_fn_onto`.

DefineSchema	(TotalDefn)
--------------	-------------

DefineSchema : term quotation -> thm

Synopsis

Defines a recursion schema

Description

`DefineSchema` may be used to declare so-called ‘schematic’ definitions, or ‘recursion schemas’. These are just recursive functions with extra free variables (also called ‘parameters’) on the right-hand side of some clauses. Such schemas have been used as a basis for program transformation systems.

`DefineSchema` takes its input in exactly the same format as `Define`.

The termination constraints of a schematic definition are collected on the hypotheses of the definition, and also on the hypotheses of the automatically proved induction theorem, but a termination proof is only attempted when the termination conditions have no occurrences of parameters. This is because, in general, termination can only be proved after some of the parameters of the scheme have been instantiated.

Failure

`DefineSchema` fails in many of the same ways as `Define`. However, it will not fail if it cannot prove termination.

Example

The following defines a schema for binary recursion.

```
- DefineSchema
  'binRec (x:'a) =
    if atomic x then (A x:'b)
      else join (binRec (left x))
                (binRec (right x))';

<<HOL message: Definition is schematic in the following variables:
  "A", "atomic", "join", "left", "right">>
Equations stored under "binRec_def".
Induction stored under "binRec_ind".

> val it =
  [|x. ~atomic x ==> R (left x) x,
   !x. ~atomic x ==> R (right x) x, WF R]
|- binRec A atomic join left right x =
  if atomic x then A x
  else
    join (binRec A atomic join left right (left x))
          (binRec A atomic join left right (right x)) : thm
```

The following defines a schema in which a termination proof is attempted successfully.

```
- DefineSchema '(map [] = []) /\ (map (h::t) = f h :: map t)';

<<HOL message: inventing new type variable names: 'a, 'b>>
<<HOL message: Definition is schematic in the following variables:
  "f">>

Equations stored under "map_def".
Induction stored under "map_ind".

> val it = [] |- (map f [] = []) /\ (map f (h::t) = f h::map f t) : thm
```

The easy termination proof is attempted because the schematic variable `f` doesn't occur in the termination conditions.

Comments

The original recursion equations, in which parameters only occur on right hand sides, is transformed into one in which the parameters become arguments to the function being defined. This is the expected behaviour. If an argument intended as a parameter occurs on the left hand side in the original recursion equations, it becomes universally quantified in the termination conditions, which is not desirable for a schema.

See also

`TotalDefn.Define`, `Defn.Hol_defn`.

<div data-bbox="161 1440 481 1487" data-label="Text"> <p>definitions</p> </div>	<div data-bbox="1212 1440 1331 1487" data-label="Text"> <p>(DB)</p> </div>
---	--

```
definitions : string -> (string * thm) list
```

Synopsis

All the definitions stored in the named theory.

Description

An invocation `definitions thy`, where `thy` is the name of a currently loaded theory segment, will return a list of the definitions stored in that theory. Each definition is paired with its name in the result. The string `"-"` may be used to denote the current theory segment.

Failure

Never fails. If `thy` is not the name of a currently loaded theory segment, the empty list is returned.

Example

```
- definitions "combin";
> val it =
  [("C_DEF", |- combin$C = (\f x y. f y x)),
   ("I_DEF", |- I = S K K),
   ("K_DEF", |- K = (\x y. x)),
   ("O_DEF", |- !f g. f o g = (\x. f (g x))),
   ("S_DEF", |- S = (\f g x. f x (g x))),
   ("W_DEF", |- W = (\f x. f x x))] : (string * thm) list
```

See also

`DB.thy`, `DB.fetch`, `DB.thms`, `DB.theorems`, `DB.axioms`, `DB.listDB`.

<code>delete_binding</code>	(Theory)
-----------------------------	----------

`delete_binding` : string -> unit

Synopsis

Remove a stored value from the current theory segment.

Description

An invocation `delete_binding s` attempts to locate an axiom, definition, or theorem that has been stored under name `s` in the current theory segment. If such a binding can be found, it is deleted.

Failure

Never fails. If the binding can't be found, then nothing is removed from the current theory segment.

Example

```
- Define 'fact x = if x=0 then 1 else x * fact (x-1)';
Equations stored under "fact_def".
Induction stored under "fact_ind".
```

```

> val it = |- fact x = (if x = 0 then 1 else x * fact (x - 1)) : thm

- current_theorems();
> val it =
  [("fact_def", |- fact x = (if x = 0 then 1 else x * fact (x - 1))),
   ("fact_ind", |- !P. (!x. (~(x = 0) ==> P (x - 1)) ==> P x) ==> !v. P v)]
  : (string * thm) list

- delete_binding "fact_ind";
> val it = () : unit

- current_theorems();
> val it =
  [("fact_def", |- fact x = (if x = 0 then 1 else x * fact (x - 1)))]
  : (string * thm) list

```

Comments

Removing a definition binding does not remove the constant(s) it introduced from the signature. Use `delete_const` for that.

Removing an axiom has the consequence that all theorems proved from it become garbage.

See also

`Theory.scrub`, `Theory.delete_type`, `Theory.delete_const`.

<div data-bbox="161 1415 512 1467" data-label="Text"> <p><code>delete_const</code></p> </div>	<div data-bbox="1096 1415 1331 1471" data-label="Text"> <p>(Theory)</p> </div>
---	--

`delete_const` : string -> unit

Synopsis

Remove a term constant from the current signature.

Description

An invocation `delete_const s` removes the constant denoted by `s` from the current HOL segment. All types, terms, and theorems that depend on that constant become garbage.

The implementation ensures that a deleted constant is never equal to a subsequently declared constant, even if it has the same name and type. Furthermore, although garbage types, terms, and theorems may exist in a session, and may even have been

stored in the current segment for export, no theorem, definition, or axiom that is garbage is exported when `export_theory` is invoked.

The prettyprinter highlights deleted constants.

Failure

If a constant named `s` has not been declared in the current segment, a warning will be issued, but an exception will not be raised.

Example

```
- Define 'foo x = if x=0 then 1 else x * foo (x-1)';
Equations stored under "foo_def".
Induction stored under "foo_ind".
> val it = |- foo x = (if x = 0 then 1 else x * foo (x - 1)) : thm

- val th = EVAL (Term 'foo 4');
> val th = |- foo 4 = 24 : thm

- delete_const "foo";
> val it = () : unit

- th;
> val it = |- scratch$old->foo<-old 4 = 24 : thm
```

Comments

A type, term, or theorem that depends on a deleted constant may be detected by invoking the appropriate ‘update’ entrypoint.

It may happen that a theorem `th` is proved with the use of another theorem `th1` that subsequently becomes garbage because a constant `c` was deleted. If `c` does not occur in `th`, then `th` does not become garbage, which may be contrary to expectation. The conservative extension property of HOL says that `th` is still provable, even in the absence of `c`.

See also

`Theory.delete_type`, `Theory.update_type`, `Theory.update_term`,
`Theory.update_thm`, `Theory.scrub`.

DELETE_CONV	(pred_setLib)
-------------	---------------

DELETE_CONV : conv -> conv

Synopsis

Reduce $\{t_1; \dots; t_n\}$ DELETE t by deleting t from $\{t_1; \dots; t_n\}$.

Description

The function DELETE_CONV is a parameterized conversion for reducing finite sets of the form $\{t_1; \dots; t_n\}$ DELETE t , where the term t and the elements of $\{t_1; \dots; t_n\}$ are of some base type ty . The first argument to DELETE_CONV is expected to be a conversion that decides equality between values of the base type ty . Given an equation $e_1 = e_2$, where e_1 and e_2 are terms of type ty , this conversion should return the theorem $\vdash (e_1 = e_2) = T$ or the theorem $\vdash (e_1 = e_2) = F$, as appropriate.

Given such a conversion `conv`, the function DELETE_CONV returns a conversion that maps a term of the form $\{t_1; \dots; t_n\}$ DELETE t to the theorem

$$\vdash \{t_1; \dots; t_n\} \text{ DELETE } t = \{t_i; \dots; t_j\}$$

where $\{t_i; \dots; t_j\}$ is the subset of $\{t_1; \dots; t_n\}$ for which the supplied equality conversion `conv` proves

$$\vdash (t_i = t) = F, \dots, \vdash (t_j = t) = F$$

and for all the elements t_k in $\{t_1; \dots; t_n\}$ but not in $\{t_i; \dots; t_j\}$, either `conv` proves $\vdash (t_k = t) = T$ or t_k is alpha-equivalent to t . That is, the reduced set $\{t_i; \dots; t_j\}$ comprises all those elements of the original set that are provably not equal to the deleted element t .

Example

In the following example, the conversion REDUCE_CONV is supplied as a parameter and used to test equality of the deleted value 2 with the elements of the set.

```
- DELETE_CONV REDUCE_CONV ‘‘{2; 1; SUC 1; 3} DELETE 2‘‘;
> val it =  $\vdash \{2; 1; SUC 1; 3\} \text{ DELETE } 2 = \{1; 3\} : \text{thm}$ 
```

‘

Failure

DELETE_CONV `conv` fails if applied to a term not of the form $\{t_1; \dots; t_n\}$ DELETE t . A call DELETE_CONV `conv` ‘‘ $\{t_1; \dots; t_n\}$ DELETE t ‘‘ fails unless for each element t_i of the set $\{t_1; \dots; t_n\}$, the term t is either alpha-equivalent to t_i or `conv` ‘‘ $t_i = t$ ‘‘ returns $\vdash (t_i = t) = T$ or $\vdash (t_i = t) = F$.

See also

pred_setLib.INSERT_CONV, numLib.REDUCE_CONV.

<div data-bbox="234 349 560 405" data-label="Text"><code>delete_type</code></div>	<div data-bbox="1173 347 1410 405" data-label="Text"><code>(Theory)</code></div>
---	--

```
delete_type : string -> unit
```

Synopsis

Remove a type operator from the signature.

Description

An invocation `delete_type s` removes the type constant denoted by `s` from the current HOL segment. All types, terms, and theorems that depend on that type should therefore disappear, as though they hadn't been constructed in the first place. Conceptually, they have become "garbage" and need to be collected. However, because of the way that HOL is implemented in ML, it is not possible to have them automatically collected. Instead, HOL tracks the currency of type and term constants and provides some consistency maintenance support.

In particular, the implementation ensures that a deleted type operator is never equal to a subsequently declared type operator with the same name (and arity). Furthermore, although garbage types, terms, and theorems may exist in a session, no theorem, definition, or axiom that is garbage is exported when `export_theory` is invoked.

The notion of garbage is hereditary. Any type, term, definition, or theorem is garbage if any of its constituents are. Furthermore, if a type operator or term constant had been defined, and its witness theorem later becomes garbage, then that type or term is garbage, as is anything built from it.

Failure

If a type constant named `s` has not been declared in the current segment, a warning will be issued, but an exception will not be raised.

Example

```
new_type ("foo", 2);
> val it = () : unit

- val thm = REFL (Term 'f:(\'a,'b)foo');
> val thm = |- f = f : thm

- delete_type "foo";
> val it = () : unit
```

```

- thm;
> val it = |- f = f : thm

- show_types := true;
> val it = () : unit

- thm;
> val it = |- (x : (('a, 'b) scratch$old->f<-old)) = x : thm

```

Comments

It's rather dodgy to withdraw constants from the HOL signature.

It is not possible to delete constants from ancestor theories.

See also

`Theory.delete_const`, `Theory.uptodate_type`, `Theory.uptodate_term`,
`Theory.uptodate_thm`, `Theory.scrub`.

<div data-bbox="161 1070 314 1120" data-label="Text">delta</div>	<div data-bbox="1182 1070 1331 1120" data-label="Text">(Lib)</div>
--	--

```
type 'a delta
```

Synopsis

A type used for telling when a function has changed its argument.

Description

The `delta` type is declared as follows:

```
datatype 'a delta = SAME | DIFF of 'a
```

The `delta` type may be used in applications where it is important to tell if a function has changed its argument or not. As an example of this, consider mapping a function over a large collection of elements. If only a few elements are changed, it makes sense to re-use all those that were not changed. This can of course be handled on an ad hoc basis; the `delta` type provides a mechanism for doing this systematically.

Comments

The `delta` type is an example of polytypism.

See also

`Lib.delta_apply`, `Lib.delta_map`, `Lib.delta_pair`.

`delta`

(Type)

`delta : hol_type`**Synopsis**

Common type variable.

DescriptionThe ML variable `Type.delta` is bound to the type variable `'a`.**See also**`Type.alpha`, `Type.beta`, `Type.gamma`, `Type.bool`.`delta_apply`

(Lib)

`delta_apply : ('a -> 'a delta) -> 'a -> 'a`**Synopsis**

Apply a function to an argument, re-using the argument if possible.

DescriptionAn application `delta_apply f x` applies `f` to `x` and, if the result is `SAME`, returns `x`. If the result is `DIFF y`, then `y` is returned.**Failure**If `f x` raises exception `e`, then `delta_apply f x` raises `e`.**Example**

Suppose we want to write a function that replaces every even integer in a list of pairs of integers with an odd one. The most basic replacement function is therefore

```
- fun ireplace i = if i mod 2 = 0 then DIFF (i+1) else SAME
```

Applying `ireplace` to an arbitrary integer would yield an element of the `int delta` type. It's not seemingly useful, but it becomes useful when used with similar functions for type operators. Then a delta function for pairs of integers is built by `delta_pair ireplace ireplace`, and a delta function for a list of pairs of integers is built by applying `delta_map`.

```

- delta_map (delta_pair ireplace ireplace)
  [(1,2), (3,5), (5,7), (4,8)];
> val it = DIFF [(1,3), (3,5), (5,7), (5,9)] : (int * int) list delta

- delta_map (delta_pair ireplace ireplace)
  [(1,3), (3,5), (5,7), (7,9)];
> val it = SAME : (int * int) list delta

```

Finally, we can move the result from the `delta` type to the actual type we are interested in.

```

- delta_apply (delta_map (delta_pair ireplace ireplace))
  [(1,2), (3,5), (5,7), (4,8)];
> val it = [(1,3), (3,5), (5,7), (5,9)] : (int * int) list

```

Comments

Used to change a function from one that returns an `'a delta` element to one that returns an `'a` element.

See also

`Lib.delta`, `Lib.delta_map`, `Lib.delta_pair`.

<div data-bbox="161 1236 427 1292" data-label="Text"> <h1 style="margin: 0;">delta_map</h1> </div>	<div data-bbox="1182 1232 1331 1288" data-label="Text"> <h1 style="margin: 0;">(Lib)</h1> </div>
--	--

```
delta_map : ('a -> 'a delta) -> 'a list -> 'a list delta
```

Synopsis

Apply a function to a list, sharing as much structure as possible.

Description

An application `delta_map f list` applies `f` to each member `[x1,...,xn]` of `list`. If all applications of `f` return `SAME`, then `delta_map f list` returns `SAME`. Otherwise, `DIFF [y1,...,yn]` is returned. If `f xi` yielded `SAME`, then `yi` is `xi`. Otherwise, `f xi` equals `DIFF yi`.

Failure

If some application of `f xi` raises `e`, then `delta_map f list` raises `e`.

Example

See the example in the documentation for `delta_apply`.

See also

`Lib.delta`, `Lib.delta_apply`, `Lib.delta_pair`.

<code>delta_pair</code>	<code>(Lib)</code>
-------------------------	--------------------

```
delta_pair : ('a -> 'a delta) ->
            ('b -> 'b delta) ->
            'a * 'b -> ('a * 'b) delta
```

Synopsis

Apply two functions to the projections of a pair, sharing as much structure as possible.

Description

An application `delta_pair f g (x,y)` applies `f` to `x` and `g` to `y`. If `f x` equals `g y` equals `SAME`, then `SAME` is returned. Otherwise `DIFF (p1,p2)` is returned, where `p1` is `x` if `f x` equals `SAME`; otherwise `p1` is `f x`. Similarly, `p2` is `y` if `g y` equals `SAME`; otherwise `p2` is `g y`.

Failure

If `f x` raises `e`, then `delta_pair f g (x,y)` raises `e`.

If `g y` raises `e`, then `delta_pair f g (x,y)` raises `e`.

Example

See the example in the documentation for `delta_apply`.

See also

`Lib.delta`, `Lib.delta_apply`, `Lib.delta_pair`.

<code>deprecate_int</code>	<code>(intLib)</code>
----------------------------	-----------------------

```
intLib.deprecate_int : unit -> unit
```

Synopsis

Makes the parser never consider integers as a numeric possibility.

Description

Calling `deprecate_int()` causes the parser to remove all of the standard numeric constants over the integers from consideration. In addition to the standard operators (+, -, * and others), this also affects numerals; after the call to `deprecate_int` these will never be parsed as integers.

This function, by affecting the global grammar, also affects the behaviour of the pretty-printer. A term that includes affected constants will print with those constants in “fully qualified form”, typically as `integer$op`, and numerals will print with a trailing `i`. (Incidentally, the parser will always read integer terms if they are presented to it in this form.)

Failure

Never fails.

Example

First we load the integer library, ensuring that integers and natural numbers both are possible when we type numeric expressions:

```
- load "intLib";
> val it = () : unit
```

Then, when we type such an expression, we’re warned that this is strictly ambiguous, and a type is silently chosen for us:

```
- val t = ‘‘2 + x‘‘;
<<HOL message: more than one resolution of overloading was possible>>
> val t = ‘‘2 + x‘‘ : term

- type_of t;
> val it = ‘‘:int‘‘ : hol_type
```

Now we can use `deprecate_int` to stop this happening, and make sure that we just get natural numbers:

```
- intLib.deprecate_int();
> val it = () : unit

- ‘‘2 + x‘‘;
> val it = ‘‘2 + x‘‘ : term

- type_of it;
> val it = ‘‘:num‘‘ : hol_type
```

The term we started out with is now printed in rather ugly fashion:

```
- t;
> val it = ``integer$int_add 2i x`` : term
```

Comments

If one wishes to simply prefer the natural numbers, say, to the integers, and yet still retain integers as a possibility, use `numLib.prefer_num` rather than this function. This function only brings about a “temporary” effect; it does not cause the change to be exported with the current theory.

See also

`intLib.prefer_int`.

DEPTH_CONSEQ_CONV	(ConseqConv)
--------------------------	---------------------

`DEPTH_CONSEQ_CONV : directed_conseq_conv -> directed_conseq_conv`

Synopsis

Applies a consequence conversion repeatedly to all the sub-terms of a term, in top-down order.

Description

`DEPTH_CONSEQ_CONV c tm` tries to apply the given conversion at toplevel. If this fails, it breaks the term `tm` down into boolean subterms. It can break up the following operators: \wedge , \vee , \sim , \implies and quantification. Then it applies the directed consequence conversion `c` to terms and iterates. Finally, it puts everything together again.

Notice that some operators switch the direction that is passed to `c`, e.g. to strengthen a term $\sim t$, `DEPTH_CONSEQ_CONV` tries to weaken `t`.

Example

Consider the expression `FEVERY P (f |+ (x1, y1) |+ (x2,y2))`. It states that all elements of the finite map `f |+ (x1, y1) |+ (x2, y2)` satisfy the predicate `P`. However, the definition of `x1` and `x2` possible hide definitions of these keys inside `f` or in case `x1 = x2` the middle update is void. You easily get into a lot of aliasing problems while proving thus a statement. However, the following theorem holds:

$$\vdash \!-\ !f \ x \ y. \text{FEVERY } P \ (f \ |+ \ (x,y)) \ /\ \ P \ (x,y) \ \implies \ \text{FEVERY } P \ (f \ |+ \ (x,y))$$

Given a directed consequence conversion c that instantiates this theorem, `DEPTH_CONSEQ_CONV` can be used to apply it repeatedly and at substructures as well:

```
DEPTH_CONSEQ_CONV c CONSEQ_CONV_STRENGTHEN_direction
  ‘‘!y2. FEVERY P (f |+ (x1, y1) |+ (x2,y2)) /\ Q z’’ =
```

```
|- (!y2. FEVERY P f /\ P (x1, y1) /\ P (x2,y2) /\ Q z) ==>
  (!y2. FEVERY P (f |+ (x1, y1) |+ (x2,y2)) /\ Q z)
```

See also

`Conv.DEPTH_CONV`, `ConseqConv.ONCE_DEPTH_CONSEQ_CONV`,
`ConseqConv.NUM_DEPTH_CONSEQ_CONV`, `ConseqConv.DEPTH_STRENGTHEN_CONSEQ_CONV`,
`ConseqConv.REDEPTH_CONSEQ_CONV`.

<div data-bbox="159 1008 453 1057" data-label="Text"> <p>DEPTH_CONV</p> </div>	<div data-bbox="1155 1008 1331 1057" data-label="Text"> <p>(Conv)</p> </div>
---	---

`DEPTH_CONV : conv -> conv`

Synopsis

Applies a conversion repeatedly to all the sub-terms of a term, in bottom-up order.

Description

`DEPTH_CONV c tm` repeatedly applies the conversion c to all the subterms of the term tm , including the term tm itself. The supplied conversion is applied repeatedly (zero or more times, as is done by `REPEATC`) to each subterm until it fails. The conversion is applied to subterms in bottom-up order.

Failure

`DEPTH_CONV c tm` never fails but can diverge if the conversion c can be applied repeatedly to some subterm of tm without failing.

Example

The following example shows how `DEPTH_CONV` applies a conversion to all subterms to which it applies:

```
- DEPTH_CONV BETA_CONV (Term ‘(\x. (\y. y + x) 1) 2’);
> val it = |- (\x. (\y. y + x)1)2 = 1 + 2 : thm
```

Here, there are two beta-redexes in the input term, one of which occurs within the other. `DEPTH_CONV BETA_CONV` applies beta-conversion to innermost beta-redex $(\lambda y. y + x) 1$ first. The outermost beta-redex is then $(\lambda x. 1 + x) 2$, and beta-conversion of this redex gives $1 + 2$.

Because `DEPTH_CONV` applies a conversion bottom-up, the final result may still contain subterms to which the supplied conversion applies. For example, in:

```
- DEPTH_CONV BETA_CONV (Term '(λf x. (f x) + 1) (λy.y) 2');
> val it = |- (λf x. (f x) + 1)(λy. y)2 = ((λy. y)2) + 1 : thm
```

the right-hand side of the result still contains a beta-redex, because the redex $(\lambda y. y)2$ is introduced by virtue of an application of `BETA_CONV` higher-up in the structure of the input term. By contrast, in the example:

```
- DEPTH_CONV BETA_CONV (Term '(λf x. (f x)) (λy.y) 2');
> val it = |- (λf x. f x)(λy. y)2 = 2 : thm
```

all beta-redexes are eliminated, because `DEPTH_CONV` repeats the supplied conversion (in this case, `BETA_CONV`) at each subterm (in this case, at the top-level term).

Uses

If the conversion `c` implements the evaluation of a function in logic, then `DEPTH_CONV c` will do bottom-up evaluation of nested applications of it. For example, the conversion `ADD_CONV` implements addition of natural number constants within the logic. Thus, the effect of:

```
- DEPTH_CONV reduceLib.ADD_CONV (Term '(1 + 2) + (3 + 4 + 5)');
> val it = |- (1 + 2) + (3 + (4 + 5)) = 15 : thm
```

is to compute the sum represented by the input term.

Comments

The implementation of this function uses failure to avoid rebuilding unchanged subterms. That is to say, during execution the exception `QConv.UNCHANGED` may be generated and later trapped. The behaviour of the function is dependent on this use of failure. So, if the conversion given as an argument happens to generate the same exception, the operation of `DEPTH_CONV` will be unpredictable.

See also

`Conv.ONCE_DEPTH_CONV`, `Conv.REDEPTH_CONV`, `Conv.TOP_DEPTH_CONV`.

DEPTH_EXISTS_CONV	(unwindLib)
--------------------------	--------------------

`DEPTH_EXISTS_CONV : (conv -> conv)`

Synopsis

Applies a conversion to the body of nested existential quantifications.

Description

DEPTH_EXISTS_CONV conv "?x1 ... xn. body" applies conv to "body" and returns a theorem of the form:

$$\vdash (\exists x_1 \dots x_n. \text{body}) = (\exists x_1 \dots x_n. \text{body}')$$

Failure

Fails if the application of conv fails.

Example

```
#DEPTH_EXISTS_CONV BETA_CONV "?x y z. (\w. x /\ y /\ z /\ w) T";;
|- (?x y z. (\w. x /\ y /\ z /\ w)T) = (?x y z. x /\ y /\ z /\ T)
```

See also

unwindLib.DEPTH_FORALL_CONV.

DEPTH_FORALL_CONV

(unwindLib)

DEPTH_FORALL_CONV : (conv -> conv)

Synopsis

Applies a conversion to the body of nested universal quantifications.

Description

DEPTH_FORALL_CONV conv "!x1 ... xn. body" applies conv to "body" and returns a theorem of the form:

$$\vdash (!x_1 \dots x_n. \text{body}) = (!x_1 \dots x_n. \text{body}')$$

Failure

Fails if the application of conv fails.

Example

```
#DEPTH_FORALL_CONV BETA_CONV "!x y z. (\w. x /\ y /\ z /\ w) T";;
|- (!x y z. (\w. x /\ y /\ z /\ w)T) = (!x y z. x /\ y /\ z /\ T)
```

See also

`unwindLib.DEPTH_EXISTS_CONV`.

`DEPTH_STRENGTHEN_CONSEQ_CONV` (ConseqConv)

`DEPTH_STRENGTHEN_CONSEQ_CONV` : `conseq_conv -> conseq_conv`

Synopsis

Applies a consequence conversion repeatedly to all the sub-terms of a term, in bottom-up order.

Description

`DEPTH_STRENGTHEN_CONSEQ_CONV c` is defined as `DEPTH_CONSEQ_CONV (K c) CONSEQ_CONV_STRENGTHEN_`. So, its just a slightly simplified interface to `DEPTH_CONSEQ_CONV`, that tries to strengthen all the time and that does not require the conversion to know about directions.

See also

`Conv.DEPTH_CONV`, `ConseqConv.ONCE_DEPTH_CONSEQ_CONV`,
`ConseqConv.NUM_DEPTH_CONSEQ_CONV`, `ConseqConv.DEPTH_CONSEQ_CONV`.

`dest_abs` (Term)

`dest_abs` : `term -> term * term`

Synopsis

Breaks apart an abstraction into abstracted variable and body.

Description

`dest_abs` is a term destructor for abstractions: if `M` is a term of the form `\v.t`, then `dest_abs M` returns `(v,t)`.

Failure

Fails if it is not given a lambda abstraction.

See also

`Term.mk_abs`, `Term.is_abs`, `Term.dest_var`, `Term.dest_const`, `Term.dest_comb`,
`boolSyntax.strip_abs`.

dest_anylet

(pairSyntax)

```
dest_anylet : term -> (term * term) list * term
```

Synopsis

Destructs arbitrary let terms.

Description

The invocation `dest_anylet M` where `M` has the form of a let-abstraction, i.e., `LET P Q`, returns a pair `([(a1,b1), ..., (an,bn)], body)`, where the first argument is a list of bindings, and the second is the body of the let. The list of bindings is required since let terms can, in general, be of the form (using surface syntax) `let a1 = b1 and ... and an = bn in body`.

Each `ai` can be a varstruct (a single variable or a tuple of variables), or a function variable applied to a sequence of varstructs.

Failure

Fails if `M` is not a let abstraction.

Example

```
- dest_anylet ``let f (x,y) = M and g z = N in g (f (a,b))``;
> val it = ([('f (x,y)', 'M'), ('g z', 'N')], 'g (f (a,b))')
```

```
- dest_anylet ``let f (x,y) = M in
                let g z = N
                in g (f (a,b))``;
> val it = ([('f (x,y)', 'M')], 'let g z = N in g (f (a,b))')
```

Uses

Programming that involves manipulation of term syntax.

See also

`boolSyntax.dest_let`, `pairSyntax.mk_anylet`, `pairSyntax.list_mk_anylet`, `pairSyntax.strip_anylet`.

dest_arb

(boolSyntax)

```
dest_arb : term -> hol_type
```

Synopsis

Extract the type of an instance of the ARB constant.

Description

If M is an instance of the constant ARB with type ty , then `dest_arb M` equals ty .

Failure

Fails if M is not an instance of ARB.

Comments

When it succeeds, an invocation of `dest_arb` is equivalent to `type_of`.

See also

`boolSyntax.mk_arb`, `boolSyntax.is_arb`.

<code>dest_bool_case</code>	<code>(boolSyntax)</code>
-----------------------------	---------------------------

```
dest_bool_case : term -> term * term * term
```

Synopsis

Destructs a case expression over `bool`.

Description

If M has the form `bool_case M1 M2 b`, then `dest_bool_case M` returns $M1, M2, b$.

Failure

Fails if M is not a full application of the `bool_case` constant.

See also

`boolSyntax.mk_bool_case`, `boolSyntax.is_bool_case`.

<code>dest_comb</code>	<code>(Term)</code>
------------------------	---------------------

```
dest_comb : term -> term * term
```

Synopsis

Breaks apart a combination (function application) into rator and rand.

Description

dest_comb is a term destructor for combinations. If term M has the form $f\ x$, then `dest_comb M` equals (f,x) .

Failure

Fails if the argument is not a function application.

See also

Term.mk_comb, Term.is_comb, Term.dest_var, Term.dest_const, Term.dest_abs, boolSyntax.strip_comb.

dest_cond	(boolSyntax)
-----------	--------------

`dest_cond : term -> term * term * term`

Synopsis

Breaks apart a conditional into the three terms involved.

Description

If M has the form `if t then t1 else t2` then `dest_cond M` returns $(t,t1,t2)$.

Failure

Fails if M is not a conditional.

See also

boolSyntax.mk_cond, boolSyntax.is_cond.

dest_conj	(boolSyntax)
-----------	--------------

`dest_conj : term -> term * term`

Synopsis

Term destructor for conjunctions.

Description

If M is a term $t1 \ /\ \ t2$, then `dest_conj M` returns $(t1,t2)$.

Failure

Fails if M is not a conjunction.

See also

`boolSyntax.mk_conj`, `boolSyntax.is_conj`, `boolSyntax.list_mk_conj`,
`boolSyntax.strip_conj`.

<code>dest_cons</code>	<code>(listSyntax)</code>
------------------------	---------------------------

`dest_cons : term -> term * term`

Synopsis

Breaks apart a ‘CONS pair’ into head and tail.

Description

`dest_cons` is a term destructor for ‘CONS pairs’. When applied to a term representing a nonempty list $[t; t_1; \dots; t_n]$ (which is equivalent to `CONS t [t1; ...; tn]`), it returns the pair of terms $(t, [t_1; \dots; t_n])$.

Failure

Fails if the term is an empty list.

See also

`listSyntax.mk_cons`, `listSyntax.is_cons`, `listSyntax.mk_list`,
`listSyntax.dest_list`, `listSyntax.is_list`.

<code>dest_const</code>	<code>(Term)</code>
-------------------------	---------------------

`dest_const : term -> string * hol_type`

Synopsis

Breaks apart a constant into name and type.

Description

`dest_const` is a term destructor for constants. If M is a constant with name c and type ty , then `dest_const M` returns (c, ty) .

Failure

Fails if M is not a constant.

Comments

In Hol98, constants also carry the theory they are declared in. A more precise and robust way to analyze a constant is with `dest_thy_const`.

See also

`Term.mk_const`, `Term.mk_thy_const`, `Term.dest_thy_const`, `Term.is_const`,
`Term.dest_abs`, `Term.dest_comb`, `Term.dest_var`.

<code>dest_disj</code>

<code>(boolSyntax)</code>

`dest_disj : term -> term * term`

Synopsis

Term destructor for disjunctions.

Description

If M is a term having the form $t_1 \ \vee \ t_2$, then `dest_disj M` returns (t_1, t_2) .

Failure

Fails if M is not a disjunction.

See also

`boolSyntax.mk_disj`, `boolSyntax.is_disj`, `boolSyntax.strip_disj`,
`boolSyntax.list_mk_disj`.

<code>dest_eq</code>

<code>(boolSyntax)</code>

`dest_eq : term -> term * term`

Synopsis

Term destructor for equality.

Description

If M is the term $t_1 = t_2$, then `dest_eq M` returns (t_1, t_2) .

Failure

Fails if M is not an equality.

See also

`boolSyntax.mk_eq`, `boolSyntax.is_eq`, `boolSyntax.lhs`, `boolSyntax.rhs`.

<code>dest_eq_ty</code>	<code>(boolSyntax)</code>
-------------------------	---------------------------

`dest_eq_ty` : `term` -> `term` * `term` * `hol_type`

Synopsis

Term destructor for equality.

Description

If M is the term $t_1 = t_2$, then `dest_eq_ty M` returns (t_1, t_2, ty) , where ty is the type of t_1 (and thus also of t_2).

Failure

Fails if M is not an equality.

Uses

Gives an efficient way to break apart an equality and get the type of the equality. Useful for obtaining that last fraction of speed when optimizing the bejeesus out of an inference rule.

See also

`boolSyntax.mk_eq`, `boolSyntax.is_eq`, `boolSyntax.lhs`, `boolSyntax.rhs`.

<code>dest_exists</code>	<code>(boolSyntax)</code>
--------------------------	---------------------------

`dest_exists` : `term` -> `term` * `term`

Synopsis

Breaks apart a existentially quantified term into quantified variable and body.

Description

If M has the form $?x. t$, then `dest_exists M` returns (x, t) .

Failure

Fails if M is not a existential quantification.

See also

`boolSyntax.mk_exists`, `boolSyntax.is_exists`, `boolSyntax.strip_exists`.

<code>dest_exists1</code>

<code>(boolSyntax)</code>

```
dest_exists1 : term -> term * term
```

Synopsis

Breaks apart a unique existence term into quantified variable and body.

Description

If M has the form $?!x. t$, then `dest_exists1 M` returns (x,t) .

Failure

Fails if M is not a unique existence term.

See also

`boolSyntax.mk_exists1`, `boolSyntax.is_exists1`.

<code>dest_forall</code>

<code>(boolSyntax)</code>

```
dest_forall : term -> term * term
```

Synopsis

Breaks apart a universally quantified term into quantified variable and body.

Description

If M has the form $!x. t$, then `dest_forall M` returns (x,t) .

Failure

Fails if M is not a universal quantification.

See also

`boolSyntax.mk_forall`, `boolSyntax.is_forall`, `boolSyntax.strip_forall`,
`boolSyntax.list_mk_forall`.

<code>dest_imp</code>	<code>(boolSyntax)</code>
-----------------------	---------------------------

```
dest_imp : term -> term * term
```

Synopsis

Breaks an implication or negation into antecedent and consequent.

Description

`dest_imp` is a term destructor for implications. It treats negations as implications with consequent F . Thus, if M is a term with the form $t1 ==> t2$, then `dest_imp M` returns $(t1, t2)$, and if M has the form $\sim t$, then `dest_imp M` returns (t, F) .

Failure

Fails if M is neither an implication nor a negation.

Comments

Destructs negations for increased functionality of HOL-style resolution. If the ability to destruct negations is not desired, as is only right, then use `dest_imp_only`.

See also

`boolSyntax.mk_imp`, `boolSyntax.dest_imp_only`, `boolSyntax.is_imp`,
`boolSyntax.is_imp_only`, `boolSyntax.strip_imp`, `boolSyntax.list_mk_imp`.

<code>dest_imp_only</code>	<code>(boolSyntax)</code>
----------------------------	---------------------------

```
dest_imp_only : term -> term * term
```

Synopsis

Breaks an implication into antecedent and consequent.

Description

If M is a term with the form $t1 ==> t2$, then `dest_imp_only M` returns $(t1, t2)$.

Failure

Fails if M is not an implication.

See also

boolSyntax.mk_imp, boolSyntax.dest_imp, boolSyntax.is_imp,
 boolSyntax.is_imp_only, boolSyntax.strip_imp, boolSyntax.list_mk_imp.

dest_let

(boolSyntax)

```
dest_let : term -> term * term
```

Synopsis

Breaks apart a let-expression.

Description

If M is a term of the form `LET M N`, then `dest_let M` returns (M,N) .

Example

```
- dest_let (Term 'let x = P /\ Q in x \/ x');
> val it = ('\x. x \/ x', 'P /\ Q') : term * term
```

Failure

Fails if M is not of the form `LET M N`.

See also

boolSyntax.mk_let, boolSyntax.is_let.

dest_list

(listSyntax)

```
dest_list : term -> term list * hol_type
```

Synopsis

Iteratively breaks apart a list term.

Description

`dest_list` is a term destructor for lists: `dest_list "[t1;...;tn]:ty list"` returns $([t1,\dots,tn], ty)$.

Failure

Fails if the term is not a list.

See also

`listSyntax.mk_list`, `listSyntax.is_list`, `listSyntax.mk_cons`,
`listSyntax.dest_cons`, `listSyntax.is_cons`.

<code>dest_neg</code>	<code>(boolSyntax)</code>
-----------------------	---------------------------

`dest_neg : term -> term`

Synopsis

Breaks apart a negation, returning its body.

Description

`dest_neg` is a term destructor for negations: if M has the form $\sim t$, then `dest_neg M` returns t .

Failure

Fails with `dest_neg` if term is not a negation.

See also

`boolSyntax.mk_neg`, `boolSyntax.is_neg`.

<code>dest_numeral</code>	<code>(numSyntax)</code>
---------------------------	--------------------------

`dest_numeral : term -> Arbnum.num`

Synopsis

Convert HOL numeral to ML bignum value.

Description

An invocation `dest_numeral tm`, where tm is a HOL numeral (a literal of type `num`), returns the corresponding ML value of type `Arbnum.num`. A numeral is a dyadic positional notation described by the following BNF:

```

<numeral> ::= 0 | NUMERAL <bits>
<bits>    ::= ZERO | BIT1 (<bits>) | BIT2 (<bits>)

```

The NUMERAL constant is used as a tag signalling that its argument is indeed a numeric literal. The ZERO constant is equal to 0, and $\text{BIT1}(n) = 2*n + 1$ while $\text{BIT2}(n) = 2*n + 2$. This representation allows asymptotically efficient operations on numeric values.

The system prettyprinter will print a numeral as a string of digits.

Example

```

- dest_numeral ``1234``;
> val it = 1234 : num

```

Failure

Fails if `tm` is not in the specified format.

See also

`numSyntax.mk_numeral`, `numSyntax.is_numeral`.

dest_pabs

(pairSyntax)

```
dest_pabs : term -> term * term
```

Synopsis

Breaks apart a paired abstraction into abstracted pair and body.

Description

`dest_pabs` is a term destructor for paired abstractions: `dest_abs "\pair. t"` returns `("pair", "t")`.

Failure

Fails with `dest_pabs` if term is not a paired abstraction.

See also

`Term.dest_abs`, `pairSyntax.mk_pabs`, `pairSyntax.is_pabs`, `pairSyntax.strip_pabs`.

dest_pair

(pairSyntax)

```
dest_pair : term -> term * term
```

Synopsis

Breaks apart a pair into two separate terms.

Description

`dest_pair` is a term destructor for pairs: if M is a term of the form (t_1, t_2) , then `dest_pair M` returns (t_1, t_2) .

Failure

Fails if M is not a pair.

See also

`pairSyntax.mk_pair`, `pairSyntax.is_pair`, `pairSyntax.strip_pair`.

<code>dest_pexists</code>	<code>(pairSyntax)</code>
---------------------------	---------------------------

`dest_pexists` : `term -> term * term`

Synopsis

Breaks apart paired existential quantifiers into the bound pair and the body.

Description

`dest_pexists` is a term destructor for paired existential quantification. The application of `dest_pexists` to `?pair. t` returns (pair, t) .

Failure

Fails with `dest_pexists` if term is not a paired existential quantification.

See also

`boolSyntax.dest_exists`, `pairSyntax.is_pexists`, `pairSyntax.strip_pexists`.

<code>dest_pforall</code>	<code>(pairSyntax)</code>
---------------------------	---------------------------

`dest_pforall` : `term -> term * term`

Synopsis

Breaks apart paired universal quantifiers into the bound pair and the body.

Description

dest_pforall is a term destructor for paired universal quantification. The application of dest_pforall to "!pair. t" returns ("pair","t").

Failure

Fails with dest_pforall if term is not a paired universal quantification.

See also

boolSyntax.dest_forall, pairSyntax.is_pforall, pairSyntax.strip_pforall.

dest_prod

(pairSyntax)

```
dest_prod : hol_type -> hol_type * hol_type
```

Synopsis

Breaks a product type into its two component types.

Description

dest_prod is a type destructor for products: dest_pair ":t1#t2" returns (":t1",":t2").

Failure

Fails with dest_prod if the argument is not a product type.

See also

pairSyntax.is_prod, pairSyntax.mk_prod.

dest_pselect

(pairSyntax)

```
dest_pselect : term -> term * term
```

Synopsis

Breaks apart a paired choice-term into the selected pair and the body.

Description

dest_pselect is a term destructor for paired choice terms. The application of dest_select to @pair. t returns (pair,t).

Failure

Fails with `dest_pselect` if term is not a paired choice-term.

See also

`boolSyntax.dest_select`, `pairSyntax.is_pselect`.

dest_ptree

(patriciaLib)

```
dest_ptree : term -> term_ptree
```

Synopsis

Term destructor for Patricia trees.

Description

The destructor `dest_ptree` will return a Patricia tree in ML that corresponds with the supplied HOL term. The ML abstract data type `term_ptree` is defined in `patriciaLib`.

Failure

The conversion will fail if the supplied term is not well constructed Patricia tree.

Example

```
- dest_ptree '(Branch 1 2 (Leaf 2 2) (Leaf 3 3))';
```

```
Exception-
```

```
  HOL_ERR
```

```
  {message = "not a valid Patricia tree", origin_function = "dest_ptree",
   origin_structure = "patricia"} raised
```

```
- dest_ptree '(Branch 0 0 (Leaf 3 3) (Leaf 2 2))';
```

```
val it = <ptree>: term_ptree
```

Comments

By default PolyML prints abstract data types in full. This can be turned off with:

```
let
```

```
  fun pp _ _ ( _: term_ptree) = PolyML.PrettyString "<ptree>"
```

```
in
```

```
  PolyML.addPrettyPrinter pp
```

```
end;
```

See also

patriciaLib.mk_ptree, patriciaLib.is_ptree.

<div style="display: flex; justify-content: space-between;"> dest_res_abstract (res_quanLib) </div>

dest_res_abstract : term -> (term # term # term)

Synopsis

Breaks apart a restricted abstract term into the quantified variable, predicate and body.

Description

dest_res_abstract is a term destructor for restricted abstraction:

```
dest_res_abstract "\var::P. t"
```

returns ("var", "P", "t").

Failure

Fails with dest_res_abstract if the term is not a restricted abstraction.

See also

res_quanLib.mk_res_abstract, res_quanLib.is_res_abstract.

<div style="display: flex; justify-content: space-between;"> dest_res_abstract (res_quanTools) </div>

dest_res_abstract : (term -> (term # term # term))

Synopsis

Breaks apart a restricted abstract term into the quantified variable, predicate and body.

Description

dest_res_abstract is a term destructor for restricted abstraction:

```
dest_res_abstract "\var::P. t"
```

returns ("var", "P", "t").

Failure

Fails with `dest_res_abstract` if the term is not a restricted abstraction.

See also

`res_quantTools.mk_res_abstract`, `res_quantTools.is_res_abstract`.

<code>dest_res_exists</code>	<code>(res_quantLib)</code>
------------------------------	-----------------------------

`dest_res_exists : term -> (term # term # term)`

Synopsis

Breaks apart a restricted existentially quantified term into the quantified variable, predicate and body.

Description

`dest_res_exists` is a term destructor for restricted existential quantification:

```
dest_res_exists "?var::P. t"
```

returns ("var", "P", "t").

Failure

Fails with `dest_res_exists` if the term is not a restricted existential quantification.

See also

`res_quantLib.mk_res_exists`, `res_quantLib.is_res_exists`,
`res_quantLib.strip_res_exists`.

<code>dest_res_exists</code>	<code>(res_quantTools)</code>
------------------------------	-------------------------------

`dest_res_exists : (term -> (term # term # term))`

Synopsis

Breaks apart a restricted existentially quantified term into the quantified variable, predicate and body.

Description

`dest_res_exists` is a term destructor for restricted existential quantification:

```
dest_res_exists "?var::P. t"
```

```
returns ("var","P","t").
```

Failure

Fails with `dest_res_exists` if the term is not a restricted existential quantification.

See also

`res_quantTools.mk_res_exists`, `res_quantTools.is_res_exists`,
`res_quantTools.strip_res_exists`.

<div style="display: flex; justify-content: space-between;"> dest_res_exists_unique (res_quantLib) </div>

```
dest_res_exists_unique : term -> (term # term # term)
```

Synopsis

Breaks apart a restricted unique existential quantified term into the quantified variable, predicate and body.

Description

`dest_res_exists_unique` is a term destructor for restricted existential quantification:

```
dest_res_exists_unique "?var::P. t"
```

```
returns ("var","P","t").
```

Failure

Fails with `dest_res_exists_unique` if the term is not a restricted existential quantification.

See also

`res_quantLib.mk_res_exists_unique`, `res_quantLib.is_res_exists_unique`.

<div style="display: flex; justify-content: space-between;"> dest_res_forall (res_quantLib) </div>
--

```
dest_res_forall : term -> (term # term # term)
```

Synopsis

Breaks apart a restricted universally quantified term into the quantified variable, predicate and body.

Description

`dest_res_forall` is a term destructor for restricted universal quantification:

```
dest_res_forall "!var::P. t"
```

returns ("var", "P", "t").

Failure

Fails with `dest_res_forall` if the term is not a restricted universal quantification.

See also

`res_quantLib.mk_res_forall`, `res_quantLib.is_res_forall`,
`res_quantLib.strip_res_forall`.

<code>dest_res_forall</code>	<code>(res_quantTools)</code>
------------------------------	-------------------------------

```
dest_res_forall : (term -> (term # term # term))
```

Synopsis

Breaks apart a restricted universally quantified term into the quantified variable, predicate and body.

Description

`dest_res_forall` is a term destructor for restricted universal quantification:

```
dest_res_forall "!var::P. t"
```

returns ("var", "P", "t").

Failure

Fails with `dest_res_forall` if the term is not a restricted universal quantification.

See also

`res_quantTools.mk_res_forall`, `res_quantTools.is_res_forall`,
`res_quantTools.strip_res_forall`.

<div style="display: flex; justify-content: space-between;"> dest_res_select (res_quanLib) </div>

```
dest_res_select : term -> (term # term # term)
```

Synopsis

Breaks apart a restricted choice quantified term into the quantified variable, predicate and body.

Description

dest_res_select is a term destructor for restricted choice quantification:

```
dest_res_select "@var::P. t"
```

returns ("var", "P", "t").

Failure

Fails with dest_res_select if the term is not a restricted choice quantification.

See also

res_quanLib.mk_res_select, res_quanLib.is_res_select.

<div style="display: flex; justify-content: space-between;"> dest_res_select (res_quanTools) </div>

```
dest_res_select : (term -> (term # term # term))
```

Synopsis

Breaks apart a restricted choice quantified term into the quantified variable, predicate and body.

Description

dest_res_select is a term destructor for restricted choice quantification:

```
dest_res_select "@var::P. t"
```

returns ("var", "P", "t").

Failure

Fails with dest_res_select if the term is not a restricted choice quantification.

See also

`res_quantools.mk_res_select`, `res_quantools.is_res_select`.

<code>dest_select</code>	<code>(boolSyntax)</code>
--------------------------	---------------------------

`dest_select` : `term` -> `term * term`

Synopsis

Breaks apart a choice term into selected variable and body.

Description

If M has the form $@v. t$ then `dest_select M` returns (v,t) .

Failure

Fails if M is not an epsilon-term.

See also

`boolSyntax.mk_select`, `boolSyntax.is_select`.

<code>dest_theory</code>	<code>(DB)</code>
--------------------------	-------------------

`dest_theory` : `string` -> `theory`

Synopsis

Return the contents of a theory.

Description

An invocation `dest_theory s` returns a structure

`THEORY(s, {types, consts, parents, axioms, definitions, theorems})`

where `types` is a list of `(string, int)` pairs that contains all the type operators declared in `s`, `consts` is a list of `(string, hol_type)` pairs enumerating all the term constants declared in `s`, `parents` is a list of strings denoting the parents of `s`, `axioms` is a list of `(string, thm)` pairs denoting the axioms asserted in `s`, `definitions` is a list of `(string, thm)` pairs denoting the definitions of `s`, and `theorems` is a list of `(string, thm)` pairs denoting the theorems proved and stored in `s`.

The call `dest_theory "-"` may be used to access the contents of the current theory.

Failure

If `s` is not the name of a loaded theory.

Example

```
- dest_theory "option";
> val it =
  Theory: option

  Parents:
    sum
    one

  Type constants:
    option 1

  Term constants:
    option_case    : 'b -> ('a -> 'b) -> 'a option -> 'b
    NONE          : 'a option
    SOME          : 'a -> 'a option
    IS_NONE       : 'a option -> bool
    option_ABS    : 'a + one -> 'a option
    IS_SOME       : 'a option -> bool
    option_REP    : 'a option -> 'a + one
    THE           : 'a option -> 'a
    OPTION_JOIN   : 'a option option -> 'a option
    OPTION_MAP    : ('a -> 'b) -> 'a option -> 'b option

  Definitions:
    option_TY_DEF  |- ?rep. TYPE_DEFINITION (\x. T) rep
    option_REP_ABS_DEF
    |- (!a. option_ABS (option_REP a) = a) /\
       !r. (\x. T) r = (option_REP (option_ABS r) = r)
    SOME_DEF      |- !x. SOME x = option_ABS (INL x)
    NONE_DEF      |- NONE = option_ABS (INR ())
    option_case_def
    |- (!u f. case u f NONE = u) /\ !u f x. case u f (SOME x) = f x
    OPTION_MAP_DEF
    |- (!f x. OPTION_MAP f (SOME x) = SOME (f x)) /\
```

```

!f. OPTION_MAP f NONE = NONE
IS_SOME_DEF  |- (!x. IS_SOME (SOME x) = T) /\ (IS_SOME NONE = F)
IS_NONE_DEF  |- (!x. IS_NONE (SOME x) = F) /\ (IS_NONE NONE = T)
THE_DEF      |- !x. THE (SOME x) = x
OPTION_JOIN_DEF
|- (OPTION_JOIN NONE = NONE) /\ !x. OPTION_JOIN (SOME x) = x

```

Theorems:

```

option_Axiom  |- !e f. ?fn. (!x. fn (SOME x) = f x) /\ (fn NONE = e)
option_induction  |- !P. P NONE /\ (!a. P (SOME a)) ==> !x. P x
SOME_11       |- !x y. (SOME x = SOME y) = (x = y)
NOT_NONE_SOME  |- !x. ~(NONE = SOME x)
NOT_SOME_NONE  |- !x. ~(SOME x = NONE)
option_nchotomy  |- !opt. (opt = NONE) \/ ?x. opt = SOME x
option_CLAUSES
|- (!x y. (SOME x = SOME y) = (x = y)) /\ (!x. THE (SOME x) = x) /\
  (!x. ~(NONE = SOME x)) /\ (!x. ~(SOME x = NONE)) /\
  (!x. IS_SOME (SOME x) = T) /\ (IS_SOME NONE = F) /\
  (!x. IS_NONE x = (x = NONE)) /\ (!x. ~IS_SOME x = (x = NONE)) /\
  (!x. IS_SOME x ==> (SOME (THE x) = x)) /\
  (!x. case NONE SOME x = x) /\ (!x. case x SOME x = x) /\
  (!x. IS_NONE x ==> (case e f x = e)) /\
  (!x. IS_SOME x ==> (case e f x = f (THE x))) /\
  (!x. IS_SOME x ==> (case e SOME x = x)) /\
  (!u f. case u f NONE = u) /\ (!u f x. case u f (SOME x) = f x) /\
  (!f x. OPTION_MAP f (SOME x) = SOME (f x)) /\
  (!f. OPTION_MAP f NONE = NONE) /\ (OPTION_JOIN NONE = NONE) /\
  !x. OPTION_JOIN (SOME x) = x
option_case_compute
|- case e f x = (if IS_SOME x then f (THE x) else e)
OPTION_MAP_EQ_SOME
|- !f x y. (OPTION_MAP f x = SOME y) = ?z. (x = SOME z) /\ (y = f z)
OPTION_MAP_EQ_NONE  |- !f x. (OPTION_MAP f x = NONE) = (x = NONE)
OPTION_JOIN_EQ_SOME
|- !x y. (OPTION_JOIN x = SOME y) = (x = SOME (SOME y))
option_case_cong
|- !M M' u f.
  (M = M') /\ ((M' = NONE) ==> (u = u')) /\
  (!x. (M' = SOME x) ==> (f x = f' x)) ==>
  (case u f M = case u' f' M')

```

: theory

Comments

A prettyprinter is installed for the type theory, but the contents may still be accessed via pattern matching.

See also

DB.print_theory.

dest_thm	(Thm)
----------	-------

```
dest_thm : thm -> term list * term
```

Synopsis

Breaks a theorem into assumption list and conclusion.

Description

dest_thm ([t1,...,tn] |- t) returns ([t1,...,tn],t).

Failure

Never fails.

Example

```
- dest_thm (ASSUME (Term 'p=T'));
> val it = (['p = T'], 'p = T') : term list * term
```

See also

Thm.concl, Thm.hyp.

dest_thy_const	(Term)
----------------	--------

```
dest_thy_const : term -> {Thy:string, Name:string, Ty:hol_type}
```

Synopsis

Breaks apart a constant into name, theory, and type.

Description

`dest_thy_const` is a term destructor for constants. If `M` is a constant, declared in theory `Thy` with name `Name`, having type `ty`, then `dest_thy_const M` returns `{Thy, Name, Ty}`, where `Ty` is equal to `ty`.

Failure

Fails if `M` is not a constant.

Comments

A more precise alternative to `dest_const`.

See also

`Term.mk_const`, `Term.dest_thy_const`, `Term.is_const`, `Term.dest_abs`, `Term.dest_comb`, `Term.dest_var`.

<code>dest_thy_type</code>	<code>(Type)</code>
----------------------------	---------------------

```
dest_thy_type
  : hol_type -> {Thy:string, Tyop:string,
                Args:hol_type list}
```

Synopsis

Breaks apart a type (other than a variable type).

Description

If `ty` is an application of a type operator `Tyop`, which was declared in theory `Thy`, to a list of types `Args`, then `dest_thy_type ty` returns `{Tyop,Thy,Args}`.

Failure

Fails if `ty` is a type variable.

Example

```
- dest_thy_type (alpha --> bool);
> val it = {Args = [':a', ':bool'], Thy = "min", Tyop = "fun"}
```

```
- try dest_thy_type alpha;
```

Exception raised at `Type.dest_thy_type`:

See also

Type.mk_thy_type, Type.dest_type, Type.mk_type, Term.mk_thy_const.

dest_type

(Type)

```
dest_type : hol_type -> string * hol_type list
```

Synopsis

Breaks apart a non-variable type.

Description

If `ty` is a type constant, then `dest_type ty` returns `(ty, [])`. If `ty` is a compound type `(ty1, ..., tyn)tyop`, then `dest_type ty` returns `(tyop, [ty1, ..., tyn])`.

Failure

Fails if `ty` is a type variable.

Example

```
- dest_type bool;  
> val it = ("bool", []) : string * hol_type list  
  
- dest_type (alpha --> bool);  
> val it = ("fun", [':a', ':bool']) : string * hol_type list
```

Comments

A more precise alternative is `dest_thy_type`, which tells which theory the type operator was declared in.

See also

Type.mk_type, Type.dest_thy_type, Type.dest_vartype.

dest_var

(Term)

```
dest_var : term -> string * hol_type
```

Synopsis

Breaks apart a variable into name and type.

Description

If M is a HOL variable, then `dest_var M` returns (v,ty) , where v is the name of the variable, and ty is its type.

Failure

Fails if M is not a variable.

See also

`Term.mk_var`, `Term.is_var`, `Term.dest_const`, `Term.dest_comb`, `Term.dest_abs`.

<code>dest_vartype</code>	<code>(Type)</code>
---------------------------	---------------------

```
dest_vartype : hol_type -> string
```

Synopsis

Breaks a type variable down to its name.

Failure

Fails with `dest_vartype` if the type is not a type variable.

Example

```
- dest_vartype alpha;
> val it = "'a" : string

- try dest_vartype bool;
```

```
Exception raised at Type.dest_vartype:
not a type variable
```

See also

`Type.mk_vartype`, `Type.is_vartype`, `Type.dest_type`.

<code>diminish_srw_ss</code>	<code>(BasicProvers)</code>
------------------------------	-----------------------------

```
diminish_srw_ss : string list -> ssfrag list
```

Synopsis

Removes named simpset fragments from the stateful simpset.

Description

A call to `diminish_srw_ss fragnames` removes the simpset fragments with names given in `fragnames` from the stateful simpset which is returned by `srw_ss()`, and which is used by `SRW_TAC`. This removal is done as a side effect.

The function also returns the simpset fragments that have been removed. This allows them to be put back into the simpset with a call to `augment_srw_ss`.

The effect of this call is not exported to descendent theories.

Failure

Never fails. A name can be provided for a fragment that does not appear in the stateful simpset. In this case, the name is just ignored, and there will be no corresponding fragment in the list that the function returns.

Example

```
- SIMP_CONV (srw_ss()) [] ‘‘MAP ($+ 1) [3;4;5]’’;
> val it = |- MAP ($+ 1) [3; 4; 5] = [4; 5; 6] : thm

- val frags = diminish_srw_ss ["REDUCE"]
> val frags =
  [Simplification set: REDUCE
  Conversions:
    REDUCE_CONV (arithmetic reduction), keyed on pattern ‘‘EVEN x’’
    REDUCE_CONV (arithmetic reduction), keyed on pattern ‘‘ODD x’’
    REDUCE_CONV (arithmetic reduction), keyed on pattern ‘‘PRE x’’
    REDUCE_CONV (arithmetic reduction), keyed on pattern ‘‘SUC x’’
  ...] : ssfrag list

- SIMP_CONV (srw_ss()) [] ‘‘MAP ($+ 1) [3;4;5]’’;
> val it = |- MAP ($+ 1) [3; 4; 5] = [1 + 3; 1 + 4; 1 + 5] : thm

- augment_srw_ss frags;
> val it = () : unit

- SIMP_CONV (srw_ss()) [] ‘‘MAP ($+ 1) [3;4;5]’’;
> val it = |- MAP ($+ 1) [3; 4; 5] = [4; 5; 6] : thm
```

See also

`BasicProvers.augment_srw_ss`, `simplib.remove_ssfrags`.

<code>directed_conseq_conv</code>	<code>(ConseqConv)</code>
-----------------------------------	---------------------------

```
type directed_conseq_conv
```

Synopsis

A type for consequence conversions that can be instructed on whether to strengthen or weaken a given term.

Description

Given a `CONSEQ_CONV_direction`, a directed consequence conversion tries to strengthen, weaken or whatever it can depending on the given direction.

See also

`ConseqConv.conseq_conv`, `ConseqConv.CONSEQ_CONV_direction`.

<code>disable_tyabbrev_printing</code>	<code>(Parse)</code>
--	----------------------

```
disable_tyabbrev_printing : string -> unit
```

Synopsis

Disables the printing of a type abbreviation.

Description

A call to `disable_tyabbrev_printing s` causes the type abbreviation mapping the string `s` to some type expansion not to be printed when an instance of the type expansion is seen.

Failure

Never fails. If there is no abbreviation of the given name, a call to `disable_tyabbrev_printing` will silently do nothing.

Example

```
- type_abbrev("LIST", ``:'a list``)
> val it = () : unit

- ``:num list``;
```



```

> val it = ``:num LIST`` : hol_type

- disable_tyabbrev_printing "LIST";
> val it = () : unit

- ``:num LIST``;
> val it = ``:num list`` : hol_type

```

Comments

When a type-abbreviation is established with the function `type_abbrev`, this alters both parsing and printing: when the new abbreviation appears in input the type parser will translate away the abbreviation. Similarly, when an instance of the abbreviation appears in a type that the printer is to output, it will replace the instance with the abbreviation.

This is generally the appropriate behaviour. However, there are a number of useful abbreviations where reversing parsing when printing is not so useful. For example, the abbreviation mapping `'a set` to `'a -> bool` is convenient, but it would be a mistake having it print because types such as that of conjunction would print as

```
(/\) : bool -> bool set
```

which is rather confusing.

As with other printing and parsing functions, there is a version of this function, `temp_disable_tyabbrev_printing` that does not cause its effect to persist with an exported theory.

See also

`Parse.type_abbrev`.

DISCARD_TAC	(Tactic)
-------------	----------

DISCARD_TAC : thm_tactic

Synopsis

Discards a theorem already present in a goal's assumptions.

Description

When applied to a theorem $A' \mid- s$ and a goal, `DISCARD_TAC` checks that s is simply `T` (true), or already exists (up to alpha-conversion) in the assumption list of the goal. In either case, the tactic has no effect. Otherwise, it fails.

```

A ?- t
===== DISCARD_TAC (A' |- s)
A ?- t

```

Failure

Fails if the above conditions are not met, i.e. the theorem's conclusion is not T or already in the assumption list (up to alpha-conversion).

See also

Tactical.POP_ASSUM, Tactical.POP_ASSUM_LIST.

<code>disch</code>	(HolKernel)
--------------------	-------------

```
disch : ((term * term list) -> term list)
```

Synopsis

Removes those elements of a list of terms that are alpha equivalent to a given term.

Description

Given a pair $(t, t1)$ of term t and term list $t1$, `disch` removes those elements of $t1$ that are alpha equivalent to t .

Example

```
disch (''\x:bool.T'', [['A = T'', 'B = 3'', '\y:bool.T'']];
['A = T', 'B = 3'] : term list
```

See also

Lib.filter.

<code>DISCH</code>	(Thm)
--------------------	-------

```
DISCH : (term -> thm -> thm)
```

Synopsis

Discharges an assumption.

Description

$$\frac{A \mid\text{-} t}{\text{-----} \text{ DISCH } u} A - \{u\} \mid\text{-} u \implies t$$
Failure

DISCH will fail if u is not boolean.

Comments

The term u need not be a hypothesis. Discharging u will remove all identical and alpha-equivalent hypotheses.

See also

Drule.DISCH_ALL, Tactic.DISCH_TAC, Thm.cont.DISCH_THEN, Tactic.FILTER_DISCH_TAC, Thm.cont.FILTER_DISCH_THEN, Drule.NEG_DISCH, Tactic.STRIP_TAC, Drule.UNDISCH, Drule.UNDISCH_ALL, Tactic.UNDISCH_TAC.

DISCH_ALL

(Drule)

DISCH_ALL : thm -> thm

Synopsis

Discharges all hypotheses of a theorem.

Description

$$\frac{A_1, \dots, A_n \mid\text{-} t}{\text{-----} \text{ DISCH_ALL}} \mid\text{-} A_1 \implies \dots \implies A_n \implies t$$
Failure

DISCH_ALL never fails. If there are no hypotheses to discharge, it will simply return the theorem unchanged.

Comments

Users should not rely on the hypotheses being discharged in any particular order. Two or more alpha-convertible hypotheses will be discharged by a single implication; users should not rely on which hypothesis appears in the implication.

See also

Thm.DISCH, Tactic.DISCH_TAC, Thm.cont.DISCH_THEN, Drule.NEG_DISCH,
 Tactic.FILTER_DISCH_TAC, Thm.cont.FILTER_DISCH_THEN, Tactic.STRIP_TAC,
 Drule.UNDISCH, Drule.UNDISCH_ALL, Tactic.UNDISCH_TAC.

DISCH_TAC

(Tactic)

DISCH_TAC : tactic

Synopsis

Moves the antecedent of an implicative goal into the assumptions.

Description

```

  A ?- u ==> v
  =====
  DISCH_TAC
  A u {u} ?- v

```

Note that DISCH_TAC treats $\sim u$ as $u \implies F$, so will also work when applied to a goal with a negated conclusion.

Failure

DISCH_TAC will fail for goals which are not implications or negations.

Uses

Solving goals of the form $u \implies v$ by rewriting v with u , although the use of DISCH_THEN is usually more elegant in such cases.

Comments

If the antecedent already appears in the assumptions, it will be duplicated.

See also

Thm.DISCH, Drule.DISCH_ALL, Thm.cont.DISCH_THEN, Tactic.FILTER_DISCH_TAC,
 Thm.cont.FILTER_DISCH_THEN, Drule.NEG_DISCH, Tactic.STRIP_TAC, Drule.UNDISCH,
 Drule.UNDISCH_ALL, Tactic.UNDISCH_TAC.

DISCH_THEN

(Thm_cont)

DISCH_THEN : (thm_tactic -> tactic)

Synopsis

Undischarges an antecedent of an implication and passes it to a theorem-tactic.

Description

DISCH_THEN removes the antecedent and then creates a theorem by ASSUMEing it. This new theorem is passed to the theorem-tactic given as DISCH_THEN's argument. The consequent tactic is then applied. Thus:

$$\text{DISCH_THEN } f \text{ (asl, } t1 \implies t2) = f(\text{ASSUME } t1) \text{ (asl, } t2)$$

For example, if

```
A ?- t
===== f (ASSUME u)
B ?- v
```

then

```
A ?- u ==> t
===== DISCH_THEN f
      B ?- v
```

Note that DISCH_THEN treats $\sim u$ as $u \implies F$.

Failure

DISCH_THEN will fail for goals which are not implications or negations.

Example

The following shows how DISCH_THEN can be used to preprocess an antecedent before adding it to the assumptions.

```
A ?- (x = y) ==> t
===== DISCH_THEN (ASSUME_TAC o SYM)
      A u {y = x} ?- t
```

In many cases, it is possible to use an antecedent and then throw it away:

```
A ?- (x = y) ==> t x
===== DISCH_THEN (\th. PURE_REWRITE_TAC [th])
      A ?- t y
```

See also

Thm.DISCH, Drule.DISCH_ALL, Tactic.DISCH_TAC, Drule.NEG_DISCH, Tactic.FILTER_DISCH_TAC, Thm.cont.FILTER_DISCH_THEN, Tactic.STRIP_TAC, Drule.UNDISCH, Drule.UNDISCH_ALL, Tactic.UNDISCH_TAC.

DISJ1

(Thm)

DISJ1 : thm -> term -> thm

Synopsis

Introduces a right disjunct into the conclusion of a theorem.

Description

$$\frac{A \mid- t1}{A \mid- t1 \ \vee \ t2} \text{ DISJ1 } (A \mid- t1) \ t2$$
Failure

Fails unless the term argument is boolean.

Example

```
- DISJ1 TRUTH F;
> val it = |- T \ / F : thm
```

See also

Tactic.DISJ1_TAC, Thm.DISJ2, Tactic.DISJ2_TAC, Thm.DISJ_CASES.

DISJ1_TAC

(Tactic)

DISJ1_TAC : tactic

Synopsis

Selects the left disjunct of a disjunctive goal.

Description

$$\frac{A \ ?- \ t1 \ \vee \ t2}{A \ ?- \ t1} \text{ DISJ1_TAC}$$

Failure

Fails if the goal is not a disjunction.

See also

Thm.DISJ1, Thm.DISJ2, Tactic.DISJ2_TAC.

DISJ2

(Thm)

DISJ2 : term -> thm -> thm

Synopsis

Introduces a left disjunct into the conclusion of a theorem.

Description

$$\begin{array}{l} A \mid- t2 \\ \hline \text{DISJ2 "t1"} \\ A \mid- t1 \ \vee \ t2 \end{array}$$
Failure

Fails if the term argument is not boolean.

Example

```
- DISJ2 F TRUTH;
> val it = |- F \/\ T : thm
```

See also

Thm.DISJ1, Tactic.DISJ1_TAC, Tactic.DISJ2_TAC, Thm.DISJ_CASES.

DISJ2_TAC

(Tactic)

DISJ2_TAC : tactic

Synopsis

Selects the right disjunct of a disjunctive goal.

Description

$$\frac{A \text{ ?- } t1 \ \vee \ t2}{\text{===== DISJ2_TAC}} \quad A \text{ ?- } t2$$
Failure

Fails if the goal is not a disjunction.

See also

Thm.DISJ1, Tactic.DISJ1_TAC, Thm.DISJ2.

DISJ_CASES**(Thm)**

DISJ_CASES : (thm -> thm -> thm -> thm)

Synopsis

Eliminates disjunction by cases.

Description

The rule DISJ_CASES takes a disjunctive theorem, and two ‘case’ theorems, each with one of the disjuncts as a hypothesis while sharing alpha-equivalent conclusions. A new theorem is returned with the same conclusion as the ‘case’ theorems, and the union of all assumptions excepting the disjuncts.

$$\frac{A \text{ |- } t1 \ \vee \ t2 \quad A1 \text{ u } \{t1\} \text{ |- } t \quad A2 \text{ u } \{t2\} \text{ |- } t}{\text{----- DISJ_CASES}} \quad A \text{ u } A1 \text{ u } A2 \text{ |- } t$$
Failure

Fails if the first argument is not a disjunctive theorem, or if the conclusions of the other two theorems are not alpha-convertible.

Example

Specializing the built-in theorem num_CASES gives the theorem:

$$\text{th} = \text{ |- } (m = 0) \ \vee \ (?n. m = \text{SUC } n)$$

Using two additional theorems, each having one disjunct as a hypothesis:

$$\begin{aligned} \text{th1} &= (m = 0 \text{ |- } (\text{PRE } m = m) = (m = 0)) \\ \text{th2} &= (?n. m = \text{SUC } n \text{ |- } (\text{PRE } m = m) = (m = 0)) \end{aligned}$$

a new theorem can be derived:

```
- DISJ_CASES th th1 th2;
> val it = |- (PRE m = m) = (m = 0) : thm
```

Comments

Neither of the ‘case’ theorems is required to have either disjunct as a hypothesis, but otherwise DISJ_CASES is pointless.

See also

Tactic.DISJ_CASES_TAC, Thm_cont.DISJ_CASES_THEN, Thm_cont.DISJ_CASES_THEN2, Drule.DISJ_CASES_UNION, Thm.DISJ1, Thm.DISJ2.

DISJ_CASES_TAC	(Tactic)
----------------	----------

DISJ_CASES_TAC : thm_tactic

Synopsis

Produces a case split based on a disjunctive theorem.

Description

Given a theorem th of the form $A \vdash u \vee v$, DISJ_CASES_TAC th applied to a goal produces two subgoals, one with u as an assumption and one with v :

$$\frac{A \text{ ?- } t}{\text{DISJ_CASES_TAC } (A \text{ |- } u \vee v)}$$

$$A \text{ u } \{u\} \text{ ?- } t \quad A \text{ u } \{v\} \text{ ?- } t$$

Failure

Fails if the given theorem does not have a disjunctive conclusion.

Example

Given the simple fact about arithmetic th , $\vdash (m = 0) \vee (?n. m = \text{SUC } n)$, the tactic DISJ_CASES_TAC th can be used to produce a case split:

```
- DISJ_CASES_TAC th ([], Term '(P:num -> bool) m');
([(['m = 0'], 'P m'),
 ([['?n. m = SUC n'], 'P m']), fn) : tactic_result
```

Uses

Performing a case analysis according to a disjunctive theorem.

See also

`Tactic.ASSUME_TAC`, `Tactic.ASM_CASES_TAC`, `Tactic.COND_CASES_TAC`,
`Thm_cont.DISJ_CASES_THEN`, `Tactic.STRUCT_CASES_TAC`.

<code>DISJ_CASES_THEN</code>	<code>(Thm_cont)</code>
------------------------------	-------------------------

`DISJ_CASES_THEN` : `thm_tactical`

Synopsis

Applies a theorem-tactic to each disjunct of a disjunctive theorem.

Description

If the theorem-tactic `f:thm->tactic` applied to either ASSUMED disjunct produces results as follows when applied to a goal `(A ?- t)`:

$$\begin{array}{ccc} A \text{ ?- } t & & A \text{ ?- } t \\ \text{=====} & f \text{ (} u \text{ |- } u \text{)} & \text{and} & \text{=====} & f \text{ (} v \text{ |- } v \text{)} \\ A \text{ ?- } t1 & & & & A \text{ ?- } t2 \end{array}$$

then applying `DISJ_CASES_THEN f (|- u \\/ v)` to the goal `(A ?- t)` produces two sub-goals.

$$\begin{array}{c} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t1 \quad A \text{ ?- } t2 \end{array} \quad \text{DISJ_CASES_THEN } f \text{ (} \text{ |- } u \text{ \\/ } v \text{)}$$
Failure

Fails if the theorem is not a disjunction. An invalid tactic is produced if the theorem has any hypothesis which is not alpha-convertible to an assumption of the goal.

Example

Given the theorem

$$th = \text{ |- } (m = 0) \ \text{ \\/ } \text{ (?n. } m = \text{SUC } n)$$

and a goal of the form `?- (PRE m = m) = (m = 0)`, applying the tactic

$$\text{DISJ_CASES_THEN ASSUME_TAC } th$$

produces two subgoals, each with one disjunct as an added assumption:

$$?n. m = \text{SUC } n \text{ ?- (PRE } m = m) = (m = 0)$$

$$m = 0 \text{ ?- (PRE } m = m) = (m = 0)$$

Uses

Building cases tactics. For example, DISJ_CASES_TAC could be defined by:

```
let DISJ_CASES_TAC = DISJ_CASES_THEN ASSUME_TAC
```

Comments

Use DISJ_CASES_THEN2 to apply different tactic generating functions to each case.

See also

Thm_cont.STRIP_THM_THEN, Thm_cont.CHOOSE_THEN, Thm_cont.CONJUNCTS_THEN,
Thm_cont.CONJUNCTS_THEN2, Tactic.DISJ_CASES_TAC, Thm_cont.DISJ_CASES_THEN2,
Thm_cont.DISJ_CASES_THENL.

DISJ_CASES_THEN2

(Thm_cont)

```
DISJ_CASES_THEN2 : (thm_tactic -> thm_tactical)
```

Synopsis

Applies separate theorem-tactics to the two disjuncts of a theorem.

Description

If the theorem-tactics f_1 and f_2 , applied to the ASSUMED left and right disjunct of a theorem $|-\ u \ \vee \ v$ respectively, produce results as follows when applied to a goal $(A \text{ ?- } t)$:

$$\begin{array}{ccc} A \text{ ?- } t & & A \text{ ?- } t \\ \text{=====} & f_1 (u \text{ |- } u) & \text{and} & \text{=====} & f_2 (v \text{ |- } v) \\ A \text{ ?- } t_1 & & & & A \text{ ?- } t_2 \end{array}$$

then applying DISJ_CASES_THEN2 $f_1 \ f_2 \ (|-\ u \ \vee \ v)$ to the goal $(A \text{ ?- } t)$ produces two subgoals.

$$\begin{array}{c} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t_1 \quad A \text{ ?- } t_2 \end{array} \quad \text{DISJ_CASES_THEN2 } f_1 \ f_2 \ (|-\ u \ \vee \ v)$$

Failure

Fails if the theorem is not a disjunction. An invalid tactic is produced if the theorem has any hypothesis which is not alpha-convertible to an assumption of the goal.

Example

Given the theorem

$$\text{th} = |- (m = 0) \ \backslash/ \ (\ ?n. m = \text{SUC } n)$$

and a goal of the form $\ ?- (\text{PRE } m = m) = (m = 0)$, applying the tactic

$$\text{DISJ_CASES_THEN2 SUBST1_TAC ASSUME_TAC th}$$

to the goal will produce two subgoals

$$\ ?n. m = \text{SUC } n \ ?- (\text{PRE } m = m) = (m = 0)$$

$$\ ?- (\text{PRE } 0 = 0) = (0 = 0)$$

The first subgoal has had the disjunct $m = 0$ used for a substitution, and the second has added the disjunct to the assumption list. Alternatively, applying the tactic

$$\text{DISJ_CASES_THEN2 SUBST1_TAC (CHOOSE_THEN SUBST1_TAC) th}$$

to the goal produces the subgoals:

$$\ ?- (\text{PRE}(\text{SUC } n) = \text{SUC } n) = (\text{SUC } n = 0)$$

$$\ ?- (\text{PRE } 0 = 0) = (0 = 0)$$
Uses

Building cases tacticals. For example, `DISJ_CASES_THEN` could be defined by:

$$\text{let DISJ_CASES_THEN } f = \text{DISJ_CASES_THEN2 } f \ f$$
See also

`Thm_cont.STRIP_THM_THEN`, `Thm_cont.CHOOSE_THEN`, `Thm_cont.CONJUNCTS_THEN`,
`Thm_cont.CONJUNCTS_THEN2`, `Thm_cont.DISJ_CASES_THEN`, `Thm_cont.DISJ_CASES_THENL`.

DISJ_CASES_THENL	(Thm_cont)
-------------------------	-------------------

`DISJ_CASES_THENL : (thm_tactic list -> thm_tactic)`

Synopsis

Applies theorem-tactics in a list to the corresponding disjuncts in a theorem.

Description

If the theorem-tactics $f_1 \dots f_n$ applied to the ASSUMED disjuncts of a theorem

$$\vdash d_1 \vee d_2 \vee \dots \vee d_n$$

produce results as follows when applied to a goal $(A \text{ ?- } t)$:

$$\begin{array}{ccc} A \text{ ?- } t & & A \text{ ?- } t \\ \text{=====} & f_1 (d_1 \vdash d_1) \text{ and } \dots \text{ and } & \text{=====} & f_n (d_n \vdash d_n) \\ A \text{ ?- } t_1 & & & A \text{ ?- } t_n \end{array}$$

then applying `DISJ_CASES_THENL [f1;...;fn] ($\vdash d_1 \vee \dots \vee d_n$)` to the goal $(A \text{ ?- } t)$ produces n subgoals.

$$\begin{array}{c} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t_1 \quad \dots \quad A \text{ ?- } t_n \end{array} \quad \text{DISJ_CASES_THENL [f1;...;fn] ($\vdash d_1 \vee \dots \vee d_n$)}$$

`DISJ_CASES_THENL` is defined using iteration, hence for theorems with more than n disjuncts, d_n would itself be disjunctive.

Failure

Fails if the number of tactic generating functions in the list exceeds the number of disjuncts in the theorem. An invalid tactic is produced if the theorem has any hypothesis which is not alpha-convertible to an assumption of the goal.

Uses

Used when the goal is to be split into several cases, where a different tactic-generating function is to be applied to each case.

See also

`Thm_cont.CHOOSE_THEN`, `Thm_cont.CONJUNCTS_THEN`, `Thm_cont.CONJUNCTS_THEN2`,
`Thm_cont.DISJ_CASES_THEN`, `Thm_cont.DISJ_CASES_THEN2`, `Thm_cont.STRIP_THM_THEN`.

DISJ_CASES_UNION

(Drule)

`DISJ_CASES_UNION : thm -> thm -> thm -> thm`

Synopsis

Makes an inference for each arm of a disjunct.

Description

Given a disjunctive theorem, and two additional theorems each having one disjunct as a hypothesis, a new theorem with a conclusion that is the disjunction of the conclusions of the last two theorems is produced. The hypotheses include the union of hypotheses of all three theorems less the two disjuncts.

$$\begin{array}{c}
 A \mid\text{- } t1 \ \vee \ t2 \quad A1 \text{ u } \{t1\} \mid\text{- } t3 \quad A2 \text{ u } \{t2\} \mid\text{- } t4 \\
 \hline
 A \text{ u } A1 \text{ u } A2 \mid\text{- } t3 \ \vee \ t4
 \end{array}
 \quad \text{DISJ_CASES_UNION}$$

Failure

Fails if the first theorem is not a disjunction.

Example

The built-in theorem LESS_CASES can be specialized to:

```
th1 = |- m < n \\/ n <= m
```

and used with two additional theorems:

```
th2 = (m < n |- (m MOD n = m))
```

```
th3 = ({0 < n, n <= m} |- (m MOD n) = ((m - n) MOD n))
```

to derive a new theorem:

```
- DISJ_CASES_UNION th1 th2 th3;
```

```
val it = [0 < n] |- (m MOD n = m) \\/ (m MOD n = (m - n) MOD n) : thm
```

See also

Thm.DISJ_CASES, Tactic.DISJ_CASES_TAC, Thm.DISJ1, Thm.DISJ2.

DISJ_IMP	(Drule)
----------	---------

DISJ_IMP : (thm -> thm)

Synopsis

Converts a disjunctive theorem to an equivalent implicative theorem.

Description

The left disjunct of a disjunctive theorem becomes the negated antecedent of the newly generated theorem.

$$\frac{A \mid- t1 \ \wedge \ t2}{A \mid- \sim t1 \implies t2} \text{ DISJ_IMP}$$
Failure

Fails if the theorem is not a disjunction.

Example

Specializing the built-in theorem LESS_CASES gives the theorem:

$$\text{th} = \mid- m < n \ \wedge \ n \leq m$$

to which DISJ_IMP may be applied:

```
- DISJ_IMP th;
> val it = \mid- \sim m < n \implies n \leq m : thm
```

See also

Thm.DISJ_CASES.

DISJ_INEQS_FALSE_CONV	(Arith)
-----------------------	---------

DISJ_INEQS_FALSE_CONV : conv

Synopsis

Proves a disjunction of conjunctions of normalised inequalities is false, provided each conjunction is unsatisfiable.

Description

DISJ_INEQS_FALSE_CONV converts an unsatisfiable normalised arithmetic formula to false. The formula must be a disjunction of conjunctions of less-than-or-equal-to inequalities. The inequalities must have the following form: Each variable must appear on only one side of the inequality and each side must be a linear sum in which any constant appears first followed by products of a constant and a variable. On each side the variables must be ordered lexicographically, and if the coefficient of the variable is 1, the 1 must appear explicitly.

Failure

Fails if the formula is not of the correct form or is satisfiable. The function will also fail on certain unsatisfiable formulae due to incompleteness of the procedure used.

Example

```
#DISJ_INEQS_FALSE_CONV
# "(1 * n) <= ((1 * m) + (1 * p)) /\
# ((1 * m) + (1 * p)) <= (1 * n) /\
# (5 + (4 * n)) <= ((3 * m) + (1 * p)) \/
# 2 <= 0";;
|- (1 * n) <= ((1 * m) + (1 * p)) /\
   ((1 * m) + (1 * p)) <= (1 * n) /\
   (5 + (4 * n)) <= ((3 * m) + (1 * p)) \/
   2 <= 0 =
F
```

See also

Arith.ARITH_FORM_NORM_CONV.

disjunction	(boolSyntax)
-------------	--------------

disjunction : term

Synopsis

Constant denoting logical disjunction.

Description

The ML variable `boolSyntax.disjunction` is bound to the term `bool$\/`.

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`, `boolSyntax.conjunction`, `boolSyntax.negation`, `boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let_tm`, `boolSyntax.arb`.

DISJUNCTS_AC	(Drule)
--------------	---------

DISJUNCTS_AC : term * term -> thm

Synopsis

Prove equivalence under idempotence, symmetry and associativity of disjunction.

Description

DISJUNCTS_AC takes a pair of terms (t_1 , t_2) and proves $\vdash t_1 = t_2$ if t_1 and t_2 are equivalent up to idempotence, symmetry and associativity of disjunction. That is, if t_1 and t_2 are two (different) arbitrarily-nested disjunctions of the same set of terms, then DISJUNCTS_AC (t_1, t_2) returns $\vdash t_1 = t_2$. Otherwise, it fails.

Failure

Fails if t_1 and t_2 are not equivalent, as described above.

Example

```
- DISJUNCTS_AC (Term '(P \\/ Q) \\/ R', Term 'R \\/ (Q \\/ R) \\/ P');
> val it = |- (P \\/ Q) \\/ R = R \\/ (Q \\/ R) \\/ P : thm
```

Uses

Used to reorder a disjunction. First sort the disjuncts in a term t_1 into the desired order (e.g., lexicographic order, for normalization) to get a new term t_2 , then call DISJUNCTS_AC(t_1, t_2).

See also

Drule.CONJUNCTS_AC.

<div data-bbox="159 1211 397 1261" data-label="Text"> <p>DIV_CONV</p> </div>	<div data-bbox="1011 1209 1331 1261" data-label="Text"> <p>(reduceLib)</p> </div>
--	---

DIV_CONV : conv

Synopsis

Calculates by inference the result of dividing, with truncation, one numeral by another.

Description

If m and n are numerals (e.g. 0, 1, 2, 3,...), then DIV_CONV " m DIV n " returns the theorem:

$$\vdash m \text{ DIV } n = s$$

where s is the numeral that denotes the result of dividing the natural number denoted by m by the natural number denoted by n , with truncation.

Failure

DIV_CONV t_m fails unless t_m is of the form " m DIV n ", where m and n are numerals, or if n denotes zero.

Example

```
#DIV_CONV "0 DIV 0";;
evaluation failed      DIV_CONV
```

```
#DIV_CONV "0 DIV 12";;
|- 0 DIV 12 = 0
```

```
#DIV_CONV "2 DIV 0";;
evaluation failed      DIV_CONV
```

```
#DIV_CONV "144 DIV 12";;
|- 144 DIV 12 = 12
```

```
#DIV_CONV "7 DIV 2";;
|- 7 DIV 2 = 3
```

<div data-bbox="234 1043 448 1102" data-label="Text"> <p><code>dom_rng</code></p> </div>	<div data-bbox="1228 1039 1414 1102" data-label="Text"> <p>(Type)</p> </div>
--	--

```
dom_rng : hol_type -> hol_type * hol_type
```

Synopsis

Breaks a function type into domain and range types.

Description

If `ty` has the form `ty1 -> ty2`, then `dom_rng ty` yields `(ty1,ty2)`.

Failure

Fails if `ty` is not a function type.

Example

```
- dom_rng (bool --> alpha);
> val it = (':bool', ':a') : hol_type * hol_type

- try dom_rng bool;
```

```
Exception raised at Type.dom_rng:
not a function type
```

See also

Type.-->, Type.dest_type, Type.dest_thy_type.

e

(proofManagerLib)

e : tactic -> proof

Synopsis

Applies a tactic to the current goal, stacking the resulting subgoals.

Description

The function `e` is part of the subgoal package. It is an abbreviation for `expand`. For a description of the subgoal package, see `set_goal`.

Failure

As for `expand`.

Uses

Doing a step in an interactive goal-directed proof.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`, `proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`, `proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`, `proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

e1

(Lib)

e1 : int -> 'a list -> 'a

Synopsis

Extracts a specified element from a list.

Description

`e1 i [x1, ..., xn]` returns `xi`. Note that the elements are numbered starting from 1, not 0.

Failure

Fails with `e1` if the integer argument is less than 1 or greater than the length of the list.

Example

```
- e1 3 [1,2,7,1];
> val it = 7 : int
```

See also

`Lib.index`.

<div data-bbox="234 792 445 846" data-label="Text"> <p><code>EL_CONV</code></p> </div>	<div data-bbox="1145 792 1414 846" data-label="Text"> <p><code>(listLib)</code></p> </div>
--	--

`EL_CONV` : `conv`

Synopsis

Computes by inference the result of indexing an element from a list.

Description

For any object language list of the form `-- [x0; ... xk; ... ; xn] --`, the result of evaluating

$$\text{EL_CONV } (\text{--} \text{ 'EL } k \text{ [x0; ... xk; ... ; xn] ' -- })$$

is the theorem

$$\vdash \text{EL } k \text{ [x0; ... ; xk; ... ; xn] } = xk$$
Failure

`EL_CONV tm` fails if `tm` is not of the form described above, or `k` is not less than the length of the list.

See also

`listLib.ELL_CONV`.

<div data-bbox="234 1821 474 1874" data-label="Text"> <p><code>ELL_CONV</code></p> </div>	<div data-bbox="1145 1821 1414 1874" data-label="Text"> <p><code>(listLib)</code></p> </div>
---	--

`ELL_CONV` : `conv`

Synopsis

Computes by inference the result of indexing an element of a list from the tail end.

Description

For any object language list of the form `--'[xn-1;...;xk;...x0]'`, the result of evaluating

```
ELL_CONV (--'ELL k [xn-1;...;xk;...;x0] '--)
```

is the theorem

```
|- ELL k [xn-1;...;xk;...;x0] = xk
```

where `k` must not be greater than the length of the list. Note that `ELL` indexes the list elements from the tail end.

Failure

`ELL_CONV tm` fails if `tm` is not of the form described above, or `k` is not less than the length of the list.

See also

`listLib.EL_CONV`.

emit_ERR

(Feedback)

`emit_ERR` : bool ref

Synopsis

Flag controlling output of `HOL_ERR` exceptions.

Description

The boolean flag `emit_ERR` tells whether an application of `HOL_ERR` should be printed. Its value is consulted by `Raise` when it attempts to print a textual representation of its argument exception. This flag is not commonly used, and it may disappear or change in the future.

The default value of `emit_ERR` is `true`.

Example

```
- Raise (mk_HOL_ERR "Module" "function" "message");
```

```
Exception raised at Module.function:
```

```
message
```

```
! Uncaught exception:
```

```
! HOL_ERR
```

```
- emit_ERR := false;
```

```
> val it = () : unit
```

```
- Raise (mk_HOL_ERR "Module" "function" "message");
```

```
! Uncaught exception:
```

```
! HOL_ERR
```

See also

Feedback, Feedback.Raise, Feedback.emit_MESG, Feedback.emit_WARNING.

emit_MESG	(Feedback)
-----------	------------

```
emit_MESG : bool ref
```

Synopsis

Flag controlling output of HOL_MESG function.

Description

The boolean flag `emit_MESG` is consulted by `HOL_MESG` when it attempts to print its argument. This flag is not commonly used, and it may disappear or change in the future.

The default value of `emit_MESG` is `true`.

Example

```
- HOL_MESG "Joy to the world.";
```

```
<<HOL message: Joy to the world.>>
```

```
- emit_MESG := false;
```

```
> val it = () : unit
```

```
- HOL_MESG "Peace on Earth.";
```

```
> val it = () : unit
```

See also

Feedback, Feedback.HOL_MESG, Feedback.emit_ERR, Feedback.emit_WARNING.

emit_WARNING

(Feedback)

emit_WARNING : bool ref

Synopsis

Flag controlling output of HOL_WARNING function.

Description

The boolean flag emit_WARNING is consulted by HOL_WARNING when it attempts to print its argument. This flag is not commonly used, and it may disappear or change in the future.

The default value of emit_WARNING is true.

Example

```
- HOL_WARNING "Clock" "watcher" "Time is running out.";
<<HOL warning: Clock.watcher: Time is running out.>>
> val it = () : unit

- emit_WARNING := false;
> val it = () : unit

- HOL_WARNING "Clock" "watcher" "Time is running out.";
> val it = () : unit
```

See also

Feedback, Feedback.HOL_WARNING, Feedback.emit_ERR, Feedback.emit_MESG.

empty_model

(holCheckLib)

empty_model : model

Synopsis

Represents a HolCheck model with no information.

Description

This is used as a starting point for building a HolCheck model, using the `set_X` functions in `holCheckLib`.

See also

`holCheckLib.holCheck`, `holCheckLib.set_init`, `holCheckLib.set_trans`,
`holCheckLib.set_flag_ric`, `holCheckLib.set_name`, `holCheckLib.set_vord`,
`holCheckLib.set_state`, `holCheckLib.set_props`.

<code>empty_rewrites</code>	<code>(Rewrite)</code>
-----------------------------	------------------------

`empty_rewrites`: `rewrites`

Synopsis

The empty database of rewrite rules.

Uses

Used to build other rewrite sets.

See also

`Rewrite.bool_rewrites`, `Rewrite.implicit_rewrites`, `Rewrite.add_rewrites`,
`Rewrite.add_implicit_rewrites`, `Rewrite.set_implicit_rewrites`.

<code>empty_tmset</code>	<code>(Term)</code>
--------------------------	---------------------

`empty_tmset` : `term set`

Synopsis

Empty set of terms.

Description

The value `empty_tmset` represents an empty set of terms. The set has a built-in ordering, which is given by `Term.compare`.

Comments

Used as a starting point for building sets of terms.

See also

`Term.compare`, `Term.empty_varset`.

<code>empty_varset</code>

<code>(Term)</code>

`empty_varset` : term set

Synopsis

Empty set of term variables.

Description

The value `empty_varset` represents an empty set of term variables. The set has a built-in ordering, which is given by `Term.var_compare`.

Comments

Used as a starting point for building sets of variables.

See also

`Term.var_compare`, `Term.empty_tmset`.

<code>end_itlist</code>

<code>(Lib)</code>

`end_itlist` : ('a -> 'a -> 'a) -> 'a list -> 'a)

Synopsis

List iteration function. Applies a binary function between adjacent elements of a list.

Description

`end_itlist` `f` [`x1`, ..., `xn`] returns `f x1 (... (f x(n-1) xn) ...)`. Returns `x` for a one-element list [`x`].

Failure

Fails if list is empty, or if an application of `f` raises an exception.

Example

```
- end_itlist (curry op+) [1,2,3,4];
> val it = 10 : int
```

See also

Lib.itlist, Lib.rev_itlist, Lib.itlist2, Lib.rev_itlist2.

<div data-bbox="236 642 474 692" data-label="Text"> <p><code>end_time</code></p> </div>	<div data-bbox="1260 638 1414 692" data-label="Text"> <p>(Lib)</p> </div>
---	---

```
end_time : Timer.cpu_timer -> unit
```

Synopsis

Check a running timer, and print out how long it has been running.

Description

An application `end_time` timer looks to see how long `timer` has been running, and prints out the elapsed runtime, garbage collection time, and system time.

Failure

Never fails.

Example

```
- val clock = start_time();
> val clock = <cpu_timer> : cpu_timer

- use "foo.sml";
> ... output omitted ...

- end_time clock;
runtime: 525.996s,    gctime: 0.000s,    systime: 525.996s.
> val it = () : unit
```

Comments

A `start_time ... end_time` pair is for use when calling `time` would be clumsy, e.g., when multiple function applications are to be timed.

See also

Lib.start_time, Lib.time.

enumerate
(Lib)

`enumerate : int -> 'a list -> (int * 'a) list`

Synopsis

Number each element of a list, in ascending order.

Description

An invocation of `enumerate i [x1, ..., xn]` returns the list `[(i,x1), (i+1,x2), ..., (i+n-1,xn)]`.

Failure

Never fails.

Example

```
- enumerate 0 ["komodo", "iguana", "gecko", "gila"];
> val it = [(0, "komodo"), (1, "iguana"), (2, "gecko"), (3, "gila")]
```

EQ_IMP_RULE
(Thm)

`EQ_IMP_RULE : thm -> thm * thm`

Synopsis

Derives forward and backward implication from equality of boolean terms.

Description

When applied to a theorem `A |- t1 = t2`, where `t1` and `t2` both have type `bool`, the inference rule `EQ_IMP_RULE` returns the theorems `A |- t1 ==> t2` and `A |- t2 ==> t1`.

$$\frac{A \text{ |- } t1 = t2}{A \text{ |- } t1 ==> t2 \quad A \text{ |- } t2 ==> t1} \text{ EQ_IMP_RULE}$$

Failure

Fails unless the conclusion of the given theorem is an equation between boolean terms.

See also

Thm.EQ_MP, Tactic.EQ_TAC, Drule.IMP_ANTISYM_RULE.

EQ_LENGTH_INDUCT_TAC	(listLib)
----------------------	-----------

EQ_LENGTH_INDUCT_TAC : tactic

Synopsis

Performs tactical proof by structural induction on two equal length lists.

Description

EQ_LENGTH_INDUCT_TAC reduces a goal $\!x\ y . (\text{LENGTH } x = \text{LENGTH } y) \implies t[x,y]$, where x and y range over lists, to two subgoals corresponding to the base and step cases in a proof by induction on the length of x and y . The induction hypothesis appears among the assumptions of the subgoal for the step case. The specification of EQ_LENGTH_INDUCT_TAC is:

$$\frac{A \text{ ?- } \!x\ y . (\text{LENGTH } x = \text{LENGTH } y) \implies t[x,y]}{\text{EQ_LENGTH_INDUCT_TAC}} \quad \begin{array}{l} A \text{ ?- } t[\text{NIL}/x] [\text{NIL}/y] \\ A \text{ u } \{ \{ \text{LENGTH } x = \text{LENGTH } y, t[x'/x, y'/y] \} \} \text{ ?-} \\ \!h\ h' . t[(\text{CONS } h\ x)/x, (\text{CONS } h'\ y)/y] \end{array}$$
Failure

EQ_LENGTH_INDUCT_TAC g fails unless the conclusion of the goal g has the form

$$\!x\ y . (\text{LENGTH } x = \text{LENGTH } y) \implies t[x,y]$$

where the variables x and y have types $(xty)\text{list}$ and $(yty)\text{list}$ for some types xty and yty . It also fails if either of the variables x or y appear free in the assumptions.

Uses

Use this tactic to perform structural induction over two lists that have identical length.

See also

listLib.LIST_INDUCT_TAC, listLib.SNOC_INDUCT_TAC,
listLib.EQ_LENGTH_SNOC_INDUCT_TAC.

EQ_LENGTH_SNOC_INDUCT_TAC

(listLib)

EQ_LENGTH_SNOC_INDUCT_TAC : tactic

Synopsis

Performs tactical proof by structural induction on two equal length lists from the tail end.

Description

EQ_LENGTH_SNOC_INDUCT_TAC reduces a goal $!x\ y . (\text{LENGTH } x = \text{LENGTH } y) \implies t[x,y]$, where x and y range over lists, to two subgoals corresponding to the base and step cases in a proof by induction on the length of x and y . The induction hypothesis appears among the assumptions of the subgoal for the step case. The specification of EQ_LENGTH_SNOC_INDUCT_TAC is:

$$\begin{array}{l} A \text{ ?- } !x\ y . (\text{LENGTH } x = \text{LENGTH } y) \implies t[x,y] \\ \text{=====} \text{EQ_LENGTH_SNOC_INDUCT_TAC} \\ A \text{ ?- } t[\text{NIL}/x] [\text{NIL}/y] \\ A\ u \ \{\{\text{LENGTH } x = \text{LENGTH } y, t[x'/x, y'/y]\}\} \text{ ?-} \\ \quad !h\ h' . t[(\text{SNOC } h\ x)/x, (\text{SNOC } h'\ y)/y] \end{array}$$
Failure

EQ_LENGTH_SNOC_INDUCT_TAC g fails unless the conclusion of the goal g has the form

$$!x\ y . (\text{LENGTH } x = \text{LENGTH } y) \implies t[x,y]$$

where the variables x and y have types $(xty)\text{list}$ and $(yty)\text{list}$ for some types xty and yty . It also fails if either of the variables x or y appear free in the assumptions.

Uses

Use this tactic to perform structural induction on two lists that have identical length.

See also

listLib.EQ_LENGTH_INDUCT_TAC, listLib.LIST_INDUCT_TAC, listLib.SNOC_INDUCT_TAC.

EQ_MP

(Thm)

EQ_MP : thm -> thm -> thm

Synopsis

Equality version of the Modus Ponens rule.

Description

When applied to theorems $A1 \vdash t1 = t2$ and $A2 \vdash t1$, the inference rule `EQ_MP` returns the theorem $A1 \cup A2 \vdash t2$.

$$\frac{A1 \vdash t1 = t2 \quad A2 \vdash t1}{A1 \cup A2 \vdash t2} \quad \text{EQ_MP}$$

Failure

Fails unless the first theorem is equational and its left side is the same as the conclusion of the second theorem (and is therefore of type `bool`), up to alpha-conversion.

See also

`Thm.EQ_IMP_RULE`, `Drule.IMP_ANTISYM_RULE`, `Thm.MP`.

EQ_TAC

(Tactic)

`EQ_TAC` : tactic

Synopsis

Reduces goal of equality of boolean terms to forward and backward implication.

Description

When applied to a goal $A \text{ ?- } t1 = t2$, where $t1$ and $t2$ have type `bool`, the tactic `EQ_TAC` returns the subgoals $A \text{ ?- } t1 \implies t2$ and $A \text{ ?- } t2 \implies t1$.

$$\frac{A \text{ ?- } t1 = t2}{A \text{ ?- } t1 \implies t2 \quad A \text{ ?- } t2 \implies t1} \quad \text{EQ_TAC}$$

Failure

Fails unless the conclusion of the goal is an equation between boolean terms.

See also

`Thm.EQ_IMP_RULE`, `Drule.IMP_ANTISYM_RULE`.

EQF_ELIM

(Drule)

EQF_ELIM : (thm -> thm)

Synopsis

Replaces equality with F by negation.

Description

$$\begin{array}{l} A \mid- tm = F \\ \hline A \mid- \sim tm \end{array} \quad \text{EQF_ELIM}$$
FailureFails if the argument theorem is not of the form $A \mid- tm = F$.**See also**

Drule.EQF_INTRO, Drule.EQT_ELIM, Drule.EQT_INTRO.

EQF_INTRO

(Drule)

EQF_INTRO : (thm -> thm)

Synopsis

Converts negation to equality with F.

Description

$$\begin{array}{l} A \mid- \sim tm \\ \hline A \mid- tm = F \end{array} \quad \text{EQF_INTRO}$$
Failure

Fails if the argument theorem is not a negation.

See also

Drule.EQF_ELIM, Drule.EQT_ELIM, Drule.EQT_INTRO.

EQT_ELIM

(Drule)

EQT_ELIM : (thm -> thm)

Synopsis

Eliminates equality with T.

Description

$$\frac{A \mid- tm = T}{A \mid- tm} \text{ EQT_ELIM}$$
FailureFails if the argument theorem is not of the form $A \mid- tm = T$.**See also**

Drule.EQT_INTRO, Drule.EQF_ELIM, Drule.EQF_INTRO.

EQT_INTRO

(Drule)

EQT_INTRO : thm -> thm

Synopsis

Introduces equality with T.

Description

$$\frac{A \mid- tm}{A \mid- tm = T} \text{ EQT_INTRO}$$
Failure

Never fails.

See also

Drule.EQT_ELIM, Drule.EQF_ELIM, Drule.EQF_INTRO.

equal	(Lib)
-------	-------

```
equal : 'a -> 'a -> bool
```

Synopsis

Curried form of ML equality

Description

In some programming situations it is useful to use equality in a curried form. Although it is easy to code up on demand, the `equal` function is provided for convenience.

Failure

Never fails.

Example

```
- filter (equal 1) [1,2,1,4,5];  
> val it = [1, 1] : int list
```

equality	(boolSyntax)
----------	--------------

```
equality : term
```

Synopsis

Constant denoting logical equality.

Description

The ML variable `boolSyntax.equality` is bound to the term `min$=`.

See also

`boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`,
`boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`,
`boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.negation`,
`boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let_tm`,
`boolSyntax.arb`.

ERR_outstream**(Feedback)**

```
ERR_outstream : TextIO.outstream ref
```

Synopsis

Reference to output stream used when printing `HOL_ERR`

Description

The value of reference cell `ERR_outstream` controls where `Raise` prints its argument.

The default value of `ERR_outstream` is `TextIO.stdErr`.

Example

```
- val ostrm = TextIO.openOut "foo";
> val ostrm = <ostream> : ostream

- ERR_outstream := ostrm;
> val it = () : unit

- Raise (mk_HOL_ERR "Foo" "bar" "incomprehensible input");
! Uncaught exception:
! HOL_ERR

- TextIO.closeOut ostrm;
> val it = () : unit

- val istrm = TextIO.openIn "foo";
> val istrm = <istream> : istream

- print (TextIO.inputAll istrm);
```

```
Exception raised at Foo.bar:
incomprehensible input
```

See also

`Feedback`, `Feedback.HOL_ERR`, `Feedback.Raise`, `Feedback.MESG_outstream`,
`Feedback.WARNING_outstream`.

ERR_to_string**(Feedback)**

ERR_to_string : (error_record -> string) ref

Synopsis

Alterable function for formatting HOL_ERR

Description

ERR_to_string is a reference to a function for formatting the argument to an application of HOL_ERR. It can be used to customize Raise.

The default value of ERR_to_string is format_ERR.

Example

```
- fun alt_ERR_report {origin_structure,origin_function,message} =  
  String.concat["This just in from ",origin_function, " at ",  
               origin_structure, " : ", message, "\n"];  
  
- ERR_to_string := alt_ERR_report;  
  
- Raise (HOL_ERR {origin_structure = "Foo",  
                 origin_function = "bar",  
                 message = "incomprehensible input"});
```

```
This just in from bar at Foo : incomprehensible input  
! Uncaught exception:  
! HOL_ERR
```

See also

Feedback, Feedback.error_record, Feedback.HOL_ERR, Feedback.Raise,
Feedback.MESG_to_string, Feedback.WARNING_to_string.

`error_record`

(Feedback)

```

type error_record = {origin_structure : string,
                    origin_function  : string,
                    message           : string}

```

Synopsis

Type abbreviation for HOL exceptions in Feedback module.

Description

The type abbreviation `error_record` declares the standard format of HOL exceptions. The `origin_structure` field denotes the module that the exception has been raised in, the `origin_function` field gives the name of the function the exception has been raised in, and the `message` field should give an explanation of why the exception has been raised.

See also

`Feedback`, `Feedback.HOL_ERR`, `Feedback.format_ERR`, `Feedback.ERR_to_string`.

`ETA_CONV`

(Drule)

`ETA_CONV` : conv

Synopsis

Performs a toplevel eta-conversion.

Description

`ETA_CONV` maps an eta-redex $\lambda x. (t\ x)$, where x does not occur free in t , to the theorem $\vdash (\lambda x. (t\ x)) = t$.

Failure

Fails if the input term is not an eta-redex.

See also

`Drule.RIGHT_ETA`, `Term.eta_conv`.

eta_conv

(Term)

```
eta_conv : term -> term
```

Synopsis

Performs one step of eta-reduction.

Description

Eta-reduction is an important operation in the lambda calculus. A step of eta-reduction may be performed by `eta_conv M`, where `M` is a lambda abstraction of the following form: $\lambda v. (N\ v)$, i.e., a lambda abstraction whose body is an application of a term `N` to the bound variable `v`. Moreover, `v` must not occur free in `M`. If this proviso is met, an invocation `eta_conv (\v. (N v))` is equal to `N`.

Failure

If `M` is not of the specified form, or if `v` occurs free in `N`.

Example

```
- eta_conv (Term '\n. PRE n');
> val it = 'PRE' : term
```

Comments

Eta-reduction embodies the principle of extensionality, which is basic to the HOL logic.

See also

`Drule.ETA_CONV`, `Drule.RIGHT_ETA`.

etyvar

(Type)

```
etyvar : hol_type
```

Synopsis

Common type variable.

Description

The ML variable `Type.etyvar` is bound to the type variable 'e.

See also

Type.alpha, Type.beta, Type.gamma, Type.delta, Type.ftyvar, Type.bool.

EVAL	(bossLib)
-------------	------------------

EVAL : conv

Synopsis

Evaluate a term by deduction.

Description

An invocation `EVAL M` symbolically evaluates `M` by applying the defining equations of constants occurring in `M`. These equations are held in a mutable datastructure that is automatically added to by `Hol_datatype`, `Define`, and `tprove`. The underlying algorithm is call-by-value with a few differences, see the entry for `CBV_CONV` for details.

Failure

Never fails, but may diverge.

Example

```
- EVAL (Term 'REVERSE (MAP (\x. x + a) [x;y;z])');
> val it = |- REVERSE (MAP (\x. x + a) [x; y; z]) = [z + a; y + a; x + a]
      : thm
```

Comments

In order for recursive functions over numbers to be applied by `EVAL`, pattern matching over `SUC` and `0` needs to be replaced by destructors. For example, the equations for `FACT` would have to be rephrased as `FACT n = if n = 0 then 1 else n * FACT (n-1)`.

See also

computeLib.CBV_CONV, computeLib.RESTR_EVAL_CONV, bossLib.EVAL_TAC, computeLib.monitoring, bossLib.Define.

EVAL_RULE	(bossLib)
------------------	------------------

EVAL_RULE : thm -> thm

Synopsis

Evaluate conclusion of a theorem.

Description

An invocation `EVAL_RULE th` symbolically evaluates the conclusion of `th` by applying the defining equations of constants which occur in the conclusion of `th`. These equations are held in a mutable datastructure that is automatically added to by `Hol_datatype`, `Define`, and `tprove`. The underlying algorithm is call-by-value with a few differences, see the entry for `CBV_CONV` for details.

Failure

Never fails, but may diverge.

Example

```
- val th = ASSUME(Term 'x = MAP FACT (REVERSE [1;2;3;4;5;6;7;8;9;10])');
> val th = [...] |- x = MAP FACT (REVERSE [1; 2; 3; 4; 5; 6; 7; 8; 9; 10])

- EVAL_RULE th;
> val it = [...] |- x = [3628800; 362880; 40320; 5040; 720; 120; 24; 6; 2; 1]

- hyp it;
> val it = ['x = MAP FACT (REVERSE [1; 2; 3; 4; 5; 6; 7; 8; 9; 10])']
```

Comments

In order for recursive functions over numbers to be applied by `EVAL_RULE`, pattern matching over `SUC` and `0` needs to be replaced by destructors. For example, the equations for `FACT` would have to be rephrased as `FACT n = if n = 0 then 1 else n * FACT (n-1)`.

See also

`bossLib.EVAL`, `bossLib.EVAL_TAC`, `computeLib.CBV_CONV`.

EVAL_TAC	(bossLib)
----------	-----------

`EVAL_TAC` : tactic

Synopsis

Evaluate a goal deductively.

Description

Applying `EVAL_TAC` to a goal $A \text{ ?- } g$ results in `EVAL` being applied to g to obtain $\text{!- } g = g'$. This theorem is used to transform the goal to $A \text{ ?- } g'$.

The notion of evaluation is based around rules for replacing constants by their (equational) definitions. Thus `EVAL_TAC` is currently suited to evaluation of expressions that look like functional programs. Evaluation of inductive relations is not currently supported.

Failure

Shouldn't fail, but may diverge.

Example

`EVAL_TAC` reduces the goal $\text{?- } P \text{ (REVERSE (FLAT [[x; y]; [a; b; c; d]])}$ to the goal

$\text{?- } P \text{ [d; c; b; a; y; x]}$

Comments

The main problem with `EVAL_TAC` is knowing when it will terminate. One typical cause of non-termination is that a constant in the goal has not been added to `the_compset`. Another is that a test in a conditional in the expression may involve a variable.

Uses

Symbolic evaluation.

See also

`bossLib.EVAL`.

<div data-bbox="234 1440 387 1489" data-label="Text"> <p>EVERY</p> </div>	<div data-bbox="1114 1440 1410 1489" data-label="Text"> <p>(Tactical)</p> </div>
--	--

`EVERY : (tactic list -> tactic)`

Synopsis

Sequentially applies all the tactics in a given list of tactics.

Description

When applied to a list of tactics $[T_1; \dots; T_n]$, and a goal g , the tactical `EVERY` applies each tactic in sequence to every subgoal generated by the previous one. This can be represented as:

`EVERY [T1;...;Tn] = T1 THEN ... THEN Tn`

If the tactic list is empty, the resulting tactic has no effect.

Failure

The application of `EVERY` to a tactic list never fails. The resulting tactic fails iff any of the component tactics do.

Comments

It is possible to use `EVERY` instead of `THEN`, but probably stylistically inferior. `EVERY` is more useful when applied to a list of tactics generated by a function.

See also

`Tactical.FIRST`, `Tactical.MAP_EVERY`, `Tactical.THEN`.

<div data-bbox="159 916 485 967" data-label="Text"> <p><code>EVERY_ASSUM</code></p> </div>	<div data-bbox="1038 916 1331 967" data-label="Text"> <p><code>(Tactical)</code></p> </div>
--	---

```
EVERY_ASSUM : (thm_tactic -> tactic)
```

Synopsis

Sequentially applies all tactics given by mapping a function over the assumptions of a goal.

Description

When applied to a theorem-tactic `f` and a goal $(\{A_1, \dots, A_n\} \text{ ?- } C)$, the `EVERY_ASSUM` tactical maps `f` over a list of ASSUMED assumptions then applies the resulting tactics, in sequence, to the goal:

$$\begin{aligned} \text{EVERY_ASSUM } f \text{ } (\{A_1, \dots, A_n\} \text{ ?- } C) \\ = (f(A_1 \text{ |- } A_1) \text{ THEN } \dots \text{ THEN } f(A_n \text{ |- } A_n)) (\{A_1, \dots, A_n\} \text{ ?- } C) \end{aligned}$$

If the goal has no assumptions, then `EVERY_ASSUM` has no effect.

Failure

The application of `EVERY_ASSUM` to a theorem-tactic and a goal fails if the theorem-tactic fails when applied to any of the ASSUMED assumptions of the goal, or if any of the resulting tactics fail when applied sequentially.

See also

`Tactical.ASSUM_LIST`, `Tactical.MAP_EVERY`, `Tactical.MAP_FIRST`, `Tactical.THEN`.

EVERY_CONJ_CONV

(Conv)

EVERY_CONJ_CONV : conv -> conv

Synopsis

Applies a conversion to every top-level conjunct in a term.

Description

The term `EVERY_CONJ_CONV c t` takes the conversion `c` and applies this to every top-level conjunct within term `t`. A top-level conjunct is a sub-term that can be reached from the root of the term by breaking apart only conjunctions. The terms affected by `c` are those that would be returned by a call to `strip_conj c`. In particular, if the term as a whole is not a conjunction, then the conversion will be applied to the whole term.

If the result of the application of the conversion to one of the conjuncts is one of the constants `true` or `false`, then one of two standard rewrites is applied, simplifying the resulting term. If one of the conjuncts is converted to `false`, then the conversion will not be applied to the remaining conjuncts (the conjuncts are worked on from left to right), and the result of the whole application will simply be `false`. Alternatively, conjuncts that are converted to `true` will not appear in the final result at all.

Failure

Fails if the conversion argument fails when applied to one of the top-level conjuncts in a term.

Example

```
- EVERY_CONJ_CONV BETA_CONV (Term'(\x. x /\ y) p');
> val it = |- (\x. x /\ y) p = p /\ y : thm
- EVERY_CONJ_CONV BETA_CONV (Term'(\y. y /\ p) q /\ (\z. z) r');
> val it = |- (\y. y /\ p) q /\ (\z. z) r = (q /\ p) /\ r : thm
```

Uses

Useful for applying a conversion to all of the “significant” sub-terms within a term without having to worry about the exact structure of its conjunctive skeleton.

See also

`Conv.EVERY_DISJ_CONV`, `Conv.RATOR_CONV`, `Conv.RAND_CONV`, `Conv.LAND_CONV`.

EVERY_CONSEQ_CONV

(ConseqConv)

EVERY_CONSEQ_CONV : (conseq_conv list -> conseq_conv)

Synopsis

Applies in sequence all the consequence conversions in a given list of conversions.

See also

ConseqConv.THEN_CONSEQ_CONV, Conv.EVERY_CONV.

EVERY_CONV

(Conv)

EVERY_CONV : (conv list -> conv)

Synopsis

Applies in sequence all the conversions in a given list of conversions.

Description

EVERY_CONV [c1;...;cn] "t" returns the result of applying the conversions c1, ..., cn in sequence to the term "t". The conversions are applied in the order in which they are given in the list. In particular, if c_i "t_i" returns |- t_i=t_{i+1} for i from 1 to n, then EVERY_CONV [c1;...;cn] "t1" returns |- t1=t(n+1). If the supplied list of conversions is empty, then EVERY_CONV returns the identity conversion. That is, EVERY_CONV [] "t" returns |- t=t.

Failure

EVERY_CONV [c1;...;cn] "t" fails if any one of the conversions c1, ..., cn fails when applied in sequence as specified above.

See also

Conv.THENC.

EVERY_DISJ_CONV

(Conv)

EVERY_DISJ_CONV : conv -> conv

Synopsis

Applies a conversion to every top-level disjunct in a term.

Description

The term `EVERY_DISJ_CONV c t` takes the conversion `c` and applies this to every top-level disjunct within term `t`. A top-level disjunct is a sub-term that can be reached from the root of the term by breaking apart only disjunctions. The terms affected by `c` are those that would be returned by a call to `strip_disj c`. In particular, if the term as a whole is not a disjunction, then the conversion will be applied to the whole term.

If the result of the application of the conversion to one of the disjuncts is one of the constants `true` or `false`, then one of two standard rewrites is applied, simplifying the resulting term. If one of the disjuncts is converted to `true`, then the conversion will not be applied to the remaining disjuncts (the disjuncts are worked on from left to right), and the result of the whole application will simply be `true`. Alternatively, disjuncts that are converted to `false` will not appear in the final result at all.

Failure

Fails if the conversion argument fails when applied to one of the top-level disjuncts in the term.

Example

```
- EVERY_DISJ_CONV BETA_CONV
  (Term'(\x. x /\ p) q \/ (\x. x) r \/ (\y. s /\ y) u');
> val it =
  |- (\x. x /\ p) q \/ (\x. x) r \/ (\y. s /\ y) u = q /\ p \/ r \/ s /\ u
  : thm
- EVERY_DISJ_CONV REDUCE_CONV '3 < x \/ 2 < 3 \/ 2 EXP 1000 < 10';
> val it = |- 3 < x \/ 2 < 3 \/ 2 EXP 1000 < 10 = T : thm
```

Uses

Useful for applying a conversion to all of the “significant” sub-terms within a term without having to worry about the exact structure of its disjunctive skeleton.

See also

`Conv.EVERY_CONJ_CONV`, `Conv.RATOR_CONV`, `Conv.RAND_CONV`, `Conv.LAND_CONV`, `numLib.REDUCE_CONV`.

EVERY_TCL	(Thm_cont)
------------------	-------------------

`EVERY_TCL : (thm_tactical list -> thm_tactical)`

Synopsis

Composes a list of theorem-tacticals.

Description

When given a list of theorem-tacticals and a theorem, `EVERY_TCL` simply composes their effects on the theorem. The effect is:

```
EVERY_TCL [tt11;...;ttl1n] = tt11 THEN_TCL ... THEN_TCL ttl1n
```

In other words, if:

```
tt11 ttac th1 = ttac th2 ... ttl1n ttac thn = ttac thn'
```

then:

```
EVERY_TCL [tt11;...;ttl1n] ttac th1 = ttac thn'
```

If the theorem-tactical list is empty, the resulting theorem-tactical behaves in the same way as `ALL_THEN`, the identity theorem-tactical.

Failure

The application to a list of theorem-tacticals never fails.

See also

`Thm_cont.FIRST_TCL`, `Thm_cont.ORELSE_TCL`, `Thm_cont.REPEAT_TCL`, `Thm_cont.THEN_TCL`.

<div data-bbox="161 1370 427 1422" data-label="Text"> <p>EXISTENCE</p> </div>	<div data-bbox="1155 1370 1331 1422" data-label="Text"> <p>(Conv)</p> </div>
--	--

`EXISTENCE : (thm -> thm)`

Synopsis

Deduces existence from unique existence.

Description

When applied to a theorem with a unique-existentially quantified conclusion, `EXISTENCE` returns the same theorem with normal existential quantification over the same variable.

```

A |- ?!x. p
-----
A |- ?x. p
EXISTENCE

```

Failure

Fails unless the conclusion of the theorem is unique-existentially quantified.

See also

`Conv.EXISTS_UNIQUE_CONV.`

<div data-bbox="236 595 557 642" data-label="Text"> <p><code>existential</code></p> </div>	<div data-bbox="1059 593 1412 649" data-label="Text"> <p><code>(boolSyntax)</code></p> </div>
--	---

`existential : term`

Synopsis

Constant denoting existential quantification.

Description

The ML variable `boolSyntax.existential` is bound to the term `bool$?`.

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.exists1`, `boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.negation`, `boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let_tm`, `boolSyntax.arb`.

<div data-bbox="236 1326 414 1370" data-label="Text"> <p><code>exists</code></p> </div>	<div data-bbox="1260 1321 1412 1373" data-label="Text"> <p><code>(Lib)</code></p> </div>
---	--

`exists : ('a -> bool) -> 'a list -> bool`

Synopsis

Check if a predicate holds somewhere in a list

Description

An invocation `exists P l` returns true if `P` holds of some element of `l`. Since there are no elements of `[]`, `exists P []` always returns false.

Failure

When searching for an element of `l` that `P` holds of, it may happen that an application of `P` to an element of `l` raises an exception. In that case, `exists P l` raises an exception.

Example

```

- exists (fn i => i mod 2 = 0) [1,3,4];
> val it = true : bool

- exists (fn _ => raise Fail "") [];
> val it = false : bool

- exists (fn _ => raise Fail "") [1];
! Uncaught exception:
! Fail ""

```

See also

Lib.all, Lib.first, Lib.tryfind.

EXISTS

(Thm)

EXISTS : term * term -> thm -> thm

Synopsis

Introduces existential quantification given a particular witness.

Description

When applied to a pair of terms and a theorem, the first term is an existentially quantified pattern indicating the desired form of the result, and the second is a witness whose substitution for the quantified variable gives a term which is the same as the conclusion of the theorem, EXISTS gives the desired theorem.

$$\begin{array}{l}
 A \vdash p[u/x] \\
 \hline
 \text{EXISTS } (?x. p, u) \\
 A \vdash ?x. p
 \end{array}$$

Failure

Fails unless the substituted pattern is the same as the conclusion of the theorem.

Example

The following examples illustrate how it is possible to deduce different things from the same theorem:

```

- EXISTS (Term '?x. x=T',T) (REFL T);
> val it = |- ?x. x = T : thm

- EXISTS (Term '?x:bool. x=x',T) (REFL T);
> val it = |- ?x. x = x : thm

```

See also

Thm.CHOOSE, Tactic.EXISTS_TAC.

exists1	(boolSyntax)
---------	--------------

exists1 : term

Synopsis

Constant denoting the unique existence quantifier.

Description

The ML variable `boolSyntax.exists1` is bound to the term `bool$?!.`

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.negation`, `boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let_tm`, `boolSyntax.arb`.

EXISTS_AND_CONV	(Conv)
-----------------	--------

EXISTS_AND_CONV : conv

Synopsis

Moves an existential quantification inwards through a conjunction.

Description

When applied to a term of the form `?x. P /\ Q`, where `x` is not free in both `P` and `Q`, `EXISTS_AND_CONV` returns a theorem of one of three forms, depending on occurrences of the variable `x` in `P` and `Q`. If `x` is free in `P` but not in `Q`, then the theorem:

$$\vdash (\exists x. P \wedge Q) = (\exists x.P) \wedge Q$$

is returned. If x is free in Q but not in P , then the result is:

$$\vdash (\exists x. P \wedge Q) = P \wedge (\exists x.Q)$$

And if x is free in neither P nor Q , then the result is:

$$\vdash (\exists x. P \wedge Q) = (\exists x.P) \wedge (\exists x.Q)$$

Failure

EXISTS_AND_CONV fails if it is applied to a term not of the form $\exists x. P \wedge Q$, or if it is applied to a term $\exists x. P \wedge Q$ in which the variable x is free in both P and Q .

See also

Conv.AND_EXISTS_CONV, Conv.EXISTS_AND_REORDER_CONV, Conv.LEFT_AND_EXISTS_CONV, Conv.RIGHT_AND_EXISTS_CONV.

<div data-bbox="161 1070 826 1120" data-label="Text"> <p>EXISTS_AND_REORDER_CONV</p> </div>	<div data-bbox="1155 1070 1331 1120" data-label="Text"> <p>(Conv)</p> </div>
--	---

EXISTS_AND_REORDER_CONV : conv

Synopsis

Moves an existential quantification inwards through a conjunction, sorting the body.

Description

When applied to a term of the form $\exists x. c_1 \wedge c_2 \wedge \dots \wedge c_n$, where x is not free in at least one of the conjuncts c_i , then EXISTS_AND_REORDER_CONV returns a theorem of the form

$$\vdash (\exists x. \dots) = (c_i \wedge c_j \wedge c_k \wedge \dots) \wedge (\exists x. c_m \wedge c_n \wedge c_p \wedge \dots)$$

where the conjuncts c_i , c_j and c_k do not have the bound variable x free, and where the conjuncts c_m , c_n and c_p do.

Failure

EXISTS_AND_REORDER_CONV fails if it is applied to a term that is not an existential. It raises UNCHANGED if the existential's body is not a conjunction, or if the body does not have any conjuncts where the bound variable does not occur, or if none of the body's conjuncts have free occurrences of the bound variable.

Comments

The conjuncts in the resulting term are kept in the same relative order as in the input term, but will all be right-associated in the two groups (because they are re-assembled with `list_mk_conj`), possibly destroying structure that existed in the original.

See also

`Conv.EXISTS_AND_CONV`.

EXISTS_ARITH_CONV

(Arith)

`EXISTS_ARITH_CONV` : `conv`

Synopsis

Partial decision procedure for non-universal Presburger natural arithmetic.

Description

`EXISTS_ARITH_CONV` is a partial decision procedure for formulae of Presburger natural arithmetic which are in prenex normal form and have all variables existentially quantified. Presburger natural arithmetic is the subset of arithmetic formulae made up from natural number constants, numeric variables, addition, multiplication by a constant, the relations `<`, `<=`, `=`, `>=`, `>` and the logical connectives `~`, `/^`, `\/`, `==>`, `=` (if-and-only-if), `!` (‘forall’) and `?` (‘there exists’). Products of two expressions which both contain variables are not included in the subset, but the function `SUC` which is not normally included in a specification of Presburger arithmetic is allowed in this HOL implementation.

Given a formula in the specified subset, the function attempts to prove that it is equal to `T` (true). The procedure is incomplete; it is not able to prove all formulae in the subset.

Failure

The function can fail in two ways. It fails if the argument term is not a formula in the specified subset, and it also fails if it is unable to prove the formula. The failure strings are different in each case.

Example

```
#EXISTS_ARITH_CONV "?m n. m < n";;
|- (?m n. m < n) = T
```

```
#EXISTS_ARITH_CONV "?m n. (2 * m) + (3 * n) = 10";;
|- (?m n. (2 * m) + (3 * n) = 10) = T
```

See also

Arith.NEGATE_CONV, Arith.FORALL_ARITH_CONV, numLib.ARITH_CONV.

EXISTS_CONSEQ_CONV	(ConseqConv)
---------------------------	---------------------

EXISTS_CONSEQ_CONV : (conseq_conv -> conseq_conv)

Synopsis

Applies a consequence conversion to the body of an existentially quantified term.

Description

If c is a consequence conversion that maps a term ‘‘ $t\ x$ ’’ to a theorem $\vdash t\ x = t'\ x$, $\vdash t'\ x \implies t\ x$ or $\vdash t\ x \implies t'\ x$, then `EXISTS_CONSEQ_CONV c` maps ‘‘ $?x. t\ x$ ’’ to $\vdash ?x. t\ x = ?x. t'\ x$, $\vdash ?x. t'\ x \implies ?x. t\ x$ or $\vdash ?x. t\ x \implies ?x. t'\ x$, respectively.

Failure

`EXISTS_CONSEQ_CONV c t` fails, if t is not an existentially quantified term or if c fails on the body of t .

See also

Conv.QUANT_CONV, ConseqConv.FORALL_CONSEQ_CONV, ConseqConv.QUANT_CONSEQ_CONV.

EXISTS_DEL1_CONV	(unwindLib)
-------------------------	--------------------

EXISTS_DEL1_CONV : conv

Synopsis

Deletes one existential quantifier.

Description

`EXISTS_DEL1_CONV "?x. t"` returns the theorem:

$$\vdash (?x. t) = t$$

provided x is not free in t .

Failure

Fails if the argument term is not an existential quantification or if x is free in t .

See also

`unwindLib.EXISTS_DEL_CONV`, `unwindLib.PRUNE_ONCE_CONV`.

<code>EXISTS_DEL_CONV</code>	<code>(unwindLib)</code>
------------------------------	--------------------------

`EXISTS_DEL_CONV` : `conv`

Synopsis

Deletes existential quantifiers.

Description

`EXISTS_DEL_CONV "?x1 ... xn. t"` returns the theorem:

$$\vdash (?x1 \dots xn. t) = t$$

provided x_1, \dots, x_n are not free in t .

Failure

Fails if any of the x 's appear free in t . The function does not perform a partial deletion; for example, if x_1 and x_2 do not appear free in t but x_3 does, the function will fail; it will not return:

$$\vdash ?x1 \dots xn. t = ?x3 \dots xn. t$$

See also

`unwindLib.EXISTS_DEL1_CONV`, `unwindLib.PRUNE_CONV`.

<code>EXISTS_EQ</code>	<code>(Drule)</code>
------------------------	----------------------

`EXISTS_EQ` : `(term -> thm -> thm)`

Synopsis

Existentially quantifies both sides of an equational theorem.

Description

When applied to a variable x and a theorem whose conclusion is equational, $A \vdash t_1 = t_2$, the inference rule `EXISTS_EQ` returns the theorem $A \vdash (?x. t_1) = (?x. t_2)$, provided the variable x is not free in any of the assumptions.

$$\frac{A \vdash t_1 = t_2}{A \vdash (?x. t_1) = (?x. t_2)} \text{ EXISTS_EQ "x" } \quad [\text{where } x \text{ is not free in } A]$$

Failure

Fails unless the theorem is equational with both sides having type `bool`, or if the term is not a variable, or if the variable to be quantified over is free in any of the assumptions.

See also

`Thm.AP_TERM`, `Drule.EXISTS_IMP`, `Drule.FORALL_EQ`, `Drule.MK_EXISTS`,
`Drule.SELECT_EQ`.

<code>EXISTS_EQ___CONSEQ_CONV</code> <code>(ConseqConv)</code>

`EXISTS_EQ___CONSEQ_CONV` : `conseq_conv`

Synopsis

Given a term of the form $(?x. P x) = (?x. Q x)$ this consequence conversion returns the theorem $\vdash (!x. (P x = Q x)) \implies ((?x. P x) = (?x. Q x))$.

See also

`ConseqConv.conseq_conv`.

<code>EXISTS_EQN_CONV</code> <code>(unwindLib)</code>
--

`EXISTS_EQN_CONV` : `conv`

Synopsis

Proves the existence of a line that has a non-recursive equation.

Description

EXISTS_EQN_CONV "?l. !y1 ... ym. l x1 ... xn = t" returns the theorem:

$$\vdash (\exists l. !y1 \dots ym. l x1 \dots xn = t) = T$$

provided l is not free in t . Both m and n may be zero.

Failure

Fails if the argument term is not of the specified form or if l appears free in t .

See also

unwindLib.PRUNE_ONCE_CONV.

<div data-bbox="234 1014 529 1066" data-label="Text"> <p>EXISTS_IMP</p> </div>	<div data-bbox="1200 1014 1410 1066" data-label="Text"> <p>(Drule)</p> </div>
--	---

EXISTS_IMP : (term -> thm -> thm)

Synopsis

Existentially quantifies both the antecedent and consequent of an implication.

Description

When applied to a variable x and a theorem $A \vdash t1 ==> t2$, the inference rule EXISTS_IMP returns the theorem $A \vdash (\exists x. t1) ==> (\exists x. t2)$, provided x is not free in the assumptions.

$$\frac{A \vdash t1 ==> t2}{A \vdash (\exists x. t1) ==> (\exists x. t2)} \quad \text{EXISTS_IMP "x"} \quad [\text{where } x \text{ is not free in } A]$$

Failure

Fails if the theorem is not implicative, or if the term is not a variable, or if the term is a variable but is free in the assumption list.

See also

Drule.EXISTS_EQ.

EXISTS_IMP_CONV

(Conv)

EXISTS_IMP_CONV : conv

Synopsis

Moves an existential quantification inwards through an implication.

Description

When applied to a term of the form $?x. P ==> Q$, where x is not free in both P and Q , EXISTS_IMP_CONV returns a theorem of one of three forms, depending on occurrences of the variable x in P and Q . If x is free in P but not in Q , then the theorem:

$$\vdash (?x. P ==> Q) = (!x.P) ==> Q$$

is returned. If x is free in Q but not in P , then the result is:

$$\vdash (?x. P ==> Q) = P ==> (?x.Q)$$

And if x is free in neither P nor Q , then the result is:

$$\vdash (?x. P ==> Q) = (!x.P) ==> (?x.Q)$$

Failure

EXISTS_IMP_CONV fails if it is applied to a term not of the form $?x. P ==> Q$, or if it is applied to a term $?x. P ==> Q$ in which the variable x is free in both P and Q .

See also

Conv.LEFT_IMP_FORALL_CONV, Conv.RIGHT_IMP_EXISTS_CONV.

EXISTS_NOT_CONV

(Conv)

EXISTS_NOT_CONV : conv

Synopsis

Moves an existential quantification inwards through a negation.

Description

When applied to a term of the form $?x. \sim P$, the conversion EXISTS_NOT_CONV returns the theorem:

$$\vdash (\exists x. \sim P) = \sim (!x. P)$$

Failure

Fails if applied to a term not of the form $\exists x. \sim P$.

See also

`Conv.FORALL_NOT_CONV`, `Conv.NOT_EXISTS_CONV`, `Conv.NOT_FORALL_CONV`.

EXISTS_OR_CONV

(Conv)

`EXISTS_OR_CONV` : `conv`

Synopsis

Moves an existential quantification inwards through a disjunction.

Description

When applied to a term of the form $\exists x. P \vee Q$, the conversion `EXISTS_OR_CONV` returns the theorem:

$$\vdash (\exists x. P \vee Q) = (\exists x.P) \vee (\exists x.Q)$$

Failure

Fails if applied to a term not of the form $\exists x. P \vee Q$.

See also

`Conv.OR_EXISTS_CONV`, `Conv.LEFT_OR_EXISTS_CONV`, `Conv.RIGHT_OR_EXISTS_CONV`.

EXISTS_TAC

(Tactic)

`EXISTS_TAC` : `(term -> tactic)`

Synopsis

Reduces existentially quantified goal to one involving a specific witness.

Description

When applied to a term u and a goal $\exists x. t$, the tactic `EXISTS_TAC` reduces the goal to $t[u/x]$ (substituting u for all free instances of x in t , with variable renaming if necessary to avoid free variable capture).


```

A ?- ?x. t
===== EXISTS_TAC "u"
A ?- t[u/x]

```

Failure

Fails unless the goal's conclusion is existentially quantified and the term supplied has the same type as the quantified variable in the goal.

Example

The goal:

```
?- ?x. x=T
```

can be solved by:

```
EXISTS_TAC ``T`` THEN REFL_TAC
```

See also

Thm.EXISTS.

exists_tyvar	(Type)
--------------	--------

```
exists_tyvar : (hol_type -> bool) -> hol_type -> bool
```

Synopsis

Checks if a type variable satisfying a given condition exists in a type.

Description

An invocation `exists_tyvar P ty` searches `ty` for a type variable satisfying the predicate `P`. The value `true` is returned if the search is successful; otherwise `false` is the result.

Failure

If `P` fails when applied to a type variable encountered in the course of searching `ty`.

Example

```

- exists_tyvar (equal beta) (alpha --> beta --> bool);
> val it = true : bool

```

Comments

This function is more efficient, in some cases, than `exists P o type_vars`.

<code>EXISTS_UNIQUE_CONV</code>	<code>(Conv)</code>
---------------------------------	---------------------

`EXISTS_UNIQUE_CONV : conv`

Synopsis

Expands with the definition of unique existence.

Description

Given a term of the form "`?!x.P[x]`", the conversion `EXISTS_UNIQUE_CONV` proves that this assertion is equivalent to the conjunction of two statements, namely that there exists at least one value `x` such that `P[x]`, and that there is at most one value `x` for which `P[x]` holds. The theorem returned is:

$$\vdash (?! x. P[x]) = (?x. P[x]) \wedge (!x x'. P[x] \wedge P[x'] \implies (x = x'))$$

where `x'` is a primed variant of `x` that does not appear free in the input term. Note that the quantified variable `x` need not in fact appear free in the body of the input term. For example, `EXISTS_UNIQUE_CONV "?!x.T"` returns the theorem:

$$\vdash (?! x. T) = (?x. T) \wedge (!x x'. T \wedge T \implies (x = x'))$$
Failure

`EXISTS_UNIQUE_CONV tm` fails if `tm` does not have the form "`?!x.P`".

See also

`Conv.EXISTENCE`.

<code>exn_to_string</code>	<code>(Feedback)</code>
----------------------------	-------------------------

`exn_to_string : exn -> string`

Synopsis

Map an exception into a string

Description

The function `exn_to_string` maps an exception to a string. However, in the case of the `Interrupt` exception, it is not mapped to a string, but is instead raised. This avoids the possibility of suppressing the propagation of `Interrupt` to the top level.

Failure

Never fails.

Example

```
- exn_to_string Interrupt;
> Interrupted.

- exn_to_string Div;
> val it = "Div" : string

- print
  (exn_to_string (mk_HOL_ERR "Foo" "bar" "incomprehensible input"));
```

```
Exception raised at Foo.bar:
incomprehensible input
> val it = () : unit
```

See also

`Feedback`, `Feedback.HOL_ERR`, `Feedback.ERR_to_string`.

EXP_CONV

(reduceLib)

EXP_CONV : conv

Synopsis

Calculates by inference the result of raising one numeral to the power of another.

Description

If `m` and `n` are numerals (e.g. 0, 1, 2, 3,...), then `EXP_CONV "m EXP n"` returns the theorem:

$$\vdash m \text{ EXP } n = s$$

where s is the numeral that denotes the result of raising the natural number denoted by m to the power of the natural number denoted by n .

Failure

`EXP_CONV tm` fails unless `tm` is of the form "`m EXP n`", where `m` and `n` are numerals.

Example

```
#EXP_CONV "0 EXP 0";;
```

```
|- 0 EXP 0 = 1
```

```
#EXP_CONV "15 EXP 0";;
```

```
|- 15 EXP 0 = 1
```

```
#EXP_CONV "12 EXP 1";;
```

```
|- 12 EXP 1 = 12
```

```
#EXP_CONV "2 EXP 6";;
```

```
|- 2 EXP 6 = 64
```

`expand`

(proofManagerLib)

```
expand : tactic -> proof
```

Synopsis

Applies a tactic to the current goal, stacking the resulting subgoals.

Description

The function `expand` is part of the subgoal package. It may be abbreviated by the function `e`. It applies a tactic to the current goal to give a new proof state. The previous state is stored on the backup list. If the tactic produces subgoals, the new proof state is formed from the old one by removing the current goal from the goal stack and adding a new level consisting of its subgoals. The corresponding justification is placed on the justification stack. The new subgoals are printed. If more than one subgoal is produced, they are printed from the bottom of the stack so that the new current goal is printed last.

If a tactic solves the current goal (returns an empty subgoal list), then its justification is used to prove a corresponding theorem. This theorem is incorporated into the justification of the parent goal and printed. If the subgoal was the last subgoal of the level,

the level is removed and the parent goal is proved using its (new) justification. This process is repeated until a level with unproven subgoals is reached. The next goal on the goal stack then becomes the current goal. This goal is printed. If all the subgoals are proved, the resulting proof state consists of the theorem proved by the justifications.

The tactic applied is a validating version of the tactic given. It ensures that the justification of the tactic does provide a proof of the goal from the subgoals generated by the tactic. It will cause failure if this is not so. The tactical `VALID` performs this validation.

For a description of the subgoal package, see `set_goal`.

Failure

`expand tac` fails if the tactic `tac` fails for the top goal. It will diverge if the tactic diverges for the goal. It will fail if there are no unproven goals. This could be because no goal has been set using `set_goal` or because the last goal set has been completely proved. It will also fail in cases when the tactic is invalid.

Example

```
- expand CONJ_TAC;
- expand CONJ_TAC;
OK..
NO_PROOFS! Uncaught exception:
! NO_PROOFS

- g '(HD[1;2;3] = 1) /\ (TL[1;2;3] = [2;3])';
> val it =
  Proof manager status: 1 proof.
  1. Incomplete:
    Initial goal:
      (HD [1; 2; 3] = 1) /\ (TL [1; 2; 3] = [2; 3])

    : proofs

- expand CONJ_TAC;
OK..
2 subgoals:
> val it =
  TL [1; 2; 3] = [2; 3]

  HD [1; 2; 3] = 1
```

```

      : proof

- expand (REWRITE_TAC[listTheory.HD]);
OK..

Goal proved.
|- HD [1; 2; 3] = 1

Remaining subgoals:
> val it =
    TL [1; 2; 3] = [2; 3]

      : proof

- expand (REWRITE_TAC[listTheory.TL]);
OK..

Goal proved.
|- TL [1; 2; 3] = [2; 3]
> val it =
    Initial goal proved.
    |- (HD [1; 2; 3] = 1) /\ (TL [1; 2; 3] = [2; 3]) : proof

```

In the following example an invalid tactic is used. It is invalid because it assumes something that is not on the assumption list of the goal. The justification adds this assumption to the assumption list so the justification would not prove the goal that was set.

```

- g '1=2';
> val it =
    Proof manager status: 2 proofs.
    2. Completed: |- (HD [1; 2; 3] = 1) /\ (TL [1; 2; 3] = [2; 3])
    1. Incomplete:
        Initial goal:
        1 = 2

      : proofs
- expand (REWRITE_TAC[ASSUME (Term '1=2')]);
OK..

```

Exception raised at Tactical.VALID:

```
Invalid tactic
! Uncaught exception:
! HOL_ERR
```

Uses

Doing a step in an interactive goal-directed proof.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`,
`proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`,
`proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`,
`proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

<div data-bbox="161 916 710 967" data-label="Text"> <p>EXPAND_ALL_BUT_CONV</p> </div>	<div data-bbox="1011 916 1331 967" data-label="Text"> <p>(unwindLib)</p> </div>
--	--

```
EXPAND_ALL_BUT_CONV : (string list -> thm list -> conv)
```

Synopsis

Unfolds, then unwinds all lines (except those specified) as much as possible, then prunes the unwound lines.

Description

`EXPAND_ALL_BUT_CONV` [`'li(k+1)'`;...;`'lim'`] `th1` when applied to the following term:

```
"?l1 ... lm. t1 /\ ... /\ ui1 /\ ... /\ uik /\ ... /\ tn"
```

returns a theorem of the form:

$$B \vdash (?l1 \dots lm. t1 \wedge \dots \wedge ui1 \wedge \dots \wedge uik \wedge \dots \wedge tn) =$$

$$(?li(k+1) \dots lim. t1' \wedge \dots \wedge tn')$$

where each t_i' is the result of rewriting t_i with the theorems in $th1$. The set of assumptions B is the union of the instantiated assumptions of the theorems used for rewriting. If none of the rewrites are applicable to a conjunct, it is unchanged. Those conjuncts that after rewriting are equations for the lines $li1, \dots, lik$ (they are denoted by $ui1, \dots, uik$) are used to unwind and the lines $li1, \dots, lik$ are then pruned.

The li 's are related by the equation:

$$\{\{li1, \dots, lik\}\} \cup \{\{li(k+1), \dots, lim\}\} = \{\{l1, \dots, lm\}\}$$

Failure

The function may fail if the argument term is not of the specified form. It will also fail if the unwound lines cannot be pruned. It is possible for the function to attempt unwinding indefinitely (to loop).

Example

```
#EXPAND_ALL_BUT_CONV ['l1']
# [ASSUME "!in out. INV (in,out) = !(t:num). out t = ~(in t)"]
# "?l1 l2.
#   INV (l1,l2) /\ INV (l2,out) /\ (!(t:num). l1 t = l2 (t-1) \/ out (t-1))";;
. |- (?l1 l2.
      INV(l1,l2) /\ INV(l2,out) /\ (!t. l1 t = l2(t - 1) \/ out(t - 1))) =
      (?l1.
        (!t. out t = ~~l1 t) /\ (!t. l1 t = ~l1(t - 1) \/ ~~l1(t - 1)))
```

See also

unwindLib.EXPAND_AUTO_CONV, unwindLib.EXPAND_ALL_BUT_RIGHT_RULE,
 unwindLib.EXPAND_AUTO_RIGHT_RULE, unwindLib.UNFOLD_CONV,
 unwindLib.UNWIND_ALL_BUT_CONV, unwindLib.PRUNE_SOME_CONV.

EXPAND_ALL_BUT_RIGHT_RULE (unwindLib)

```
EXPAND_ALL_BUT_RIGHT_RULE : (string list -> thm list -> thm -> thm)
```

Synopsis

Unfolds, then unwinds all lines (except those specified) as much as possible, then prunes the unwound lines.

Description

EXPAND_ALL_BUT_RIGHT_RULE ['li(k+1)';...;'lim'] th1 behaves as follows:

```
A |- !z1 ... zr.
      t = ?l1 ... lm. t1 /\ ... /\ u1 /\ ... /\ uk /\ ... /\ tn
-----
B u A |- !z1 ... zr. t = ?li(k+1) ... lim. t1' /\ ... /\ tn'
```


where each t_i' is the result of rewriting t_i with the theorems in $th1$. The set of assumptions B is the union of the instantiated assumptions of the theorems used for rewriting. If none of the rewrites are applicable to a conjunct, it is unchanged. Those conjuncts that after rewriting are equations for the lines l_{i1}, \dots, l_{ik} (they are denoted by u_{i1}, \dots, u_{ik}) are used to unwind and the lines l_{i1}, \dots, l_{ik} are then pruned.

The l_i 's are related by the equation:

$$\{\{l_{i1}, \dots, l_{ik}\}\} \cup \{\{l_{i(k+1)}, \dots, l_{im}\}\} = \{\{l_1, \dots, l_m\}\}$$

Failure

The function may fail if the argument theorem is not of the specified form. It will also fail if the unwound lines cannot be pruned. It is possible for the function to attempt unwinding indefinitely (to loop).

Example

```
#EXPAND_ALL_BUT_RIGHT_RULE ['l1']
# [ASSUME "!in out. INV (in,out) = !(t:num). out t = ~(in t)"]
# (ASSUME
#   "!(in:num->bool) out.
#     DEV(in,out) =
#       ?l1 l2.
#     INV (l1,l2) /\ INV (l2,out) /\ (!(t:num). l1 t = in t \/ out (t-1))");;
.. |- !in out.
    DEV(in,out) =
      (?l1. (!t. out t = ~~l1 t) /\ (!t. l1 t = in t \/ ~~l1(t - 1)))
```

See also

`unwindLib.EXPAND_AUTO_RIGHT_RULE`, `unwindLib.EXPAND_ALL_BUT_CONV`,
`unwindLib.EXPAND_AUTO_CONV`, `unwindLib.UNFOLD_RIGHT_RULE`,
`unwindLib.UNWIND_ALL_BUT_RIGHT_RULE`, `unwindLib.PRUNE_SOME_RIGHT_RULE`.

EXPAND_AUTO_CONV

(unwindLib)

`EXPAND_AUTO_CONV : (thm list -> conv)`

Synopsis

Unfolds, then unwinds as much as possible, then prunes the unwound lines.

Description

`EXPAND_AUTO_CONV th1` when applied to the following term:

```
"?l1 ... lm. t1 /\ ... /\ ui1 /\ ... /\ uik /\ ... /\ tn"
```

returns a theorem of the form:

$$B \vdash (?l1 \dots lm. t1 \wedge \dots \wedge ui1 \wedge \dots \wedge uik \wedge \dots \wedge tn) =$$

$$(?li(k+1) \dots lim. t1' \wedge \dots \wedge tn')$$

where each t_i' is the result of rewriting t_i with the theorems in $th1$. The set of assumptions B is the union of the instantiated assumptions of the theorems used for rewriting. If none of the rewrites are applicable to a conjunct, it is unchanged. After rewriting, the function decides which of the resulting terms to use for unwinding, by performing a loop analysis on the graph representing the dependencies of the lines.

Suppose the function decides to unwind $li1, \dots, lik$ using the terms $ui1', \dots, uik'$ respectively. Then, after unwinding, the lines $li1, \dots, lik$ are pruned (provided they have been eliminated from the right-hand sides of the conjuncts that are equations, and from the whole of any other conjuncts) resulting in the elimination of $ui1', \dots, uik'$.

The li 's are related by the equation:

$$\{\{li1, \dots, lik\}\} \cup \{\{li(k+1), \dots, lim\}\} = \{\{l1, \dots, lm\}\}$$

The loop analysis allows the term to be unwound as much as possible without the risk of looping. The user is left to deal with the recursive equations.

Failure

The function may fail if the argument term is not of the specified form. It also fails if there is more than one equation for any line variable.

Example

```
#EXPAND_AUTO_CONV
# [ASSUME "!in out. INV (in,out) = !(t:num). out t = ~(in t)"]
# "?l1 l2.
#   INV (l1,l2) /\ INV (l2,out) /\ (!(t:num). l1 t = l2 (t-1) \/ out (t-1))";;
. |- (?l1 l2.
      INV(l1,l2) /\ INV(l2,out) /\ (!t. l1 t = l2(t - 1) \/ out(t - 1))) =
      (?l2.
        (!t. l2 t = ~(l2(t - 1) \/ ~l2(t - 1))) /\ (!t. out t = ~l2 t))
```

See also

`unwindLib.EXPAND_ALL_BUT_CONV`, `unwindLib.EXPAND_AUTO_RIGHT_RULE`,
`unwindLib.EXPAND_ALL_BUT_RIGHT_RULE`, `unwindLib.UNFOLD_CONV`,
`unwindLib.UNWIND_AUTO_CONV`, `unwindLib.PRUNE_SOME_CONV`.

EXPAND_AUTO_RIGHT_RULE

(unwindLib)

EXPAND_AUTO_RIGHT_RULE : (thm list -> thm -> thm)

Synopsis

Unfolds, then unwinds as much as possible, then prunes the unwound lines.

Description

EXPAND_AUTO_RIGHT_RULE th1 behaves as follows:

$$\begin{array}{l}
 A \mid- !z1 \dots zr. \\
 \quad t = ?l1 \dots lm. t1 \wedge \dots \wedge ui1 \wedge \dots \wedge uik \wedge \dots \wedge tn \\
 \hline
 B \text{ u } A \mid- !z1 \dots zr. t = ?li(k+1) \dots lim. t1' \wedge \dots \wedge tn'
 \end{array}$$

where each t_i' is the result of rewriting t_i with the theorems in $th1$. The set of assumptions B is the union of the instantiated assumptions of the theorems used for rewriting. If none of the rewrites are applicable to a conjunct, it is unchanged. After rewriting, the function decides which of the resulting terms to use for unwinding, by performing a loop analysis on the graph representing the dependencies of the lines.

Suppose the function decides to unwind $li1, \dots, lik$ using the terms $ui1', \dots, uik'$ respectively. Then, after unwinding, the lines $li1, \dots, lik$ are pruned (provided they have been eliminated from the right-hand sides of the conjuncts that are equations, and from the whole of any other conjuncts) resulting in the elimination of $ui1', \dots, uik'$.

The li 's are related by the equation:

$$\{\{li1, \dots, lik\}\} \text{ u } \{\{li(k+1), \dots, lim\}\} = \{\{l1, \dots, lm\}\}$$

The loop analysis allows the term to be unwound as much as possible without the risk of looping. The user is left to deal with the recursive equations.

Failure

The function may fail if the argument theorem is not of the specified form. It also fails if there is more than one equation for any line variable.

Example

```

#EXPAND_AUTO_RIGHT_RULE
# [ASSUME "!in out. INV (in,out) = !(t:num). out t = ~(in t)"]
# (ASSUME
#   "!(in:num->bool) out.

```

```
#   DEV(in,out) =
#   ?l1 l2.
#   INV (l1,l2) /\ INV (l2,out) /\ (!(t:num). l1 t = in t \/ out (t-1))");;
.. |- !in out. DEV(in,out) = (!t. out t = ~(in t \/ out(t - 1)))
```

See also

unwindLib.EXPAND_ALL_BUT_RIGHT_RULE, unwindLib.EXPAND_AUTO_CONV,
 unwindLib.EXPAND_ALL_BUT_CONV, unwindLib.UNFOLD_RIGHT_RULE,
 unwindLib.UNWIND_AUTO_RIGHT_RULE, unwindLib.PRUNE_SOME_RIGHT_RULE.

<div data-bbox="236 797 443 855" data-label="Text"> <p>expandf</p> </div>	<div data-bbox="917 797 1412 855" data-label="Text"> <p>(proofManagerLib)</p> </div>
---	--

expandf : (tactic -> unit)

Synopsis

Applies a tactic to the current goal, stacking the resulting subgoals.

Description

The function `expandf` is a faster version of `expand`. It does not use a validated version of the tactic. That is, no check is made that the justification of the tactic does prove the goal from the subgoals it generates. If an invalid tactic is used, the theorem ultimately proved may not match the goal originally set. Alternatively, failure may occur when the justifications are applied in which case the theorem would not be proved. For a description of the subgoal package, see under `set_goal`.

Failure

Calling `expandf tac` fails if the tactic `tac` fails for the top goal. It will diverge if the tactic diverges for the goal. It will fail if there are no unproven goals. This could be because no goal has been set using `set_goal` or because the last goal set has been completely proved. If an invalid tactic, whose justification actually fails, has been used earlier in the proof, `expandf tac` may succeed in applying `tac` and apparently prove the current goal. It may then fail as it applies the justifications of the tactics applied earlier.

Example

```
- g 'HD[1;2;3] = 1';

'HD[1;2;3] = 1'
```

```

() : void

- expandf (REWRITE_TAC[HD;TL]);;
OK..
goal proved
|- HD[1;2;3] = 1

```

Previous subproof:

```

goal proved
() : void

```

The following example shows how the use of an invalid tactic can yield a theorem which does not correspond to the goal set.

```

- set_goal([], Term '1=2');
'1 = 2'

() : void

- expandf (REWRITE_TAC[ASSUME (Term'1=2')]);
OK..
goal proved
. |- 1 = 2

```

Previous subproof:

```

goal proved
() : void

```

The proof assumed something which was not on the assumption list. This assumption appears in the assumption list of the theorem proved, even though it was not in the goal. An attempt to perform the proof using `expand` fails. The validated version of the tactic detects that the justification produces a theorem which does not correspond to the goal set. It therefore fails.

Uses

Saving CPU time when doing goal-directed proofs, since the extra validation is not done. Redoing proofs quickly that are already known to work.

Comments

The CPU time saved may cause misery later. If an invalid tactic is used, this will only be discovered when the proof has apparently been finished and the justifications are applied.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`,
`proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`,
`proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`,
`proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

<code>export_rewrites</code>	<code>(BasicProvers)</code>
------------------------------	-----------------------------

`export_rewrites : string list -> unit`

Synopsis

Exports theorems so that they merge with the “stateful” rewriter’s `simpset`.

Description

A call to `export_rewrites strlist` causes the theorems named by the strings in `strlist` to be merged into the `simpset` value maintained behind the function `srw_ss()`, both in the current session and also when the theory generated by the script file is loaded.

The theory is also augmented with an element in its signature of the form `<thymname>_rwts` of type `simpLib.ssfrag`. This value is the collection of all the theorems specified in calls to `export_rewrites`.

Multiple calls to `export_rewrites` cumulatively add to the list of theorems being exported.

Failure

Fails if any of the strings in the list does not correspond to the name of a theorem, definition or axiom of the current theory segment.

Comments

This function is useful for ensuring that the stateful rewriter is augmented as theories are loaded. This in turn means that users of these theories don’t need to learn the names of their “obvious” theorems. Because theorems can not be removed from the stateful rewriter’s underlying `simpset`, choice of “obvious” theorems needs to be done with care.

See also

`bossLib.augment_srw_ss`, `bossLib.srw_ss`, `bossLib.SRW_TAC`.

<code>export_theory</code>	<code>(Theory)</code>
----------------------------	-----------------------

`export_theory : unit -> unit`

Synopsis

Write a theory segment to disk.

Description

An invocation `export_theory()` saves the current theory segment to disk. All parents, definitions, axioms, and stored theorems of the segment are saved in such a way that, when the theory is loaded from disk in a later session, the full theory in place at the time `export_theory` was called is re-instated.

If the current theory segment is named `thy`, then `export_theory()` will create ML files `thyTheory.sig` and `thyTheory.sml`, in the current directory at the time `export_theory` is invoked. These files need to be compiled before they become usable. In the standard way of doing things, the `Holmake` facility will handle this task.

Once a theory segment has been exported and compiled, it is available for use. It can be brought into an interactive proof session via

```
load "thyTheory";
```

When the segment is loaded, its parents, axioms, theorems, and definitions are incorporated into the current theory (recall that this notion is different than the current theory segment).

Failure

A call to `export_theory` may fail if the disk file cannot be opened. A call to `export_theory` will also fail if some bindings are such that the name of the binding is not a valid ML identifier. In that case, `export_theory` will report all such bad names. These can be changed with `set_MLname`, and then `export_theory` may be attempted again.

Example

```
- save_thm("foo", REFL (Term 'x:bool'));
> val it = |- x = x : thm

- export_theory();
Exporting theory "scratch" ... done.
> val it = () : unit
```

Comments

Note that `export_theory` exports the state of the theory, and not that of the ML environment. If one wants to restore the state of the ML environment in existence at the time `export_theory()` is invoked, special steps have to be taken; see `adjoin_to_theory`.

See also

`Theory.new_theory`, `Theory.adjoin_to_theory`, `Theory.set_MLname`.

EXT**(Drule)**

EXT : thm -> thm

Synopsis

Derives equality of functions from extensional equivalence.

DescriptionWhen applied to a theorem $A \vdash !x. t1\ x = t2\ x$, the inference rule EXT returns the theorem $A \vdash t1 = t2$.
$$\frac{A \vdash !x. t1\ x = t2\ x}{A \vdash t1 = t2} \quad \text{EXT} \quad [\text{where } x \text{ is not free in } t1 \text{ or } t2]$$
FailureFails if the theorem does not have the form indicated above, or if the variable x is free in either of the functions $t1$ or $t2$.**Comments**This rule is expressed as an equivalence in the theorem `boolTheory.FUN_EQ_THM`.**See also**`Thm.AP_THM`, `Drule.ETA_CONV`, `Conv.FUN_EQ_CONV`.**EXT_CONSEQ_REWRITE_CONV****(ConseqConv)**

EXT_CONSEQ_REWRITE_CONV : conv list -> thm list -> (thm list * thm list * thm list) -> di

Synopsis

Applies CONSEQ_REWRITE_CONV interleaved with conversions and rewrites.

Description

CONSEQ_REWRITE_CONV often results in theorems of the following form

$$\vdash (!x. T) \wedge (T \wedge (T \wedge T)) \wedge (\backslash x. P)\ y \wedge T \implies \text{something}$$

The problem is that `CONSEQ_REWRITE_CONV` applies consequence conversions, but no normal convs or simplifications. This is changed by `EXT_CONSEQ_REWRITE_CONV`. `EXT_CONSEQ_REWRITE_CONV` gets a list of conversions and a list of rewrite theorems. Moreover there are the parameters of `CONSEQ_REWRITE_CONV`. It then applies these conversions (e.g. `DEPTH_CONV BETA_CONV`) and a `REWRITE_CONV` with the given theorem list interleaved with `CONSEQ_REWRITE_CONV`. As a result the theorem above might look now like

```
|- P y ==> something
```

See also

`ConseqConv.CONSEQ_REWRITE_CONV`.

<code>EXT_DEPTH_CONSEQ_CONV</code>	<code>(ConseqConv)</code>
------------------------------------	---------------------------

```
EXT_DEPTH_CONSEQ_CONV : conseq_conv_congruence list -> int option -> bool -> directed_conseq_c
```

Synopsis

The general depth consequence conversion of which `DEPTH_CONSEQ_CONV`, `REDEPTH_CONSEQ_CONV`, `ONCE_DEPTH_CONSEQ_CONV` etc are just instantiations.

Description

`DEPTH_CONSEQ_CONV` and similar conversions are able apply a consequence conversion by breaking down the structure of a term using lemmata about \wedge , \vee , \sim , \implies and quantification. Thereby, these conversions collect various amounts of context information.

`EXT_DEPTH_CONSEQ_CONV congruence_list cache_opt step_opt redepth convL` is the conversion used by these other depth conversions. Its interface allows one to add to the given list of boolean combinations and thus allow the conversion of parts of user-defined predicates. This is done using `congruence_list`. However, let's consider the other parameters first: `cache_opt` determines which cache to use: `NONE` means no caching; a standard cache that stores everything is configured by `CONSEQ_CONV_default_cache_opt`.

The number of steps taken is determined by `step_opt`. `NONE` means arbitrarily many; `SOME n` means at most `n`. `ONCE_DEPTH_CONSEQ_CONV` for example uses `SOME 1`. The parameter `redepth` determines whether modified terms should be revisited and `convL` is a basically a list of directed consequence conversions of the conversions that should be applied at subpositions. Its entries consist of a flag, whether to apply the conversion before or after descending into subterms; the weight (i.e. the number of counted steps) for the conversion, and a function from the context (a list of theorems) to the conversion.

The first parameter `congruence_list` is a list of congruences that determine how to break down terms. Each element of this list has to be a function `congruence context sys dir t` which returns a pair of the number of performed steps and a resulting theorem. `sys` is a callback that allows to apply the depth conversion recursively to subterms. `context` gives the context that can be used, but is normally just interesting for the conversions. If you ignore the number of steps, the congruence is otherwise a directed consequence conversion. If the congruence can't be applied, it should either fail or raise an `UNCHANGED` exception. The callback `sys` gets the number of already performed steps, a direction and a term. It then returns a accumulated number of steps and a `thm` option. It never fails. The number of steps is used to abort if the maximum number of globally allowed steps has been reached. The first call of `sys` should get 0, then the accumulated number has to be passed. The congruence should return the finally, accumulated number of steps. As an example, a congruence for implications is implemented by

```
fun CONSEQ_CONV_CONGRUENCE___imp_simple_context context sys dir t =
  let
    val (b1,b2) = dest_imp t;

    (* simplify the precondition *)
    val (n1, thm1_opt) = sys [] 0 (CONSEQ_CONV_DIRECTION_NEGATE dir) b1;

    (* what did it simplify to? *)
    val a2 = CONSEQ_CONV___OPT_GET_SIMPLIFIED_TERM
              thm1_opt
              (CONSEQ_CONV_DIRECTION_NEGATE dir)
              b1;

    (* if precond is false, one does not need to process the conclusion *)
    val abort_cond = same_const a2 F;

    (* otherwise process the conclusion and add the precond as
       additional context *)
    val (n2, thm2_opt) = if abort_cond then (n1, NONE)
                          else sys [a2] n1 dir b2;

    (* abort, if nothing was done *)
    val _ = if (isSome thm1_opt) orelse (isSome thm2_opt) orelse
              abort_cond
            then ()
            else raise UNCHANGED;
```

```

(* get theorems, if necessary create them and get the additional
   context as an additional implication *)
val thm1 = conseq_conv_congruence_EXPAND_THM_OPT (thm1_opt, b1, NONE);
val thm2 = conseq_conv_congruence_EXPAND_THM_OPT (thm2_opt, b2, SOME a2);

(* apply congruence rule for these theorems *)
val cong_thm =
  if (dir = CONSEQ_CONV_STRENGTHEN_direction) then
    IMP_CONG_simple_imp_strengthen
  else IMP_CONG_simple_imp_weaken
val thm3 = MATCH_MP cong_thm (CONJ thm1 thm2)

(* simplify output: (F ==> X) = X etc.
   val thm4 = CONV_RULE (dir_conv dir trivial_imp_simp) thm3
               handle HOL_ERR _ => thm3
in
  (n2, thm4)
end handle HOL_ERR _ => raise CONSEQ_CONV_congruence_expectation;

```

See also

ConseqConv.DEPTH_CONSEQ_CONV, ConseqConv.REDEPTH_CONSEQ_CONV,
 ConseqConv.ONCE_DEPTH_CONSEQ_CONV, ConseqConv.NUM_DEPTH_CONSEQ_CONV.

F	(boolSyntax)
---	--------------

F : term

Synopsis

Constant denoting falsity.

Description

The ML variable `boolSyntax.F` is bound to the term `bool$F`.

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`,
`boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`,
`boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.negation`,
`boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let_tm`,
`boolSyntax.arb`.

fail**(Feedback)**

```
fail : unit -> 'a
```

Synopsis

Raise a `HOL_ERR`.

Description

The function `fail` raises a `HOL_ERR` with default values. This is useful when detailed error tracking is not necessary.

Failure

Always fails.

Example

```
- fail() handle e => Raise e;
```

```
Exception raised at ??.??:
```

```
fail
```

```
! Uncaught exception:
```

```
! HOL_ERR
```

See also

`Feedback`, `Feedback.failwith`, `Feedback.Raise`, `Feedback.HOL_ERR`.

FAIL_TAC**(Tactical)**

```
FAIL_TAC : (string -> tactic)
```

Synopsis

Tactic which always fails, with the supplied string.

Description

Whatever goal it is applied to, `FAIL_TAC s` always fails with the string `s`.

Failure

The application of `FAIL_TAC` to a string never fails; the resulting tactic always fails.

Example

The following example uses the fact that if a tactic `t1` solves a goal, then the tactic `t1 THEN t2` never results in the application of `t2` to anything, because `t1` produces no subgoals. In attempting to solve the following goal:

```
?- x => T | T
```

the tactic

```
REWRITE_TAC[] THEN FAIL_TAC 'Simple rewriting failed to solve goal'
```

will fail with the message provided, whereas:

```
CONV_TAC COND_CONV THEN FAIL_TAC 'Using COND_CONV failed to solve goal'
```

will silently solve the goal because `COND_CONV` reduces it to just `?- T`.

See also

`Tactical.ALL_TAC`, `Tactical.NO_TAC`.

`failwith`

(Feedback)

```
failwith : string -> 'a
```

Synopsis

Raise a `HOL_ERR`.

Description

The function `failwith` raises a `HOL_ERR` with default values. This is useful when detailed error tracking is not necessary.

`failwith` differs from `fail` in that it takes an extra string argument, which is typically used to tell which function `failwith` is being called from.

Failure

Always fails.

Example

```
- failwith "foo" handle e => Raise e;
```

```
Exception raised at ??failwith:
```

```
foo
```

```
! Uncaught exception:
```

```
! HOL_ERR
```

See also

Feedback, Feedback.fail, Feedback.Raise, Feedback.HOL_ERR.

FALSE_CONSEQ_CONV

(ConseqConv)

```
FALSE_CONSEQ_CONV : conseq_conv
```

Synopsis

Given a term t of type `bool` this consequence conversion returns the theorem $\vdash F \implies t$.

See also

ConseqConv.TRUE_CONSEQ_CONV, ConseqConv.REFL_CONSEQ_CONV,
ConseqConv.TRUE_FALSE_REFL_CONSEQ_CONV.

FCP_ss

(fcpLib)

```
FCP_ss : ssfrag
```

Synopsis

A simpset fragment for simplifying finite Cartesian product expressions.

Example

```
simpLib.SSFRAG{ac = [], congs = [], convs = [], dprocs = [], filter = NONE,
  rewrs =
    [|- !i. i < dimindex (:'b) ==> ($FCP g ' i = g i),
      |- !g. (FCP i. g ' i) = g,
      |- !x y. (x = y) = !i. i < dimindex (:'b) ==> (x ' i = y ' i)]}
: ssfrag
```

See also

wordsLib.WORD_BIT_EQ_ss.

Feedback

```
structure Feedback
```

Synopsis

Module for messages, warnings, errors, and tracing of HOL functions.

Description

The `Feedback` structure provides facilities for raising and viewing HOL errors, and also for monitoring tools as they run.

fetch

(DB)

```
fetch : string -> string -> thm
```

Synopsis

Fetch a theorem by theory and name.

Description

An invocation `fetch thy name` searches through the currently loaded theory segments in an attempt to find a theorem, axiom, or definition stored under `name` in theory `thy`.

Failure

If the specified theorem, axiom, or definition cannot be located.

Example

```
- DB.fetch "bool" "NOT_FORALL_THM";
> val it = |- !P. ~(!x. P x) = ?x. ~P x : thm
```

See also

DB.thms, DB.thy, DB.theorems, DB.axioms, DB.definitions.

filter**(Lib)**

```
filter : ('a -> bool) -> 'a list -> 'a list
```

Synopsis

Filters a list to the sublist of elements satisfying a predicate.

Description

`filter P l` applies `P` to every element of `l`, returning a list of those that satisfy `P`, in the order they appeared in the original list.

Failure

If `P x` fails for some element `x` of `l`.

Comments

Identical to `List.filter` from the Standard ML Basis Library.

See also

`Lib.mapfilter`, `Lib.partition`.

FILTER_ASM_REWRITE_RULE**(Rewrite)**

```
FILTER_ASM_REWRITE_RULE : ((term -> bool) -> thm list -> thm -> thm)
```

Synopsis

Rewrites a theorem including built-in rewrites and some of the theorem's assumptions.

Description

This function implements selective rewriting with a subset of the assumptions of the theorem. The first argument (a predicate on terms) is applied to all assumptions, and the ones which return `true` are used (along with the set of basic tautologies and the given theorem list) to rewrite the theorem. See `GEN_REWRITE_RULE` for more information on rewriting.

Failure

`FILTER_ASM_REWRITE_RULE` does not fail. Using `FILTER_ASM_REWRITE_RULE` may result in a diverging sequence of rewrites. In such cases `FILTER_ONCE_ASM_REWRITE_RULE` may be used.

Uses

This rule can be applied when rewriting with all assumptions results in divergence. Typically, the predicate can model checks as to whether a certain variable appears on the left-hand side of an equational assumption, or whether the assumption is in disjunctive form.

Another use is to improve performance when there are many assumptions which are not applicable. Rewriting, though a powerful method of proving theorems in HOL, can result in a reduced performance due to the pattern matching and the number of primitive inferences involved.

See also

Rewrite.ASM_REWRITE_RULE, Rewrite.FILTER_ONCE_ASM_REWRITE_RULE,
 Rewrite.FILTER_PURE_ASM_REWRITE_RULE, Rewrite.FILTER_PURE_ONCE_ASM_REWRITE_RULE,
 Rewrite.GEN_REWRITE_RULE, Rewrite.ONCE_REWRITE_RULE, Rewrite.PURE_REWRITE_RULE,
 Rewrite.REWRITE_RULE.

<div data-bbox="161 994 798 1046" data-label="Text"> <p><code>FILTER_ASM_REWRITE_TAC</code></p> </div>	<div data-bbox="1067 994 1329 1046" data-label="Text"> <p><code>(Rewrite)</code></p> </div>
--	---

```
FILTER_ASM_REWRITE_TAC : ((term -> bool) -> thm list -> tactic)
```

Synopsis

Rewrites a goal including built-in rewrites and some of the goal's assumptions.

Description

This function implements selective rewriting with a subset of the assumptions of the goal. The first argument (a predicate on terms) is applied to all assumptions, and the ones which return `true` are used (along with the set of basic tautologies and the given theorem list) to rewrite the goal. See `GEN_REWRITE_TAC` for more information on rewriting.

Failure

`FILTER_ASM_REWRITE_TAC` does not fail, but it can result in an invalid tactic if the rewrite is invalid. This happens when a theorem used for rewriting has assumptions which are not alpha-convertible to assumptions of the goal. Using `FILTER_ASM_REWRITE_TAC` may result in a diverging sequence of rewrites. In such cases `FILTER_ONCE_ASM_REWRITE_TAC` may be used.

Uses

This tactic can be applied when rewriting with all assumptions results in divergence, or in an unwanted proof state. Typically, the predicate can model checks as to whether a

certain variable appears on the left-hand side of an equational assumption, or whether the assumption is in disjunctive form. Thus it allows choice of assumptions to rewrite with in a position-independent fashion.

Another use is to improve performance when there are many assumptions which are not applicable. Rewriting, though a powerful method of proving theorems in HOL, can result in a reduced performance due to the pattern matching and the number of primitive inferences involved.

See also

Rewrite.ASM_REWRITE_TAC, Rewrite.FILTER_ONCE_ASM_REWRITE_TAC,
 Rewrite.FILTER_PURE_ASM_REWRITE_TAC, Rewrite.FILTER_PURE_ONCE_ASM_REWRITE_TAC,
 Rewrite.GEN_REWRITE_TAC, Rewrite.ONCE_REWRITE_TAC, Rewrite.PURE_REWRITE_TAC,
 Rewrite.REWRITE_TAC.

<div data-bbox="234 920 558 972" data-label="Text"> <h2 style="margin: 0;">FILTER_CONV</h2> </div>	<div data-bbox="1144 920 1410 972" data-label="Text"> (listLib) </div>
--	---

`FILTER_CONV : conv -> conv`

Synopsis

Computes by inference the result of applying a predicate to the elements of a list.

Description

`FILTER_CONV` takes a conversion `conv` and a term `tm` in the following form:

```
FILTER P [x0; ...xn]
```

It returns the theorem

```
|- FILTER P [x0; ...xn] = [...xi...]
```

where for every `xi` occurring in the right-hand side of the resulting theorem, `conv (--'P xi'--)` returns a theorem `|- P xi = T`.

Failure

`FILTER_CONV conv tm` fails if `tm` is not of the form described above.

Example

Evaluating

```
FILTER_CONV bool_EQ_CONV (--'FILTER ($= T) [T;F;T]'--);
```

returns the following theorem:

|- FILTER(\$= T) [T;F;T] = [T;T]

In general, if the predicate P is an explicit lambda abstraction ($\lambda x. P x$), the conversion should be in the form

(BETA_CONV THENC conv')

See also

listLib.FOLDL_CONV, listLib.FOLDR_CONV, listLib.list_FOLD_CONV.

FILTER_DISCH_TAC
(Tactic)

FILTER_DISCH_TAC : (term -> tactic)

Synopsis

Conditionally moves the antecedent of an implicative goal into the assumptions.

Description

FILTER_DISCH_TAC will move the antecedent of an implication into the assumptions, provided its parameter does not occur in the antecedent.

```

A ?- u ==> v
===== FILTER_DISCH_TAC w
A u {u} ?- v
    
```

Note that DISCH_TAC treats $\sim u$ as $u ==> F$. Unlike DISCH_TAC, the antecedent will be STRIPed into its various components before being ASSUMED. This stripping includes generating multiple goals for case-analysis of disjunctions. Also, unlike DISCH_TAC, should any component of the discharged antecedent directly imply or contradict the goal, then this simplification will also be made. Again, unlike DISCH_TAC, FILTER_DISCH_TAC will not duplicate identical or alpha-equivalent assumptions.

Failure

FILTER_DISCH_TAC will fail if a term which is identical, or alpha-equivalent to w occurs free in the antecedent, or if the theorem is not an implication or a negation.

Comments

FILTER_DISCH_TAC w behaves like FILTER_DISCH_THEN STRIP_ASSUME_TAC w.

See also

Thm.DISCH, Drule.DISCH_ALL, Tactic.DISCH_TAC, Thm_cont.DISCH_THEN,
 Thm_cont.FILTER_DISCH_THEN, Drule.NEG_DISCH, Tactic.STRIP_TAC, Drule.UNDISCH,
 Drule.UNDISCH_ALL, Tactic.UNDISCH_TAC.

FILTER_DISCH_THEN	(Thm_cont)
--------------------------	-------------------

`FILTER_DISCH_THEN : (thm_tactic -> term -> tactic)`

Synopsis

Conditionally gives to a theorem-tactic the antecedent of an implicative goal.

Description

If `FILTER_DISCH_THEN`'s second argument, a term, does not occur in the antecedent, then `FILTER_DISCH_THEN` removes the antecedent and then creates a theorem by `ASSUME`ing it. This new theorem is passed to `FILTER_DISCH_THEN`'s first argument, which is subsequently expanded. For example, if

```

A ?- t
===== f (ASSUME u)
B ?- v

```

then

```

A ?- u ==> t
===== FILTER_DISCH_THEN f
B ?- v

```

Note that `FILTER_DISCH_THEN` treats `~u` as `u ==> F`.

Failure

`FILTER_DISCH_THEN` will fail if a term which is identical, or alpha-equivalent to `w` occurs free in the antecedent. `FILTER_DISCH_THEN` will also fail if the theorem is an implication or a negation.

Comments

`FILTER_DISCH_THEN` is most easily understood by first understanding `DISCH_THEN`.

Uses

For preprocessing an antecedent before moving it to the assumptions, or for using antecedents and then throwing them away.

See also

Thm.DISCH, Drule.DISCH_ALL, Tactic.DISCH_TAC, Thm_cont.DISCH_THEN,
 Tactic.FILTER_DISCH_TAC, Drule.NEG_DISCH, Tactic.STRIP_TAC, Drule.UNDISCH,
 Drule.UNDISCH_ALL, Tactic.UNDISCH_TAC.

FILTER_GEN_TAC

(Tactic)

FILTER_GEN_TAC : (term -> tactic)

Synopsis

Strips off a universal quantifier, but fails for a given quantified variable.

Description

When applied to a term s and a goal $A \text{ ?- } !x. t$, the tactic `FILTER_GEN_TAC` fails if the quantified variable x is the same as s , but otherwise advances the goal in the same way as `GEN_TAC`, i.e. returns the goal $A \text{ ?- } t[x'/x]$ where x' is a variant of x chosen to avoid clashing with any variables free in the goal's assumption list. Normally x' is just x .

```

A ?- !x. t
===== FILTER_GEN_TAC "s"
A ?- t[x'/x]

```

Failure

Fails if the goal's conclusion is not universally quantified or the quantified variable is equal to the given term.

See also

Thm.GEN, Tactic.GEN_TAC, Thm.GENL, Drule.GEN_ALL, Thm.SPEC, Drule.SPECL,
 Drule.SPEC_ALL, Tactic.SPEC_TAC, Tactic.STRIP_TAC.

FILTER_ONCE_ASM_REWRITE_RULE

(Rewrite)

FILTER_ONCE_ASM_REWRITE_RULE : ((term -> bool) -> thm list -> thm -> thm)

Synopsis

Rewrites a theorem once including built-in rewrites and some of its assumptions.

Description

The first argument is a predicate applied to the assumptions. The theorem is rewritten with the assumptions for which the predicate returns `true`, the given list of theorems, and the tautologies stored in `basic_rewrites`. It searches the term of the theorem once, without applying rewrites recursively. Thus it avoids the divergence which can result from the application of `FILTER_ASM_REWRITE_RULE`. For more information on rewriting rules, see `GEN_REWRITE_RULE`.

Failure

Never fails.

Uses

This function is useful when rewriting with a subset of assumptions of a theorem, allowing control of the number of rewriting passes.

See also

`Rewrite.ASM_REWRITE_RULE`, `Rewrite.FILTER_ASM_REWRITE_RULE`,
`Rewrite.FILTER_PURE_ASM_REWRITE_RULE`, `Rewrite.FILTER_PURE_ONCE_ASM_REWRITE_RULE`,
`Rewrite.GEN_REWRITE_RULE`, `Rewrite.ONCE_ASM_REWRITE_RULE`, `Conv.ONCE_DEPTH_CONV`,
`Rewrite.PURE_ASM_REWRITE_RULE`, `Rewrite.PURE_ONCE_ASM_REWRITE_RULE`,
`Rewrite.PURE_REWRITE_RULE`, `Rewrite.REWRITE_RULE`.

<code>FILTER_ONCE_ASM_REWRITE_TAC</code> <code>(Rewrite)</code>

```
FILTER_ONCE_ASM_REWRITE_TAC : ((term -> bool) -> thm list -> tactic)
```

Synopsis

Rewrites a goal once including built-in rewrites and some of its assumptions.

Description

The first argument is a predicate applied to the assumptions. The goal is rewritten with the assumptions for which the predicate returns `true`, the given list of theorems, and the tautologies stored in `basic_rewrites`. It searches the term of the goal once, without applying rewrites recursively. Thus it avoids the divergence which can result from the application of `FILTER_ASM_REWRITE_TAC`. For more information on rewriting tactics, see `GEN_REWRITE_TAC`.

Failure

Never fails.

Uses

This function is useful when rewriting with a subset of assumptions of a goal, allowing control of the number of rewriting passes.

See also

Rewrite.ASM_REWRITE_TAC, Rewrite.FILTER_ASM_REWRITE_TAC,
 Rewrite.FILTER_PURE_ASM_REWRITE_TAC, Rewrite.FILTER_PURE_ONCE_ASM_REWRITE_TAC,
 Rewrite.GEN_REWRITE_TAC, Rewrite.ONCE_ASM_REWRITE_TAC, Conv.ONCE_DEPTH_CONV,
 Rewrite.PURE_ASM_REWRITE_TAC, Rewrite.PURE_ONCE_ASM_REWRITE_TAC,
 Rewrite.PURE_REWRITE_TAC, Rewrite.REWRITE_TAC.

FILTER_PGEN_TAC

(PairRules)

FILTER_PGEN_TAC : (term -> tactic)

Synopsis

Strips off a paired universal quantifier, but fails for a given quantified pair.

Description

When applied to a term q and a goal $A \text{ ?- } !p. t$, the tactic FILTER_PGEN_TAC fails if the quantified pair p is the same as p , but otherwise advances the goal in the same way as PGEN_TAC, i.e. returns the goal $A \text{ ?- } t[p'/p]$ where p' is a variant of p chosen to avoid clashing with any variables free in the goal's assumption list. Normally p' is just p .

```

  A ?- !p. t
  =====
  FILTER_PGEN_TAC "q"
  A ?- t[p'/p]

```

Failure

Fails if the goal's conclusion is not a paired universal quantifier or the quantified pair is equal to the given term.

See also

Tactic.FILTER_GEN_TAC, PairRules.PGEN, PairRules.PGEN_TAC, PairRules.PGENL,
 PairRules.PSPEC, PairRules.PSPECL, PairRules.PSPEC_ALL, PairRules.PSPEC_TAC,
 PairRules.PSTRIP_TAC.

FILTER_PSTRIP_TAC

(PairRules)

FILTER_PSTRIP_TAC : (term -> tactic)

Synopsis

Conditionally strips apart a goal by eliminating the outermost connective.

Description

Stripping apart a goal in a more careful way than is done by `PSTRIP_TAC` may be necessary when dealing with quantified terms and implications. `FILTER_PSTRIP_TAC` behaves like `PSTRIP_TAC`, but it does not strip apart a goal if it contains a given term.

If u is a term, then `FILTER_PSTRIP_TAC u` is a tactic that removes one outermost occurrence of one of the connectives `!`, `==>`, `~` or `/\` from the conclusion of the goal t , provided the term being stripped does not contain u . `FILTER_PSTRIP_TAC` will strip paired universal quantifications. A negation $\sim t$ is treated as the implication $t ==> F$. `FILTER_PSTRIP_TAC` also breaks apart conjunctions without applying any filtering.

If t is a universally quantified term, `FILTER_PSTRIP_TAC u` strips off the quantifier:

$$\begin{array}{l} A \text{ ?- } !p. v \\ \hline \text{===== } \text{FILTER_PSTRIP_TAC "u"} \quad \text{[where } p \text{ is not } u\text{]} \\ A \text{ ?- } v[p'/p] \end{array}$$

where p' is a primed variant of the pair p that does not contain any variables that appear free in the assumptions A . If t is a conjunction, no filtering is done and `FILTER_PSTRIP_TAC` simply splits the conjunction:

$$\begin{array}{l} A \text{ ?- } v /\ w \\ \hline \text{===== } \text{FILTER_PSTRIP_TAC "u"} \\ A \text{ ?- } v \quad A \text{ ?- } w \end{array}$$

If t is an implication and the antecedent does not contain a free instance of u , then `FILTER_PSTRIP_TAC u` moves the antecedent into the assumptions and recursively splits the antecedent according to the following rules (see `PSTRIP_ASSUME_TAC`):

$$\begin{array}{l} A \text{ ?- } v_1 /\ \dots /\ v_n ==> v \\ \hline \text{=====} \\ A \text{ } u \{v_1, \dots, v_n\} \text{ ?- } v \end{array} \qquad \begin{array}{l} A \text{ ?- } v_1 \ \backslash / \ \dots \ \backslash / \ v_n ==> v \\ \hline \text{=====} \\ A \text{ } u \{v_1\} \text{ ?- } v \ \dots \ A \text{ } u \{v_n\} \text{ ?- } v \end{array}$$

$$\begin{array}{l} A \text{ ?- } (?p. w) ==> v \\ \hline \text{=====} \\ A \text{ } u \{w[p'/p]\} \text{ ?- } v \end{array}$$

where p' is a variant of the pair p .

Failure

`FILTER_PSTRIP_TAC u (A, t)` fails if t is not a universally quantified term, an implication, a negation or a conjunction; or if the term being stripped contains u in the sense described above (conjunction excluded).

Uses

`FILTER_PSTRIP_TAC` is used when stripping outer connectives from a goal in a more delicate way than `PSTRIP_TAC`. A typical application is to keep stripping by using the tactic `REPEAT (FILTER_PSTRIP_TAC u)` until one hits the term `u` at which stripping is to stop.

See also

`PairRules.PGEN_TAC`, `PairRules.PSTRIP_GOAL_THEN`, `PairRules.FILTER_PSTRIP_THEN`, `PairRules.PSTRIP_TAC`, `Tactic.FILTER_STRIP_TAC`.

FILTER_PSTRIP_THEN

(PairRules)

`FILTER_PSTRIP_THEN` : (thm_tactic -> term -> tactic)

Synopsis

Conditionally strips a goal, handing an antecedent to the theorem-tactic.

Description

Given a theorem-tactic `ttac`, a term `u` and a goal (A, t) , `FILTER_STRIP_THEN ttac u` removes one outer connective (`!`, `==>`, or `~`) from `t`, if the term being stripped does not contain a free instance of `u`. Note that `FILTER_PSTRIP_THEN` will strip paired universal quantifiers. A negation `~t` is treated as the implication `t ==> F`. The theorem-tactic `ttac` is applied only when stripping an implication, by using the antecedent stripped off. `FILTER_PSTRIP_THEN` also breaks conjunctions.

`FILTER_PSTRIP_THEN` behaves like `PSTRIP_GOAL_THEN`, if the term being stripped does not contain a free instance of `u`. In particular, `FILTER_PSTRIP_THEN PSTRIP_ASSUME_TAC` behaves like `FILTER_PSTRIP_TAC`.

Failure

`FILTER_PSTRIP_THEN ttac u (A, t)` fails if `t` is not a paired universally quantified term, an implication, a negation or a conjunction; or if the term being stripped contains the term `u` (conjunction excluded); or if the application of `ttac` fails, after stripping the goal.

Uses

`FILTER_PSTRIP_THEN` is used to manipulate intermediate results using theorem-tactics, after stripping outer connectives from a goal in a more delicate way than `PSTRIP_GOAL_THEN`.

See also

`PairRules.PGEN_TAC`, `PairRules.PSTRIP_GOAL_THEN`, `Thm.cont.FILTER_STRIP_THEN`, `PairRules.PSTRIP_TAC`, `PairRules.FILTER_PSTRIP_TAC`.

<code>FILTER_PURE_ASM_REWRITE_RULE</code>	<code>(Rewrite)</code>
---	------------------------

```
FILTER_PURE_ASM_REWRITE_RULE : ((term -> bool) -> thm list -> thm ->thm)
```

Synopsis

Rewrites a theorem with some of the theorem's assumptions.

Description

This function implements selective rewriting with a subset of the assumptions of the theorem. The first argument (a predicate on terms) is applied to all assumptions, and the ones which return `true` are used to rewrite the goal. See `GEN_REWRITE_RULE` for more information on rewriting.

Failure

`FILTER_PURE_ASM_REWRITE_RULE` does not fail. Using `FILTER_PURE_ASM_REWRITE_RULE` may result in a diverging sequence of rewrites. In such cases `FILTER_PURE_ONCE_ASM_REWRITE_RULE` may be used.

Uses

This rule can be applied when rewriting with all assumptions results in divergence. Typically, the predicate can model checks as to whether a certain variable appears on the left-hand side of an equational assumption, or whether the assumption is in disjunctive form.

Another use is to improve performance when there are many assumptions which are not applicable. Rewriting, though a powerful method of proving theorems in HOL, can result in a reduced performance due to the pattern matching and the number of primitive inferences involved.

See also

`Rewrite.ASM_REWRITE_RULE`, `Rewrite.FILTER_ASM_REWRITE_RULE`,
`Rewrite.FILTER_ONCE_ASM_REWRITE_RULE`, `Rewrite.FILTER_PURE_ONCE_ASM_REWRITE_RULE`,
`Rewrite.GEN_REWRITE_RULE`, `Rewrite.ONCE_REWRITE_RULE`, `Rewrite.PURE_REWRITE_RULE`,
`Rewrite.REWRITE_RULE`.

<code>FILTER_PURE_ASM_REWRITE_TAC</code>	<code>(Rewrite)</code>
--	------------------------

```
FILTER_PURE_ASM_REWRITE_TAC : ((term -> bool) -> thm list -> tactic)
```

Synopsis

Rewrites a goal with some of the goal's assumptions.

Description

This function implements selective rewriting with a subset of the assumptions of the goal. The first argument (a predicate on terms) is applied to all assumptions, and the ones which return `true` are used to rewrite the goal. See `GEN_REWRITE_TAC` for more information on rewriting.

Failure

`FILTER_PURE_ASM_REWRITE_TAC` does not fail, but it can result in an invalid tactic if the rewrite is invalid. This happens when a theorem used for rewriting has assumptions which are not alpha-convertible to assumptions of the goal. Using `FILTER_PURE_ASM_REWRITE_TAC` may result in a diverging sequence of rewrites. In such cases `FILTER_PURE_ONCE_ASM_REWRITE_TAC` may be used.

Uses

This tactic can be applied when rewriting with all assumptions results in divergence, or in an unwanted proof state. Typically, the predicate can model checks as to whether a certain variable appears on the left-hand side of an equational assumption, or whether the assumption is in disjunctive form. Thus it allows choice of assumptions to rewrite with in a position-independent fashion.

Another use is to improve performance when there are many assumptions which are not applicable. Rewriting, though a powerful method of proving theorems in HOL, can result in a reduced performance due to the pattern matching and the number of primitive inferences involved.

See also

`Rewrite.ASM_REWRITE_TAC`, `Rewrite.FILTER_ASM_REWRITE_TAC`,
`Rewrite.FILTER_ONCE_ASM_REWRITE_TAC`, `Rewrite.FILTER_PURE_ONCE_ASM_REWRITE_TAC`,
`Rewrite.GEN_REWRITE_TAC`, `Rewrite.ONCE_REWRITE_TAC`, `Rewrite.PURE_REWRITE_TAC`,
`Rewrite.REWRITE_TAC`.

FILTER_PURE_ONCE_ASM_REWRITE_RULE
 (Rewrite)

`FILTER_PURE_ONCE_ASM_REWRITE_RULE` : ((term -> bool) -> thm list -> thm -> thm)

Synopsis

Rewrites a theorem once using some of its assumptions.

Description

The first argument is a predicate applied to the assumptions. The theorem is rewritten with the assumptions for which the predicate returns `true` and the given list of theorems. It searches the term of the theorem once, without applying rewrites recursively. Thus it avoids the divergence which can result from the application of `FILTER_PURE_ASM_REWRITE_RULE`. For more information on rewriting rules, see `GEN_REWRITE_RULE`.

Failure

Never fails.

Uses

This function is useful when rewriting with a subset of assumptions of a theorem, allowing control of the number of rewriting passes.

See also

`Rewrite.ASM_REWRITE_RULE`, `Rewrite.FILTER_ASM_REWRITE_RULE`,
`Rewrite.FILTER_ONCE_ASM_REWRITE_RULE`, `Rewrite.FILTER_PURE_ASM_REWRITE_RULE`,
`Rewrite.GEN_REWRITE_RULE`, `Rewrite.ONCE_ASM_REWRITE_RULE`, `Conv.ONCE_DEPTH_CONV`,
`Rewrite.PURE_ASM_REWRITE_RULE`, `Rewrite.PURE_ONCE_ASM_REWRITE_RULE`,
`Rewrite.PURE_REWRITE_RULE`, `Rewrite.REWRITE_RULE`.

`FILTER_PURE_ONCE_ASM_REWRITE_TAC (Rewrite)`

```
FILTER_PURE_ONCE_ASM_REWRITE_TAC : ((term -> bool) -> thm list -> tactic)
```

Synopsis

Rewrites a goal once using some of its assumptions.

Description

The first argument is a predicate applied to the assumptions. The goal is rewritten with the assumptions for which the predicate returns `true` and the given list of theorems. It searches the term of the goal once, without applying rewrites recursively. Thus it avoids the divergence which can result from the application of `FILTER_PURE_ASM_REWRITE_TAC`. For more information on rewriting tactics, see `GEN_REWRITE_TAC`.

Failure

Never fails.

Uses

This function is useful when rewriting with a subset of assumptions of a goal, allowing control of the number of rewriting passes.

See also

Rewrite.ASM_REWRITE_TAC, Rewrite.FILTER_ASM_REWRITE_TAC,
 Rewrite.FILTER_ONCE_ASM_REWRITE_TAC, Rewrite.FILTER_PURE_ASM_REWRITE_TAC,
 Rewrite.GEN_REWRITE_TAC, Rewrite.ONCE_ASM_REWRITE_TAC, Conv.ONCE_DEPTH_CONV,
 Rewrite.PURE_ASM_REWRITE_TAC, Rewrite.PURE_ONCE_ASM_REWRITE_TAC,
 Rewrite.PURE_REWRITE_TAC, Rewrite.REWRITE_TAC.

FILTER_STRIP_TAC
(Tactic)

FILTER_STRIP_TAC : (term -> tactic)

Synopsis

Conditionally strips apart a goal by eliminating the outermost connective.

Description

Stripping apart a goal in a more careful way than is done by STRIP_TAC may be necessary when dealing with quantified terms and implications. FILTER_STRIP_TAC behaves like STRIP_TAC, but it does not strip apart a goal if it contains a given term.

If *u* is a term, then FILTER_STRIP_TAC *u* is a tactic that removes one outermost occurrence of one of the connectives **!**, **==>**, **~** or **/** from the conclusion of the goal *t*, provided the term being stripped does not contain *u*. A negation **~t** is treated as the implication *t* ==> F. FILTER_STRIP_TAC *u* also breaks apart conjunctions without applying any filtering.

If *t* is a universally quantified term, FILTER_STRIP_TAC *u* strips off the quantifier:

$$\begin{array}{l}
 A \text{ ?- } !x.v \\
 \text{===== FILTER_STRIP_TAC "u" [where x is not u]} \\
 A \text{ ?- } v[x'/x]
 \end{array}$$

where *x'* is a primed variant that does not appear free in the assumptions *A*. If *t* is a conjunction, no filtering is done and FILTER_STRIP_TAC *u* simply splits the conjunction:

$$\begin{array}{l}
 A \text{ ?- } v /\ w \\
 \text{===== FILTER_STRIP_TAC "u"} \\
 A \text{ ?- } v \quad A \text{ ?- } w
 \end{array}$$

If t is an implication and the antecedent does not contain a free instance of u , then `FILTER_STRIP_TAC u` moves the antecedent into the assumptions and recursively splits the antecedent according to the following rules (see `STRIP_ASSUME_TAC`):

$$\frac{A \text{ ?- } v_1 \wedge \dots \wedge v_n \implies v}{A \text{ u } \{v_1, \dots, v_n\} \text{ ?- } v}$$

$$\frac{A \text{ ?- } v_1 \vee \dots \vee v_n \implies v}{A \text{ u } \{v_1\} \text{ ?- } v \dots A \text{ u } \{v_n\} \text{ ?- } v}$$

$$\frac{A \text{ ?- } ?x.w \implies v}{A \text{ u } \{w[x'/x]\} \text{ ?- } v}$$

where x' is a variant of x .

Failure

`FILTER_STRIP_TAC u (A, t)` fails if t is not a universally quantified term, an implication, a negation or a conjunction; or if the term being stripped contains u in the sense described above (conjunction excluded).

Example

When trying to solve the goal

```
?- !n. m <= n /\ n <= m ==> (m = n)
```

the universally quantified variable n can be stripped off by using

```
FILTER_STRIP_TAC "m:num"
```

and then the implication can be stripped apart by using

```
FILTER_STRIP_TAC "m:num = n"
```

Uses

`FILTER_STRIP_TAC` is used when stripping outer connectives from a goal in a more delicate way than `STRIP_TAC`. A typical application is to keep stripping by using the tactic `REPEAT (FILTER_STRIP_TAC u)` until one hits the term u at which stripping is to stop.

See also

`Tactic.CONJ_TAC`, `Tactic.FILTER_DISCH_TAC`, `Thm_cont.FILTER_DISCH_THEN`,
`Tactic.FILTER_GEN_TAC`, `Tactic.STRIP_ASSUME_TAC`, `Tactic.STRIP_TAC`.

<code>FILTER_STRIP_THEN</code>	<code>(Thm_cont)</code>
--------------------------------	-------------------------

```
FILTER_STRIP_THEN : (thm_tactic -> term -> tactic)
```

Synopsis

Conditionally strips a goal, handing an antecedent to the theorem-tactic.

Description

Given a theorem-tactic `ttac`, a term `u` and a goal (A, t) , `FILTER_STRIP_THEN ttac u` removes one outer connective (`!`, `==>`, or `~`) from `t`, if the term being stripped does not contain a free instance of `u`. A negation `~t` is treated as the implication `t ==> F`. The theorem-tactic `ttac` is applied only when stripping an implication, by using the antecedent stripped off. `FILTER_STRIP_THEN` also breaks conjunctions.

`FILTER_STRIP_THEN` behaves like `STRIP_GOAL_THEN`, if the term being stripped does not contain a free instance of `u`. In particular, `FILTER_STRIP_THEN STRIP_ASSUME_TAC` behaves like `FILTER_STRIP_TAC`.

Failure

`FILTER_STRIP_THEN ttac u (A, t)` fails if `t` is not a universally quantified term, an implication, a negation or a conjunction; or if the term being stripped contains the term `u` (conjunction excluded); or if the application of `ttac` fails, after stripping the goal.

Example

When solving the goal

```
?- (n = 1) ==> (n * n = n)
```

the application of `FILTER_STRIP_THEN SUBST1_TAC "m:num"` results in the goal

```
?- 1 * 1 = 1
```

Uses

`FILTER_STRIP_THEN` is used when manipulating intermediate results using theorem-tactics, after stripping outer connectives from a goal in a more delicate way than `STRIP_GOAL_THEN`.

See also

`Tactic.CONJ_TAC`, `Tactic.FILTER_DISCH_TAC`, `Thm.cont.FILTER_DISCH.THEN`, `Tactic.FILTER_GEN_TAC`, `Tactic.FILTER_STRIP_TAC`, `Tactic.STRIP_ASSUME_TAC`, `Tactic.STRIP_GOAL_THEN`.

<div data-bbox="159 1816 285 1868" data-label="Text"> <p>find</p> </div>	<div data-bbox="1212 1816 1329 1870" data-label="Text"> <p>(DB)</p> </div>
--	--

`find : string -> data list`

Synopsis

Search for theory element by name fragment.

Description

An invocation `DB.find s` returns a list of theory elements which have been stored with a name in which `s` occurs as a proper substring, ignoring case distinctions. All currently loaded theory segments are searched.

Failure

Never fails. If nothing suitable can be found, the empty list is returned.

Example

```

- DB.find "inc";
> val it =
  [(("arithmetic", "MULT_INCREASES"),
    (|- !m n. 1 < m /\ 0 < n ==> SUC n <= m * n, Thm)),
   (("bool", "BOOL_EQ_DISTINCT"), (|- ~(T = F) /\ ~(F = T), Thm)),
   (("list", "list_distinct"), (|- !a1 a0. ~([ ] = a0::a1), Thm)),
   (("sum", "sum_distinct"), (|- !x y. ~(INL x = INR y), Thm)),
   (("sum", "sum_distinct1"), (|- !x y. ~(INR y = INL x), Thm))]
: ((string * string) * (thm * class)) list

```

Uses

Finding theorems in interactive proof sessions.

See also

`DB.match`, `DB.apropos`, `DB.thy`, `DB.theorems`.

`find_term`

(HolKernel)

```
find_term : (term -> bool) -> term -> term
```

Synopsis

Finds a sub-term satisfying a predicate.

Description

A call to `find_term P t` returns a sub-term of `t` that satisfies the predicate `P` if there is one. Otherwise it raises a `HOL_ERR` exception. The search is done in a top-down, left-to-right order (i.e., rators of combs are examined before rands).

Failure

Fails if the predicate fails when applied to any of the sub-terms of the term argument. Also fails if there is no sub-term satisfying the predicate.

Example

```
- find_term Literal.is_numeral '2 + x + 3';
> val it = '2' : term

- find_term Literal.is_numeral 'x + y';
Exception HOL_ERR {...}
```

See also

HolKernel.bvk_find_term, HolKernel.find_terms.

<div data-bbox="161 965 453 1014" data-label="Text"><code>find_terms</code></div>	<div data-bbox="1011 965 1331 1014" data-label="Text"><code>(HolKernel)</code></div>
---	--

```
find_terms : (term -> bool) -> term -> term list
```

Synopsis

Traverses a term, returning a list of sub-terms satisfying a predicate.

Description

A call to `find_terms P t` returns a list of sub-terms of `t` that satisfy `P`. The resulting list is ordered as if the traversal had been bottom-up and right-to-left (i.e., the rands of combs visited before their rators). The term `t` is itself considered a possible sub-term of `t`.

Failure

Only fails if the predicate fails on one of the term's sub-terms.

Example

```
- find_terms (fn _ => true) 'x + y';
> val it = ['y', 'x', '$+', '$+ x', 'x + y']

- find_terms Literal.is_numeral 'x + y';
> val it = [] : term list

- find_terms Literal.is_numeral '1 + x + 2 + y';
> val it = ['2', '1'] : term list
```

See also

HolKernel.bvk_find_term, HolKernel.find_term.

FINITE_CONV	(pred_setLib)
-------------	---------------

FINITE_CONV : conv

Synopsis

Proves finiteness of sets of the form $\{t_1; \dots; t_n\}$.

Description

The conversion FINITE_CONV expects its term argument to be an assertion of the form FINITE $\{t_1; \dots; t_n\}$. Given such a term, the conversion returns the theorem

$$\vdash \text{FINITE } \{t_1; \dots; t_n\} = T$$
Example

```
- FINITE_CONV ‘FINITE {1;2;3}‘;
> val it =  $\vdash \text{FINITE}\{1;2;3\} = T$  : thm

- FINITE_CONV ‘FINITE ({}:num->bool)‘;
> val it =  $\vdash \text{FINITE } \{\} = T$  : thm
```

Failure

Fails if applied to a term not of the form FINITE $\{t_1; \dots; t_n\}$.

first	(Lib)
-------	-------

first : ('a -> bool) -> 'a list -> 'a

Synopsis

Return first element in list that predicate holds of.

Description

An invocation `first P [x1,...,xk,...xn]` returns `xk` if `P xk` returns `true` and `P xi` ($1 \leq i < k$) equals `false`.

Failure

If `P xi` is `false` for every element in `list`, then `first P list` raises an exception. When searching for an element of `list` that `P` holds of, it may happen that an application of `P` to an element of `list` raises an exception `e`. In that case, `first P list` also raises `e`.

Example

```
- first (fn i => i mod 2 = 0) [1,3,4,5];
> val it = 4 : int
```

```
- first (fn i => i mod 2 = 0) [1,3,5,7];
! Uncaught exception:
! HOL_ERR
```

```
- first (fn _ => raise Fail "") [1];
! Uncaught exception:
! Fail ""
```

See also

`Lib.exists`, `Lib.tryfind`, `Lib.all`.

<div data-bbox="159 1417 314 1467" data-label="Text"> <p>FIRST</p> </div>	<div data-bbox="1038 1415 1331 1467" data-label="Text"> <p>(Tactical)</p> </div>
--	---

`FIRST : (tactic list -> tactic)`

Synopsis

Applies the first tactic in a tactic list which succeeds.

Description

When applied to a list of tactics `[T1;...;Tn]`, and a goal `g`, the tactical `FIRST` tries applying the tactics to the goal until one succeeds. If the first tactic which succeeds is `Tm`, then the effect is the same as just `Tm`. Thus `FIRST` effectively behaves as follows:

$$\text{FIRST } [T1; \dots; Tn] = T1 \text{ ORELSE } \dots \text{ ORELSE } Tn$$

Failure

The application of `FIRST` to a tactic list never fails. The resulting tactic fails iff all the component tactics do when applied to the goal, or if the tactic list is empty.

See also

`Tactical.EVERY`, `Tactical.ORELSE`.

FIRST_ASSUM

(Tactical)

```
FIRST_ASSUM : (thm_tactic -> tactic)
```

Synopsis

Maps a theorem-tactic over the assumptions, applying first successful tactic.

Description

The tactic

```
FIRST_ASSUM ttac ([A1; ...; An], g)
```

has the effect of applying the first tactic which can be produced by `ttac` from the `ASSUMED` assumptions $(A1 \mid - A1)$, ..., $(An \mid - An)$ and which succeeds when applied to the goal. Failures of `ttac` to produce a tactic are ignored.

Failure

Fails if `ttac (Ai \mid - Ai)` fails for every assumption A_i , or if the assumption list is empty, or if all the tactics produced by `ttac` fail when applied to the goal.

Example

The tactic

```
FIRST_ASSUM (\asm. CONTR_TAC asm ORELSE ACCEPT_TAC asm)
```

searches the assumptions for either a contradiction or the desired conclusion. The tactic

```
FIRST_ASSUM MATCH_MP_TAC
```

searches the assumption list for an implication whose conclusion matches the goal, reducing the goal to the antecedent of the corresponding instance of this implication.

See also

`Tactical.ASSUM_LIST`, `Tactical.EVERY`, `Tactical.EVERY_ASSUM`, `Tactical.FIRST`, `Tactical.MAP EVERY`, `Tactical.MAP_FIRST`.

FIRST_CONSEQ_CONV

(ConseqConv)

FIRST_CONSEQ_CONV : (conseq_conv list -> conseq_conv)

Synopsis

Apply the first of the conversions in a given list that succeeds.

See also

ConseqConv.ORELSE_CONSEQ_CONV, Conv.FIRST_CONV.

FIRST_CONV

(Conv)

FIRST_CONV : (conv list -> conv)

Synopsis

Apply the first of the conversions in a given list that succeeds.

Description

FIRST_CONV [c1;...;cn] "t" returns the result of applying to the term "t" the first conversion c_i that succeeds when applied to "t". The conversions are tried in the order in which they are given in the list.

Failure

FIRST_CONV [c1;...;cn] "t" fails if all the conversions c_1, \dots, c_n fail when applied to the term "t". FIRST_CONV cs "t" also fails if cs is the empty list.

See also

Conv.ORELSEC.

FIRST_PROVE

(Tactical)

FIRST_PROVE : (tactic list -> tactic)

Synopsis

Applies the first tactic in a tactic list which completely proves the goal.

Description

When applied to a list of tactics $[T_1; \dots; T_n]$, and a goal g , the tactical `FIRST_PROVE` tries applying the tactics to the goal until one proves the goal. If the first tactic which proves the goal is T_m , then the effect is the same as just T_m . Thus `FIRST_PROVE` effectively behaves as follows:

$$\text{FIRST_PROVE } [T_1; \dots; T_n] = (T_1 \text{ THEN NO_TAC}) \text{ ORELSE } \dots \text{ ORELSE } (T_n \text{ THEN NO_TAC})$$
Failure

The application of `FIRST_PROVE` to a tactic list never fails. The resulting tactic fails iff none of the supplied tactics completely proves the goal by itself, or if the tactic list is empty.

See also

`Tactical.EVERY`, `Tactical.ORELSE`, `Tactical.FIRST`.

<div data-bbox="234 1140 502 1191" data-label="Text"> <p><code>FIRST_TCL</code></p> </div>	<div data-bbox="1114 1140 1410 1191" data-label="Text"> <p><code>(Thm_cont)</code></p> </div>
--	---

`FIRST_TCL` : (thm_tactical list -> thm_tactical)

Synopsis

Applies the first theorem-tactical in a list which succeeds.

Description

When applied to a list of theorem-tacticals, a theorem-tactic and a theorem, `FIRST_TCL` returns the tactic resulting from the application of the first theorem-tactical to the theorem-tactic and theorem which succeeds. The effect is the same as:

$$\text{FIRST_TCL } [tt1; \dots; tt1n] = tt1 \text{ ORELSE_TCL } \dots \text{ ORELSE_TCL } tt1n$$
Failure

`FIRST_TCL` fails iff each tactic in the list fails when applied to the theorem-tactic and theorem. This is trivially the case if the list is empty.

See also

`Thm_cont.EVERY_TCL`, `Thm_cont.ORELSE_TCL`, `Thm_cont.REPEAT_TCL`, `Thm_cont.THEN_TCL`.

FIRST_X_ASSUM

(Tactical)

```
Tactical.FIRST_X_ASSUM : thm_tactic -> tactic
```

Synopsis

Maps a theorem-tactic over the assumptions, applying first successful tactic and removing the assumption that gave rise to the successful tactic.

Description

The tactic

```
FIRST_X_ASSUM ttac ([A1; ...; An], g)
```

has the effect of applying the first tactic which can be produced by `ttac` from the ASSUMED assumptions $(A_1 \vdash A_1), \dots, (A_n \vdash A_n)$ and which succeeds when applied to the goal. The assumption which produced the successful theorem-tactic is removed from the assumption list (before `ttac` is applied). Failures of `ttac` to produce a tactic are ignored.

Failure

Fails if `ttac (Ai ⊢ Ai)` fails for every assumption A_i , or if the assumption list is empty, or if all the tactics produced by `ttac` fail when applied to the goal.

Example

The tactic

```
FIRST_X_ASSUM SUBST_ALL_TAC
```

searches the assumptions for an equality and causes its right hand side to be substituted for its left hand side throughout the goal and assumptions. It also removes the equality from the assumption list. Using `FIRST_ASSUM` above would leave an equality on the assumption list of the form $x = x$. The tactic

```
FIRST_X_ASSUM MATCH_MP_TAC
```

searches the assumption list for an implication whose conclusion matches the goal, reducing the goal to the antecedent of the corresponding instance of this implication and removing the implication from the assumption list.

Comments

The “X” in the name of this tactic is a mnemonic for the “crossing out” or removal of the assumption found.

See also

Tactical.ASSUM_LIST, Tactical.EVERY, Tactical.PAT_ASSUM, Tactical.EVERY_ASSUM, Tactical.FIRST, Tactical.MAP EVERY, Tactical.MAP_FIRST, Thm_cont.UNDISCH_THEN.

FIRSTN_CONV	(listLib)
-------------	-----------

FIRSTN_CONV : conv

Synopsis

Computes by inference the result of taking the initial n elements of a list.

Description

For any object language list of the form $--'[x_0; \dots x_{(n-k)}; \dots; x_{(n-1)}]'$, the result of evaluating

$$\text{FIRSTN_CONV } (--'\text{FIRSTN } k [x_0; \dots x_{(n-k)}; \dots; x_{(n-1)}]'$$

is the theorem

$$|- \text{FIRSTN } k [x_0; \dots; x_{(n-k)}; \dots; x_{(n-1)}] = [x_0; \dots; x_{(n-k)}]$$
Failure

FIRSTN_CONV t_m fails if t_m is not of the form described above, or k is greater than the length of the list.

FLAT_CONV	(listLib)
-----------	-----------

FLAT_CONV : conv

Synopsis

Computes by inference the result of flattening a list of lists.

Description

FLAT_CONV takes a term t_m in the following form:

$$\text{FLAT } [[x_{00}; \dots x_{0n}]; \dots; [x_{m0}; \dots x_{mn}]]$$

It returns the theorem

```
|- FLAT [[x00;...x0n];...;[xm0;...xmn]] = [x00;...x0n;...;xm0;...xmn]
```

Failure

FLAT_CONV tm fails if tm is not of the form described above.

Example

Evaluating

```
FLAT_CONV (--'FLAT [[0;2;4];[0;1;2;3;4]]'--);
```

returns the following theorem:

```
|- FLAT[[0;2;4];[0;1;2;3;4]] = [0;2;4;0;1;2;3;4]
```

See also

listLib.FOLDL_CONV, listLib.FOLDR_CONV, listLib.list_FOLD_CONV.

<div data-bbox="161 1144 370 1193" data-label="Text"> <h1 style="font-size: 2em; margin: 0;">flatten</h1> </div>	<div data-bbox="1182 1144 1331 1196" data-label="Text"> (Lib) </div>
--	---

```
flatten : 'a list list -> 'a list
```

Synopsis

Removes one level of bracketing from a list.

Description

An invocation `flatten [[x11,...,x1k1],...,[xn1,...,xnkn]]` yields the list `[x1,...,x1k1,...,xn1,...,xnkn]`.

Failure

Never fails.

Example

```
- flatten [[1,2,3],[],[4,5]];
> val it = [1, 2, 3, 4, 5] : int list

- flatten ([[[]]] : int list list list);
> val it = [[]] : int list list
```

FLATTEN_CONJ_CONV

(unwindLib)

FLATTEN_CONJ_CONV : conv

Synopsis

Flattens a ‘tree’ of conjunctions.

Description

FLATTEN_CONJ_CONV "t1 /\ ... /\ tn" returns a theorem of the form:

$$\vdash t1 \wedge \dots \wedge tn = u1 \wedge \dots \wedge un$$

where the right-hand side of the equation is a flattened version of the left-hand side.

Failure

Never fails.

Example

```
#FLATTEN_CONJ_CONV "(a /\ (b /\ c)) /\ ((d /\ e) /\ f)";;
|- (a /\ b /\ c) /\ (d /\ e) /\ f = a /\ b /\ c /\ d /\ e /\ f
```

FOLDL_CONV

(listLib)

FOLDL_CONV : conv -> conv

Synopsis

Computes by inference the result of applying a function to the elements of a list.

Description

FOLDL_CONV takes a conversion conv and a term tm in the following form:

$$\text{FOLDL } f \ e \ [x_0; \dots; x_n]$$

It returns the theorem

$$\vdash \text{FOLDL } f \ e \ [x_0; \dots; x_n] = tm'$$

where tm' is the result of applying the function f iteratively to the successive elements of the list and the result of the previous application starting from the tail end of the list. During each iteration, an expression $f\ e_i\ x_i$ is evaluated. The user supplied conversion $conv$ is used to derive a theorem

$$\vdash f\ e_i\ x_i = e(i+1)$$

which is used in the next iteration.

Failure

FOLDL_CONV $conv\ tm$ fails if tm is not of the form described above.

Example

To sum the elements of a list, one can use FOLDL_CONV with ADD_CONV from the library `num_lib`.

```
- load_library_in_place num_lib;
- FOLDL_CONV Num_lib.ADD_CONV (--'FOLDL $+ 0 [0;1;2;3]'--);
|- FOLDL $+ 0 [0;1;2;3] = 6
```

In general, if the function f is an explicit lambda abstraction $(\lambda x\ x'.\ t[x,x'])$, the conversion should be in the form

```
((RATOR_CONV BETA_CONV) THENC BETA_CONV THENC conv')
```

where $conv'$ applied to $t[x,x']$ returns the theorem

$$\vdash t[x,x'] = e''.$$

See also

`listLib.FOLDR_CONV`, `listLib.list_FOLD_CONV`.

FOLDR_CONV

(listLib)

FOLDR_CONV : conv -> conv

Synopsis

Computes by inference the result of applying a function to the elements of a list.

Description

FOLDR_CONV takes a conversion $conv$ and a term tm in the following form:

```
FOLDR f e [x0;...xn]
```

It returns the theorem

```
|- FOLDR f e [x0;...xn] = tm'
```

where tm' is the result of applying the function f iteratively to the successive elements of the list and the result of the previous application starting from the tail end of the list. During each iteration, an expression $f\ x_i\ e_i$ is evaluated. The user supplied conversion $conv$ is used to derive a theorem

```
|- f x_i e_i = e(i+1)
```

which is used in the next iteration.

Failure

`FOLDR_CONV conv tm` fails if tm is not of the form described above.

Example

To sum the elements of a list, one can use `FOLDR_CONV` with `ADD_CONV` from the library `num_lib`.

```
- load_library_in_place num_lib;
- FOLDR_CONV Num_lib.ADD_CONV (--'FOLDR $+ 0 [0;1;2;3]'--);
|- FOLDR $+ 0[0;1;2;3] = 6
```

In general, if the function f is an explicit lambda abstraction $(\lambda x\ x'.\ t[x,x'])$, the conversion should be in the form

```
((RATOR_CONV BETA_CONV) THENC BETA_CONV THENC conv')
```

where $conv'$ applied to $t[x,x']$ returns the theorem

```
|-t[x,x'] = e''.
```

See also

`listLib.FOLDL_CONV`, `listLib.list.FOLD_CONV`.

<div data-bbox="236 1814 331 1863" data-label="Text"> <p><code>for</code></p> </div>	<div data-bbox="1260 1814 1412 1863" data-label="Text"> <p>(Lib)</p> </div>
--	---

```
for : int -> int -> (int -> 'a) -> 'a list
```

Synopsis

Functional 'for' loops.

Description

An application `for b t f` is equal to `[f b, f (b+1), ..., f t]`. If `b` is greater than `t`, the empty list is returned.

Failure

If `f i` fails for `b <= i <= t`.

Example

```
- for 97 122 Char.chr;  
> val it =  
  ["a", "b", "c", "d", "e", "f", "g", "h", "i", "j", "k", "l",  
   "m", "n", "o", "p", "q", "r", "s", "t", "u", "v", "w", "x",  
   "y", "z"] : char list
```

See also

`Lib.for_se`.

<code>for_se</code>

<code>(Lib)</code>

```
for_se : int -> int -> (int -> unit) -> unit
```

Synopsis

Side-effecting 'for' loops.

Description

An application `for_se b t f` is equal to `(f b; f (b+1); ...; f t)`. If `b` is greater than `t`, then `for_se b t f` does no evaluation, in particular `f b` is not evaluated.

Failure

If `f i` fails for `b <= i <= t`.

Example

```
- let val A = Array.array(26, #" ")
  in
    for_se 0 25 (fn i => Array.update(A,i, Char.chr (i+97)))
    ; for_se 0 25 (print o Char.toString o curry Array.sub A)
    ; print "\n"
  end;
```

```
abcdefghijklmnopqrstuvwxy
z
> val it = () : unit
```

See also

Lib.for.

FORALL_AND_CONV

(Conv)

FORALL_AND_CONV : conv

Synopsis

Moves a universal quantification inwards through a conjunction.

Description

When applied to a term of the form $\!x. P \wedge Q$, the conversion FORALL_AND_CONV returns the theorem:

$$\vdash (\!x. P \wedge Q) = (\!x.P) \wedge (\!x.Q)$$

Failure

Fails if applied to a term not of the form $\!x. P \wedge Q$.

See also

Conv.AND_FORALL_CONV, Conv.LEFT_AND_FORALL_CONV, Conv.RIGHT_AND_FORALL_CONV.

FORALL_ARITH_CONV

(Arith)

FORALL_ARITH_CONV : conv

Synopsis

Partial decision procedure for non-existential Presburger natural arithmetic.

Description

FORALL_ARITH_CONV is a partial decision procedure for formulae of Presburger natural arithmetic which are in prenex normal form and have all variables either free or universally quantified. Presburger natural arithmetic is the subset of arithmetic formulae made up from natural number constants, numeric variables, addition, multiplication by a constant, the relations $<$, $<=$, $=$, $>=$, $>$ and the logical connectives \sim , \wedge , \vee , \implies , \iff , \iff (if-and-only-if), $!$ ('forall') and $?$ ('there exists'). Products of two expressions which both contain variables are not included in the subset, but the function SUC which is not normally included in a specification of Presburger arithmetic is allowed in this HOL implementation.

Given a formula in the specified subset, the function attempts to prove that it is equal to T (true). The procedure only works if the formula would also be true of the non-negative rationals; it cannot prove formulae whose truth depends on the integral properties of the natural numbers.

Failure

The function can fail in two ways. It fails if the argument term is not a formula in the specified subset, and it also fails if it is unable to prove the formula. The failure strings are different in each case.

Example

```
#FORALL_ARITH_CONV "m < SUC m";;
|- m < (SUC m) = T

#FORALL_ARITH_CONV "!m n p q. m <= p /\ n <= q ==> (m + n) <= (p + q)";;
|- (!m n p q. m <= p /\ n <= q ==> (m + n) <= (p + q)) = T

#FORALL_ARITH_CONV "!m n. ~(SUC (2 * m) = 2 * n)";;
evaluation failed      FORALL_ARITH_CONV -- cannot prove formula
```

See also

Arith.NEGATE_CONV, Arith.EXISTS_ARITH_CONV, numLib.ARITH_CONV,
Arith.ARITH_FORM_NORM_CONV, Arith.DISJ_INEQS_FALSE_CONV.

FORALL_CONJ_CONV	(unwindLib)
------------------	-------------

FORALL_CONJ_CONV : conv

Synopsis

Moves universal quantifiers down through a tree of conjunctions.

Description

`FORALL_CONJ_CONV` "`!x1 ... xm. t1 /\ ... /\ tn`" returns the theorem:

$$\begin{aligned} &|- !x1 \dots xm. t1 /\ \dots /\ tn = \\ &\quad (!x1 \dots xm. t1) /\ \dots /\ (!x1 \dots xm. tn) \end{aligned}$$

where the original term can be an arbitrary tree of conjunctions. The structure of the tree is retained in both sides of the equation.

Failure

Never fails.

Example

```
#FORALL_CONJ_CONV "! (x:*) (y:*) (z:*) . (a /\ b) /\ c";;
|- (!x y z. (a /\ b) /\ c) = ((!x y z. a) /\ (!x y z. b)) /\ (!x y z. c)
```

```
#FORALL_CONJ_CONV "T";;
|- T = T
```

```
#FORALL_CONJ_CONV "! (x:*) (y:*) (z:*) . T";;
|- (!x y z. T) = (!x y z. T)
```

See also

`unwindLib.CONJ_FORALL_CONV`, `unwindLib.FORALL_CONJ_ONCE_CONV`,
`unwindLib.CONJ_FORALL_ONCE_CONV`, `unwindLib.FORALL_CONJ_RIGHT_RULE`,
`unwindLib.CONJ_FORALL_RIGHT_RULE`.

<code>FORALL_CONJ_ONCE_CONV</code>

<code>(unwindLib)</code>

`FORALL_CONJ_ONCE_CONV` : `conv`

Synopsis

Moves a single universal quantifier down through a tree of conjunctions.

Description

`FORALL_CONJ_ONCE_CONV` "`!x. t1 /\ ... /\ tn`" returns the theorem:

$$\vdash !x. t1 \wedge \dots \wedge tn = (!x. t1) \wedge \dots \wedge (!x. tn)$$

where the original term can be an arbitrary tree of conjunctions. The structure of the tree is retained in both sides of the equation.

Failure

Fails if the argument term is not of the required form. The body of the term need not be a conjunction.

Example

```
#FORALL_CONJ_ONCE_CONV "!x. ((x \\/ a) /\ (x \\/ b)) /\ (x \\/ c)";;
|- (!x. ((x \\/ a) /\ (x \\/ b)) /\ (x \\/ c)) =
  ((!x. x \\/ a) /\ (!x. x \\/ b)) /\ (!x. x \\/ c)
```

```
#FORALL_CONJ_ONCE_CONV "!x. x \\/ a";;
|- (!x. x \\/ a) = (!x. x \\/ a)
```

```
#FORALL_CONJ_ONCE_CONV "!x. ((x \\/ a) /\ (y \\/ b)) /\ (x \\/ c)";;
|- (!x. ((x \\/ a) /\ (y \\/ b)) /\ (x \\/ c)) =
  ((!x. x \\/ a) /\ (!x. y \\/ b)) /\ (!x. x \\/ c)
```

See also

`unwindLib.CONJ_FORALL_ONCE_CONV`, `unwindLib.FORALL_CONJ_CONV`,
`unwindLib.CONJ_FORALL_CONV`, `unwindLib.FORALL_CONJ_RIGHT_RULE`,
`unwindLib.CONJ_FORALL_RIGHT_RULE`.

FORALL_CONJ_RIGHT_RULE

(unwindLib)

FORALL_CONJ_RIGHT_RULE : (thm -> thm)

Synopsis

Moves universal quantifiers down through a tree of conjunctions.

Description

$$A \vdash !z1 \dots zr. t = ?y1 \dots yp. !x1 \dots xm. t1 \wedge \dots \wedge tn$$

$$A \vdash !z1 \dots zr.$$

$$t = ?y1 \dots yp. (!x1 \dots xm. t1) \wedge \dots \wedge (!x1 \dots xm. tn)$$

Failure

Fails if the argument theorem is not of the required form, though either or both of r and p may be zero.

See also

`unwindLib.CONJ_FORALL_RIGHT_RULE`, `unwindLib.FORALL_CONJ_CONV`,
`unwindLib.CONJ_FORALL_CONV`, `unwindLib.FORALL_CONJ_ONCE_CONV`,
`unwindLib.CONJ_FORALL_ONCE_CONV`.

FORALL_CONSEQ_CONV	(ConseqConv)
---------------------------	---------------------

`FORALL_CONSEQ_CONV` : (conseq_conv -> conseq_conv)

Synopsis

Applies a consequence conversion to the body of a universally-quantified term.

Description

If c is a consequence conversion that maps a term ‘‘ $t\ x$ ’’ to a theorem $\vdash t\ x = t'\ x$, $\vdash t'\ x \implies t\ x$ or $\vdash t\ x \implies t'\ x$, then `FORALL_CONSEQ_CONV c` maps ‘‘ $\forall x. t\ x$ ’’ to $\vdash \forall x. t\ x = \forall x. t'\ x$, $\vdash \forall x. t'\ x \implies \forall x. t\ x$ or $\vdash \forall x. t\ x \implies \forall x. t'\ x$, respectively.

Failure

`FORALL_CONSEQ_CONV c t` fails, if t is not a all-quantified term or if c fails on the body of t .

See also

`Conv.QUANT_CONV`, `ConseqConv.EXISTS_CONSEQ_CONV`, `ConseqConv.QUANT_CONSEQ_CONV`.

FORALL_EQ	(Drule)
------------------	----------------

`FORALL_EQ` : (term -> thm -> thm)

Synopsis

Universally quantifies both sides of an equational theorem.

Description

When applied to a variable x and a theorem $A \vdash t1 = t2$, whose conclusion is an equation between boolean terms, `FORALL_EQ` returns the theorem $A \vdash (!x. t1) = (!x. t2)$, unless the variable x is free in any of the assumptions.

$$\frac{A \vdash t1 = t2}{A \vdash (!x. t1) = (!x. t2)} \quad \text{FORALL_EQ "x"} \quad [\text{where } x \text{ is not free in } A]$$

Failure

Fails if the theorem is not an equation between boolean terms, or if the supplied term is not simply a variable, or if the variable is free in any of the assumptions.

See also

`Thm.AP_TERM`, `Drule.EXISTS_EQ`, `Drule.SELECT_EQ`.

<code>FORALL_EQ___CONSEQ_CONV</code>	<code>(ConseqConv)</code>
--------------------------------------	---------------------------

`FORALL_EQ___CONSEQ_CONV` : `conseq_conv`

Synopsis

Given a term of the form $(!x. P \ x) = (!x. Q \ x)$ this consequence conversion returns the theorem $\vdash (!x. (P \ x = Q \ x)) \implies ((!x. P \ x) = (!x. Q \ x))$.

See also

`ConseqConv.conseq_conv`.

<code>FORALL_IMP_CONV</code>	<code>(Conv)</code>
------------------------------	---------------------

`FORALL_IMP_CONV` : `conv`

Synopsis

Moves a universal quantification inwards through an implication.

Description

When applied to a term of the form $!x. P \implies Q$, where x is not free in both P and Q , `FORALL_IMP_CONV` returns a theorem of one of three forms, depending on occurrences of the variable x in P and Q . If x is free in P but not in Q , then the theorem:

$$\vdash (\!x. P \implies Q) = (?x.P) \implies Q$$

is returned. If x is free in Q but not in P , then the result is:

$$\vdash (\!x. P \implies Q) = P \implies (\!x.Q)$$

And if x is free in neither P nor Q , then the result is:

$$\vdash (\!x. P \implies Q) = (?x.P) \implies (\!x.Q)$$

Failure

FORALL_IMP_CONV fails if it is applied to a term not of the form $\!x. P \implies Q$, or if it is applied to a term $\!x. P \implies Q$ in which the variable x is free in both P and Q .

See also

Conv.LEFT_IMP_EXISTS_CONV, Conv.RIGHT_IMP_FORALL_CONV.

FORALL_NOT_CONV	(Conv)
-----------------	--------

FORALL_NOT_CONV : conv

Synopsis

Moves a universal quantification inwards through a negation.

Description

When applied to a term of the form $\!x. \sim P$, the conversion FORALL_NOT_CONV returns the theorem:

$$\vdash (\!x. \sim P) = \sim(?x. P)$$

Failure

Fails if applied to a term not of the form $\!x. \sim P$.

See also

Conv.EXISTS_NOT_CONV, Conv.NOT_EXISTS_CONV, Conv.NOT_FORALL_CONV.

FORALL_OR_CONV	(Conv)
----------------	--------

FORALL_OR_CONV : conv

Synopsis

Moves a universal quantification inwards through a disjunction.

Description

When applied to a term of the form $\lambda x. P \vee Q$, where x is not free in both P and Q , `FORALL_OR_CONV` returns a theorem of one of three forms, depending on occurrences of the variable x in P and Q . If x is free in P but not in Q , then the theorem:

$$\vdash (\lambda x. P \vee Q) = (\lambda x.P) \vee Q$$

is returned. If x is free in Q but not in P , then the result is:

$$\vdash (\lambda x. P \vee Q) = P \vee (\lambda x.Q)$$

And if x is free in neither P nor Q , then the result is:

$$\vdash (\lambda x. P \vee Q) = (\lambda x.P) \vee (\lambda x.Q)$$

Failure

`FORALL_OR_CONV` fails if it is applied to a term not of the form $\lambda x. P \vee Q$, or if it is applied to a term $\lambda x. P \vee Q$ in which the variable x is free in both P and Q .

See also

`Conv.OR_FORALL_CONV`, `Conv.LEFT_OR_FORALL_CONV`, `Conv.RIGHT_OR_FORALL_CONV`.

forget_history	(proofManagerLib)
----------------	-------------------

```
forget_history : unit -> unit
```

Synopsis

Clears the proof history.

Description

The function `forget_history` is part of the `subgoal` package. A call to `forget_history` clears the history of saved proof states. Subsequent calls to `backup` or `restart` will behave as if the initial goal was the state at the time of the call to `forget_history`. For a description of the `subgoal` package, see `set_goal`.

Failure

The function `forget_history` only fails if no goalstack is being managed.

Uses

Hiding an automatic preprocessing phase of a proof before handing it to the user.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`,
`proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`,
`proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`,
`proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

FORK_CONV

(Conv)

`FORK_CONV : (conv * conv) -> conv`

Synopsis

Applies a pair of conversions to the arguments of a binary operator.

Description

If the conversion c_1 maps a term t_1 to the theorem $\vdash t_1 = t_1'$, and the conversion c_2 maps t_2 to $\vdash t_2 = t_2'$, then the conversion `FORK_CONV (c1, c2)` maps terms of the form $f\ t_1\ t_2$ to theorems of the form $\vdash f\ t_1\ t_2 = f\ t_1'\ t_2'$.

Failure

`FORK_CONV (c1, c2) t` will fail if t is not of the general form $f\ t_1\ t_2$, or if c_1 fails when applied to t_1 , or if c_2 fails when applied to t_2 , or if c_1 or c_2 aren't really conversions, and thereby fail to return appropriate equational theorems.

Example

```
- FORK_CONV (BETA_CONV, REDUCE_CONV) (Term'(\x. x + 1)y * (10 DIV 3)');
> val it = \vdash (\x. x + 1) y * (10 DIV 3) = (y + 1) * 3 : thm
```

See also

`Conv.BINOP_CONV`, `Conv.LAND_CONV`, `Conv.RAND_CONV`, `Conv.RATOR_CONV`,
`numLib.REDUCE_CONV`.

format_ERR

(Feedback)

`format_ERR : error_record -> string`

Synopsis

Maps argument record of `HOL_ERR` to a string

Description

The `format_ERR` function maps the argument of an application of `HOL_ERR` to a string. It is the default function used by `ERR_to_string`.

Failure

Never fails.

Example

```
- print
  (format_ERR {origin_structure = "Foo",
              origin_function = "bar",
              message = "incomprehensible input"});
```

```
Exception raised at Foo.bar:
incomprehensible input
> val it = () : unit
```

See also

`Feedback`, `Feedback.ERR_to_string`, `Feedback.format_MESG`, `Feedback.format_WARNING`.

<code>format_MESG</code>

<code>(Feedback)</code>

`format_MESG` : string -> string

Synopsis

Maps argument of `HOL_MESG` to a string

Description

The `format_MESG` function maps a string to a string. Usually, the input string is the argument of an invocation of `HOL_MESG`. `format_MESG` is the default function used by `MESG_to_string`.

Failure

Never fails.

Example

```
- print (format_MESG "Hello world.");
<<HOL message: Hello world.>>
```

See also

Feedback, Feedback.MESG_to_string, Feedback.format_ERR, Feedback.format_WARNING.

<code>format_WARNING</code>	<code>(Feedback)</code>
-----------------------------	-------------------------

`format_WARNING` : string -> string -> string -> string

Synopsis

Maps arguments of `HOL_WARNING` to a string

Description

The `format_WARNING` function maps three strings to a string. Usually, the input strings are the arguments to an invocation of `HOL_WARNING`. `format_WARNING` is the default function used by `WARNING_to_string`.

Failure

Never fails.

Example

```
- print (format_WARNING "Module" "function" "Gadzooks!");
<<HOL warning: Module.function: Gadzooks!>>
```

See also

Feedback, Feedback.WARNING_to_string, Feedback.format_ERR, Feedback.format_MESG.

<code>free_in</code>	<code>(Term)</code>
----------------------	---------------------

`free_in` : term -> term -> bool

Synopsis

Tests if one term is free in another.

Description

When applied to two terms t_1 and t_2 , the function `free_in` returns `true` if t_1 is free in t_2 , and `false` otherwise. It is not necessary that t_1 be simply a variable. A term M occurs free in N when there is some occurrence of M in N such that each free variable of M in that occurrence is not bound by a binder in N .

Failure

Never fails.

Example

In the following example `free_in` returns `false` because the x in `SUC x` in the second term is bound:

```
- free_in "SUC x" "!x. SUC x = x + 1";
> val it = false : bool
```

whereas the following call returns `true` because the first instance of x in the second term is free, even though there is also a bound instance:

```
- free_in "x:bool" "!y. x /\ ?x. x = y";
> val it = true : bool
```

See also

`Term.free_vars`, `Term.FVL`.

<div data-bbox="161 1350 426 1402" data-label="Text"> <p><code>free_vars</code></p> </div>	<div data-bbox="1155 1350 1331 1402" data-label="Text"> <p>(Term)</p> </div>
--	--

`free_vars` : term -> term list

Synopsis

Returns the set of free variables in a term.

Description

An invocation `free_vars tm` returns a list representing the set of term variables occurring in tm .

Failure

Never fails.

Example

```
- free_vars (Term 'x /\ y /\ y ==> x');
> val it = ['y', 'x'] : term list
```

Comments

Code should not depend on how elements are arranged in the result of `free_vars`.

`free_vars` is not efficient for large terms with many free variables. Demanding applications should be coded with FVL.

See also

`Term.FVL`, `Term.free_vars_lr`, `Term.free_vars_l`, `Term.empty_varset`, `Type.type_vars`.

<code>free_vars_lr</code>	<code>(Term)</code>
---------------------------	---------------------

```
free_vars_lr : term -> term list
```

Synopsis

Returns the set of free variables in a term, in order.

Description

An invocation `free_vars_lr ty` returns a list representing the set of type variables occurring in `ty`. The list will be in order of variable occurrence when scanning the parse tree of the term from left to right. This is usually, but need not be, the textual order when the term is printed.

Failure

Never fails.

Example

```
- free_vars_lr (Term 'x /\ y /\ y ==> z');
> val it = ['x', 'y', 'z'] : term list
```

Comments

`free_vars_lr` is not efficient for large terms with many free variables. More strenuous applications should use high performance set implementations available in the Standard ML Basis Library.

Uses

`free_vars_lr` can be used to build pleasing quantifier prefixes.

See also

Term.FVL, Term.free_vars, Term.empty_varset, Type.type_vars.

<div data-bbox="159 486 453 537" data-label="Text"> <p><code>free_varsl</code></p> </div>	<div data-bbox="1155 486 1331 537" data-label="Text"> <p><code>(Term)</code></p> </div>
---	---

`free_varsl : term list -> term list`

Synopsis

Returns the set of free variables in a list of terms.

Description

An invocation `free_varsl [t1,...,tn]` returns a list representing the set of free term variables occurring in `t1,...,tn`.

Failure

Never fails.

Example

```
- free_varsl [Term 'x /\ y /\ y ==> x',
             Term '!x. x ==> p ==> y'];
> val it = ['x', 'y', 'p'] : term list
```

Comments

Code should not depend on how elements are arranged in the result of `free_varsl`.

`free_varsl` is not efficient for large terms with many free variables. Demanding applications should be coded with FVL.

See also

Term.FVL, Term.free_vars_lr, Term.free_vars, Term.empty_varset, Type.type_vars.

<div data-bbox="159 1706 312 1756" data-label="Text"> <p><code>frees</code></p> </div>	<div data-bbox="1038 1706 1331 1756" data-label="Text"> <p><code>(hol188Lib)</code></p> </div>
--	--

`frees : term -> term list`

Synopsis

Returns a list of the variables which are free in a term.

Description

`frees` is equivalent to `rev o Term.free_vars`.

Failure

Never fails.

Comments

Superseded by `Term.free_vars`.

See also

`hol88Lib.freesl`, `Term.free_vars`.

<code>freesl</code>	<code>(hol88Lib)</code>
---------------------	-------------------------

`freesl` : `term list -> term list`

Synopsis

Returns a list of the free variables in a list of terms.

Description

`freesl` is equivalent to `rev o Term.free_varsl`.

Failure

Never fails.

Comments

Superseded by `Term.free_varsl`.

See also

`hol88Lib.frees`, `Term.free_varsl`.

<code>FREEZE_THEN</code>	<code>(Tactic)</code>
--------------------------	-----------------------

`FREEZE_THEN` : `thm_tactical`

Synopsis

'Freezes' a theorem to prevent instantiation of its free variables.

Description

`FREEZE_THEN` expects a tactic-generating function $f : \text{thm} \rightarrow \text{tactic}$ and a theorem $(A1 \mid - w)$ as arguments. The tactic-generating function f is applied to the theorem $(w \mid - w)$. If this tactic generates the subgoal:

```
A ?- t
===== f (w | - w)
A ?- t1
```

then applying `FREEZE_THEN f (A1 | - w)` to the goal $(A \mid - t)$ produces the subgoal:

```
A ?- t
===== FREEZE_THEN f (A1 | - w)
A ?- t1
```

Since the term w is a hypothesis of the argument to the function f , none of the free variables present in w may be instantiated or generalized. The hypothesis is discharged by `PROVE_HYP` upon the completion of the proof of the subgoal.

Failure

Failures may arise from the tactic-generating function. An invalid tactic arises if the hypotheses of the theorem are not alpha-convertible to assumptions of the goal.

Example

Given the goal $(["b < c"; "a < b"], "(SUC a) <= c")$, and the specialized variant of the theorem `LESS_TRANS`:

```
th = | - !p. a < b /\ b < p ==> a < p
```

`IMP_RES_TAC th` will generate several unneeded assumptions:

```
{b < c, a < b, a < c, !p. c < p ==> b < p, !a'. a' < a ==> a' < b}
?- (SUC a) <= c
```

which can be avoided by first ‘freezing’ the theorem, using the tactic

```
FREEZE_THEN IMP_RES_TAC th
```

This prevents the variables a and b from being instantiated.

```
{b < c, a < b, a < c} ?- (SUC a) <= c
```

Uses

Used in serious proof hacking to limit the matches achievable by resolution and rewriting.

See also

Thm.ASSUME, Tactic.IMP_RES_TAC, Drule.PROVE_HYP, Tactic.RES_TAC, Conv.REWR_CONV.

<code>front_last</code>	<code>(Lib)</code>
-------------------------	--------------------

`Lib.front_last : 'a list -> 'a list * 'a`

Synopsis

Takes a non-empty list `L` and returns a pair `(front,last)` such that `front @ [last] = L`.

Failure

Fails if the list is empty.

Example

```
- front_last [1];
> val it = ([],1) : int list * int

- front_last [1,2,3];
> val it = ([1,2],3) : int list * int
```

See also

`Lib.butlast`, `Lib.last`.

<code>fst</code>	<code>(Lib)</code>
------------------	--------------------

`fst : ('a * 'b) -> 'a`

Synopsis

Extracts the first component of a pair.

Description

`fst (x,y)` returns `x`.

Failure

Never fails. However, notice that `fst (x,y,z)` fails to typecheck, since `(x,y,z)` is not a pair.

Example

```

- fst (1, "foo");
> val it = 1 : int

- fst (1, "foo", []);
! Toplevel input:
! fst (1, "foo", []);
! ~~~~~
! Type clash: expression of type
!   'g * 'h * 'i
! cannot have type
!   'j * 'k
! because the tuple has the wrong number of components

- fst (1, ("foo", []));
> val it = 1 : int

```

See also

Lib.snd.

<div data-bbox="159 1178 341 1236" data-label="Text"> <p>ftyvar</p> </div>	<div data-bbox="1155 1173 1332 1236" data-label="Text"> <p>(Type)</p> </div>
--	--

ftyvar : hol_type

Synopsis

Common type variable.

Description

The ML variable `Type.ftyvar` is bound to the type variable 'f.

See also

`Type.alpha`, `Type.beta`, `Type.gamma`, `Type.delta`, `Type.etyvar`, `Type.bool`.

<div data-bbox="159 1816 542 1872" data-label="Text"> <p>FULL_SIMP_TAC</p> </div>	<div data-bbox="1067 1816 1332 1872" data-label="Text"> <p>(bossLib)</p> </div>
---	---

`simpLib.FULL_SIMP_TAC` : `simpset -> thm list -> tactic`

Synopsis

Simplifies the goal (assumptions as well as conclusion) with the given simpset.

Description

FULL_SIMP_TAC is a powerful simplification tactic that simplifies all of a goal. It proceeds by applying simplification to each assumption of the goal in turn, accumulating simplified assumptions as it goes. These simplified assumptions are used to simplify further assumptions, and all of the simplified assumptions are used as additional rewrites when the conclusion of the goal is simplified.

In addition, simplified assumptions are added back onto the goal using the equivalent of STRIP_ASSUME_TAC and this causes automatic skolemization of existential assumptions, case splits on disjunctions, and the separate assumption of conjunctions. If an assumption is simplified to TRUTH, then this is left on the assumption list. If an assumption is simplified to falsity, this proves the goal.

Failure

FULL_SIMP_TAC never fails, but it may diverge.

Example

Here FULL_SIMP_TAC is used to prove a goal:

```
> FULL_SIMP_TAC arith_ss [] (map Term ['x = 3', 'x < 2'],
                               Term '?y. x * y = 51')
- val it = ([], fn) : tactic_result
```

Using LESS_OR_EQ |- !m n. m <= n = m < n \vee (m = n), a useful case split can be induced in the next goal:

```
> FULL_SIMP_TAC bool_ss [LESS_OR_EQ] (map Term ['x <= y', 'x < z'],
                                         Term 'x + y < z');
- val it =
  ([(['x < y', 'x < z'], 'x + y < z'),
   (['x = y', 'x < z'], 'y + y < z')], fn)
  : tactic_result
```

Note that the equality $x = y$ is not used to simplify the subsequent assumptions, but is used to simplify the conclusion of the goal.

Comments

The application of STRIP_ASSUME_TAC to simplified assumptions means that FULL_SIMP_TAC can cause unwanted case-splits and other undesirable transformations to occur in one's assumption list. If one wants to apply the simplifier to assumptions without this occurring, the best approach seems to be the use of RULE_ASSUM_TAC and SIMP_RULE.

See also

bossLib.ASM_SIMP_TAC, bossLib.SIMP_CONV, bossLib.SIMP_RULE, bossLib.SIMP_TAC.

FULL_SIMP_TAC	(simpLib)
---------------	-----------

FULL_SIMP_TAC : simpset -> thm list -> tactic

Synopsis

Simplify a term with the given simpset and theorems.

Description

bossLib.FULL_SIMP_TAC is identical to simpLib.FULL_SIMP_TAC.

See also

bossLib.FULL_SIMP_TAC.

FULL_STRUCT_CASES_TAC	(Tactic)
-----------------------	----------

FULL_STRUCT_CASES_TAC : thm_tactic

Synopsis

A form of STRUCT_CASES_TAC that also applies the case analysis to the assumption list.

Description

See STRUCT_CASES_TAC.

Failure

Fails unless provided with a theorem that is a conjunction of (possibly multiply existentially quantified) terms which assert the equality of a variable with some given terms.

Example

Suppose we have the goal:

```
~(1:(*)list = []) ?- (LENGTH l) > 0
```

then we can get rid of the universal quantifier from the inbuilt list theorem list_CASES:

```
list_CASES = !l. (l = []) \ / (?t h. l = CONS h t)
```

and then use `FULL_STRUCT_CASES_TAC`. This amounts to applying the following tactic:

```
FULL_STRUCT_CASES_TAC (SPEC_ALL list_CASES)
```

which results in the following two subgoals:

```
~(CONS h t = []) ?- (LENGTH(CONS h t)) > 0
```

```
~([] = []) ?- (LENGTH[]) > 0
```

Note that this is a rather simple case, since there are no constraints, and therefore the resulting subgoals have no extra assumptions.

Uses

Generating a case split from the axioms specifying a structure.

See also

`Tactic.ASM_CASES_TAC`, `Tactic.BOOL_CASES_TAC`, `Tactic.COND_CASES_TAC`,
`Tactic.DISJ_CASES_TAC`, `Tactic.STRUCT_CASES_TAC`.

FUN_EQ_CONV

(Conv)

`FUN_EQ_CONV` : conv

Synopsis

Equates normal and extensional equality for two functions.

Description

The conversion `FUN_EQ_CONV` embodies the fact that two functions are equal precisely when they give the same results for all values to which they can be applied. When supplied with a term argument of the form `f = g`, where `f` and `g` are functions of type `ty1->ty2`, `FUN_EQ_CONV` returns the theorem:

$$\vdash (f = g) = (!x. f x = g x)$$

where `x` is a variable of type `ty1` chosen by the conversion.

Failure

`FUN_EQ_CONV tm` fails if `tm` is not an equation `f = g`, where `f` and `g` are functions.

Uses

Used for proving equality of functions.

See also

`Drule.EXT`, `Conv.X_FUN_EQ_CONV`.

<code>funpow</code>

<code>(Lib)</code>

```
funpow : int -> ('a -> 'a) -> 'a -> 'a
```

Synopsis

Iterates a function a fixed number of times.

Description

`funpow n f x` applies `f` to `x`, `n` times, giving the result `f (f ... (f x) ...)` where the number of `f`'s is `n`. If `n` is not positive, the result is `x`.

Failure

`funpow n f x` fails if any of the `n` applications of `f` fail.

Example

Apply `t1` three times to a list:

```
- funpow 3 t1 [1,2,3,4,5];  
> [4, 5] : int list
```

Apply `t1` zero times:

```
- funpow 0 t1 [1,2,3,4,5];  
> [1; 2; 3; 4; 5] : int list
```

Apply `t1` six times to a list of only five elements:

```
- funpow 6 t1 [1,2,3,4,5];  
! Uncaught exception:  
! List.Empty
```

See also

`Lib.repeat`.

FVL

(Term)

```
FVL : term list -> term set -> term set
```

Synopsis

Efficient computation of the set of free variables in a list of terms.

Description

An invocation `FVL [t1,...,tn] v` adds the set of free variables found in `t1,...,tn` to the accumulator `v`.

Failure

Never fails.

Example

```
- FVL [Term 'v1 /\ v2 ==> v2 \/ v3'] empty_varset;
> val it = <set> : term set

- HOLset.listItems it;
> val it = ['v1', 'v2', 'v3'] : term list
```

Comments

Preferable to `free_vars1` when the number of free variables becomes large.

See also

`HOLset`, `Term.empty_varset`, `Term.free_vars1`, `Term.free_vars`.

g

(proofManagerLib)

```
g : term frag list -> proofs
```

Synopsis

Initializes the subgoal package with a new goal which has no assumptions.

Description

The call

```
g 'tm'
```

is equivalent to

```
set_goal([],Term'tm')
```

and clearly more convenient if a goal has no assumptions. For a description of the subgoal package, see `set_goal`.

Failure

Fails unless the argument term has type `bool`.

Example

```
- g '(HD[1;2;3] = 1) /\ (TL[1;2;3] = [2;3])';
> val it =
  Proof manager status: 1 proof.
  1. Incomplete:
      Initial goal:
      (HD [1; 2; 3] = 1) /\ (TL [1; 2; 3] = [2; 3])
```

```
: GoalstackPure.proofs
```

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`, `proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`, `proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`, `proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

<div data-bbox="161 1583 314 1635" data-label="Text"> <p>gamma</p> </div>	<div data-bbox="1155 1576 1332 1637" data-label="Text"> <p>(Type)</p> </div>
---	--

```
gamma : hol_type
```

Synopsis

Common type variable.

Description

The ML variable `Type.gamma` is bound to the type variable `'c`.

See also

Type.alpha, Type.beta, Type.delta, Type.bool.

GE_CONV	(reduceLib)
----------------	--------------------

GE_CONV : conv

Synopsis

Proves result of less-than-or-equal-to ordering on two numerals.

Description

If m and n are both numerals (e.g. 0, 1, 2, 3,...), then GE_CONV " $m \geq n$ " returns the theorem:

$$\vdash (m \geq n) = T$$

if the natural number denoted by m is greater than or equal to that denoted by n , or

$$\vdash (m \geq n) = F$$

otherwise.

Failure

GE_CONV t_m fails unless t_m is of the form " $m \geq n$ ", where m and n are numerals.

Example

```
#GE_CONV "15 >= 14";;
|- 15 >= 14 = T
```

```
#GE_CONV "100 >= 100";;
|- 100 >= 100 = T
```

```
#GE_CONV "0 >= 107";;
|- 0 >= 107 = F
```

GEN	(Thm)
------------	--------------

GEN : term -> thm -> thm

Synopsis

Generalizes the conclusion of a theorem.

Description

When applied to a term x and a theorem $A \vdash t$, the inference rule `GEN` returns the theorem $A \vdash !x. t$, provided x is a variable not free in any of the assumptions. There is no compulsion that x should be free in t .

$$\frac{A \vdash t}{A \vdash !x. t} \text{ GEN } x \quad [\text{where } x \text{ is not free in } A]$$

Failure

Fails if x is not a variable, or if it is free in any of the assumptions.

Example

The following example shows how the above side-condition prevents the derivation of the theorem $x=T \vdash !x. x=T$, which is clearly invalid.

```
- show_types := true;
> val it = () : unit

- val t = ASSUME (Term 'x=T');
> val t = [.] |- (x :bool) = T : thm

- try (GEN (Term 'x:bool')) t;
Exception raised at Thm.GEN:
variable occurs free in hypotheses
! Uncaught exception:
! HOL_ERR
```

See also

`Thm.GENL`, `Drule.GEN_ALL`, `Tactic.GEN_TAC`, `Thm.SPEC`, `Drule.SPECL`, `Drule.SPEC_ALL`, `Tactic.SPEC_TAC`.

GEN_ALL	(Drule)
---------	---------

`GEN_ALL : thm -> thm`

Synopsis

Generalizes the conclusion of a theorem over its own free variables.

Description

When applied to a theorem $A \vdash t$, the inference rule `GEN_ALL` returns the theorem $A \vdash !x1 \dots xn. t$, where the x_i are all the variables, if any, which are free in t but not in the assumptions.

$$\frac{A \vdash t}{A \vdash !x1 \dots xn. t} \text{ GEN_ALL}$$

Failure

Never fails.

Comments

Sometimes people write code that depends on the order of the quantification. They shouldn't.

See also

`Thm.GEN`, `Thm.GENL`, `Thm.SPEC`, `Drule.SPECL`, `Drule.SPEC_ALL`, `Tactic.SPEC_TAC`.

<div data-bbox="236 1319 445 1368" data-label="Text"> <p><code>GEN_ALL</code></p> </div>	<div data-bbox="1115 1319 1412 1368" data-label="Text"> <p><code>(hol88Lib)</code></p> </div>
--	---

`GEN_ALL : thm -> thm`

Synopsis

Generalizes the conclusion of a theorem over its own free variables.

Description

When applied to a theorem $A \vdash t$, the inference rule `GEN_ALL` returns the theorem $A \vdash !x1 \dots xn. t$, where the x_i are all the variables, if any, which are free in t but not in the assumptions.

$$\frac{A \vdash t}{A \vdash !x1 \dots xn. t} \text{ GEN_ALL}$$

Failure

Never fails.

Comments

Superseded by `Drule.GEN_ALL`, which, however, may return a different result. That is why `GEN_ALL` is in `ho188Lib`. Sometimes people write code that depends on the order of the quantification. They shouldn't.

See also

`Drule.GEN_ALL`.

GEN_ALPHA_CONV

(Drule)

`GEN_ALPHA_CONV : term -> conv`

Synopsis

Renames the bound variable of an abstraction, a quantified term, or other binder application.

Description

The conversion `GEN_ALPHA_CONV` provides alpha conversion for lambda abstractions of the form $\lambda y.t$, quantified terms of the forms $!y.t$, $?y.t$ or $?!y.t$, and epsilon terms of the form $@y.t$. In general, if B is a binder constant, then `GEN_ALPHA_CONV` implements alpha conversion for applications of the form $B y.t$.

If tm is an abstraction $\lambda y.t$ or an application of a binder to an abstraction $B y.t$, where the bound variable y has type ty , and if x is a variable also of type ty , then `GEN_ALPHA_CONV x tm` returns one of the theorems:

$$\begin{aligned} |- (\lambda y.t) &= (\lambda x'. t[x'/y]) \\ |- (B y.t) &= (B x'. t[x'/y]) \end{aligned}$$

depending on whether the input term is $\lambda y.t$ or $B y.t$ respectively. The variable $x' : ty$ in the resulting theorem is a primed variant of x chosen so as not to be free in the term provided as the second argument to `GEN_ALPHA_CONV`.

Failure

`GEN_ALPHA_CONV x tm` fails if x is not a variable, or if tm does not have one of the forms $\lambda y.t$ or $B y.t$, where B is a binder. `GEN_ALPHA_CONV x tm` also fails if tm does have one of these forms, but types of the variables x and y differ.

See also

Thm.ALPHA, Drule.ALPHA_CONV, boolSyntax.new_binder_definition.

GEN_BETA_CONV	(PairedLamda)
----------------------	----------------------

GEN_BETA_CONV : conv

Synopsis

Beta-reduces single or paired beta-redexes, creating a paired argument if needed.

Description

The conversion GEN_BETA_CONV will perform beta-reduction of simple beta-redexes in the manner of BETA_CONV, or of tupled beta-redexes in the manner of PAIRED_BETA_CONV. Unlike the latter, it will force through a beta-reduction by introducing arbitrarily nested pair destructors if necessary. The following shows the action for one level of pairing; others are similar.

$$\text{GEN_BETA_CONV } "\lambda(x,y). t) p" = t[(\text{FST } p)/x, (\text{SND } p)/y]$$
Failure

GEN_BETA_CONV tm fails if tm is neither a simple nor a tupled beta-redex.

Example

The following examples show the action of GEN_BETA_CONV on tupled redexes. In the following, it acts in the same way as PAIRED_BETA_CONV:

```
- pairLib.GEN_BETA_CONV (Term '(λ(x,y). x + y) (1,2)');
val it = |- (λ(x,y). x + y)(1,2) = 1 + 2 : thm
```

whereas in the following, the operand of the beta-redex is not a pair, so FST and SND are introduced:

```
- pairLib.GEN_BETA_CONV (Term '(λ(x,y). x + y) numpair');
> val it = |- (λ(x,y). x + y) numpair = FST numpair + SND numpair : thm
```

The introduction of FST and SND will be done more than once as necessary:

```
- pairLib.GEN_BETA_CONV (Term '(λ(w,x,y,z). w + x + y + z) (1,triple)');
> val it =
  |- (λ(w,x,y,z). w + x + y + z) (1,triple) =
    1 + FST triple + FST (SND triple) + SND (SND triple) : thm
```

See also

Thm.BETA_CONV, PairedLambda.PAIRED_BETA_CONV.

<div data-bbox="161 504 541 555" data-label="Text"> <p>GEN_MESON_TAC</p> </div>	<div data-bbox="1038 504 1331 555" data-label="Text"> <p>(mesonLib)</p> </div>
--	--

GEN_MESON_TAC : int -> int -> int -> thm list -> tactic

Synopsis

Performs first order proof search to prove the goal, using both the given theorems and the assumptions in the search.

Description

GEN_MESON_TAC is the function which provides the underlying implementation of the model elimination solver used by both MESON_TAC and ASM_MESON_TAC. The three integer parameters correspond to various ways in which the search can be tuned.

The first is the minimum depth at which to search. Setting this to a number greater than zero can save time if its clear that there will not be a proof of such a small depth. ASM_MESON_TAC and MESON_TAC always use a value of 0 for this parameter.

The second is the maximum depth to which to search. Setting this low will stop the search taking too long, but may cause the engine to miss proofs it would otherwise find. The setting of this variable for ASM_MESON_TAC and MESON_TAC is done through the reference variable mesonLib.max_depth. This is set to 30 by default, but most proofs do not need anything like this depth.

The third parameter is the increment used to increase the depth of search done by the proof search procedure.

The approach used is iterative deepening, so with a call to

```
GEN_MESON_TAC mn mx inc
```

the algorithm looks for a proof of depth mn , then for one of depth $mn + inc$, then at depth $mn + 2 * inc$ etc. Once the depth gets greater than mx , the proof search stops.

Failure

GEN_MESON_TAC fails if it searches to a depth equal to the second integer parameter without finding a proof. Shouldn't fail otherwise.

Uses

The construction of tailored versions of MESON_TAC and ASM_MESON_TAC.

See also

mesonLib.ASM_MESON_TAC, mesonLib.MESON_TAC.

GEN_ALPHA_CONV

(PairRules)

GEN_ALPHA_CONV : term -> conv

Synopsis

Renames the bound pair of a paired abstraction, quantified term, or other binder.

Description

The conversion GEN_ALPHA_CONV provides alpha conversion for lambda abstractions of the form $\lambda p.t$, quantified terms of the forms $!p.t$, $?p.t$ or $?!p.t$, and epsilon terms of the form $@p.t$.

The renaming of pairs is as described for ALPHA_CONV.

Failure

GEN_ALPHA_CONV q tm fails if q is not a variable, or if tm does not have one of the required forms. GEN_ALPHA_CONV q tm also fails if tm does have one of these forms, but types of the variables p and q differ.

See also

Drule.GEN_ALPHA_CONV, PairRules.ALPHA, PairRules.ALPHA_CONV.

GEN_REWRITE_CONV

(Rewrite)

GEN_REWRITE_CONV : ((conv -> conv) -> thm list -> thm list -> conv)

Synopsis

Rewrites a term, selecting terms according to a user-specified strategy.

Description

Rewriting in HOL is based on the use of equational theorems as left-to-right replacements on the subterms of an object theorem. This replacement is mediated by the use of REWR_CONV, which finds matches between left-hand sides of given equations in a term and applies the substitution.

Equations used in rewriting are obtained from the theorem lists given as arguments to the function. These are at first transformed into a form suitable for rewriting. Conjunctions are separated into individual rewrites. Theorems with conclusions of the form " $\sim t$ " are transformed into the corresponding equations " $t = F$ ". Theorems " t " which are not equations are cast as equations of form " $t = T$ ".

If a theorem is used to rewrite a term, its assumptions are added to the assumptions of the returned theorem. The matching involved uses variable instantiation. Thus, all free variables are generalized, and terms are instantiated before substitution. Theorems may have universally quantified variables.

The theorems with which rewriting is done are divided into two groups, to facilitate implementing other rewriting tools. However, they are considered in an order-independent fashion. (That is, the ordering is an implementation detail which is not specified.)

The search strategy for finding matching subterms is the first argument to the rule. Matching and substitution may occur at any level of the term, according to the specified search strategy: the whole term, or starting from any subterm. The search strategy also specifies the depth of the search: recursively up to an arbitrary depth until no matches occur, once over the selected subterm, or any more complex scheme.

Failure

GEN_REWRITE_CONV fails if the search strategy fails. It may also cause a non-terminating sequence of rewrites, depending on the search strategy used.

Uses

This conversion is used in the system to implement all other rewrites conversions, and may provide a user with a method to fine-tune rewriting of terms.

Example

Suppose we have a term of the form:

$$(1 + 2) + 3 = (3 + 1) + 2$$

and we would like to rewrite the left-hand side with the theorem ADD_SYM without changing the right hand side. This can be done by using:

```
GEN_REWRITE_CONV (RATOR_CONV o ONCE_DEPTH_CONV) [] [ADD_SYM] mythm
```

Other rules, such as ONCE_REWRITE_CONV, would match and substitute on both sides, which would not be the desirable result.

As another example, REWRITE_CONV could be implemented as

```
GEN_REWRITE_CONV TOP_DEPTH_CONV basic_rewrites
```

which specifies that matches should be searched recursively starting from the whole term of the theorem, and `basic_rewrites` must be added to the user defined set of theorems employed in rewriting.

See also

`Rewrite.ONCE_REWRITE_CONV`, `Rewrite.PURE_REWRITE_CONV`, `Conv.REWR_CONV`,
`Rewrite.REWRITE_CONV`.

GEN_REWRITE_RULE	(Rewrite)
-------------------------	------------------

`GEN_REWRITE_RULE : ((conv -> conv) -> thm list -> thm list -> thm -> thm)`

Synopsis

Rewrites a theorem, selecting terms according to a user-specified strategy.

Description

Rewriting in HOL is based on the use of equational theorems as left-to-right replacements on the subterms of an object theorem. This replacement is mediated by the use of `REWR_CONV`, which finds matches between left-hand sides of given equations in a term and applies the substitution.

Equations used in rewriting are obtained from the theorem lists given as arguments to the function. These are at first transformed into a form suitable for rewriting. Conjunctions are separated into individual rewrites. Theorems with conclusions of the form " $\sim t$ " are transformed into the corresponding equations " $t = F$ ". Theorems " t " which are not equations are cast as equations of form " $t = T$ ".

If a theorem is used to rewrite the object theorem, its assumptions are added to the assumptions of the returned theorem, unless they are alpha-convertible to existing assumptions. The matching involved uses variable instantiation. Thus, all free variables are generalized, and terms are instantiated before substitution. Theorems may have universally quantified variables.

The theorems with which rewriting is done are divided into two groups, to facilitate implementing other rewriting tools. However, they are considered in an order-independent fashion. (That is, the ordering is an implementation detail which is not specified.)

The search strategy for finding matching subterms is the first argument to the rule. Matching and substitution may occur at any level of the term, according to the specified search strategy: the whole term, or starting from any subterm. The search strategy also specifies the depth of the search: recursively up to an arbitrary depth until no matches occur, once over the selected subterm, or any more complex scheme.

Failure

GEN_REWRITE_RULE fails if the search strategy fails. It may also cause a non-terminating sequence of rewrites, depending on the search strategy used.

Uses

This rule is used in the system to implement all other rewriting rules, and may provide a user with a method to fine-tune rewriting of theorems.

Example

Suppose we have a theorem of the form:

$$\text{thm} = |- (1 + 2) + 3 = (3 + 1) + 2$$

and we would like to rewrite the left-hand side with the theorem ADD_SYM without changing the right hand side. This can be done by using:

```
GEN_REWRITE_RULE (RATOR_CONV o ONCE_DEPTH_CONV) [] [ADD_SYM] mythm
```

Other rules, such as ONCE_REWRITE_RULE, would match and substitute on both sides, which would not be the desirable result.

As another example, REWRITE_RULE could be implemented as

```
GEN_REWRITE_RULE TOP_DEPTH_CONV basic_rewrites
```

which specifies that matches should be searched recursively starting from the whole term of the theorem, and basic_rewrites must be added to the user defined set of theorems employed in rewriting.

See also

Rewrite.ASM_REWRITE_RULE, Rewrite.FILTER_ASM_REWRITE_RULE,
Rewrite.ONCE_REWRITE_RULE, Rewrite.PURE_REWRITE_RULE, Conv.REWR_CONV,
Rewrite.REWRITE_RULE.

GEN_REWRITE_TAC	(Rewrite)
------------------------	------------------

```
GEN_REWRITE_TAC : ((conv -> conv) -> thm list -> thm list -> tactic)
```

Synopsis

Rewrites a goal, selecting terms according to a user-specified strategy.

Description

Distinct rewriting tactics differ in the search strategies used in finding subterms on which to apply substitutions, and the built-in theorems used in rewriting. In the case of `REWRITE_TAC`, this is a recursive traversal starting from the body of the goal's conclusion part, while in the case of `ONCE_REWRITE_TAC`, for example, the search stops as soon as a term on which a substitution is possible is found. `GEN_REWRITE_TAC` allows a user to specify a more complex strategy for rewriting.

The basis of pattern-matching for rewriting is the notion of conversions, through the application of `REWR_CONV`. Conversions are rules for mapping terms with theorems equating the given terms to other semantically equivalent ones.

When attempting to rewrite subterms recursively, the use of conversions (and therefore rewrites) can be automated further by using functions which take a conversion and search for instances at which they are applicable. Examples of these functions are `ONCE_DEPTH_CONV` and `RAND_CONV`. The first argument to `GEN_REWRITE_TAC` is such a function, which specifies a search strategy; i.e. it specifies how subterms (on which substitutions are allowed) should be searched for.

The second and third arguments are lists of theorems used for rewriting. The order in which these are used is not specified. The theorems need not be in equational form: negated terms, say " $\sim t$ ", are transformed into the equivalent equational form " $t = F$ ", while other non-equational theorems with conclusion of form " t " are cast as the corresponding equations " $t = T$ ". Conjunctions are separated into the individual components, which are used as distinct rewrites.

Failure

`GEN_REWRITE_TAC` fails if the search strategy fails. It may also cause a non-terminating sequence of rewrites, depending on the search strategy used. The resulting tactic is invalid when a theorem which matches the goal (and which is thus used for rewriting it with) has a hypothesis which is not alpha-convertible to any of the assumptions of the goal. Applying such an invalid tactic may result in a proof of a theorem which does not correspond to the original goal.

Uses

Detailed control of rewriting strategy, allowing a user to specify a search strategy.

Example

Given a goal such as:

$$?- a - (b + c) = a - (c + b)$$

we may want to rewrite only one side of it with a theorem, say `ADD_SYM`. Rewriting tactics which operate recursively result in divergence; the tactic `ONCE_REWRITE_TAC [ADD_SYM]` rewrites on both sides to produce the following goal:


```
?- a - (c + b) = a - (b + c)
```

as ADD_SYM matches at two positions. To rewrite on only one side of the equation, the following tactic can be used:

```
GEN_REWRITE_TAC (RAND_CONV o ONCE_DEPTH_CONV) [] [ADD_SYM]
```

which produces the desired goal:

```
?- a - (c + b) = a - (c + b)
```

As another example, one can write a tactic which will behave similarly to REWRITE_TAC but will also include ADD_CLAUSES in the set of theorems to use always:

```
let ADD_REWRITE_TAC = GEN_REWRITE_TAC TOP_DEPTH_CONV
                      (ADD_CLAUSES . basic_rewrites) ;;
```

See also

Rewrite.ASM_REWRITE_TAC, Rewrite.GEN_REWRITE_RULE, Rewrite.ONCE_REWRITE_TAC, Rewrite.PURE_REWRITE_TAC, Conv.REWR_CONV, Rewrite.REWRITE_TAC.

GEN_TAC	(Tactic)
---------	----------

GEN_TAC : tactic

Synopsis

Strips the outermost universal quantifier from the conclusion of a goal.

Description

When applied to a goal $A \text{ ?- } !x. t$, the tactic GEN_TAC reduces it to $A \text{ ?- } t[x'/x]$ where x' is a variant of x chosen to avoid clashing with any variables free in the goal's assumption list. Normally x' is just x .

```
A ?- !x. t
===== GEN_TAC
A ?- t[x'/x]
```

Failure

Fails unless the goal's conclusion is universally quantified.

Uses

The tactic `REPEAT GEN_TAC` strips away any universal quantifiers, and is commonly used before tactics relying on the underlying term structure.

See also

`Tactic.FILTER_GEN_TAC`, `Thm.GEN`, `Thm.GENL`, `Drule.GEN_ALL`, `Thm.SPEC`, `Drule.SPECL`, `Drule.SPEC_ALL`, `Tactic.SPEC_TAC`, `Tactic.STRIP_TAC`, `Tactic.X_GEN_TAC`.

<code>gen_tyvar</code>	(Type)
------------------------	--------

```
gen_tyvar : unit -> hol_type
```

Synopsis

Generate a fresh type variable

Description

An invocation `gen_tyvar()` generates a type variable `tyv` not seen in the current session. Furthermore, the concrete syntax of `tyv` is such that `tyv` is not obtainable by `mk_vartype`, or by parsing.

Failure

Never fails.

Example

```
- gen_tyvar();
> val it = ':%gen_tyvar%1' : hol_type

- try Type ':%gen_tyvar%1';
```

Exception raised at `Parse.hol_type` parser:

Couldn't make any sense with remaining input of `:%gen_tyvar%1"`

```
- try mk_vartype "%gen_tyvar%1";
```

Exception raised at `Type.mk_vartype`:

incorrect syntax

Comments

In general, the actual name returned by `gen_tyvar` should not be relied on.

Uses

Useful for coding some proof procedures.

See also

`Term.genvar`, `Term.variant`.

<div data-bbox="161 721 285 770" data-label="Text">GENL</div>	<div data-bbox="1182 719 1331 772" data-label="Text">(Thm)</div>
---	--

`GENL : term list -> thm -> thm`

Synopsis

Generalizes zero or more variables in the conclusion of a theorem.

Description

When applied to a term list $[x_1, \dots, x_n]$ and a theorem $A \vdash t$, the inference rule `GENL` returns the theorem $A \vdash !x_1 \dots x_n. t$, provided none of the variables x_i are free in any of the assumptions. It is not necessary that any or all of the x_i should be free in t .

$$\frac{A \vdash t}{A \vdash !x_1 \dots x_n. t} \text{ GENL } [x_1, \dots, x_n] \quad [\text{where no } x_i \text{ is free in } A]$$

Failure

Fails unless all the terms in the list are variables, none of which are free in the assumption list.

See also

`Thm.GEN`, `Drule.GEN_ALL`, `Tactic.GEN_TAC`, `Thm.SPEC`, `Drule.SPECL`, `Drule.SPEC_ALL`, `Tactic.SPEC_TAC`.

<div data-bbox="161 1814 512 1868" data-label="Text">GENLIST_CONV</div>	<div data-bbox="1067 1814 1331 1868" data-label="Text">(listLib)</div>
---	--

`GENLIST_CONV : conv`

Synopsis

Computes by inference the result of generating a list from a function.

Description

For an arbitrary function f , numeral constant n and conversion to evaluate f , conv the result of evaluating

```
GENLIST_CONV conv (--'GENLIST f n'--)
```

is the theorem

```
|- GENLIST f x = [x0;x1...xi...x(n-1)]
```

where each x_i is the result of evaluating $\text{conv} (--'f i'--)$

Example

Evaluating $\text{GENLIST_CONV BETA_CONV} (--'GENLIST (\backslash n . n) 4'--)$ will return the following theorem:

```
|- GENLIST (\backslash n . n) 4 = [0; 1; 2; 3]
```

Failure

GENLIST_CONV tm fails if tm is not of the form described above, or if any call $\text{conv} (--'f i'--)$ fails.

<div data-bbox="234 1290 416 1341" data-label="Text"> <p><code>genvar</code></p> </div>	<div data-bbox="1230 1283 1410 1337" data-label="Text"> <p>(Term)</p> </div>
---	--

`genvar` : type -> term

Synopsis

Returns a variable whose name has not been used previously.

Description

When given a type, `genvar` returns a variable of that type whose name has not been used for a variable or constant in the HOL session so far.

Failure

Never fails.

Example

The following indicates the typical stylized form of the names (this should not be relied on, of course):

```

- genvar bool;
> val it = '%%genvar%%1380' : term

- genvar (Type ':num');
> val it = '%%genvar%%1381' : term

```

Note that one can anticipate `genvar`:

```

- mk_var("%%genvar%%1382",bool);
> val it = '%%genvar%%1382' : term

- genvar bool;
> val it = '%%genvar%%1382' : term

```

This shortcoming could be guarded against, but it doesn't seem worth it currently. It doesn't seem to affect the soundness of the implementation of HOL; at worst, a proof procedure may fail because it doesn't have a sufficiently fresh variable.

Uses

The unique variables are useful in writing derived rules, for specializing terms without having to worry about such things as free variable capture. If the names are to be visible to a typical user, the function `variant` can provide rather more meaningful names.

See also

`Drule.GSPEC`, `Term.variant`.

<div data-bbox="161 1359 368 1415" data-label="Text"> <p>genvars</p> </div>	<div data-bbox="1155 1355 1331 1411" data-label="Text"> <p>(Term)</p> </div>
--	--

```
genvars : hol_type -> int -> term list
```

Synopsis

Generate a specified number of fresh variables.

Description

An invocation `genvars ty n` will invoke `genvar` `n` times and return the resulting list of variables.

Failure

Never fails. If `n` is less-than-or-equal to zero, the empty list is returned.

Example

```
- genvars alpha 3;
> val it = ['%genvar%%1558', '%genvar%%1559', '%genvar%%1560'] : term list
```

See also

Term.genvar, Term.mk_var.

genvarstruct

(pairSyntax)

genvarstruct : hol_type -> term

Synopsis

Returns a pair structure of variables whose names have not been previously used.

Description

When given a product type, genvarstruct returns a paired structure of variables whose names have not been used for variables or constants in the HOL session so far. The structure of the term returned will be identical to the structure of the argument.

Failure

Never fails.

Example

The following example illustrates the behaviour of genvarstruct:

```
- genvarstruct (type_of (Term '((1,2),(x:'a,x:'a))'));
> val it = '((%genvar%%1535,%genvar%%1536),%genvar%%1537,%genvar%%1538)'
      : term
```

Uses

Unique variables are useful in writing derived rules, for specializing terms without having to worry about such things as free variable capture. It is often important in such rules to keep the same structure. If not, genvar will be adequate. If the names are to be visible to a typical user, the function pvariant can provide rather more meaningful names.

See also

Term.genvar, PairRules.GPSPEC, pairSyntax.pvariant.

get_flag_abs	(holCheckLib)
--------------	---------------

```
get_flag_abs : model -> bool
```

Synopsis

Returns whether or not HolCheck will attempt abstraction when checking this model.

See also

holCheckLib.holCheck, holCheckLib.set_flag_abs.

get_flag_ric	(holCheckLib)
--------------	---------------

```
get_flag_ric : model -> bool
```

Synopsis

Returns whether or not the transition system for this HolCheck model is synchronous (conjunctive). Throws an exception if this information has not been set.

See also

holCheckLib.holCheck, holCheckLib.set_flag_ric.

get_init	(holCheckLib)
----------	---------------

```
get_init : model -> term
```

Synopsis

Returns the term describing the initial states of the HolCheck model. Throws an exception if no initial states have been set.

See also

holCheckLib.holCheck, holCheckLib.set_init.

<code>get_name</code>	<code>(holCheckLib)</code>
-----------------------	----------------------------

```
get_name : model -> string option
```

Synopsis

Returns the name of the HolCheck model, if one has been set.

See also

`holCheckLib.holCheck`, `holCheckLib.set_name`.

<code>get_props</code>	<code>(holCheckLib)</code>
------------------------	----------------------------

```
get_props : model -> (string * term) list
```

Synopsis

Returns the properties that will be checked for this HolCheck model. Throws an exception if no properties have been set.

See also

`holCheckLib.holCheck`, `holCheckLib.set_props`.

<code>get_results</code>	<code>(holCheckLib)</code>
--------------------------	----------------------------

```
get_results : model -> (term_bdd * thm option * term list option) list option
```

Synopsis

Returns the results of model checking the HolCheck model, if the model has been checked.

Description

The order of results in the list corresponds to the order of properties in the list of properties to be checked for the model. The latter list can be recovered via `holCheckLib.get_props`.

Each result is a triple. the first component contains the BDD representation of the set of states satisfying the property. If the check succeeded, the second component contains a theorem certifying that the property holds in the model i.e. it holds in the initial states. The third component contains a counterexample or witness trace, if one could be recovered.

Example

For the mod-8 counter example used as a running example in the online reference, we obtain the following results for the property that the most significant bit eventually goes high:

```
- holCheckLib.get_results m;
> val it =
  SOME [(<term_bdd>,
        SOME|- CTL_MODEL_SAT ct1KS (C_EF (C_BOOL (B_PROP (\(v0,v1,v2). v2))),
        SOME [“(F,F,F)”, “(T,F,F)”, “(F,T,F)”, “(T,T,F)”, “(F,F,T)”])]
  : (term_bdd * thm option * term list option) list option
```

The first component contains the BDD representation of the set of states satisfying the property. The second component contains a formal theorem certifying the property. The third component contains a witness trace that counts up to 4.

See also

holCheckLib.holCheck, holCheckLib.set_props, holCheckLib.prove_model.

<div data-bbox="159 1326 427 1377" data-label="Text"> <p>get_state</p> </div>	<div data-bbox="957 1321 1331 1373" data-label="Text"> <p>(holCheckLib)</p> </div>
---	--

get_state : model -> term option

Synopsis

Returns the state tuple used internally by HolCheck for this model, if one has been set.

See also

holCheckLib.holCheck, holCheckLib.set_state.

<div data-bbox="159 1818 426 1872" data-label="Text"> <p>get_trans</p> </div>	<div data-bbox="957 1814 1331 1865" data-label="Text"> <p>(holCheckLib)</p> </div>
---	--

get_trans : model -> (string * term) list

Synopsis

Returns a description of the transition system of the HolCheck model. Throws an exception if no transition system has been set.

See also

`holCheckLib.holCheck`, `holCheckLib.set_trans`, `holCheckLib.get_flag_ric`.

<code>get_vord</code>	<code>(holCheckLib)</code>
-----------------------	----------------------------

`get_vord : model -> string list option`

Synopsis

Returns the BDD variable ordering used by HolCheck for this model, if one has been set.

See also

`holCheckLib.holCheck`, `holCheckLib.set_vord`.

<code>GPSPEC</code>	<code>(PairRules)</code>
---------------------	--------------------------

`GPSPEC : (thm -> thm)`

Synopsis

Specializes the conclusion of a theorem with unique pairs.

Description

When applied to a theorem $A \vdash !p_1 \dots p_n. t$, where the number of universally quantified variables may be zero, `GPSPEC` returns $A \vdash t[g_1/p_1] \dots [g_n/p_n]$, where the g_i is paired structures of the same structure as p_i and made up of distinct variables, chosen by `genvar`.

$$\frac{A \vdash !p_1 \dots p_n. t}{A \vdash t[g_1/p_1] \dots [g_n/p_n]} \text{ GPSPEC}$$

Failure

Never fails.

Uses

GPSPEC is useful in writing derived inference rules which need to specialize theorems while avoiding using any variables that may be present elsewhere.

See also

Drule.GSPEC, PairRules.PGEN, PairRules.PGENL, Term.genvar, PairRules.PGEN_TAC, PairRules.PSPEC, PairRules.PSPECL, PairRules.PSPEC_ALL, PairRules.PSPEC_TAC, PairRules.PSPEC_PAIR.

GSPEC	(Drule)
-------	---------

GSPEC : (thm -> thm)

Synopsis

Specializes the conclusion of a theorem with unique variables.

Description

When applied to a theorem $A \vdash !x_1 \dots x_n. t$, where the number of universally quantified variables may be zero, GSPEC returns $A \vdash t[g_1/x_1] \dots [g_n/x_n]$, where the g_i are distinct variable names of the appropriate type, chosen by `genvar`.

$$\frac{A \vdash !x_1 \dots x_n. t}{A \vdash t[g_1/x_1] \dots [g_n/x_n]} \text{ GSPEC}$$
Failure

Never fails.

Uses

GSPEC is useful in writing derived inference rules which need to specialize theorems while avoiding using any variables that may be present elsewhere.

See also

Thm.GEN, Thm.GENL, Term.genvar, Drule.GEN_ALL, Tactic.GEN_TAC, Thm.SPEC, Drule.SPECL, Drule.SPEC_ALL, Tactic.SPEC_TAC.

GSUBST_TAC	(Tactic)
-------------------	-----------------

`GSUBST_TAC : ((term * term) list -> term -> term) -> thm list -> tactic`

Synopsis

Makes term substitutions in a goal using a supplied substitution function.

Description

`GSUBST_TAC` is the basic substitution tactic by means of which other tactics such as `SUBST_OCCS_TAC` and `SUBST_TAC` are defined. Given a list $[(v_1, w_1), \dots, (v_k, w_k)]$ of pairs of terms and a term w , a substitution function replaces occurrences of w_j in w with v_j according to a specific substitution criterion. Such a criterion may be, for example, to substitute all the occurrences or only some selected ones of each w_j in w .

Given a substitution function `sfm`, `GSUBST_TAC sfm [A1|-t1=u1, ..., An|-tn=un] (A, t)` replaces occurrences of t_i in t with u_i according to `sfm`.

$$\frac{A \text{ ?- } t}{\text{===== } \text{GSUBST_TAC sfm [A1|-t1=u1, \dots, An|-tn=un]} \\ A \text{ ?- } t[u_1, \dots, u_n/t_1, \dots, t_n]}$$

The assumptions of the theorems used to substitute with are not added to the assumptions A of the goal, while they are recorded in the proof. If any A_i is not a subset of A (up to alpha-conversion), then `GSUBST_TAC sfm [A1|-t1=u1, ..., An|-tn=un]` results in an invalid tactic.

`GSUBST_TAC` automatically renames bound variables to prevent free variables in u_i becoming bound after substitution.

Failure

`GSUBST_TAC sfm [th1, ..., thn] (A, t)` fails if the conclusion of each theorem in the list is not an equation. No change is made to the goal if the occurrences to be substituted according to the substitution function `sfm` do not appear in t .

Uses

`GSUBST_TAC` is used to define substitution tactics such as `SUBST_OCCS_TAC` and `SUBST_TAC`. It may also provide the user with a tool for tailoring substitution tactics.

See also

`Tactic.SUBST1_TAC`, `Tactic.SUBST_OCCS_TAC`, `Tactic.SUBST_TAC`.

GSYM	(Conv)
------	--------

GSYM : thm -> thm

Synopsis

Reverses the first equation(s) encountered in a top-down search.

Description

The inference rule GSYM reverses the first equation(s) encountered in a top-down search of the conclusion of the argument theorem. An equation will be reversed iff it is not a proper subterm of another equation. If a theorem contains no equations, it will be returned unchanged.

$$\frac{A \mid- \dots(s_1 = s_2)\dots(t_1 = t_2)\dots}{A \mid- \dots(s_2 = s_1)\dots(t_2 = t_1)\dots} \text{ GSYM}$$

Failure

Never fails, and never loops infinitely.

Example

```
- arithmeticTheory.ADD;
> val it = |- (!n. 0 + n = n) /\ (!m n. (SUC m) + n = SUC(m + n)) : thm

- GSYM arithmeticTheory.ADD;
> val it = |- (!n. n = 0 + n) /\ (!m n. SUC(m + n) = (SUC m) + n) : thm
```

See also

Drule.NOT_EQ_SYM, Thm.REFL, Thm.SYM.

GT_CONV	(reduceLib)
---------	-------------

GT_CONV : conv

Synopsis

Proves result of greater-than ordering on two numerals.

Description

If m and n are both numerals (e.g. 0, 1, 2, 3,...), then `GT_CONV "m > n"` returns the theorem:

$$\vdash (m > n) = T$$

if the natural number denoted by m is greater than that denoted by n , or

$$\vdash (m > n) = F$$

otherwise.

Failure

`GT_CONV tm` fails unless tm is of the form " $m > n$ ", where m and n are numerals.

Example

```
#GT_CONV "100 > 10";;
|- 100 > 10 = T
```

```
#GT_CONV "15 > 15";;
|- 15 > 15 = F
```

```
#GT_CONV "11 > 27";;
|- 11 > 27 = F
```

<code>guess_lengths</code>	<code>(wordsLib)</code>
----------------------------	-------------------------

```
guess_lengths : unit -> unit
```

Synopsis

Turns on word length guessing.

Description

A call to `guess_lengths` adds a post-processing stage to the term parser: the function `inst_word_lengths` is used to instantiate type variables that are the return type of `word_concat` and `word_extract`.

Example

```

- load "wordsLib";
...
- show_types := true;
> val it = () : unit
- ``(7 >< 5) a @@ (4 >< 0) a``;
<<HOL message: inventing new type variable names: 'a, 'b, 'c, 'd>>
> val it =
  ``(((7 :num) >< (5 :num)) (a :bool['d]) :bool['a]) @@
    (((4 :num) >< (0 :num)) a :bool['b'])`` : term
- wordsLib.guess_lengths();
> val it = () : unit
- ``(7 >< 5) a @@ (4 >< 0) a``;
<<HOL message: inventing new type variable names: 'a, 'b, 'c, 'd>>
<<HOL message: assigning word length(s): 'a <- 3, 'b <- 5 and 'c <- 8>>
> val it =
  ``(((7 :num) >< (5 :num)) (a :bool['d]) :bool[3]) @@
    (((4 :num) >< (0 :num)) a :bool[5])`` : term
- type_of it;
> val it = ``:bool[8]`` : hol_type

```

See also

wordsLib.inst_word_lengths, wordsLib.notify_word_length_guesses.

HALF_MK_ABS	(Drule)
-------------	---------

HALF_MK_ABS : (thm -> thm)

Synopsis

Converts a function definition to lambda-form.

Description

When applied to a theorem $A \vdash !x. t1\ x = t2$, whose conclusion is a universally quantified equation, HALF_MK_ABS returns the theorem $A \vdash t1 = \lambda x. t2$.

$$\frac{A \vdash !x. t1\ x = t2}{A \vdash t1 = (\lambda x. t2)} \quad \text{HALF_MK_ABS} \quad [\text{where } x \text{ is not free in } t1]$$

Failure

Fails unless the theorem is a singly universally quantified equation whose left-hand side is a function applied to the quantified variable, or if the variable is free in that function.

See also

`Drule.ETA_CONV`, `Drule.MK_ABS`, `Thm.MK_COMB`, `Drule.MK_EXISTS`.

<div data-bbox="234 647 587 696" data-label="Text"> <h2 style="margin: 0;">HALF_MK_PABS</h2> </div>	<div data-bbox="1086 647 1410 696" data-label="Text"> <h2 style="margin: 0;">(PairRules)</h2> </div>
---	--

`HALF_MK_PABS` : (thm -> thm)

Synopsis

Converts a function definition to lambda-form.

Description

When applied to a theorem $A \vdash !p. t1\ p = t2$, whose conclusion is a universally quantified equation, `HALF_MK_PABS` returns the theorem $A \vdash t1 = (\backslash p. t2)$.

$$\frac{A \vdash !p. t1\ p = t2}{A \vdash t1 = (\backslash p. t2)} \quad \text{HALF_MK_PABS} \quad [\text{where } p \text{ is not free in } t1]$$
Failure

Fails unless the theorem is a singly paired universally quantified equation whose left-hand side is a function applied to the quantified pair, or if any of the the variables in the quantified pair is free in that function.

See also

`Drule.HALF_MK_ABS`, `PairRules.PETA_CONV`, `PairRules.MK_PABS`, `PairRules.MK_PEXISTS`.

<div data-bbox="234 1704 360 1751" data-label="Text"> <h2 style="margin: 0;">hash</h2> </div>	<div data-bbox="1260 1704 1410 1751" data-label="Text"> <h2 style="margin: 0;">(Lib)</h2> </div>
---	--

`hash` : int -> string -> int * int -> int

Synopsis

Hash function for strings.

Description

An invocation `hash i s (j,k)` takes an integer `i` and uses that to construct a function that, given a string `s`, will produce values approximately equally distributed among the numbers less than `i`. The argument `j` gives an index in the string to start from. The `k` argument is an accumulator, which is useful when hashing a collection of strings.

Failure

Never fails.

Example

```
- hash 13 "ishkabibble" (0,0);  
> val it = 5 : int
```

Comments

For better results, the `i` parameter should be a prime.

This is probably not an industrial strength hash function.

hidden

(Parse)

```
hidden : string -> bool
```

Synopsis

Checks to see if a given name has been hidden.

Description

A call `hidden c` where `c` is the name of a constant, will check to see if the given name had been hidden by a previous call to `Parse.hide`.

Failure

Never fails.

Comments

The hiding of a constant only affects the quotation parser; the constant is still there in a theory.

See also

`Parse.hide`, `Parse.reveal`.

hide**(Parse)**

```
hide : string -> ({Name : string, Thy : string} list *
                 {Name : string, Thy : string} list)
```

Synopsis

Stops the quotation parser from recognizing a constant.

Description

A call `hide c` where `c` is a string that maps to one or more constants, will prevent the quotation parser from parsing it as such; it will just be parsed as a variable. (A string maps to a set of possible constants because of the possibility of overloading.) The function returns two lists. Both specify constants by way of pairs of strings. The first list is of constants that the string might have mapped to in parsing (specifically, in the `absyn_to_term` stage of parsing), and the second is the list of constants that would have tried to be printed as the string. It is important to note that the two lists need not be the same.

The effect can be reversed by `Parse.update_overload_maps`. The function `reveal` is only the inverse of `hide` if the only constants mapped to by the string all have that string as their names. (These constants will all be in different theories.)

Failure

Never fails.

Comments

The hiding of a constant only affects the quotation parser; the constant is still there in a theory. Further, (re-)defining a string hidden with `hide` will reveal it once more. The `hide` function's effect is temporary; it is not exported with a theory. A more permanent hiding effect is possible with use of the `remove_ovl_mapping` function.

See also

`Parse.hidden`, `Parse.known_constants`, `Parse.remove_ovl_mapping`, `Parse.reveal`, `Parse.set_known_constants`, `Parse.update_overload_maps`.

HO_MATCH_ABBREV_TAC**(Q)**

```
Q.HO_MATCH_ABBREV_TAC : term quotation -> tactic
```

Synopsis

Introduces abbreviations by doing a higher-order match against the goal.

Description

This tactic is just like `Q.MATCH_ABBREV_TAC`, but does a higher-order match against the goal rather than a first order match. See the documentation for `MATCH_ABBREV_TAC` for more details.

Example

The goal

```
?- !n. (n + 1) * (n - 1) = n * n - 1
```

is transformed by `Q.HO_MATCH_ABBREV_TAC '!k. P k'` to

```
Abbrev(P = (\n. (n + 1) * (n - 1) = n * n - 1)) ?- !k. P k
```

Note how the bound variable changes to match that used in the pattern.

See also

`Q.ABBREV_TAC`, `Q.MATCH_ABBREV_TAC`.

Hol_datatype	(bossLib)
--------------	-----------

`Hol_datatype : type quotation -> unit`

Synopsis

Define a concrete datatype.

Description

Many formalizations require the definition of new types. For example, ML-style datatypes are commonly used to model the abstract syntax of programming languages and the state-space of elaborate transition systems. In HOL, such datatypes (at least, those that are inductive, or, alternatively, have a model in an initial algebra) may be specified using the invocation `Hol_datatype <spec>`, where `<spec>` should conform to the following grammar:

```
spec ::= [ <binding> ; ]* <binding>
```

```
binding ::= <ident> = [ <clause> | ]* <clause>
          | <ident> = <| [ <ident> : <type> ; ]* <ident> : <type> |>
```

```

clause ::= <ident>
        | <ident> of [<type> => ]* <type>

```

When a datatype is successfully defined, a number of standard theorems are automatically proved about the new type: the constructors of the type are proved to be injective and disjoint, induction and case analysis theorems are proved, and each type also has a ‘size’ function defined for it. All these theorems are stored in the current theory and added to a database accessed via the functions in `TypeBase`.

The notation used to declare datatypes is, unfortunately, not the same as that of ML. For example, an ML declaration

```

datatype ('a,'b) btree = Leaf of 'a
                       | Node of ('a,'b) btree * 'b * ('a,'b) btree

```

would most likely be declared in HOL as

```

Hol_datatype 'btree = Leaf of 'a
              | Node of btree => 'b => btree'

```

The `=>` notation in a HOL datatype description is intended to replace `*` in an ML datatype description, and highlights the fact that, in HOL, constructors are by default curried. Note also that any type parameters for the new type are not allowed; they are inferred from the right hand side of the binding. The type variables in the specification become arguments to the new type operator in alphabetic order.

When a record type is defined, the parser is adjusted to allow new syntax (appropriate for records), and a number of useful simplification theorems are also proved. The most useful of the latter are automatically stored in the `TypeBase` and can be inspected using the `simpls_of` function. For further details on record types, see the `DESCRIPTION`.

Example

In the following, we shall give an overview of the kinds of types that may be defined by `Hol_datatype`.

To start, enumerated types can be defined as in the following example:

```

Hol_datatype 'enum = A1 | A2 | A3 | A4 | A5
                  | A6 | A7 | A8 | A9 | A10
                  | A11 | A12 | A13 | A14 | A15
                  | A16 | A17 | A18 | A19 | A20
                  | A21 | A22 | A23 | A24 | A25
                  | A26 | A27 | A28 | A29 | A30'

```

Other non-recursive types may be defined as well:

```
Hol_datatype 'foo = N of num
              | B of bool
              | Fn of 'a -> 'b
              | Pr of 'a # 'b'
```

Turning to recursive types, we can define a type of binary trees where the leaves are numbers.

```
- Hol_datatype 'tree = Leaf of num
                | Node of tree => tree'
```

We have already seen a type of binary trees having polymorphic values at internal nodes. This time, we will declare it in "paired" format.

```
Hol_datatype 'tree = Leaf of 'a
              | Node of tree # 'b # tree'
```

This specification seems closer to the declaration that one might make in ML, but is more difficult to deal with in proof than the curried format used above.

The basic syntax of the named lambda calculus is easy to describe:

```
- load "stringTheory";
> val it = () : unit

- Hol_datatype 'lambda = Var of string
                | Const of 'a
                | Comb of lambda => lambda
                | Abs of lambda => lambda'
```

The syntax for 'de Bruijn' terms is roughly similar:

```
Hol_datatype 'dB = Var of string
              | Const of 'a
              | Bound of num
              | Comb of dB => dB
              | Abs of dB'
```

Arbitrarily branching trees may be defined by allowing a node to hold the list of its subtrees. In such a case, leaf nodes do not need to be explicitly declared.

```
Hol_datatype 'ntree = Node of 'a => ntree list'
```

A type of 'first order terms' can be declared as follows:

```
Hol_datatype 'term = Var of string
              | Fnapp of string # term list'
```

Mutally recursive types may also be defined. The following, extracted by Elsa Gunter from the Definition of Standard ML, captures a subset of Core ML.

```
Hol_datatype
  'atexp = var_exp of string
        | let_exp of dec => exp ;

  exp = aexp    of atexp
        | app_exp of exp => atexp
        | fn_exp  of match ;

  match = match  of rule
        | match1 of rule => match ;

  rule = rule of pat => exp ;

  dec = val_dec  of valbind
        | local_dec of dec => dec
        | seq_dec   of dec => dec ;

  valbind = bind  of pat => exp
          | bind1 of pat => exp => valbind
          | rec_bind of valbind ;

  pat = wild_pat
        | var_pat of string'
```

Simple record types may be introduced using the <| ... |> notation.

```
Hol_datatype 'state = <| Reg1 : num; Reg2 : num; Waiting : bool |>'
```

The use of record types may be recursive. For example, the following declaration could be used to formalize a simple file system.

```
Hol_datatype
  'file = Text of string
        | Dir  of directory
  ;
  directory = <| owner : string ;
              files : (string # file) list |>'
```

Failure

Now we address some types that cannot be declared with `Hol_datatype`. In some cases

they cannot exist in HOL at all; in others, the type can be built in the HOL logic, but `Hol.datatype` is not able to make the definition.

First, an empty type is not allowed in HOL, so the following attempt is doomed to fail.

```
Hol_datatype 'foo = A of foo'
```

So called 'nested types', which are occasionally quite useful, cannot at present be built with `Hol.datatype`:

```
Hol_datatype 'btree = Leaf of 'a
              | Node of ('a # 'a) btree'
```

Co-inductive types may not currently be built with `Hol.datatype`:

```
Hol_datatype 'lazylist = Nil
              | Cons of 'a # (one -> lazylist)'
```

This type can however be built in HOL: see `l1istTheory`.

Finally, for cardinality reasons, HOL does not allow the following attempt to model the untyped lambda calculus as a set (note the `->` in the clause for the `Abs` constructor):

```
Hol_datatype 'lambda = Var of string
              | Const of 'a
              | Comb of lambda => lambda
              | Abs of lambda -> lambda'
```

Instead, one would have to build a theory of complete partial orders (or something similar) with which to model the untyped lambda calculus.

Comments

The consequences of an invocation of `Hol.datatype` are stored in the current theory segment and in `TypeBase`. The principal consequences of a datatype definition are the primitive recursion and induction theorems. These provide the ability to define simple functions over the type, and an induction principle for the type. For a type named `ty`, the primitive recursion theorem is stored under `ty_Axiom` and the induction theorem is put under `ty_induction`. Other consequences include the distinctness of constructors (`ty_distinct`), and the injectivity of constructors (`ty_11`). A 'degenerate' version of `ty_induction` is also stored under `ty_nchotomy`: it provides for reasoning by cases on the construction of elements of `ty`. Finally, some special-purpose theorems are stored: `ty_case_cong` gives a congruence theorem for "case" statements on elements of `ty`. These case statements are introduced by `ty_case_def`. Also, a definition of the "size" of the type is added to the current theory, under the name `ty_size_def`.

For example, invoking

```
Hol_datatype 'tree = Leaf of num
              | Node of tree => tree';
```

results in the definitions

```
tree_case_def =
  |- (!f f1 a. case f f1 (Leaf a) = f a) /\
     !f f1 a0 a1. case f f1 (Node a0 a1) = f1 a0 a1

tree_size_def
  |- (!a. tree_size (Leaf a) = 1 + a) /\
     !a0 a1. tree_size (Node a0 a1) = 1 + (tree_size a0 + tree_size a1)
```

being added to the current theory. The following theorems about the datatype are also stored in the current theory.

```
tree_Axiom
  |- !f0 f1.
     ?fn. (!a. fn (Leaf a) = f0 a) /\
          !a0 a1. fn (Node a0 a1) = f1 a0 a1 (fn a0) (fn a1)

tree_induction
  |- !P. (!n. P (Leaf n)) /\
        (!t t0. P t /\ P t0 ==> P (Node t t0))
        ==>
        !t. P t

tree_nchotomy |- !t. (?n. t = Leaf n) \/ ?t' t0. t = Node t' t0

tree_11
  |- (!a a'. (Leaf a = Leaf a') = (a = a')) /\
     !a0 a1 a0' a1'. (Node a0 a1 = Node a0' a1') = (a0=a0') /\ (a1=a1')

tree_distinct |- !a1 a0 a. ~(Leaf a = Node a0 a1)

tree_case_cong
  |- !M M' f f1.
     (M = M') /\
     (!a. (M' = Leaf a) ==> (f a = f' a)) /\
     (!a0 a1. (M' = Node a0 a1) ==> (f1 a0 a1 = f1' a0 a1))
     ==>
     (case f f1 M = case f' f1' M')
```


When a type involving records is defined, many more definitions are made and added to the current theory.

A definition of mutually recursive types results in the above theorems and definitions being added for each of the defined types.

See also

Definition.new_type_definition, TotalDefn.Define, IndDefLib.Hol_reln, TypeBase.

<div data-bbox="159 694 399 748" data-label="Text"> <p>Hol_defn</p> </div>	<div data-bbox="1067 694 1331 748" data-label="Text"> <p>(bossLib)</p> </div>
--	---

Hol_defn : string -> term quotation -> defn

Synopsis

General-purpose function definition facility.

Description

Hol_defn allows one to define functions, recursive functions in particular, while deferring termination issues. Hol_defn should be used when Define or xDefine fails, or when the context required by Define or xDefine is too much.

Hol_defn takes the same arguments as xDefine.

Hol_defn s q automatically constructs termination constraints for the function specified by q, defines the function, derives the specified equations, and proves an induction theorem. All these results are packaged up in the returned defn value. The defn type is best thought of as an intermediate step in the process of deriving the unconstrained equations and induction theorem for the function.

The termination conditions constructed by Hol_defn are for a function that takes a single tuple as an argument. This is an artifact of the way that recursive functions are modelled.

A prettyprinter, which prints out a summary of the known information on the results of Hol_defn, has been installed in the interactive system.

Hol_defn may be found in bossLib and also in Defn.

Failure

Hol_defn s q fails if s is not an alphanumeric identifier.

Hol_defn s q fails if q fails to parse or typecheck.

Hol_defn may extract unsatisfiable termination conditions when asked to define a higher-order recursion involving a higher-order function that the termination condition extraction mechanism of Hol_defn is unaware of.

Example

Here we attempt to define a quick-sort function `qsort`:

```
- Hol_defn "qsort"
  '(qsort ___ [] = []) /\
  (qsort ord (x::rst) =
    APPEND (qsort ord (FILTER ($~ o ord x) rst))
    (x :: qsort ord (FILTER (ord x) rst)))';

<<HOL message: inventing new type variable names: 'a>>
> val it =
  HOL function definition (recursive)

Equation(s) :
  [...]
|- (qsort v0 [] = []) /\
  (qsort ord (x::rst) =
    APPEND (qsort ord (FILTER ($~ o ord x) rst))
    (x::qsort ord (FILTER (ord x) rst)))

Induction :
  [...]
|- !P.
  (!v0. P v0 []) /\
  (!ord x rst.
    P ord (FILTER ($~ o ord x) rst) /\
    P ord (FILTER (ord x) rst) ==> P ord (x::rst))
  ==> !v v1. P v v1

Termination conditions :
0. WF R
1. !rst x ord. R (ord,FILTER ($~ o ord x) rst) (ord,x::rst)
2. !rst x ord. R (ord,FILTER (ord x) rst) (ord,x::rst)
```

In the following we give an example of how to use `Hol_defn` to define a nested recursion. In processing this definition, an auxiliary function `N_aux` is defined. The termination conditions of `N` are phrased in terms of `N_aux` for technical reasons.

```
- Hol_defn "ninety1"
  'N x = if x>100 then x-10
        else N(N(x+11))';
```

```

> val it =
  HOL function definition (nested recursion)

Equation(s) :
  [...] |- N x = (if x > 100 then x - 10 else N (N (x + 11)))

Induction :
  [...]
  |- !P.
    (!x. (~(x > 100) ==> P (x + 11)) /\
      (~(x > 100) ==> P (N (x + 11))) ==> P x)
    ==>
    !v. P v

Termination conditions :
  0. WF R
  1. !x. ~(x > 100) ==> R (x + 11) x
  2. !x. ~(x > 100) ==> R (N_aux R (x + 11)) x

```

Comments

An invocation of `Hol_defn` is usually the first step in a multi-step process that ends with unconstrained recursion equations for a function, along with an induction theorem. `Hol_defn` is used to construct the function and synthesize its termination conditions; next, one invokes `tgoal` to set up a goal to prove termination of the function. The termination proof usually starts with an invocation of `WF_REL_TAC`. After the proof is over, the desired recursion equations and induction theorem are available for further use.

It is occasionally important to understand, at least in part, how `Hol_defn` constructs termination constraints. In some cases, it is necessary for users to influence this process in order to have correct termination constraints extracted. The process is driven by so-called congruence theorems for particular HOL constants. For example, suppose we were interested in defining a ‘destructor-style’ version of the factorial function over natural numbers:

```
fact n = if n=0 then 1 else n * fact (n-1).
```

In the absence of a congruence theorem for the ‘if-then-else’ construct, `Hol_defn` would extract the termination constraints

```

0. WF R
1. !n. R (n - 1) n

```

which are unprovable, because the context of the recursive call has not been taken account of. This example is in fact not a problem for HOL, since the following congruence theorem is known to `Hol_defn`:

```
|- !b b' x x' y y'.
    (b = b') /\
    (b' ==> (x = x')) /\
    (~b' ==> (y = y')) ==>
    ((if b then x else y) = (if b' then x' else y'))
```

This theorem is interpreted by `Hol_defn` as an ordered sequence of instructions to follow when the termination condition extractor hits an ‘if-then-else’. The theorem is read as follows:

When an instance ‘if B then X else Y’ is encountered while the extractor traverses the function definition, do the following:

1. Go into B and extract termination conditions `TCs(B)` from any recursive calls in it. This returns a theorem `TCs(B) |- B = B'`.
2. Assume B' and extract termination conditions from any recursive calls in X. This returns a theorem `TCs(X) |- X = X'`. Each element of `TCs(X)` will have the form "`B' ==> M`".
3. Assume `~B'` and extract termination conditions from any recursive calls in Y. This returns a theorem `TCs(Y) |- Y = Y'`. Each element of `TCs(Y)` will have the form "`~B' ==> M`".
4. By equality reasoning with (1), (2), and (3), derive

```
TCs(B) u TCs(X) u TCs(Y)
|-
(if B then X else Y) = (if B' then X' else Y')
```

5. Replace "if B then X else Y" by "if B' then X' else Y'".

The accumulated termination conditions are propagated until the extraction process finishes, and appear as hypotheses in the final result. In our example, context is properly accounted for in recursive calls under either branch of an ‘if-then-else’. Thus the extracted termination conditions for fact are

- 0. WF R
- 1. !n. ~ (n = 0) ==> R (n - 1) n

and are easy to prove.

Now we discuss congruence theorems for higher-order functions. A ‘higher-order’ recursion is one in which a higher-order function is used to apply the recursive function to arguments. In order for the correct termination conditions to be proved for such a recursion, congruence rules for the higher order function must be known to the termination condition extraction mechanism. Congruence rules for common higher-order functions, e.g., MAP, EVERY, and EXISTS for lists, are already known to the mechanism. However, at times, one must manually prove and install a congruence theorem for a higher-order function.

For example, suppose we define a higher-order function SIGMA for summing the results of a function in a list. We then use SIGMA in the definition of a function for summing the results of a function in a arbitrarily (finitely) branching tree.

```
- Define '(SIGMA f [] = 0) /\
      (SIGMA f (h::t) = f h + SIGMA f t)';

- Hol_datatype 'ltree = Node of 'a => ltree list';
> val it = () : unit

- Defn.Hol_defn
  "ltree_sigma"      (* higher order recursion *)
  'ltree_sigma f (Node v tl) = f v + SIGMA (ltree_sigma f) tl';

> val it =
  HOL function definition (recursive)

Equation(s) :
  [...] |- ltree_sigma f (Node v tl)
          = f v + SIGMA (\a. ltree_sigma f a) tl

Induction :
  [...] |- !P. (!f v tl. (!a. P f a) ==> P f (Node v tl))
          ==> !v v1. P v v1

Termination conditions :
  0. WF R
  1. !tl v f a. R (f,a) (f,Node v tl) : defn
```

The termination conditions for `ltree_sigma` seem to require finding a wellfounded relation R such that the pair (f, a) is R -less than $(f, \text{Node } v \text{ } tl)$. However, this is a hopeless task, since there is no relation between a and $\text{Node } v \text{ } tl$, besides the fact that they are both `ltrees`. The termination condition extractor has not performed properly, because it didn't know a congruence rule for `SIGMA`. Such a congruence theorem is the following:

```
SIGMA_CONG =
|- !l1 l2 f g.
    (l1=l2) /\ (!x. MEM x l2 ==> (f x = g x)) ==>
    (SIGMA f l1 = SIGMA g l2)
```

Once `Hol_defn` has been told about this theorem, via `write_congs`, the termination conditions extracted for the definition are provable, since a is a proper subterm of $\text{Node } v \text{ } tl$.

```
- local open DefnBase
  in
  val _ = write_congs (SIGMA_CONG::read_congs())
  end;

- Defn.Hol_defn
  "ltree_sigma"
  'ltree_sigma f (Node v tl) = f v + SIGMA (ltree_sigma f) tl';

> val it =
  HOL function definition (recursive)

  Equation(s) : ... (* as before *)
  Induction : ... (* as before *)

  Termination conditions :
  0. WF R
  1. !v f tl a. MEM a tl ==> R (f,a) (f,Node v tl)
```

One final point : for every HOL datatype defined by application of `Hol_datatype`, a congruence theorem is automatically proved for the 'case' constant for that type, and stored in the `TypeBase`. For example, the following congruence theorem for `num_case` is stored in the `TypeBase`:

```
|- !f' f b' b M' M.
    (M = M') /\
    ((M' = 0) ==> (b = b')) /\
```

```
(!n. (M' = SUC n) ==> (f n = f' n))
==>
(num_case b f M = num_case b' f' M')
```

This allows the contexts of recursive calls in branches of ‘case’ expressions to be tracked.

See also

Defn.tgoal, Defn.tprove, bossLib.WF_REL_TAC, bossLib.Define, bossLib.xDefine, bossLib.Hol_datatype.

Hol_defn	(Defn)
----------	--------

Hol_defn : string -> term quotation -> thm

Synopsis

Function definition facility.

Description

bossLib.Hol_defn is identical to Defn.Hol_defn.

See also

bossLib.Hol_defn.

HOL_ERR	(Feedback)
---------	------------

HOL_ERR : {message : string, origin_function : string,
 origin_structure : string} -> exn

Synopsis

Standard HOL exception

Description

HOL_ERR is the single exception that HOL functions are expected to raise when they encounter an anomalous situation.

Example

Building an application of HOL_ERR and binding it to an ML variable

```

val test_exn =
  HOL_ERR {origin_structure = "Foo",
           origin_function = "bar",
           message = "incomprehensible input"};

yields

```

```

val test_exn = HOL_ERR : exn

```

One can scrutinize the contents of an application of `HOL_ERR` by pattern matching:

```

- val HOL_ERR r = test_exn;

> val r = {message = "incomprehensible input",
           origin_function = "bar",
           origin_structure = "Foo"}

```

In current ML implementations supporting HOL, exceptions that propagate to the top level without being handled do not print informatively:

```

- raise test_exn;
! Uncaught exception:
! HOL_ERR

```

In such cases, the functions `Raise` and `exn_to_string` can be used to obtain useful information:

```

- Raise test_exn;

Exception raised at Foo.bar:
incomprehensible input
! Uncaught exception:
! HOL_ERR

- print(exn_to_string test_exn);

Exception raised at Foo.bar:
incomprehensible input
> val it = () : unit

```

See also

`Feedback`, `Feedback.error_record`, `Feedback.mk_HOL_ERR`, `Feedback.Raise`, `Feedback.exn_to_string`.

HOL_MESG

(Feedback)

```
HOL_MESG : string -> unit
```

Synopsis

Prints out a message in a special format.

Description

HOL_MESG prints out its argument after formatting it a bit. The formatting is controlled by the function held in `MESG_to_string`, which is `format_MESG` by default. The output stream that the message is printed on is controlled by `MESG_outstream`, and is `TextIO.stdout` by default.

There are three kinds of informative messages that the `Feedback` structure supports: errors, warnings, and messages. Errors are signalled by the raising of an exception built from `HOL_ERR`; warnings, which are printed by `HOL_WARNING`, are less severe than errors, and lead to a warning message being printed; finally, messages have no pejorative weight at all, and may be freely employed, via `HOL_MESG`, to keep users informed in the normal course of processing.

Failure

The invocation fails if the formatting or output routines fail.

Example

```
- HOL_MESG "Ack.";
  <<HOL message: Ack.>>
```

See also

`Feedback`, `Feedback.HOL_ERR`, `Feedback.Raise`, `Feedback.HOL_WARNING`, `Feedback.MESG_to_string`, `Feedback.format_MESG`, `Feedback.MESG_outstream`.

Hol_reln

(bossLib)

```
Hol_reln : term quotation -> (thm * thm * thm)
```

Synopsis

Defines inductive relations.

Description

The `Ho1_reln` function is used to define inductively characterised relations. It takes a term quotation as input and attempts to define the relations there specified. The input term quotation must parse to a term that conforms to the following grammar:

```



```

The `sv1` terms that appear after a constant name are so-called "schematic variables". The same variables must always follow the same constant name throughout the definition. These variables and the names of the constants-to-be must not be quantified over in each `<clause>`. Otherwise, a `<clause>` must not include any free variables. (The universal quantifiers at the head of the clause can be used to bind free variables, but it is also permissible to use existential quantification in the hypotheses. If a clause has no free variables, it is permissible to have no universal quantification.)

The `Ho1_reln` function may be used to define multiple relations. These may or may not be mutually recursive. The clauses for each relation need not be contiguous.

The function returns three theorems. Each is also saved in the current theory segment. The first is a conjunction of implications that will be the same as the input term quotation. This theorem is saved under the name `<stem>_rules`, where `<stem>` is the name of the first relation defined by the function. The second is the induction principle for the relations, saved under the name `<stem>_ind`. The third is the cases theorem for the relations, saved under the name `<stem>_cases`. The cases theorem is of the form

```

(!a0 .. an. R1 a0 .. an = <R1's first rule possibility> \/
                        <R1's second rule possibility> \/ ...)
      /\
(!a0 .. am. R2 a0 .. am = <R2's first rule possibility> \/
                        <R2's second rule possibility> \/ ...)
      /\
...

```

Failure

The `Ho1_reln` function will fail if the provided quotation does not parse to a term of the specified form. It will also fail if a clause's only free variables do not follow a relation name, or if a relation name is followed by differing schematic variables. If the definition principle can not prove that the characterisation is inductive (as would

happen if a hypothesis included a negated occurrence of one of the relation names), then the same theorems are returned, but with extra assumptions stating the required inductive property.

If the name of the new constants are such that they will produce invalid SML identifiers when bound in a theory file, using `export_theory` will fail, and suggest the use of `set_MLname` to fix the problem.

Example

Defining ODD and EVEN:

```
- Hol_reln 'EVEN 0 /\
          (!n. ODD n ==> EVEN (n + 1)) /\
          (!n. EVEN n ==> ODD (n + 1))';
> val it =
  (|- EVEN 0 /\ (!n. ODD n ==> EVEN (n + 1)) /\
    !n. EVEN n ==> ODD (n + 1),

  |- !EVEN' ODD'.
    EVEN' 0 /\ (!n. ODD' n ==> EVEN' (n + 1)) /\
    (!n. EVEN' n ==> ODD' (n + 1)) ==>
    (!a0. EVEN a0 ==> EVEN' a0) /\ !a1. ODD a1 ==> ODD' a1,

  |- (!a0. EVEN a0 = (a0 = 0) \/\
      ?n. (a0 = n + 1) /\ ODD n) /\
    !a1. ODD a1 = ?n. (a1 = n + 1) /\ EVEN n)

  : thm * thm * thm
```

Defining reflexive and transitive closure, using a schematic variable. This is appropriate because it is `RTC R` that has the inductive characterisation, not `RTC` itself.

```
- Hol_reln '(!x. RTC R x x) /\
          (!x z. (?y. R x y /\ RTC R y z) ==> RTC R x z)';
<<HOL message: inventing new type variable names: 'a>>
> val it =
  (|- !R. (!x. RTC R x x) /\
    !x z. (?y. R x y /\ RTC R y z) ==> RTC R x z,

  |- !R RTC'.
    (!x. RTC' x x) /\
    (!x z. (?y. R x y /\ RTC' y z) ==> RTC' x z) ==>
    !a0 a1. RTC R a0 a1 ==> RTC' a0 a1,
```

```

|- !R a0 a1. RTC R a0 a1 =
      (a1 = a0) \ / ?y. R a0 y /\ RTC R y a1)

: thm * thm * thm

```

Comments

Being a definition principle, the `Hol_reln` function takes a quotation rather than a term. The structure `IndDefRules` provides functions for applying the results of an invocation of `Hol_reln`.

See also

`bossLib.Define`, `bossLib.Hol_datatype`, `IndDefRules`.

<code>Hol_reln</code>	<code>(IndDefLib)</code>
-----------------------	--------------------------

`Hol_reln : term quotation -> thm * thm * thm`

Synopsis

Definition facility for inductive predicates.

Description

`bossLib.Hol_reln` is identical to `IndDefLib.Hol_reln`.

See also

`bossLib.Hol_reln`.

<code>hol_type</code>	<code>(Type)</code>
-----------------------	---------------------

`eqtype hol_type`

Synopsis

Type of HOL types.

Description

The ML type `hol_type` represents the type of HOL types.

Comments

Since `hol_type` is an ML eqtype, any two `hol_types` `ty1` and `ty2` can be tested for equality by `ty1 = ty2`.

See also

`Term.term`.

<div data-bbox="159 636 485 685" data-label="Text"> <p>HOL_WARNING</p> </div>	<div data-bbox="1038 636 1331 685" data-label="Text"> <p>(Feedback)</p> </div>
--	---

`HOL_WARNING : string -> string -> string -> unit`

Synopsis

Prints out a message in a special format.

Description

There are three kinds of informative messages that the `Feedback` structure supports: errors, warnings, and messages. Errors are signalled by the raising of an exception built from `HOL_ERR`; warnings, which are printed by `HOL_WARNING`, are less severe than errors, and lead only to a formatted message being printed; finally, messages have no pejorative weight at all, and may be freely employed, via `HOL_MESG`, to keep users informed in the normal course of processing.

`HOL_WARNING` prints out its arguments after formatting them. The formatting is controlled by the function held in `WARNING_to_string`, which is `format_WARNING` by default. The output stream that the message is printed on is controlled by `WARNING_outstream`, and is `TextIO.stdout` by default.

A call `HOL_WARNING s1 s2 s3` is formatted with the assumption that `s1` and `s2` are the names of the module and function, respectively, from which the warning is emitted. The string `s3` is the actual warning message.

Failure

The invocation fails if the formatting or output routines fail.

Example

```
- HOL_WARNING "Module" "function" "stern message.";
<<HOL warning: Module.function: stern message.>>
```

See also

`Feedback`, `Feedback.HOL_ERR`, `Feedback.Raise`, `Feedback.HOL_MESG`, `Feedback.WARNING_to_string`, `Feedback.format_WARNING`, `Feedback.WARNING_outstream`.

holCheck**(holCheckLib)**`holCheck : model -> model`**Synopsis**

Basic symbolic model checker.

Description

User specifies a model by specifying (at least) the initial states, a labelled transition system, and a list of CTL or mu-calculus properties. This model is then passed to the model checker which returns the model with the results of the checking filled in. These can be recovered by calling `get_results` on the returned model and are presented as a list of : the BDD semantics of each property, a theorem if the property holds in the model, and a counterexample or witness trace if appropriate.

Failure

`holCheck` should not fail, except on malformed input e.g. mu-calculus properties that are not well-formed mu-formulas or a supplied state tuple that does not include all state variables etc.

Example

We choose a mod-8 counter as our example, which starts at 0 and counts up to 7, and then loops from 0 again. We wish to show that the most significant bit eventually goes high.

1. Load the HolCheck library:

```
- load "holCheckLib"; open holCheckLib; (* we don't show the output from the "open"
> val it = () : unit
```

2. Specify the labelled transition system as a list of (string, term) pairs, where each string is a transition label and each term represents a transition relation (three booleans required to encode numbers 0-7; next-state variable values indicated by priming; note we expand the xor, since HolCheck requires purely propositional terms) :

```
- val xor_def = Define 'xor x y = (x \ / y) /\ ~(x=y)';
  val TS = List.map (I ## (rhs o concl o (fn tm => REWRITE_CONV [xor_def] tm handle
                                [("v0", '(v0'~v0)'), ("v1", '(v1' = xor v0 v1)'),
                                ("v2", '(v2' = xor v0 v1)')]) : thm)
  Definition has been stored under "xor_def".
> val xor_def = |- !x y. xor x y = (x \ / y) /\ ~(x = y) : thm
> val TS =
```

```

[("v0", "'v0' = ~v0'"), ("v1", "'v1' = (v0 \\/ v1) /\ ~v0'"),
 ("v2", "'v2' = (v0 /\ v1 \\/ v2) /\ ~v0 /\ v1 = v2'")] :
(string * term) list

```

3. Specify the initial states (counter starts at 0):

```

- val S0 = "'~v0 /\ ~v1 /\ ~v2';
> val S0 = "'~v0 /\ ~v1 /\ ~v2' : term

```

4. Specify whether the transitions happen synchronously (it does):

```

- val ric = true;
> val ric = true : bool

```

5. Set up the state tuple:

```

- val state = mk_state S0 TS;
> val state = '(v0,v1,v2)' : term

```

6. Specify a property (there exists a future in which the most significant bit will go high) :

```

- val ctf = ("ef_msb_high", 'C_EF (C_BOOL (B_PROP ^ (pairSyntax.mk_pabs(state, 'v2:bool'
> val ctf = ("ef_msb_high", 'C_EF (C_BOOL (B_PROP (\(v0,v1,v2). v2))' : string * term

```

Note how atomic propositions are represented as functions on the state.

7. Create the model:

```

- val m = ((set_init S0) o (set_trans TS) o (set_flag_ric ric) o (set_state state) o (s
> val m = <model> : model

```

8. Call the model checker:

```

- val m2 = holCheck m;
> val m2 = model : <model>

```

9. Examine the results:

```

- get_results m2;
> val it =
  SOME [(<term_bdd>,
        SOME [.....]
          |- CTL_MODEL_SAT ctfKS (C_EF (C_BOOL (B_PROP (\(v0,v1,v2). v2)))),
        SOME [ ' (~v0,~v1,~v2)', '(v0,~v1,~v2)', '(~v0,v1,~v2)',
              '(v0,v1,~v2)', '(~v0,~v1,v2)' ]]) :
(term_bdd * thm option * term list option) list option

```

The result is a list of triples, one triple per property checked. The first component contains the BDD representation of the set of states satisfying the property. The second component contains a theorem certifying that the property holds in the model i.e. it holds in the initial states. The third contains a witness trace that counts up to 4, at which point v_2 goes high.

Note that since we did not supply a name for the model (via `holCheckLib.set_name`), the system has chosen the default name `ctlKS`, which stands for "CTL Kripke structure", since models are internally represented formally as Kripke structures.

10. Verify the proof:

```
- val m3 = prove_model m2; (* we don't show the prove_model "chatting" messages here *)
> val m3 = <model> : model
```

11. Examine the verified results:

```
- get_results m3;
> val it =
  SOME [(<term_bdd>,
        SOME|- CTL_MODEL_SAT ctlKS (C_EF (C_BOOL (B_PROP (\(v0,v1,v2). v2))))),
        SOME [‘‘(~v0,~v1,~v2)‘‘, ‘‘(v0,~v1,~v2)‘‘, ‘‘(~v0,v1,~v2)‘‘,
              ‘‘(v0,v1,~v2)‘‘, ‘‘(~v0,~v1,v2)‘‘]]] :
  (term_bdd * thm option * term list option) list option
```

Note that the theorem component now has no assumptions. Any assumptions to the `term_bdd` would also have been discharged.

Comments

For more detail, read the section on the `HolCheck` library in the `HOL System Description`.

See also

`holCheckLib.empty_model`, `holCheckLib.get_init`, `holCheckLib.get_trans`,
`holCheckLib.get_flag_ric`, `holCheckLib.get_name`, `holCheckLib.get_vord`,
`holCheckLib.get_state`, `holCheckLib.get_props`, `holCheckLib.get_results`,
`holCheckLib.get_flag_abs`, `holCheckLib.set_init`, `holCheckLib.set_trans`,
`holCheckLib.set_flag_ric`, `holCheckLib.set_name`, `holCheckLib.set_vord`,
`holCheckLib.set_state`, `holCheckLib.set_props`, `holCheckLib.set_flag_abs`,
`holCheckLib.mk_state`, `holCheckLib.prove_model`.

<h1 style="font-size: 2em; margin: 0;">hyp</h1>	<h1 style="font-size: 2em; margin: 0;">(Thm)</h1>
---	---

`hyp : thm -> term list`

Synopsis

Returns the hypotheses of a theorem.

Description

When applied to a theorem $A \vdash \tau$, the function `hyp` returns A , the list of hypotheses of the theorem.

Failure

Never fails.

Comments

The order in which hypotheses are returned can not be relied on.

See also

`Thm.dest_thm`, `Thm.concl`.

I

(Lib)

`I : 'a -> 'a`

Synopsis

Performs identity operation: $I \ x = x$.

Failure

Never fails.

See also

`Lib`, `Lib.##`, `Lib.A`, `Lib.B`, `Lib.C`, `Lib.K`, `Lib.S`, `Lib.W`.

IMAGE_CONV

(pred_setLib)

`IMAGE_CONV : conv -> conv -> conv`

Synopsis

Compute the image of a function on a finite set.

Description

The function `IMAGE_CONV` is a parameterized conversion for computing the image of a function $f:ty_1 \rightarrow ty_2$ on a finite set $\{t_1; \dots; t_n\}$ of type $ty_1 \rightarrow bool$. The first argument to `IMAGE_CONV` is expected to be a conversion that computes the result of applying the function f to each element of this set. When applied to a term $f\ t_i$, this conversion should return a theorem of the form $\vdash (f\ t_i) = r_i$, where r_i is the result of applying the function f to the element t_i . This conversion is used by `IMAGE_CONV` to compute a theorem of the form

$$\vdash \text{IMAGE } f \{t_1; \dots; t_n\} = \{r_1; \dots; r_n\}$$

The second argument to `IMAGE_CONV` is used (optionally) to simplify the resulting image set $\{r_1; \dots; r_n\}$ by removing redundant occurrences of values. This conversion is expected to decide equality of values of the result type ty_2 ; given an equation $e_1 = e_2$, where e_1 and e_2 are terms of type ty_2 , the conversion should return either $\vdash (e_1 = e_2) = T$ or $\vdash (e_1 = e_2) = F$, as appropriate.

Given appropriate conversions `conv1` and `conv2`, the function `IMAGE_CONV` returns a conversion that maps a term of the form `IMAGE f {t1; ...; tn}` to the theorem

$$\vdash \text{IMAGE } f \{t_1; \dots; t_n\} = \{r_j; \dots; r_k\}$$

where `conv1` proves a theorem of the form $\vdash (f\ t_i) = r_i$ for each element t_i of the set $\{t_1; \dots; t_n\}$, and where the set $\{r_j; \dots; r_k\}$ is the smallest subset of $\{r_1; \dots; r_n\}$ such no two elements are alpha-equivalent and `conv2` does not map $r_l = r_m$ to the theorem $\vdash (r_l = r_m) = T$ for any pair of values r_l and r_m in $\{r_j; \dots; r_k\}$. That is, $\{r_j; \dots; r_k\}$ is the set obtained by removing multiple occurrences of values from the set $\{r_1; \dots; r_n\}$, where the equality conversion `conv2` (or alpha-equivalence) is used to determine which pairs of terms in $\{r_1; \dots; r_n\}$ are equal.

Example

The following is a very simple example in which `REFL` is used to construct the result of applying the function f to each element of the set $\{1; 2; 1; 4\}$, and `NO_CONV` is the supplied ‘equality conversion’.

```
- IMAGE_CONV REFL NO_CONV ‘‘IMAGE (f:num->num) {1; 2; 1; 4}‘‘;
> val it =  $\vdash$  IMAGE f {1; 2; 1; 4} = {f 2; f 1; f 4} : thm
```

The result contains only one occurrence of $f\ 1$, even though `NO_CONV` always fails, since `IMAGE_CONV` simplifies the resulting set by removing elements that are redundant up to alpha-equivalence.

For the next example, we construct a conversion that maps `SUC n` for any numeral n to the numeral standing for the successor of n .

```

- fun SUC_CONV tm =
  let open numLib Arbnum
      val n = dest_numeral (rand tm)
      val sucn = mk_numeral (n + one)
  in
    SYM (num_CONV sucn)
  end;

> val SUC_CONV = fn : term -> thm

```

The result is a conversion that inverts num_CONV:

```

- numLib.num_CONV ``4``;
> val it = |- 4 = SUC 3 : thm

- SUC_CONV ``SUC 3``;
> val it = |- SUC 3 = 4 : thm

```

The conversion SUC_CONV can then be used to compute the image of the successor function on a finite set:

```

- IMAGE_CONV SUC_CONV NO_CONV ``IMAGE SUC {1; 2; 1; 4}``;
> val it = |- IMAGE SUC {1; 2; 1; 4} = {3; 2; 5} : thm

```

Note that 2 (= SUC 1) appears only once in the resulting set.

Finally, here is an example of using IMAGE_CONV to compute the image of a paired addition function on a set of pairs of numbers:

```

- IMAGE_CONV (pairLib.PAIRED_BETA_CONV THENC reduceLib.ADD_CONV)
  numLib.REDUCE_CONV
  ``IMAGE (\(n,m).n+m) {(1,2), (3,4), (0,3), (1,3)}``;
> val it = |- IMAGE (\(n,m). n + m) {(1,2); (3,4); (0,3); (1,3)} = {7; 3; 4}

```

Failure

IMAGE_CONV conv1 conv2 fails if applied to a term not of the form IMAGE f {t1;...;tn}. An application of IMAGE_CONV conv1 conv2 to a term IMAGE f {t1;...;tn} fails unless for all ti in the set {t1;...;tn}, evaluating conv1 ``f ti`` returns |- (f ti) = ri for some ri.

IMP_ANTISYM_RULE	(Drule)
------------------	---------

IMP_ANTISYM_RULE : thm -> thm -> thm

Synopsis

Deduces equality of boolean terms from forward and backward implications.

Description

When applied to the theorems $A1 \vdash t1 ==> t2$ and $A2 \vdash t2 ==> t1$, the inference rule `IMP_ANTISYM_RULE` returns the theorem $A1 \cup A2 \vdash t1 = t2$.

$$\frac{A1 \vdash t1 ==> t2 \quad A2 \vdash t2 ==> t1}{A1 \cup A2 \vdash t1 = t2} \text{IMP_ANTISYM_RULE}$$

Failure

Fails unless the theorems supplied are a complementary implicative pair as indicated above.

See also

`Thm.EQ_IMP_RULE`, `Thm.EQ_MP`, `Tactic.EQ_TAC`.

IMP_CANON	(Drule)
------------------	----------------

`IMP_CANON` : (thm -> thm list)

Synopsis

Puts theorem into a ‘canonical’ form.

Description

`IMP_CANON` puts a theorem in ‘canonical’ form by removing quantifiers and breaking apart conjunctions, as well as disjunctions which form the antecedent of implications. It applies the following transformation rules:

$$\frac{A \vdash t1 \wedge t2}{A \vdash t1 \quad A \vdash t2} \quad \frac{A \vdash !x. t}{A \vdash t} \quad \frac{A \vdash (t1 \wedge t2) ==> t}{A \vdash t1 ==> (t2 ==> t)}$$

$$\frac{A \vdash (t1 \vee t2) ==> t}{A \vdash t1 ==> t \quad A \vdash t2 ==> t} \quad \frac{A \vdash (?x. t1) ==> t2}{A \vdash t1[x'/x] ==> t2}$$

Failure

Never fails, but if there is no scope for one of the above reductions, merely gives a list whose only member is the original theorem.

Comments

This is a rather ad-hoc inference rule, and its use is not recommended.

See also

Thm.CONJUNCT1, Thm.CONJUNCT2, Drule.CONJUNCTS, Thm.DISJ1, Thm.DISJ2, Thm.EXISTS, Thm.SPEC.

IMP_CONJ

(Drule)

IMP_CONJ : (thm -> thm -> thm)

Synopsis

Conjoints antecedents and consequents of two implications.

Description

When applied to theorems $A1 \vdash p \implies r$ and $A2 \vdash q \implies s$, the IMP_CONJ inference rule returns the theorem $A1 \cup A2 \vdash p \wedge q \implies r \wedge s$.

$$\frac{A1 \vdash p \implies r \quad A2 \vdash q \implies s}{A1 \cup A2 \vdash p \wedge q \implies r \wedge s} \text{ IMP_CONJ}$$

Failure

Fails unless the conclusions of both theorems are implicative.

See also

Thm.CONJ.

IMP_CONV

(reduceLib)

IMP_CONV : conv

Synopsis

Simplifies certain implicational expressions.

Description

If t_m corresponds to one of the forms given below, where t is an arbitrary term of type `bool`, then `IMP_CONV t_m` returns the corresponding theorem. Note that in the last case the antecedent and consequent need only be alpha-equivalent rather than strictly identical.

```
IMP_CONV "T ==> t" = |- T ==> t = t
IMP_CONV "t ==> T" = |- t ==> T = T
IMP_CONV "F ==> t" = |- F ==> t = T
IMP_CONV "t ==> F" = |- t ==> F = ~t
IMP_CONV "t ==> t" = |- t ==> t = T
```

Failure

`IMP_CONV t_m` fails unless t_m has one of the forms indicated above.

Example

```
#IMP_CONV "T ==> F";;
|- T ==> F = F

#IMP_CONV "F ==> x";;
|- F ==> x = T

#IMP_CONV "(!z:(num)list. z = z) ==> (!x:(num)list. x = x)";;
|- (!z. z = z) ==> (!x. x = x) = T
```

IMP_ELIM	(Drule)
-----------------	----------------

```
IMP_ELIM : (thm -> thm)
```

Synopsis

Transforms `|- s ==> t` into `|- ~ s \ / t` .

Description

When applied to a theorem `A |- s ==> t` , the inference rule `IMP_ELIM` returns the theorem `A |- ~ s \ / t` .

$$\begin{array}{l} A \mid\text{- } s \implies t \\ \text{-----} \quad \text{IMP_ELIM} \\ A \mid\text{- } \sim s \ \backslash / \ t \end{array}$$
Failure

Fails unless the theorem is implicative.

See also

Thm.NOT_INTRO, Thm.NOT_ELIM.

IMP_RES_FORALL_CONV	(res_quanLib)
---------------------	---------------

IMP_RES_FORALL_CONV : conv

Synopsis

Converts an implication to a restricted universal quantification.

Description

When applied to a term of the form $\!x. x \text{ IN } P \implies Q$, the conversion IMP_RES_FORALL_CONV returns the theorem:

$$\mid\text{- } (\!x. x \text{ IN } P \implies Q) = \!x::P. Q$$
Failure

Fails if applied to a term not of the form $\!x. x \text{ IN } P \implies Q$.

See also

res_quanLib.RES_FORALL_CONV.

IMP_RES_FORALL_CONV	(res_quanTools)
---------------------	-----------------

IMP_RES_FORALL_CONV : conv

Synopsis

Converts an implication to a restricted universal quantification.

Description

When applied to a term of the form $\!x.P \ x \implies Q$, the conversion IMP_RES_FORALL_CONV returns the theorem:

$$\text{|- } (!x. P\ x \implies Q) = !x::P. Q$$

Failure

Fails if applied to a term not of the form $!x.P\ x \implies Q$.

See also

`res_quantTools.RES_FORALL_CONV`.

<div data-bbox="237 694 558 745" data-label="Text"> <h1 style="margin: 0;">IMP_RES_TAC</h1> </div>	<div data-bbox="1171 694 1412 745" data-label="Text"> <h1 style="margin: 0;">(Tactic)</h1> </div>
--	---

`IMP_RES_TAC : thm_tactic`

Synopsis

Enriches assumptions by repeatedly resolving an implication with them.

Description

Given a theorem `th`, the theorem-tactic `IMP_RES_TAC` uses `RES_CANON` to derive a canonical list of implications, each of which has the form:

$$A \text{ |- } u_1 \implies u_2 \implies \dots \implies u_n \implies v$$

`IMP_RES_TAC` then tries to repeatedly ‘resolve’ these theorems against the assumptions of a goal by attempting to match the antecedents u_1, u_2, \dots, u_n (in that order) to some assumption of the goal (i.e. to some candidate antecedents among the assumptions). If all the antecedents can be matched to assumptions of the goal, then an instance of the theorem

$$A\ u\ \{a_1, \dots, a_n\} \text{ |- } v$$

called a ‘final resolvent’ is obtained by repeated specialization of the variables in the implicative theorem, type instantiation, and applications of modus ponens. If only the first i antecedents u_1, \dots, u_i can be matched to assumptions and then no further matching is possible, then the final resolvent is an instance of the theorem:

$$A\ u\ \{a_1, \dots, a_i\} \text{ |- } u_{(i+1)} \implies \dots \implies v$$

All the final resolvents obtained in this way (there may be several, since an antecedent u_i may match several assumptions) are added to the assumptions of the goal, in the stripped form produced by using `STRIP_ASSUME_TAC`. If the conclusion of any final resolvent is a contradiction ‘F’ or is alpha-equivalent to the conclusion of the goal, then `IMP_RES_TAC` solves the goal.

Failure

Never fails.

See also

Thm_cont.IMP_RES_THEN, Drule.RES_CANON, Tactic.RES_TAC, Thm_cont.RES_THEN.

IMP_RES_THEN

(Thm_cont)

IMP_RES_THEN : thm_tactical

Synopsis

Resolves an implication with the assumptions of a goal.

Description

The function `IMP_RES_THEN` is the basic building block for resolution in HOL. This is not full higher-order, or even first-order, resolution with unification, but simply one way simultaneous pattern-matching (resulting in term and type instantiation) of the antecedent of an implicative theorem to the conclusion of another theorem (the candidate antecedent).

Given a theorem-tactic `ttac` and a theorem `th`, the theorem-tactical `IMP_RES_THEN` uses `RES_CANON` to derive a canonical list of implications from `th`, each of which has the form:

$$A_i \mid - !x_1 \dots x_n. u_i \implies v_i$$

`IMP_RES_THEN` then produces a tactic that, when applied to a goal $A \ ?- \ g$ attempts to match each antecedent u_i to each assumption $a_j \mid - \ a_j$ in the assumptions A . If the antecedent u_i of any implication matches the conclusion a_j of any assumption, then an instance of the theorem $A_i \ u \ \{a_j\} \mid - \ v_i$, called a ‘resolvent’, is obtained by specialization of the variables x_1, \dots, x_n and type instantiation, followed by an application of modus ponens. There may be more than one canonical implication and each implication is tried against every assumption of the goal, so there may be several resolvents (or, indeed, none).

Tactics are produced using the theorem-tactic `ttac` from all these resolvents (failures of `ttac` at this stage are filtered out) and these tactics are then applied in an unspecified sequence to the goal. That is,

$$\text{IMP_RES_THEN } ttac \ th \ (A \ ?- \ g)$$

has the effect of:

```
MAP EVERY (mapfilter ttac [... , (Ai u {aj} |- vi) , ...]) (A ?- g)
```

where the theorems $A_i \cup \{a_j\} \vdash v_i$ are all the consequences that can be drawn by a (single) matching modus-ponens inference from the assumptions of the goal $A \text{ ?- } g$ and the implications derived from the supplied theorem th . The sequence in which the theorems $A_i \cup \{a_j\} \vdash v_i$ are generated and the corresponding tactics applied is unspecified.

Failure

Evaluating `IMP_RES_THEN ttac th` fails if the supplied theorem th is not an implication, or if no implications can be derived from th by the transformation process described under the entry for `RES_CANON`. Evaluating `IMP_RES_THEN ttac th (A ?- g)` fails if no assumption of the goal $A \text{ ?- } g$ can be resolved with the implication or implications derived from th . Evaluation also fails if there are resolvents, but for every resolvent $A_i \cup \{a_j\} \vdash v_i$ evaluating the application `ttac (A_i u {a_j} |- v_i)` fails—that is, if for every resolvent `ttac` fails to produce a tactic. Finally, failure is propagated if any of the tactics that are produced from the resolvents by `ttac` fails when applied in sequence to the goal.

Example

The following example shows a straightforward use of `IMP_RES_THEN` to infer an equational consequence of the assumptions of a goal, use it once as a substitution in the conclusion of goal, and then ‘throw it away’. Suppose the goal is:

$$a + n = a \text{ ?- } !k. k - n = k$$

By the built-in theorem:

$$\text{ADD_INV_0} = \vdash !m n. (m + n = m) ==> (n = 0)$$

the assumption of this goal implies that n equals 0. A single-step resolution with this theorem followed by substitution:

$$\text{IMP_RES_THEN SUBST1_TAC ADD_INV_0}$$

can therefore be used to reduce the goal to:

$$a + n = a \text{ ?- } !k. k - 0 = k$$

Here, a single resolvent $a + n = a \vdash n = 0$ is obtained by matching the antecedent of `ADD_INV_0` to the assumption of the goal. This is then used to substitute 0 for n in the conclusion of the goal.

See also

`Tactic.IMP_RES_TAC`, `Drule.MATCH_MP`, `Drule.RES_CANON`, `Tactic.RES_TAC`, `Thm.cont.RES_THEN`.

IMP_TRANS

(Drule)

```
IMP_TRANS : (thm -> thm -> thm)
```

Synopsis

Implements the transitivity of implication.

Description

When applied to theorems $A1 \vdash t1 \implies t2$ and $A2 \vdash t2 \implies t3$, the inference rule IMP_TRANS returns the theorem $A1 \cup A2 \vdash t1 \implies t3$.

$$\frac{A1 \vdash t1 \implies t2 \quad A2 \vdash t2 \implies t3}{A1 \cup A2 \vdash t1 \implies t3} \text{ IMP_TRANS}$$

Failure

Fails unless the theorems are both implicative, with the consequent of the first being the same as the antecedent of the second (up to alpha-conversion).

See also

Drule.IMP_ANTISYM_RULE, Thm.SYM, Thm.TRANS.

implication

(boolSyntax)

```
implication : term
```

Synopsis

Constant denoting logical implication.

Description

The ML variable `boolSyntax.implication` is bound to the term `min$==>`.

See also

`boolSyntax.equality`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`,
`boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`,
`boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.negation`,

`boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let_tm`,
`boolSyntax.arb`.

`implicit_rewrites`

(Rewrite)

`implicit_rewrites: unit -> rewrites`

Synopsis

Contains a number of theorems used, by default, in rewriting.

Description

The variable `implicit_rewrites` holds a collection of rewrite rules commonly used to simplify expressions. These rules include the clause for reflexivity:

`|- !x. (x = x) = T`

as well as rules to reason about equality:

`|- !t.
 ((T = t) = t) /\ ((t = T) = t) /\ ((F = t) = ~t) /\ ((t = F) = ~t)`

Negations are manipulated by the following clauses:

`|- (!t. ~~t = t) /\ (~T = F) /\ (~F = T)`

The set of tautologies includes truth tables for conjunctions, disjunctions, and implications:

`|- !t.
 (T /\ t = t) /\
 (t /\ T = t) /\
 (F /\ t = F) /\
 (t /\ F = F) /\
 (t /\ t = t)`

`|- !t.
 (T \/ t = T) /\
 (t \/ T = T) /\
 (F \/ t = t) /\
 (t \/ F = t) /\
 (t \/ t = t)`

`|- !t.`

```

(T ==> t = t) /\
(t ==> T = T) /\
(F ==> t = T) /\
(t ==> t = T) /\
(t ==> F = ~t)

```

Simple rules for reasoning about conditionals are given by:

```
|- !t1 t2. ((T => t1 | t2) = t1) /\ ((F => t1 | t2) = t2)
```

Rewriting with the following tautologies allows simplification of universally and existentially quantified variables and abstractions:

```

|- !t. (!x. t) = t
|- !t. (?x. t) = t
|- !t1 t2. (\x. t1)t2 = t1

```

The value of `implicit_rewrites` can be augmented by `add_implicit_rewrites` and altered by `set_implicit_rewrites`.

The initial value of `implicit_rewrites` is `bool_rewrites`.

Uses

The rewrite rules held in `implicit_rewrites` are automatically included in the simplifications performed by some of the rewriting tools.

See also

`Rewrite.GEN_REWRITE_RULE`, `Rewrite.GEN_REWRITE_TAC`, `Rewrite.REWRITE_RULE`, `Rewrite.REWRITE_TAC`, `Rewrite.bool_rewrites`, `Rewrite.set_implicit_rewrites`, `Rewrite.add_implicit_rewrites`.

<div data-bbox="162 1529 370 1581" data-label="Text"> <p>IN_CONV</p> </div>	<div data-bbox="957 1529 1331 1588" data-label="Text"> <p>(pred_setLib)</p> </div>
--	--

`IN_CONV` : `conv -> conv`

Synopsis

Decision procedure for membership in finite sets.

Description

The function `IN_CONV` is a parameterized conversion for proving or disproving membership assertions of the general form:

$$t \text{ IN } \{t_1, \dots, t_n\}$$

where $\{t_1; \dots; t_n\}$ is a set of type $ty \rightarrow \text{bool}$ and t is a value of the base type ty . The first argument to `IN_CONV` is expected to be a conversion that decides equality between values of the base type ty . Given an equation $e_1 = e_2$, where e_1 and e_2 are terms of type ty , this conversion should return the theorem $\vdash (e_1 = e_2) = T$ or the theorem $\vdash (e_1 = e_2) = F$, as appropriate.

Given such a conversion, the function `IN_CONV` returns a conversion that maps a term of the form $t \text{ IN } \{t_1; \dots; t_n\}$ to the theorem

$$\vdash t \text{ IN } \{t_1; \dots; t_n\} = T$$

if t is alpha-equivalent to any t_i , or if the supplied conversion proves $\vdash (t = t_i) = T$ for any t_i . If the supplied conversion proves $\vdash (t = t_i) = F$ for every t_i , then the result is the theorem

$$\vdash t \text{ IN } \{t_1; \dots; t_n\} = F$$

In all other cases, `IN_CONV` will fail.

Example

In the following example, the conversion `REDUCE_CONV` is supplied as a parameter and used to test equality of the candidate element 1 with the actual elements of the given set.

```
- IN_CONV REDUCE_CONV ``2 IN {0;SUC 1;3}``;
> val it = |- 2 IN {0; SUC 1; 3} = T : thm
```

The result is `T` because `REDUCE_CONV` is able to prove that 2 is equal to `SUC 1`. An example of a negative result is:

```
- IN_CONV REDUCE_CONV ``1 IN {0;2;3}``;
> val it = |- 1 IN {0; 2; 3} = F : thm
```

Finally the behaviour of the supplied conversion is irrelevant when the value to be tested for membership is alpha-equivalent to an actual element:

```
- IN_CONV NO_CONV ``1 IN {3;2;1}``;
> val it = |- 1 IN {3; 2; 1} = T : thm
```

The conversion `NO_CONV` always fails, but `IN_CONV` is nonetheless able in this case to prove the required result.

Failure

`IN_CONV conv` fails if applied to a term that is not of the form $t \text{ IN } \{t_1; \dots; t_n\}$. A call `IN_CONV conv t IN {t1; ...; tn}` fails unless the term t is alpha-equivalent to some t_i ,

or conv ‘‘t = ti’’ returns $\vdash (t = ti) = T$ for some ti, or conv ‘‘t = ti’’ returns $\vdash (t = ti) = F$ for every ti.

See also

numLib.REDUCE_CONV.

ind

(Type)

ind : hol_type

Synopsis

Basic type constant.

Description

The ML variable Type.ind is bound to the HOL type constant ind. The axiom INFINITY_AX in boolTheory states that ind represents an infinite set of individuals.

See also

Type.bool, Type.-->.

IndDefRules

structure IndDefRules

Synopsis

Tom Melham’s inference support for inductive definitions

Description

IndDefRules provides support for reasoning about inductively defined relations, including a general induction tactic, and an entrypoint for deriving so-called ‘strong’ rule induction.

index

(Lib)

index : ('a -> bool) -> 'a list -> int

Synopsis

Finds index of first list element for which predicate holds.

Description

An application `index P l` returns the index (0-based) to the first element (in a left-to-right scan) of `l` that `P` holds of.

Failure

If `P` doesn't hold of any element of `l`, then `index P l` fails. If `P x` fails for any `x` encountered in the scan, then `index P l` fails.

Example

```
- index (equal 3) [1,2,3];
> val it = 2 : int

- let fun even i = (i mod 2 = 0)
  in try (index even) [1,3,5,7,9]
  end;
```

Exception raised at `Lib.index`:

```
no such element
! Uncaught exception:
! HOL_ERR
```

```
- index (equal 3 o hd) [[1], [], [2,3]];
! Uncaught exception:
! Empty
```

See also

`Lib.el`.

<div data-bbox="237 1697 416 1747" data-label="Text"> <p>Induct</p> </div>	<div data-bbox="1002 1695 1414 1749" data-label="Text"> <p>(BasicProvers)</p> </div>
---	--

`Induct` : tactic

Synopsis

`Induct` on leading universally quantified variable in a goal.

Description

`bossLib.Induct` is identical to `BasicProvers.Induct`.

See also

`bossLib.Induct`.

Induct

(bossLib)

`Induct` : tactic

Synopsis

Performs structural induction over the type of the goal's outermost universally quantified variable.

Description

Given a universally quantified goal, `Induct` attempts to perform an induction based on the type of the leading universally quantified variable. The induction theorem to be used is looked up in the `TypeBase` database, which holds useful facts about the system's defined types. `Induct` may also be used to reason about mutually recursive types.

Failure

`Induct` fails if the goal is not universally quantified, or if the type of the variable universally quantified does not have an induction theorem in the `TypeBase` database.

Example

If attempting to prove

```
!list. LENGTH (REVERSE list) = LENGTH list
```

one can apply `Induct` to begin a proof by induction on `list`.

```
- e Induct;
```

This results in the base and step cases of the induction as new goals.

```
?- LENGTH (REVERSE []) = LENGTH []
```

```
LENGTH (REVERSE list) = LENGTH list
```

```
?- !h. LENGTH (REVERSE (h::list)) = LENGTH (h::list)
```

The same tactic can be used for induction over numbers. For example expanding the goal

```
?- !n. n > 2 ==> !x y z. ~(x EXP n + y EXP n = z EXP n)
```

with `Induct` yields the two goals

```
?- 0 > 2 ==> !x y z. ~(x EXP 0 + y EXP 0 = z EXP 0)
```

```
n > 2 ==> !x y z. ~(x EXP n + y EXP n = z EXP n)
```

```
?- SUC n > 2 ==> !x y z. ~(x EXP SUC n + y EXP SUC n = z EXP SUC n)
```

`Induct` can also be used to perform induction on mutually recursive types. For example, given the datatype

```
Hol_datatype
  'exp = VAR of string          (* variables *)
    | IF of bexp => exp => exp  (* conditional *)
    | APP of string => exp list (* function application *)
  ;
  bexp = EQ of exp => exp       (* boolean expressions *)
    | LEQ of exp => exp
    | AND of bexp => bexp
    | OR of bexp => bexp
    | NOT of bexp'
```

one can use `Induct` to prove that all objects of type `exp` and `bexp` are of a non-zero size. (Recall that size definitions are automatically defined for datatypes.) Typically, mutually recursive types lead to mutually recursive induction schemes having multiple predicates. The scheme for the above definition has 3 predicates: `P0`, `P1`, and `P2`, which respectively range over expressions, boolean expressions, and lists of expressions.

```
|- !P0 P1 P2.
  (!a. P0 (VAR a)) /\
  (!b e e0. P1 b /\ P0 e /\ P0 e0 ==> P0 (IF b e e0)) /\
  (!l. P2 l ==> !b. P0 (APP b l)) /\
  (!e e0. P0 e /\ P0 e0 ==> P1 (EQ e e0)) /\
  (!e e0. P0 e /\ P0 e0 ==> P1 (LEQ e e0)) /\
  (!b b0. P1 b /\ P1 b0 ==> P1 (AND b b0)) /\
  (!b b0. P1 b /\ P1 b0 ==> P1 (OR b b0)) /\
  (!b. P1 b ==> P1 (NOT b)) /\
  P2 [] /\
  (!e l. P0 e /\ P2 l ==> P2 (e::l))
  ==>
  (!e. P0 e) /\ (!b. P1 b) /\ !l. P2 l
```

Invoking `Induct` on a goal such as

```
!e. 0 < exp_size e
```

yields the three subgoals

```
?- !s. 0 < exp_size (APP s l)
```

```
[ 0 < exp_size e, 0 < exp_size e' ] ?- 0 < exp_size (IF b e e')
```

```
?- !s. 0 < exp_size (VAR s)
```

In this case, `P1` and `P2` have been vacuously instantiated in the application of `Induct`, since it detects that only `P0` is needed. However, it is also possible to use `Induct` to start the proofs of

```
(!e. 0 < exp_size e) /\ (!b. 0 < bexp_size b)
```

and

```
(!e. 0 < exp_size e) /\
(!b. 0 < bexp_size b) /\
(!list. 0 < exp1_size list)
```

See also

`bossLib.Induct_on`, `bossLib.completeInduct_on`, `bossLib.measureInduct_on`, `Prim_rec.INDUCT_THEN`, `bossLib.Cases`, `bossLib.Hol_datatype`, `proofManagerLib.g`, `proofManagerLib.e`.

Induct_on

(BasicProvers)

```
Induct_on : term -> tactic
```

Synopsis

Induct on given term.

Description

`bossLib.Induct_on` is identical to `BasicProvers.Induct_on`.

See also

`bossLib.Induct_on`.

<div data-bbox="237 349 502 400" data-label="Text"><code>Induct_on</code></div>	<div data-bbox="1144 349 1412 400" data-label="Text"><code>(bossLib)</code></div>
---	---

```
Induct_on : term -> tactic
```

Synopsis

Performs structural induction, using the type of the given term.

Description

Given a term M , `Induct_on` attempts to perform an induction based on the type of M . The induction theorem to be used is extracted from the `TypeBase` database, which holds useful facts about the system's defined types.

`Induct_on` can be used to specify variables that are buried in the quantifier prefix, i.e., not the leading quantified variable. `Induct_on` can also perform induction on non-variable terms. If M is a non-variable term that does not occur bound in the goal, then `Induct_on` equates M to a new variable v (one not occurring in the goal), moves all hypotheses in which free variables of M occur to the conclusion of the goal, adds the antecedent $v = M$, and quantifies all free variables of M before universally quantifying v and then finally inducting on v .

`Induct_on` may also be used to apply an induction theorem coming from declaration of a mutually recursive datatype.

Failure

`Induct_on` fails if an induction theorem corresponding to the type of M is not found in the `TypeBase` database.

Example

If attempting to prove

```
!x. LENGTH (REVERSE x) = LENGTH x
```

one can apply `Induct_on 'x'` to begin a proof by induction on the list structure of x . In this case, `Induct_on` serves as an explicit version of `Induct`.

See also

`bossLib.Induct`, `bossLib.completeInduct_on`, `bossLib.measureInduct_on`,
`Prim_rec.INDUCT_THEN`, `bossLib.Cases`, `bossLib.Hol_datatype`, `proofManagerLib.g`,
`proofManagerLib.e`.

INDUCT_TAC

(numLib)

INDUCT_TAC : tactic

Synopsis

Performs tactical proof by mathematical induction on the natural numbers.

Description

INDUCT_TAC reduces a goal $!n.P[n]$, where n has type `num`, to two subgoals corresponding to the base and step cases in a proof by mathematical induction on n . The induction hypothesis appears among the assumptions of the subgoal for the step case. The specification of INDUCT_TAC is:

$$\frac{A \text{ ?- } !n. P}{\text{A ?- P[0/n] \quad A u \{P\} \text{ ?- P[SUC n'/n]}} \text{INDUCT_TAC}$$

where n' is a primed variant of n that does not appear free in the assumptions A (usually, n' just equals n). When INDUCT_TAC is applied to a goal of the form $!n.P$, where n does not appear free in P , the subgoals are just $A \text{ ?- } P$ and $A \text{ u } \{P\} \text{ ?- } P$.

Failure

INDUCT_TAC g fails unless the conclusion of the goal g has the form $!n.t$, where the variable n has type `num`.

INDUCT_THEN

(Prim_rec)

INDUCT_THEN : (thm -> thm_tactic -> tactic)

Synopsis

Structural induction tactic for automatically-defined concrete types.

Description

The function INDUCT_THEN implements structural induction tactics for arbitrary concrete recursive types of the kind definable by `define_type`. The first argument to INDUCT_THEN is a structural induction theorem for the concrete type in question. This theorem must have the form of an induction theorem of the kind returned by `prove_induction_thm`.

When applied to such a theorem, the function `INDUCT_THEN` constructs specialized tactic for doing structural induction on the concrete type in question.

The second argument to `INDUCT_THEN` is a function that determines what is to be done with the induction hypotheses in the goal-directed proof by structural induction. Suppose that `th` is a structural induction theorem for a concrete data type `ty`, and that `A ?- !x.P` is a universally-quantified goal in which the variable `x` ranges over values of type `ty`. If the type `ty` has `n` constructors `C1, ..., Cn` and '`Ci(vs)`' represents a (curried) application of the `i`th constructor to a sequence of variables, then if `ttac` is a function that maps the induction hypotheses `hypi` of the `i`th subgoal to the tactic:

$$\frac{A \text{ ?- } P[C_i(vs)/x]}{\text{MAP_EVERY } ttac \text{ hypi}} \\ A1 \text{ ?- } G_i$$

then `INDUCT_THEN th ttac` is an induction tactic that decomposes the goal `A ?- !x.P` into a set of `n` subgoals, one for each constructor, as follows:

$$\frac{A \text{ ?- } !x.P}{A1 \text{ ?- } G1 \quad \dots \quad An \text{ ?- } Gn} \text{INDUCT_THEN } th \text{ } ttac$$

The resulting subgoals correspond to the cases in a structural induction on the variable `x` of type `ty`, with induction hypotheses treated as determined by `ttac`.

Failure

`INDUCT_THEN th ttac g` fails if `th` is not a structural induction theorem of the form returned by `prove_induction_thm`, or if the goal does not have the form `A ?- !x:ty.P` where `ty` is the type for which `th` is the induction theorem, or if `ttac` fails for any subgoal in the induction.

Example

The built-in structural induction theorem for lists is:

```
|- !P. P[] /\ (!t. P t ==> (!h. P(CONS h t))) ==> (!l. P l)
```

When `INDUCT_THEN` is applied to this theorem, it constructs and returns a specialized induction tactic (parameterized by a theorem-tactic) for doing induction on lists:

```
- val LIST_INDUCT_THEN = INDUCT_THEN listTheory.list_INDUCT;
```

The resulting function, when supplied with the `thm_tactic ASSUME_TAC`, returns a tactic that decomposes a goal `?- !l.P[l]` into the base case `?- P[NIL]` and a step case `P[l] ?- !h. P[CONS h l]`, where the induction hypothesis `P[l]` in the step case has been put on the assumption list. That is, the tactic:

```
LIST_INDUCT_THEN ASSUME_TAC
```

does structural induction on lists, putting any induction hypotheses that arise onto the assumption list:

$$\frac{A \text{ ?- } !l. P}{A \text{ |- } P[\text{NIL}/l] \quad A \text{ u } \{P[l'/l]\} \text{ ?- } !h. P[(\text{CONS } h \text{ } l')/l]}$$

Likewise `LIST_INDUCT_THEN STRIP_ASSUME_TAC` will also do induction on lists, but will strip induction hypotheses apart before adding them to the assumptions (this may be useful if P is a conjunction or a disjunction, or is existentially quantified). By contrast, the tactic:

```
LIST_INDUCT_THEN MP_TAC
```

will decompose the goal as follows:

$$\frac{A \text{ ?- } !l. P}{A \text{ |- } P[\text{NIL}/l] \quad A \text{ ?- } P[l'/l] \implies !h. P[(\text{CONS } h \text{ } l')/l]}$$

That is, the induction hypothesis becomes the antecedent of an implication expressing the step case in the induction, rather than an assumption of the step-case subgoal.

See also

`Prim_rec.new_recursive_definition`, `Prim_rec.prove_cases_thm`,
`Prim_rec.prove_constructors_distinct`, `Prim_rec.prove_constructors_one_one`,
`Prim_rec.prove_induction_thm`, `Prim_rec.prove_rec_fn_exists`.

Induct_word	(wordsLib)
-------------	------------

```
Induct_word : tactic
```

Synopsis

Initiate an induction on the value of a word.

Description

The tactic `Induct_word` makes use of the tactic `bossLib.recInduct wordsTheory.WORD_INDUCT`.

Example

Given the goal

```
?- !w:word8. P w
```

one can apply `Induct_word` to begin a proof by induction.

```
- e Induct_word
```

This results in the base and step cases of the induction as new goals.

```
?- P 0w
```

```
[SUC n < 256, P (n2w n)] ?- P (n2w (SUC n))
```

See also

`bossLib.recInduct`.

<div data-bbox="236 918 416 965" data-label="Text"> <h1 style="margin: 0;">insert</h1> </div>	<div data-bbox="1260 913 1414 967" data-label="Text"> <h1 style="margin: 0;">(Lib)</h1> </div>
---	--

```
insert ''a -> ''a list -> ''a list
```

Synopsis

Add an element to a list if it is not already there.

Description

If `x` is already in `list`, then `insert x list` equals `list`. Otherwise, `x` becomes an element of `list`.

Failure

Never fails.

Example

```
- insert 1 [3,2];
> val it = [1, 3, 2] : int list
```

```
- insert 1 it;
> val it = [1, 3, 2] : int list
```

Comments

In some programming situations, it is convenient to implement sets by lists, in which case `insert` may be helpful. However, such an implementation is only suitable for small sets.

A high-performance implementation of finite sets may be found in structure `HOLset`.

ML equality types are used in the implementation of `insert` and its kin. This limits its applicability to types that allow equality. For other types, typically abstract ones, use the ‘op_’ variants.

One should not write code that depends on where the ‘list-as-set’ algorithms place elements in the list which is being considered as a set.

See also

`Lib.op_insert`, `Lib.mem`, `Lib.mk_set`, `Lib.union`, `Lib.U`, `Lib.set_diff`,
`Lib.subtract`, `Lib.intersect`, `Lib.null_intersection`, `Lib.set_eq`.

INSERT_CONV

(pred_setLib)

`INSERT_CONV : conv -> conv`

Synopsis

Reduce `t INSERT {t1;...;t;...;tn}` to `{t1;...;t;...;tn}`.

Description

The function `INSERT_CONV` is a parameterized conversion for reducing finite sets of the form `t INSERT {t1;...;tn}`, where `{t1;...;tn}` is a set of type `ty->bool` and `t` is equal to some element `ti` of this set. The first argument to `INSERT_CONV` is expected to be a conversion that decides equality between values of the base type `ty`. Given an equation `e1 = e2`, where `e1` and `e2` are terms of type `ty`, this conversion should return the theorem `|- (e1 = e2) = T` or the theorem `|- (e1 = e2) = F`, as appropriate.

Given such a conversion, the function `INSERT_CONV` returns a conversion that maps a term of the form `t INSERT {t1;...;tn}` to the theorem

$$|- t \text{ INSERT } \{t_1; \dots; t_n\} = \{t_1; \dots; t_n\}$$

if `t` is alpha-equivalent to any `ti` in the set `{t1, ..., tn}`, or if the supplied conversion proves `|- (t = ti) = T` for any `ti`.

Example

In the following example, the conversion `REDUCE_CONV` is supplied as a parameter and used to test equality of the inserted value 2 with the remaining elements of the set.

```
- INSERT_CONV REDUCE_CONV ‘‘2 INSERT {1;SUC 1;3}‘‘;
> val it = |- {2; 1; SUC 1; 3} = {1; SUC 1; 3} : thm
```

In this example, the supplied conversion `REDUCE_CONV` is able to prove that `2` is equal to `SUC 1` and the set is therefore reduced. Note that `2 INSERT {1; SUC 1; 3}` is just `{2; 1; SUC 1; 3}`.

A call to `INSERT_CONV` fails when the value being inserted is provably not equal to any of the remaining elements:

```
- INSERT_CONV REDUCE_CONV ‘‘1 INSERT {2;3}’’;
! Uncaught exception:
! HOL_ERR
```

But this failure can, if desired, be caught using `TRY_CONV`.

The behaviour of the supplied conversion is irrelevant when the inserted value is alpha-equivalent to one of the remaining elements:

```
- INSERT_CONV NO_CONV ‘‘y INSERT {x;y;z}’’;
> val it = |- {y; x; y; z} = {x; y; z} : thm
```

The conversion `NO_CONV` always fails, but `INSERT_CONV` is nonetheless able in this case to prove the required result.

Note that `DEPTH_CONV(INSERT_CONV conv)` can be used to remove duplicate elements from a finite set, but the following conversion is faster:

```
- fun SETIFY_CONV conv tm =
  (SUB_CONV (SETIFY_CONV conv)
   THENC
   TRY_CONV (INSERT_CONV conv)) tm;
> val SETIFY_CONV = fn : conv -> conv

- SETIFY_CONV REDUCE_CONV ‘‘{1;2;1;3;2;4;3;5;6}’’;
> val it = |- {1; 2; 1; 3; 2; 4; 3; 5; 6} = {1; 2; 4; 3; 5; 6} : thm
```

Failure

`INSERT_CONV conv` fails if applied to a term not of the form `t INSERT {t1; ... ; tn}`. A call `INSERT_CONV conv ‘‘t INSERT {t1; ... ; tn}’’` fails unless `t` is alpha-equivalent to some `ti`, or `conv ‘‘t = ti’’` returns `|- (t = ti) = T` for some `ti`.

See also

`pred_setLib.DELETE_CONV`, `numLib.REDUCE_CONV`.

<code>inst</code>	<code>(Term)</code>
-------------------	---------------------

`inst : (hol_type,hol_type)subst -> term -> term`

Synopsis

Performs type instantiations in a term.

Description

The function `inst` should be used as follows:

```
inst [{redex_1, residue_1}, ..., {redex_n, residue_n}] tm
```

where each ‘redex’ is a `hol_type` variable, and each ‘residue’ is a `hol_type` and `tm` a term to be type-instantiated. This call will replace each occurrence of a `redex` in `tm` by its associated `residue`. Replacement is done in parallel, i.e., once a `redex` has been replaced by its `residue`, at some place in the term, that `residue` at that place will not itself be replaced in the current call. Bound term variables may be renamed in order to preserve the term structure.

Failure

Never fails. A `redex` that is not a variable is simply ignored.

Example

```
- show_types := true;
> val it = () : unit

- inst [alpha |-> Type':num'] (Term'(x:'a) = (x:'a)')
> val it = '(x :num) = x' : term

- inst [bool |-> Type':num'] (Term'x:bool');
> val it = '(x :bool)' : term

- inst [alpha |-> bool] (mk_abs(Term'x:bool',Term'x:'a'))
> val it = '\(x' :bool). (x :bool)' : term
```

See also

`Type.type_subst`, `Lib.|->`.

INST	(Thm)
------	-------

INST : (term,term) subst -> thm -> thm

Synopsis

Instantiates free variables in a theorem.

Description

INST is a rule for substituting arbitrary terms for free variables in a theorem.

$$\begin{array}{c}
 A \mid- t \qquad \text{INST } [x_1 \mid- t_1, \dots, x_n \mid- t_n] \\
 \hline
 A[t_1, \dots, t_n/x_1, \dots, x_n] \\
 \mid- \\
 t[t_1, \dots, t_n/x_1, \dots, x_n]
 \end{array}$$

Failure

Fails if, for $1 \leq i \leq n$, some x_i is not a variable, or if some x_i has a different type than its intended replacement t_i .

Example

In the following example a theorem is instantiated for a specific term:

```

- load"arithmeticTheory";

- CONJUNCT1 arithmeticTheory.ADD_CLAUSES;
> val it = |- 0 + m = m : thm

- INST [‘m:num‘ ‘|-> ‘2*x‘]
      (CONJUNCT1 arithmeticTheory.ADD_CLAUSES);

val it = |- 0 + (2 * x) = 2 * x : thm

```

See also

Drule.INST_TY_TERM, Thm.INST_TYPE, Drule.ISPEC, Drule.ISPECL, Thm.SPEC, Drule.SPECL, Drule.SUBS, Term.subst, Thm.SUBST, Lib.|->.

INST_TY_TERM

(Drule)

```

INST_TY_TERM :
(term,term)subst * (hol_type,hol_type)subst -> thm -> thm

```

Synopsis

Instantiates terms and types of a theorem.

Description

INST_TY_TERM instantiates types in a theorem, in the same way INST_TYPE does. Then it instantiates some or all of the free variables in the resulting theorem, in the same way as INST.

Failure

INST_TY_TERM fails under the same conditions as either INST or INST_TYPE fail.

See also

Thm.INST, Thm.INST_TYPE, Drule.ISPEC, Thm.SPEC, Drule.SUBS, Thm.SUBST.

INST_TYPE	(Thm)
-----------	-------

INST_TYPE : (hol_type,hol_type) subst -> thm -> thm

Synopsis

Instantiates types in a theorem.

Description

INST_TYPE is a primitive rule in the HOL logic, which allows instantiation of type variables.

$$\frac{A \mid- t}{A[ty_1, \dots, tyn/vty_1, \dots, vtyn] \mid- t[ty_1, \dots, tyn/vty_1, \dots, vtyn]} \text{ INST_TYPE}[vty_1 \mid- \rightarrow ty_1, \dots, vtyn \mid- \rightarrow tyn]$$

Type substitution is performed throughout the hypotheses and the conclusion. Variables will be renamed if necessary to prevent distinct bound variables becoming identical after the instantiation.

Failure

Never fails.

Uses

INST_TYPE enables polymorphic theorems to be used at any type.

Example

Supposing one wanted to specialize the theorem EQ_SYM_EQ for particular values, the first attempt could be to use SPECL as follows:

```
- SPECL ['a:num', 'b:num'] EQ_SYM_EQ;
uncaught exception HOL_ERR
```

The failure occurred because `EQ_SYM_EQ` contains polymorphic types. The desired specialization can be obtained by using `INST_TYPE`:

```
- load "numTheory";

- SPECL [Term 'a:num', Term'b:num']
      (INST_TYPE [alpha |-> Type':num'] EQ_SYM_EQ);

> val it = |- (a = b) = (b = a) : thm
```

See also

`Term.inst`, `Thm.INST`, `Drule.INST_TY_TERM`, `Lib.|->`.

inst_word_lengths

(wordsLib)

```
inst_word_lengths : term -> term
```

Synopsis

Guess and instantiate word index type variables in a term.

Description

The function `inst_word_lengths` tries to instantiate type variables that correspond with the return type of `word_concat` and `word_extract`.

Example

```
- load "wordsLib";
...
- wordsLib.inst_word_lengths '(7 >< 5) a @@ (4 >< 0) a'';
<<HOL message: inventing new type variable names: 'a, 'b, 'c, 'd>>
<<HOL message: assigning word length(s): 'a <- 3, 'b <- 5 and 'c <- 8>>
> val it =
  '(((7 :num) >< (5 :num)) (a :bool['d]) :bool[3]) @@
    (((4 :num) >< (0 :num)) a :bool[5])'' : term
- type_of it;
> val it = '' :bool[8]'' : hol_type
```

Comments

The function `guess_lengths` adds `inst_word_lengths` as a post-processing stage to the term parser.

See also

`wordsLib.guess_lengths`, `wordsLib.notify_word_length_guesses`.

<div data-bbox="162 663 596 714" data-label="Text"> <p><code>INSTANCE_T_CONV</code></p> </div>	<div data-bbox="1125 663 1331 714" data-label="Text"> <p><code>(Arith)</code></p> </div>
--	--

```
INSTANCE_T_CONV : ((term -> term list) -> conv -> conv)
```

Synopsis

Function which allows a proof procedure to work on substitution instances of terms that are in the domain of the procedure.

Description

This function generalises a conversion that is used to prove formulae true. It does this by first replacing any syntactically unacceptable subterms with variables. It then attempts to prove the resulting generalised formula and if successful it re-instantiates the variables.

The first argument should be a function which computes a list of subterms of a term which are syntactically unacceptable to the proof procedure. This function should include in its result any variables that do not appear in other subterms returned. The second argument is the proof procedure to be generalised; this should be a conversion which when successful returns an equation between the argument formula and `T` (true).

Failure

Fails if either of the applications of the argument functions fail, or if the conversion does not return an equation of the correct form.

Example

```
#FORALL_ARITH_CONV "!f m (n:num). (m < (f n)) ==> (m <= (f n))";;
evaluation failed      FORALL_ARITH_CONV -- formula not in the allowed subset

#INSTANCE_T_CONV non_presburger_subterms FORALL_ARITH_CONV
# "!f m (n:num). (m < (f n)) ==> (m <= (f n))";;
|- (!f m n. m < (f n) ==> m <= (f n)) = T
```

int_sort**(Lib)**

```
int_sort : int list -> int list
```

Synopsis

Sorts a list of integers using the \leq relation.

Description

The call `int_sort list` is equal to `sort (curry (op <=))`. That is, it is the specialization of `sort` to the usual notion of less-than-or-equal on ML integers.

Failure

Never fails.

Example

A simple example is:

```
- int_sort [3, 1, 4, 1, 5, 9, 2, 6, 5, 3, 5, 8, 9, 7, 9];  
> val it = [1, 1, 2, 3, 3, 4, 5, 5, 5, 6, 7, 8, 9, 9, 9] : int list
```

Comments

The Standard ML Basis Library also provides implementations of sorting.

See also

`Lib.sort`.

int_to_string**(Lib)**

```
int_to_string : int -> string
```

Synopsis

Translates an integer into a string.

Description

An application `int_to_string i` returns the printable form of `i`.

Failure

Never fails.

Example


```
- int_to_string 12323;
> val it = "12323" : string

- int_to_string ~1;
> val it = "~1" : string
```

Comments

Equivalent functionality can be found in the Standard ML Basis Library function `Int.toString`.

See also

`Lib.string_to_int`.

<code>intersect</code>

<code>(Lib)</code>

```
intersect : 'a list -> 'a list -> 'a list
```

Synopsis

Computes the intersection of two ‘sets’.

Description

`intersect l1 l2` returns a list consisting of those elements of `l1` that also appear in `l2`.

Failure

Never fails.

Example

```
- intersect [1,2,3] [3,5,4,1];
> val it = [1, 3] : int list
```

Comments

Do not make the assumption that the order of items in the list returned by `intersect` is fixed. Later implementations may use different algorithms, and return a different concrete result while still meeting the specification.

A high-performance implementation of finite sets may be found in structure `HOLset`.

ML equality types are used in the implementation of `intersect` and its kin. This limits its applicability to types that allow equality. For other types, typically abstract ones, use the ‘`op_`’ variants.

See also

Lib.op_intersect, Lib.union, Lib.U, Lib.mk_set, Lib.mem, Lib.insert, Lib.set_eq, Lib.set_diff.

IPSPEC	(PairRules)
---------------	--------------------

IPSPEC : (term -> thm -> thm)

Synopsis

Specializes a theorem, with type instantiation if necessary.

Description

This rule specializes a paired quantification as does PSPEC; it differs from it in also instantiating the type if needed:

$$\frac{A \mid- !p:ty.tm}{A \mid- tm[q/p]} \quad \text{IPSPEC "q:ty'"}$$

(where q is free for p in tm , and ty' is an instance of ty).

Failure

IPSPEC fails if the input theorem is not universally quantified, if the type of the given term is not an instance of the type of the quantified variable, or if the type variable is free in the assumptions.

See also

Drule.ISPEC, Drule.INST_TY_TERM, Thm.INST_TYPE, PairRules.IPSPECL, PairRules.PSPEC, DB.match.

IPSPECL	(PairRules)
----------------	--------------------

IPSPECL : (term list -> thm -> thm)

Synopsis

Specializes a theorem zero or more times, with type instantiation if necessary.

Description

IPSPECL is an iterative version of IPSPEC

$$\frac{A \vdash !p_1 \dots p_n. tm}{A \vdash t[q_1, \dots, q_n/p_1, \dots, p_n]} \text{ IPSPECL } ["q_1", \dots, "q_n"]$$

(where q_i is free for p_i in tm).

Failure

IPSPECL fails if the list of terms is longer than the number of quantified variables in the term, if the type instantiation fails, or if the type variable being instantiated is free in the assumptions.

See also

Drule.ISPECL, Thm.INST_TYPE, Drule.INST_TY_TERM, PairRules.IPSPEC, Thm.SPEC, PairRules.PSPECL.

is_abs

(Term)

is_abs : (term -> bool)

Synopsis

Tests a term to see if it is an abstraction.

Description

is_abs "\var. t" returns true. If the term is not an abstraction the result is false.

Failure

Never fails.

See also

Term.mk_abs, Term.dest_abs, Term.is_var, Term.is_const, Term.is_comb.

is_arb

(boolSyntax)

is_arb : term -> bool

Synopsis

Tests a term to see if it's an instance of ARB.

Description

Returns `true` if and only if `M` has the form `ARB`.

Uses

None known.

See also

`boolSyntax.mk_arb`, `boolSyntax.dest_arb`.

<code>is_bool_case</code>	<code>(boolSyntax)</code>
---------------------------	---------------------------

```
is_bool_case : term -> bool
```

Synopsis

Tests a case expression over `bool`.

Description

If `M` has the form `bool_case M1 M2 b`, then `is_bool_case M` returns `true`. Otherwise, it returns `false`.

Failure

Never fails.

See also

`boolSyntax.mk_bool_case`, `boolSyntax.dest_bool_case`.

<code>is_comb</code>	<code>(Term)</code>
----------------------	---------------------

```
is_comb : term -> bool
```

Synopsis

Tests a term to see if it is a combination (function application).

Description

If term `M` has the form `f x`, then `is_comb M` equals `true`. Otherwise, the result is `false`.

Failure

Never fails

See also

Term.mk_comb, Term.dest_comb, Term.is_var, Term.is_const, Term.is_abs.

is_cond

(boolSyntax)

is_cond : term -> bool

Synopsis

Tests a term to see if it is a conditional.

Description

If M has the form `if t then t1 else t2` then `is_cond M` returns `true`. If the term is not a conditional the result is `false`.

Failure

Never fails.

See also

boolSyntax.mk_cond, boolSyntax.dest_cond.

is_conj

(boolSyntax)

is_conj : term -> bool

Synopsis

Tests a term to see if it is a conjunction.

Description

If M has the form `t1 /\ t2`, then `is_conj M` returns `true`. If M is not a conjunction the result is `false`.

Failure

Never fails.

See also

`boolSyntax.mk_conj`, `boolSyntax.dest_conj`.

<code>is_cons</code>	<code>(listSyntax)</code>
----------------------	---------------------------

`is_cons` : (term -> bool)

Synopsis

Tests a term to see if it is an application of `CONS`.

Description

`is_cons` returns true of a term representing a non-empty list. Otherwise it returns false.

Failure

Never fails.

See also

`listSyntax.mk_cons`, `listSyntax.dest_cons`, `listSyntax.mk_list`,
`listSyntax.dest_list`, `listSyntax.is_list`.

<code>is_const</code>	<code>(Term)</code>
-----------------------	---------------------

`is_const` : term -> bool

Synopsis

Tests a term to see if it is a constant.

Description

If `c` is an instance of a previously declared HOL constant, then `is_const c` returns true; otherwise the result is false.

Failure

Never fails.

See also

`Term.mk_const`, `Term.dest_const`, `Term.is_var`, `Term.is_comb`, `Term.is_abs`.

is_disj

(boolSyntax)

is_disj : term -> bool

Synopsis

Tests a term to see if it is a disjunction.

Description

If M has the form $t1 \ \vee \ t2$, then `is_disj M` returns `true`. If M is not a disjunction the result is `false`.

Failure

Never fails.

See also

boolSyntax.mk_disj, boolSyntax.dest_disj.

IS_EL_CONV

(listLib)

IS_EL_CONV : conv -> conv

Synopsis

Computes by inference the result of testing whether a list contains a certain element.

Description

IS_EL_CONV takes a conversion `conv` and a term `tm` in the following form:

$$\text{IS_EL } x \ [x_0; \dots; x_n]$$

It returns the theorem

$$\vdash \text{IS_EL } x \ [x_0; \dots; x_n] = F$$

if for every x_i occurred in the list, `conv (--'x = xi'--)` returns a theorem $\vdash P \ x_i = F$, otherwise, if for at least one x_i , evaluating `conv (--'P xi'--)` returns the theorem $\vdash P \ x_i = T$, then it returns the theorem

$$\vdash \text{IS_EL } P \ [x_0; \dots; x_n] = T$$

Failure

`IS_EL_CONV conv tm` fails if `tm` is not of the form described above, or failure occurs when evaluating `conv (--'x = xi'--)` for some `xi`.

Example

Evaluating

```
IS_EL_CONV bool_EQ_CONV (--'IS_EL T [T;F;T]'--);
```

returns the following theorem:

```
|- IS_EL($= T) [F;F] = F
```

See also

`listLib.SOME_EL_CONV`, `listLib.ALL_EL_CONV`, `listLib.FOLDL_CONV`,
`listLib.FOLDR_CONV`, `listLib.list_FOLD_CONV`.

<code>is_eq</code>	<code>(boolSyntax)</code>
--------------------	---------------------------

```
is_eq : term -> bool
```

Synopsis

Tests a term to see if it is an equation.

Description

If `M` has the form `t1 = t2` then `is_eq M` returns `true`. If `M` is not an equation the result is `false`.

Failure

Never fails.

See also

`boolSyntax.mk_eq`, `boolSyntax.dest_eq`.

<code>is_exists</code>	<code>(boolSyntax)</code>
------------------------	---------------------------

```
is_exists : term -> bool
```


Synopsis

Tests a term to see if it is an existential quantification.

Description

If M has the form $?v. t$ then `is_exists M` returns `true`. If the term is not an existential quantification the result is `false`.

Failure

Never fails.

See also

`boolSyntax.mk_exists`, `boolSyntax.dest_exists`.

```
is_exists1
```

```
(boolSyntax)
```

```
is_exists1 : term -> bool
```

Synopsis

Tests a term to see if it is a unique existence term.

Description

If M has the form $?!v. t$ then `is_exists1 M` returns `true`. If the term is not a unique existence quantification the result is `false`.

Failure

Never fails.

See also

`boolSyntax.mk_exists1`, `boolSyntax.dest_exists`.

```
is_forall
```

```
(boolSyntax)
```

```
is_forall : term -> bool
```

Synopsis

Tests a term to see if it is a universal quantification.

Description

If M is a term with the form $\lambda x. t$, then `is_forall M` returns `true`. If M is not a universal quantification the result is `false`.

Failure

Never fails.

See also

`boolSyntax.mk_forall`, `boolSyntax.dest_forall`.

<code>is_gen_tyvar</code>	(Type)
---------------------------	--------

```
is_gen_tyvar : hol_type -> bool
```

Synopsis

Checks if a type variable has been created by `gen_tyvar`.

Failure

Never fails.

Example

```
- is_gen_tyvar (gen_tyvar());
> val it = true : bool
```

```
- is_gen_tyvar bool;
> val it = false : bool
```

See also

`Type.gen_tyvar`.

<code>is_genvar</code>	(Term)
------------------------	--------

```
is_genvar : term -> bool
```

Synopsis

Tells if a variable has been built by invoking `genvar`.

Description

`is_genvar v` attempts to tell if `v` has been created by a call to `genvar`.

Failure

Never fails.

Example

```
- is_genvar (genvar bool);
> val it = true : bool

- is_genvar (mk_var ("%%genvar%%3",bool));
> val it = true : bool
```

Comments

As the second example shows, it is possible to fool `is_genvar`. However, it is useful for derived proof tools which use it as part of their internal operations.

See also

`Term.is_var`, `Term.genvar`, `Type.is_gen_tyvar`, `Type.gen_tyvar`.

`is_imp`

`(boolSyntax)`

```
is_imp : term -> bool
```

Synopsis

Tests a term to see if it is an implication or a negation.

Description

If `M` has the form `t1 ==> t2`, or the form `~t`, then `is_imp M` returns `true`. If the term is neither an implication nor a negation the result is `false`.

Failure

Never fails.

Comments

Yields true of negations because `dest_imp` destructs negations (for backwards compatibility with PPLAMBDA). Use `is_imp_only` if you don't want this behaviour.

See also

`boolSyntax.mk_imp`, `boolSyntax.dest_imp`, `boolSyntax.is_imp_only`,
`boolSyntax.dest_imp_only`.

`is_imp_only``(boolSyntax)`

```
is_imp_only : term -> bool
```

Synopsis

Tests a term to see if it is an implication.

Description

If M has the form $t_1 \implies t_2$ then `is_imp_only M` returns `true`. If the term is not an implication, the result is `false`.

Failure

Never fails.

See also

`boolSyntax.is_imp`, `boolSyntax.mk_imp`, `boolSyntax.dest_imp`,
`boolSyntax.dest_imp_only`, `boolSyntax.list_mk_imp`, `boolSyntax.strip_imp`.

`is_let``(boolSyntax)`

```
is_let : term -> bool
```

Synopsis

Tests a term to see if it is a `let`-expression.

Description

If tm is a term of the form `LET M N`, then `dest_let tm` returns `true`. Otherwise, it returns `false`.

Failure

Never fails.

Example

```
- Term 'LET f x';
<<HOL message: inventing new type variable names: 'a, 'b>>
> val it = 'LET f x' : term

- is_let it;
> val it = true : bool

- is_let (Term 'let x = P /\ Q in x \/ x');
> val it = true : bool
```

See also

boolSyntax.mk_let, boolSyntax.dest_let.

<code>is_list</code>

<code>(listSyntax)</code>

is_list : (term -> bool)

Synopsis

Tests a term to see if it is a list.

Description

is_list returns true of a term representing a list. Otherwise it returns false.

Failure

Never fails.

See also

listSyntax.mk_list, listSyntax.dest_list, listSyntax.mk_cons,
listSyntax.dest_cons, listSyntax.is_cons.

<code>is_neg</code>

<code>(boolSyntax)</code>

is_neg : term -> bool

Synopsis

Tests a term to see if it is a negation.

Description

If M has the form $\sim t$, then `is_neg M` returns `true`. If the term is not a negation the result is `false`.

Failure

Never fails.

See also

`boolSyntax.mk_neg`, `boolSyntax.dest_neg`.

`is_numeral` `(numSyntax)`

```
is_numeral : term -> bool
```

Synopsis

Check if HOL term is a numeral.

Description

An invocation `is_numeral tm`, where tm is a HOL term with the following form

```
<numeral> ::= 0 | NUMERAL <bits>
<bits>    ::= ZERO | BIT1 (<bits>) | BIT2 (<bits>)
```

returns `true`; otherwise, `false` is returned. The `NUMERAL` constant is used as a tag signalling that its argument is indeed a numeric literal. The `ZERO` constant is equal to 0, and $\text{BIT1}(n) = 2 * n + 1$ while $\text{BIT2}(n) = 2 * n + 2$. This representation allows asymptotically efficient operations on numeric values.

The system prettyprinter will print a numeral as a string of digits.

Example

```
- is_numeral ``1234``;
> val it = true : bool
```

Failure

Fails if tm is not in the specified format.

See also

`numSyntax.dest_numeral`, `numSyntax.mk_numeral`.

`is_pabs``(pairSyntax)`

```
is_pabs : term -> bool
```

Synopsis

Tests a term to see if it is a paired abstraction.

Description

`is_pabs "\pair. t"` returns `true`. If the term is not a paired abstraction the result is `false`.

Failure

Never fails.

See also

`Term.is_abs`, `pairSyntax.mk_pabs`, `pairSyntax.dest_pabs`.

`is_pair``(pairSyntax)`

```
is_pair : (term -> bool)
```

Synopsis

Tests a term to see if it is a pair.

Description

`is_pair "(t1,t2)"` returns `true`. If the term is not a pair the result is `false`.

Failure

Never fails.

See also

`pairSyntax.mk_pair`, `pairSyntax.dest_pair`.

`is_pexists``(pairSyntax)`

```
is_pexists : (term -> bool)
```

Synopsis

Tests a term to see if it as a paired existential quantification.

Description

`is_pexists "?pair. t"` returns true. If the term is not a paired existential quantification the result is false.

Failure

Never fails.

See also

`boolSyntax.is_exists`, `pairSyntax.dest_pexists`.

<code>is_pforall</code>	<code>(pairSyntax)</code>
-------------------------	---------------------------

`is_pforall` : (term -> bool)

Synopsis

Tests a term to see if it is a paired universal quantification.

Description

`is_pforall "!pair. t"` returns true. If the term is not a a paired universal quantification the result is false.

Failure

Never fails.

See also

`boolSyntax.is_forall`, `pairSyntax.dest_pforall`.

<code>is_prenex</code>	<code>(Arith)</code>
------------------------	----------------------

`is_prenex` : (term -> bool)

Synopsis

Determines whether a formula is in prenex normal form.

Description

This function returns true if the term it is given as argument is in prenex normal form. If the term is not a formula the result will be true provided there are no nested Boolean expressions involving quantifiers.

Failure

Never fails.

Example

```
#is_prenex "!x. ?y. x \\/ y";;
true : bool
```

```
#is_prenex "!x. x ==> (?y. x /\ y)";;
false : bool
```

Uses

Useful for determining whether it is necessary to apply a prenex normaliser to a formula before passing it to a function which requires the formula to be in prenex normal form.

See also

Arith.PRENEX_CONV.

<div data-bbox="161 1254 539 1310" data-label="Text"> <p>is_presburger</p> </div>	<div data-bbox="1125 1254 1331 1305" data-label="Text"> <p>(Arith)</p> </div>
---	---

is_presburger : (term -> bool)

Synopsis

Determines whether a formula is in the Presburger subset of arithmetic.

Description

This function returns true if the argument term is a formula in the Presburger subset of natural number arithmetic. Presburger natural arithmetic is the subset of arithmetic formulae made up from natural number constants, numeric variables, addition, multiplication by a constant, the natural number relations $<$, $<=$, $=$, $>=$, $>$ and the logical connectives \sim , \wedge , \vee , $==>$, $=$ (if-and-only-if), $!$ ('forall') and $?$ ('there exists').

Products of two expressions which both contain variables are not included in the subset, but the function `SUC` which is not normally included in a specification of Presburger arithmetic is allowed in this HOL implementation. This function also considers subtraction and the predecessor function, `PRE`, to be part of the subset.

Failure

Never fails.

Example

```
#is_presburger "!m n p. m < (2 * n) /\ (n + n) <= p ==> m < SUC p";;
true : bool
```

```
#is_presburger "!m n p q. m < (n * p) /\ (n * p) < q ==> m < q";;
false : bool
```

```
#is_presburger "(m <= n) ==> !p. (m < SUC(n + p))";;
true : bool
```

```
#is_presburger "(m + n) - m = n";;
true : bool
```

Uses

Useful for determining whether a decision procedure for Presburger arithmetic is applicable to a term.

See also

Arith.non_presburger_subterms, Arith.FORALL_ARITH_CONV, Arith.EXISTS_ARITH_CONV, Arith.is_prenex.

<div data-bbox="236 1366 448 1424" data-label="Text"> <p><code>is_prod</code></p> </div>	<div data-bbox="1058 1366 1412 1424" data-label="Text"> <p><code>(pairSyntax)</code></p> </div>
--	---

```
is_prod : hol_type -> bool
```

Synopsis

Tests a type to see if it is a product type.

Description

If `ty` is a type of the form `ty1 # ty2`, then `is_prod ty` returns true.

Failure

Never fails.

See also

`pairSyntax.dest_prod`, `pairSyntax.mk_prod`.

is_pselect

(pairSyntax)

```
is_pselect : (term -> bool)
```

Synopsis

Tests a term to see if it is a paired choice-term.

Description

`is_select "@pair. t"` returns true. If the term is not a paired choice-term the result is false.

Failure

Never fails.

See also

`boolSyntax.is_select`, `pairSyntax.dest_pselect`.

is_ptree

(patriciaLib)

```
is_ptree : term -> bool
```

Synopsis

Term recogniser for Patricia trees.

Description

The destructor `is_ptree` will return true if, and only if, the supplied term is a well-constructed, ground Patricia tree.

Example

```
- is_ptree 't:unit ptree';  
val it = false: bool
```

```
- is_ptree 'Branch 1 2 (Leaf 2 2) (Leaf 3 3)';  
val it = false: bool
```

```
- is_ptree 'Branch 0 0 (Leaf 1 1) (Leaf 2 2)';  
val it = true: bool
```

See also

patriciaLib.mk_ptree, patriciaLib.dest_ptree.

<div data-bbox="236 495 445 551" data-label="Text"> <p><code>is_pvar</code></p> </div>	<div data-bbox="1059 495 1414 551" data-label="Text"> <p><code>(pairSyntax)</code></p> </div>
--	---

`is_pvar : (term -> bool)`

Synopsis

Tests a term to see if it is a paired structure of variables.

Description

`is_pvar "pvar"` returns true iff `pvar` is a paired structure of variables. For example, `((a:*,b:*), (d:*,e:*))` is a paired structure of variables, `(1,2)` is not.

Failure

Never fails.

See also

`Term.is_var`.

<div data-bbox="236 1308 673 1359" data-label="Text"> <p><code>is_res_abstract</code></p> </div>	<div data-bbox="1029 1308 1414 1364" data-label="Text"> <p><code>(res_quanLib)</code></p> </div>
--	--

`is_res_abstract : term -> bool`

Synopsis

Tests a term to see if it is a restricted abstraction.

Description

`is_res_abstract "\var::P. t"` returns true. If the term is not a restricted abstraction the result is false.

Failure

Never fails.

See also

`res_quanLib.mk_res_abstract`, `res_quanLib.dest_res_abstract`.

is_res_abstract	(res_quantTools)
-----------------	------------------

is_res_abstract : (term -> bool)

Synopsis

Tests a term to see if it is a restricted abstraction.

Description

is_res_abstract "\var::P. t" returns true. If the term is not a restricted abstraction the result is false.

Failure

Never fails.

See also

res_quantTools.mk_res_abstract, res_quantTools.dest_res_abstract.

is_res_exists	(res_quantLib)
---------------	----------------

is_res_exists : term -> bool

Synopsis

Tests a term to see if it is a restricted existential quantification.

Description

is_res_exists "?var::P. t" returns true. If the term is not a restricted existential quantification the result is false.

Failure

Never fails.

See also

res_quantLib.mk_res_exists, res_quantLib.dest_res_exists.

is_res_exists	(res_quantTools)
---------------	------------------

is_res_exists : (term -> bool)

Synopsis

Tests a term to see if it is a restricted existential quantification.

Description

`is_res_exists "?var::P. t"` returns true. If the term is not a restricted existential quantification the result is false.

Failure

Never fails.

See also

`res_quantTools.mk_res_exists`, `res_quantTools.dest_res_exists`.

<code>is_res_exists_unique</code>	<code>(res_quantLib)</code>
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`is_res_exists_unique : term -> bool`

Synopsis

Tests a term to see if it is a restricted unique existential quantification.

Description

`is_res_exists_unique "?!var::P. t"` returns true. If the term is not a restricted unique existential quantification the result is false.

Failure

Never fails.

See also

`res_quantLib.mk_res_exists_unique`, `res_quantLib.dest_res_exists_unique`.

<code>is_res_forall</code>	<code>(res_quantLib)</code>
----------------------------	-----------------------------

`is_res_forall : term -> bool`

Synopsis

Tests a term to see if it is a restricted universal quantification.

Description

is_res_forall "!var::P. t" returns true. If the term is not a restricted universal quantification the result is false.

Failure

Never fails.

See also

res_quanLib.mk_res_forall, res_quanLib.dest_res_forall.

is_res_forall	(res_quanTools)
---------------	-----------------

is_res_forall : (term -> bool)

Synopsis

Tests a term to see if it is a restricted universal quantification.

Description

is_res_forall "!var::P. t" returns true. If the term is not a restricted universal quantification the result is false.

Failure

Never fails.

See also

res_quanTools.mk_res_forall, res_quanTools.dest_res_forall.

is_res_select	(res_quanLib)
---------------	---------------

is_res_select : term -> bool

Synopsis

Tests a term to see if it is a restricted choice quantification.

Description

is_res_select "@var::P. t" returns true. If the term is not a restricted choice quantification the result is false.

Failure

Never fails.

See also

`res_quanLib.mk_res_select`, `res_quanLib.dest_res_select`.

<code>is_res_select</code>	<code>(res_quanTools)</code>
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`is_res_select` : (term -> bool)

Synopsis

Tests a term to see if it is a restricted choice quantification.

Description

`is_res_select "@var::P. t"` returns `true`. If the term is not a restricted choice quantification the result is `false`.

Failure

Never fails.

See also

`res_quanTools.mk_res_select`, `res_quanTools.dest_res_select`.

<code>is_select</code>	<code>(boolSyntax)</code>
------------------------	---------------------------

`is_select` : (term -> bool)

Synopsis

Tests a term to see if it is a choice binding.

Description

`is_select "@var. t"` returns `true`. If the term is not an epsilon-term the result is `false`.

Failure

Never fails.

See also

boolSyntax.mk_select, boolSyntax.dest_select.

is_type**(Type)**

is_type : hol_type -> bool

Synopsis

Tests whether a HOL type is not a type variable.

Description

is_type ty returns true if ty is an application of a type operator and false otherwise.

Failure

Never fails.

See also

Type.op_arity, Type.mk_type, Type.mk_thy_type, Type.dest_type,
Type.dest_thy_type.

is_var**(Term)**

is_var : term -> bool

Synopsis

Tests a term to see if it is a variable.

Description

If M is a HOL variable, then is_var M returns true. If the term is not a variable the result is false.

Failure

Never fails.

See also

Term.mk_var, Term.dest_var, Term.is_const, Term.is_comb, Term.is_abs.

<code>is_vartype</code>	<code>(Type)</code>
-------------------------	---------------------

```
is_vartype : type -> bool
```

Synopsis

Tests a type to see if it is a type variable.

Failure

Never fails.

Example

```
- is_vartype Type.alpha;
> val it = true : bool

- is_vartype bool;
> val it = false : bool

- is_vartype (Type ':'a -> bool');
> val it = false : bool
```

See also

`Type.mk_vartype`, `Type.dest_vartype`.

<code>isEmpty</code>	<code>(Tag)</code>
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```
isEmpty : tag -> bool
```

Synopsis

Tells if a tag is empty.

Description

An invocation `isEmpty t` returns `true` just in case `t` is the empty tag. Only theorems built solely by HOL proof have an empty tag.

Failure

Never fails.

Example

```
- Tag.isEmpty (Thm.tag NOT_FORALL_THM);
> val it = true : bool
```

See also

Thm.tag, Thm.mk_oracle_thm.

ISPEC	(Drule)
-------	---------

ISPEC : (term -> thm -> thm)

Synopsis

Specializes a theorem, with type instantiation if necessary.

Description

This rule specializes a quantified variable as does SPEC; it differs from it in also instantiating the type if needed:

$$\frac{A \vdash !x:ty.tm}{A \vdash tm[t/x]} \text{ ISPEC } "t:ty'"$$

(where t is free for x in tm , and ty' is an instance of ty).

Failure

ISPEC fails if the input theorem is not universally quantified, if the type of the given term is not an instance of the type of the quantified variable, or if the type variable is free in the assumptions.

See also

Drule.INST_TY_TERM, Thm.INST_TYPE, Drule.ISPECL, Thm.SPEC, Term.match_term.

ISPECL	(Drule)
--------	---------

ISPECL : term list -> thm -> thm

Synopsis

Specializes a theorem zero or more times, with type instantiation if necessary.

Description

ISPECL is an iterative version of ISPEC

$$\frac{A \mid- !x_1 \dots x_n.t}{A \mid- t[t_1, \dots, t_n/x_1, \dots, x_n]} \quad \text{ISPECL } [t_1, \dots, t_n]$$

(where t_i is free for x_i in t).

Failure

ISPECL fails if the list of terms is longer than the number of quantified variables in the term, if the type instantiation fails, or if the type variable being instantiated is free in the assumptions.

See also

Thm.INST_TYPE, Drule.INST_TY_TERM, Drule.ISPEC, Drule.PART_MATCH, Thm.SPEC, Drule.SPECL.

<code>istream</code>	<code>(Lib)</code>
----------------------	--------------------

type ('a,'b) istream

Synopsis

Type of imperative streams

Description

The type ('a,'b) istream is an abstract type of imperative streams. These may be created with `mk_istream`, advanced by `next`, accessed by `state`, and reset with `reset`.

Comments

Purely functional streams are well-known in functional programming, and more elegant. However, this type proved useful in implementing some imperative 'gensym'-like algorithms used in HOL.

See also

`Lib.mk_istream`, `Lib.next`, `Lib.state`, `Lib.reset`.

<code>itlist</code>	<code>(Lib)</code>
---------------------	--------------------

`itlist : ('a -> 'b -> 'b) -> 'a list -> 'b -> 'b`

Synopsis

List iteration function. Applies a binary function between adjacent elements of a list.

Description

`itlist f [x1,...,xn] b` returns

```
f x1 (f x2 ... (f xn b)...) 
```

An invocation `itlist f list b` returns `b` if `list` is empty.

Failure

Fails if some application of `f` fails.

Example

```
- itlist (curry op+) [1,2,3,4] 0;
val it = 10 : int
```

See also

`Lib.itlist2`, `Lib.rev_itlist`, `Lib.rev_itlist2`, `Lib.end_itlist`.

<div data-bbox="161 1240 370 1290" data-label="Text"><code>itlist2</code></div>	<div data-bbox="1182 1240 1331 1290" data-label="Text"><code>(Lib)</code></div>
---	---

```
itlist2 : ('a -> 'b -> 'c -> 'c) -> 'a list -> 'b list -> 'c -> 'c
```

Synopsis

Applies a function to corresponding elements of 2 lists.

Description

`itlist2 f [x1,...,xn] [y1,...,yn] z` returns

```
f x1 y1 (f x2 y2 ... (f xn yn z)...) 
```

An invocation `itlist2 f list1 list2 b` returns `b` if `list1` and `list2` are empty.

Failure

Fails if the two lists are of different lengths, or if one of the applications of `f` fails.

Example

```
- itlist2 (fn x => fn y => fn z => (x,y)::z) [1,2] [3,4] [];
> val it = [(1,3), (2,4)] : (int * int) list
```

See also

Lib.itlist, Lib.rev_itlist, Lib.rev_itlist2, Lib.end_itlist.

K

(Lib)

K : 'a -> 'b -> 'a

Synopsis

Forms a constant function: $K \ x \ y = x$.

Failure

Never fails.

See also

Lib.##, Lib.A, Lib.B, Lib.C, Lib.I, Lib.S, Lib.W.

known_constants

(Parse)

Parse.known_constants : unit -> string list

Synopsis

Returns the list of constants known to the parser.

Description

A call to this functions returns the list of constants that will be treated as such by the parser. Those constants with names not on the list will be parsed as if they were variables.

Failure

Never fails.

See also

Parse.hide, Parse.reveal, Parse.set_known_constants.

LAND_CONV	(Conv)
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LAND_CONV : conv -> conv

Synopsis

Applies a conversion to the left-hand argument of a binary operator.

Description

If c is a conversion that maps a term t_1 to the theorem $\vdash t_1 = t_1'$, then the conversion `LAND_CONV c` maps applications of the form $f\ t_1\ t_2$ to theorems of the form:

$$\vdash f\ t_1\ t_2 = f\ t_1'\ t_2$$

Failure

`LAND_CONV c tm` fails if tm is not an application where the rator of the application is in turn another application, or if tm has this form but the conversion c fails when applied to the term t_2 . The function returned by `LAND_CONV c` may also fail if the ML function $c:term \rightarrow thm$ is not, in fact, a conversion (i.e. a function that maps a term t to a theorem $\vdash t = t'$).

Example

```
- LAND_CONV REDUCE_CONV (Term '(3 + 5) * 7');
> val it = |- (3 + 5) * 7 = 8 * 7 : thm
```

See also

`Conv.ABS_CONV`, `Conv.BINOP_CONV`, `Conv.RAND_CONV`, `Conv.RATOR_CONV`, `numLib.REDUCE_CONV`.

last	(Lib)
------	-------

last : 'a list -> 'a

Synopsis

Computes the last element of a list.

Description

`last [x1, ..., xn]` returns `xn`.

Failure

Fails if the list is empty.

See also

`Lib.butlast`, `Lib.el`, `Lib.front_last`.

<div data-bbox="234 698 501 752" data-label="Text"> <p><code>LAST_CONV</code></p> </div>	<div data-bbox="1144 698 1412 752" data-label="Text"> <p><code>(listLib)</code></p> </div>
--	--

`LAST_CONV` : `conv`

Synopsis

Computes by inference the result of taking the last element of a list.

Description

For any object language list of the form `--'[x0; ...; x(n-1)]'--`, the result of evaluating

$$\text{LAST_CONV } (\text{--}'\text{LAST } [x_0; \dots; x_{(n-1)}] \text{'--})$$

is the theorem

$$\vdash \text{LAST } [x_0; \dots; x_{(n-1)}] = x_{(n-1)}$$
Failure

`LAST_CONV tm` fails if `tm` is an empty list.

<div data-bbox="234 1518 702 1570" data-label="Text"> <p><code>LAST_EXISTS_CONV</code></p> </div>	<div data-bbox="1228 1518 1412 1570" data-label="Text"> <p><code>(Conv)</code></p> </div>
---	---

`LAST_EXISTS_CONV` : `conv -> conv`

Synopsis

Applies a conversion to the last existential quantifier (and its body) in a chain.

Description

Application of `LAST_EXISTS_CONV c` to the term `'?x1 .. xn x. body'` will apply `c` to the term `'?x. body'`. If the result of this application is the theorem `|- (?x. body) = t`, then the result of the whole will be

$$\vdash (\?x_1 \dots x_n x. \text{body}) = (\?x_1 \dots x_n. t)$$

Failure

Fails if the term is not existentially quantified, or if the conversion c fails when it is applied.

See also

Conv.BINDER_CONV, Conv.LAST_FORALL_CONV, Conv.STRIP_QUANT_CONV.

LAST_FORALL_CONV

(Conv)

LAST_FORALL_CONV : conv -> conv

Synopsis

Applies a conversion to the last universal quantifier (and its body) in a chain.

Description

Application of LAST_FORALL_CONV v to the term ‘‘ $\!x_1 \dots x_n x. \text{body}$ ’’ will apply c to the term ‘‘ $\!x. \text{body}$ ’’. If the result of this application is the theorem $\vdash (\!x. \text{body}) = t$, then the result of the whole will be

$$\vdash (\?x_1 \dots x_n x. \text{body}) = (\?x_1 \dots x_n. t)$$

Failure

Fails if the term is not universally quantified, or if the conversion c fails when it is applied.

See also

Conv.BINDER_CONV, Conv.LAST_EXISTS_CONV, Conv.STRIP_QUANT_CONV.

LASTN_CONV

(listLib)

LASTN_CONV : conv

Synopsis

Computes by inference the result of taking the last n elements of a list.

Description

For any object language list of the form $--' [x_0; \dots x_{(n-k)}; \dots; x_{(n-1)}] '--$, the result of evaluating

$$\text{LASTN_CONV } (--' \text{LASTN } k [x_0; \dots x_{(n-k)}; \dots; x_{(n-1)}] '--)$$

is the theorem

$$\vdash \text{LASTN } k [x_0; \dots; x_{(n-k)}; \dots; x_{(n-1)}] = [x_{(n-k)}; \dots; x_{(n-1)}]$$
Failure

$\text{LASTN_CONV } t_m$ fails if t_m is not of the form described above, or k is greater than the length of the list.

<div data-bbox="234 992 445 1043" data-label="Text"> <p>LE_CONV</p> </div>	<div data-bbox="1086 992 1414 1043" data-label="Text"> <p>(reduceLib)</p> </div>
---	--

$\text{LE_CONV} : \text{conv}$

Synopsis

Proves result of less-than-or-equal-to ordering on two numerals.

Description

If m and n are both numerals (e.g. 0, 1, 2, 3,...), then $\text{LE_CONV } "m \leq n"$ returns the theorem:

$$\vdash (m \leq n) = \text{T}$$

if the natural number denoted by m is less than or equal to that denoted by n , or

$$\vdash (m \leq n) = \text{F}$$

otherwise.

Failure

$\text{LE_CONV } t_m$ fails unless t_m is of the form $"m \leq n"$, where m and n are numerals.

Example

```
#LE_CONV "12 <= 198";;
|- 12 <= 198 = T
```

```
#LE_CONV "46 <= 46";;
|- 46 <= 46 = T
```

```
#LE_CONV "13 <= 12";;
|- 13 <= 12 = F
```

LEAST_ELIM_TAC	(numLib)
----------------	----------

LEAST_ELIM_TAC : tactic

Synopsis

Eliminates a LEAST term from the current goal

Description

LEAST_ELIM_TAC searches the goal it is applied to for free sub-terms involving the LEAST operator, of the form \$LEAST P (P will usually be an abstraction). If such a term is found, the tactic produces a new goal where instances of the LEAST-term have disappeared. The resulting goal will require the proof that there exists a value satisfying P, and that a minimal value satisfies the original goal.

Thus, LEAST_ELIM_TAC can be seen as a higher-order match against the theorem

```
|- !P Q.
    (?n. P x) /\ (!n. (!m. m < n ==> ~P m) /\ P n ==> Q n) ==>
    Q ($LEAST P)
```

where the new goal is the antecedent of the implication. (This theorem is LEAST_ELIM, from theory *while*.)

Failure

The tactic fails if there is no free LEAST-term in the goal.

Example

When applied to the goal

```
?- (LEAST n. 4 < n) = 5
```

the tactic LEAST_ELIM_TAC produces

$$?- (\exists n. 4 < n) \wedge !n. (!m. m < n ==> \sim(4 < m)) \wedge 4 < n ==> (n = 5)$$

Comments

This tactic assumes that there is indeed a least number satisfying the given predicate. If there is not, then the `LEAST`-term will have an arbitrary value, and the proof should proceed by showing that the enclosing predicate `Q` holds for all possible numbers.

If there are multiple different `LEAST`-terms in the goal, then `LEAST_ELIM_TAC` will pick the first free `LEAST`-term returned by the standard `find_terms` function.

See also

`Tactic.SELECT_ELIM_TAC`.

<code>LEFT_AND_EXISTS_CONV</code>	<code>(Conv)</code>
-----------------------------------	---------------------

`LEFT_AND_EXISTS_CONV` : `conv`

Synopsis

Moves an existential quantification of the left conjunct outwards through a conjunction.

Description

When applied to a term of the form $(\exists x.P) \wedge Q$, the conversion `LEFT_AND_EXISTS_CONV` returns the theorem:

$$\vdash (\exists x.P) \wedge Q = (\exists x'. P[x'/x] \wedge Q)$$

where `x'` is a primed variant of `x` that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $(\exists x.P) \wedge Q$.

See also

`Conv.AND_EXISTS_CONV`, `Conv.EXISTS_AND_CONV`, `Conv.RIGHT_AND_EXISTS_CONV`.

<code>LEFT_AND_FORALL_CONV</code>	<code>(Conv)</code>
-----------------------------------	---------------------

`LEFT_AND_FORALL_CONV` : `conv`

Synopsis

Moves a universal quantification of the left conjunct outwards through a conjunction.

Description

When applied to a term of the form $(!x.P) \wedge Q$, the conversion `LEFT_AND_FORALL_CONV` returns the theorem:

$$\vdash (!x.P) \wedge Q = (!x'. P[x'/x]) \wedge Q$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $(!x.P) \wedge Q$.

See also

`Conv.AND_FORALL_CONV`, `Conv.FORALL_AND_CONV`, `Conv.RIGHT_AND_FORALL_CONV`.

LEFT_AND_PEXISTS_CONV

(PairRules)

`LEFT_AND_PEXISTS_CONV` : `conv`

Synopsis

Moves a paired existential quantification of the left conjunct outwards through a conjunction.

Description

When applied to a term of the form $(?p. t) \wedge u$, the conversion `LEFT_AND_PEXISTS_CONV` returns the theorem:

$$\vdash (?p. t) \wedge u = (?p'. t[p'/p]) \wedge u$$

where p' is a primed variant of the pair p that does not contains variables free in the input term.

Failure

Fails if applied to a term not of the form $(?p. t) \wedge u$.

See also

`Conv.LEFT_AND_EXISTS_CONV`, `PairRules.AND_PEXISTS_CONV`,
`PairRules.PEXISTS_AND_CONV`, `PairRules.RIGHT_AND_PEXISTS_CONV`.

LEFT_AND_PFORALL_CONV	(PairRules)
-----------------------	-------------

LEFT_AND_PFORALL_CONV : conv

Synopsis

Moves a paired universal quantification of the left conjunct outwards through a conjunction.

Description

When applied to a term of the form $(!p. t) \wedge u$, the conversion LEFT_AND_PFORALL_CONV returns the theorem:

$$\vdash (!p. t) \wedge u = (!p'. t[p'/p] \wedge u)$$

where p' is a primed variant of p that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $(!p. t) \wedge u$.

See also

Conv.LEFT_AND_FORALL_CONV, PairRules.AND_PFORALL_CONV,
PairRules.PFORALL_AND_CONV, PairRules.RIGHT_AND_PFORALL_CONV.

LEFT_IMP_EXISTS_CONV	(Conv)
----------------------	--------

LEFT_IMP_EXISTS_CONV : conv

Synopsis

Moves an existential quantification of the antecedent outwards through an implication.

Description

When applied to a term of the form $(?x.P) ==> Q$, the conversion LEFT_IMP_EXISTS_CONV returns the theorem:

$$\vdash (?x.P) ==> Q = (!x'. P[x'/x] ==> Q)$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $(?x.P) ==> Q$.

See also

`Conv.FORALL_IMP_CONV`, `Conv.RIGHT_IMP_FORALL_CONV`.

LEFT_IMP_FORALL_CONV

(Conv)

LEFT_IMP_FORALL_CONV : conv

Synopsis

Moves a universal quantification of the antecedent outwards through an implication.

Description

When applied to a term of the form $(!x.P) ==> Q$, the conversion `LEFT_IMP_FORALL_CONV` returns the theorem:

$$\vdash (!x.P) ==> Q = (?x'. P[x'/x]) ==> Q$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $(!x.P) ==> Q$.

See also

`Conv.EXISTS_IMP_CONV`, `Conv.RIGHT_IMP_FORALL_CONV`.

LEFT_IMP_PEXISTS_CONV

(PairRules)

LEFT_IMP_PEXISTS_CONV : conv

Synopsis

Moves a paired existential quantification of the antecedent outwards through an implication.

Description

When applied to a term of the form $(?p. t) ==> u$, the conversion `LEFT_IMP_PEXISTS_CONV` returns the theorem:

$$\vdash (\text{?}p. t) \implies u = (!p'. t[p'/p]) \implies u$$

where p' is a primed variant of the pair p that does not contain any variables that appear free in the input term.

Failure

Fails if applied to a term not of the form $(\text{?}p. t) \implies u$.

See also

`Conv.LEFT_IMP_EXISTS_CONV`, `PairRules.PFORALL_IMP_CONV`,
`PairRules.RIGHT_IMP_PFORALL_CONV`.

<code>LEFT_IMP_PFORALL_CONV</code>	<code>(PairRules)</code>
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`LEFT_IMP_PFORALL_CONV` : `conv`

Synopsis

Moves a paired universal quantification of the antecedent outwards through an implication.

Description

When applied to a term of the form $(!p. t) \implies u$, the conversion `LEFT_IMP_PFORALL_CONV` returns the theorem:

$$\vdash (!p. t) \implies u = (\text{?}p'. t[p'/p]) \implies u$$

where p' is a primed variant of the pair p that does not contain any variables that appear free in the input term.

Failure

Fails if applied to a term not of the form $(!p. t) \implies u$.

See also

`Conv.LEFT_IMP_FORALL_CONV`, `PairRules.PEXISTS_IMP_CONV`,
`PairRules.RIGHT_IMP_PFORALL_CONV`.

<code>LEFT_LIST_PBETA</code>	<code>(PairRules)</code>
------------------------------	--------------------------

`LEFT_LIST_PBETA` : `(thm -> thm)`

Synopsis

Iteratively beta-reduces a top-level paired beta-redex on the left-hand side of an equation.

Description

When applied to an equational theorem, LEFT_LIST_PBETA applies paired beta-reduction over a top-level chain of beta-redexes to the left-hand side (only). Variables are renamed if necessary to avoid free variable capture.

$$\frac{A \vdash (\lambda p_1 \dots p_n. t) q_1 \dots q_n = s}{A \vdash t[q_1/p_1] \dots [q_n/p_n] = s} \text{ LEFT_LIST_BETA}$$

Failure

Fails unless the theorem is equational, with its left-hand side being a top-level paired beta-redex.

See also

Drule.RIGHT_LIST_BETA, PairRules.PBETA_CONV, PairRules.PBETA_RULE, PairRules.PBETA_TAC, PairRules.LIST_PBETA_CONV, PairRules.LEFT_PBETA, PairRules.RIGHT_PBETA, PairRules.RIGHT_LIST_PBETA.

LEFT_OR_EXISTS_CONV

(Conv)

LEFT_OR_EXISTS_CONV : conv

Synopsis

Moves an existential quantification of the left disjunct outwards through a disjunction.

Description

When applied to a term of the form $(?x.P) \vee Q$, the conversion LEFT_OR_EXISTS_CONV returns the theorem:

$$\vdash (?x.P) \vee Q = (?x'. P[x'/x] \vee Q)$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $(?x.P) \vee Q$.

See also

Conv.EXISTS_OR_CONV, Conv.OR_EXISTS_CONV, Conv.RIGHT_OR_EXISTS_CONV.

LEFT_OR_FORALL_CONV (Conv)

LEFT_OR_FORALL_CONV : conv

Synopsis

Moves a universal quantification of the left disjunct outwards through a disjunction.

Description

When applied to a term of the form $(!x.P) \vee Q$, the conversion LEFT_OR_FORALL_CONV returns the theorem:

$$\vdash (!x.P) \vee Q = (!x'. P[x'/x] \vee Q)$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $(!x.P) \vee Q$.

See also

Conv.OR_FORALL_CONV, Conv.FORALL_OR_CONV, Conv.RIGHT_OR_FORALL_CONV.

LEFT_OR_PEXISTS_CONV (PairRules)

LEFT_OR_PEXISTS_CONV : conv

Synopsis

Moves a paired existential quantification of the left disjunct outwards through a disjunction.

Description

When applied to a term of the form $(?p. t) \vee u$, the conversion LEFT_OR_PEXISTS_CONV returns the theorem:

$$\vdash (?p. t) \vee u = (?p'. t[p'/p] \vee u)$$

where p' is a primed variant of the pair p that does not contain any variables free in the input term.

Failure

Fails if applied to a term not of the form $(?p. t) \ \forall \ u$.

See also

`Conv.LEFT_OR_EXISTS_CONV`, `PairRules.PEXISTS_OR_CONV`, `PairRules.OR_PEXISTS_CONV`, `PairRules.RIGHT_OR_PEXISTS_CONV`.

LEFT_OR_PFORALL_CONV	(PairRules)
----------------------	-------------

`LEFT_OR_PFORALL_CONV` : `conv`

Synopsis

Moves a paired universal quantification of the left disjunct outwards through a disjunction.

Description

When applied to a term of the form $(!p. t) \ \forall \ u$, the conversion `LEFT_OR_FORALL_CONV` returns the theorem:

$$\vdash (!p. t) \ \forall \ u = (!p'. t[p'/p]) \ \forall \ u$$

where p' is a primed variant of the pair p that does not contain any variables that appear free in the input term.

Failure

Fails if applied to a term not of the form $(!p. t) \ \forall \ u$.

See also

`Conv.LEFT_OR_FORALL_CONV`, `PairRules.OR_PFORALL_CONV`, `PairRules.PFORALL_OR_CONV`, `PairRules.RIGHT_OR_PFORALL_CONV`.

LEFT_PBETA	(PairRules)
------------	-------------

`LEFT_PBETA` : `(thm -> thm)`

Synopsis

Beta-reduces a top-level paired beta-redex on the left-hand side of an equation.

Description

When applied to an equational theorem, `LEFT_PBETA` applies paired beta-reduction at top level to the left-hand side (only). Variables are renamed if necessary to avoid free variable capture.

$$\frac{A \vdash (\lambda x. t1) t2 = s}{A \vdash t1[t2/x] = s} \quad \text{LEFT_PBETA}$$

Failure

Fails unless the theorem is equational, with its left-hand side being a top-level paired beta-redex.

See also

`Drule.RIGHT_BETA`, `PairRules.PBETA_CONV`, `PairRules.PBETA_RULE`,
`PairRules.PBETA_TAC`, `PairRules.RIGHT_PBETA`, `PairRules.RIGHT_LIST_PBETA`,
`PairRules.LEFT_LIST_PBETA`.

<code>LENGTH_CONV</code>	<code>(listLib)</code>
--------------------------	------------------------

`LENGTH_CONV` : `conv`

Synopsis

Computes by inference the length of an object-language list.

Description

For any object language list of the form `-- '[x1;x2;...;xn] '--`, where `x1`, `x2`, ..., `xn` are arbitrary terms of the same type, the result of evaluating

`LENGTH_CONV (-- '[LENGTH [x1;x2;...;xn] '--)`

is the theorem

`\vdash LENGTH [x1;x2;...;xn] = n`

where n is the numeral constant that denotes the length of the list.

Failure

LENGTH_CONV tm fails if tm is not of the form `--'LENGTH [x1;x2;...;xn] '--` or `--'LENGTH [] '--`.

let_tm

(boolSyntax)

let_tm : term

Synopsis

Constant denoting let expressions.

Description

The ML variable `boolSyntax.let_tm` is bound to the term `bool$LET`.

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`, `boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.bool_case`, `boolSyntax.arb`.

lhand

(boolSyntax)

term -> term

Synopsis

Returns the left-hand argument of a binary application.

Description

A call to `lhand t` returns `x` in those situations where `t` is of the form `'f x y'`.

Failure

Fails if the argument is not of the required form.

Example

```
- lhs "3 + 2";
> val it = "3" : term
```

Comments

The name `lhs` is an abbreviation of “left-hand”, but `rand` is so-named as an abbreviation of “operand”. Nonetheless, `rand` does return the right-hand argument of a binary application.

See also

`Term.rand`, `Term.rator`.

<code>lhs</code>	<code>(boolSyntax)</code>
------------------	---------------------------

`lhs : term -> term`

Synopsis

Returns the left-hand side of an equation.

Description

If `M` has the form `t1 = t2` then `lhs M` returns `t1`.

Failure

Fails if the term is not an equation.

See also

`boolSyntax.rhs`, `boolSyntax.dest_eq`, `boolSyntax.mk_eq`.

doc.

<code>Lib.doc</code>

```
structure Lib
```

Synopsis

Collection of commonly used functions

Description

`Lib` is a collection of functions that have been found useful in writing the HOL system.

Comments

The SML Basis Library offers alternatives to some of the functions found in `Lib`.

<code>line_name</code>	<code>(unwindLib)</code>
------------------------	--------------------------

`line_name : (term -> string)`

Synopsis

Computes the line name of an equation.

Description

`line_name "!y1 ... ym. f x1 ... xn = t"` returns the string `'f'`.

Failure

Fails if the argument term is not of the specified form.

See also

`unwindLib.line_var`.

<code>line_var</code>	<code>(unwindLib)</code>
-----------------------	--------------------------

`line_var : (term -> term)`

Synopsis

Computes the line variable of an equation.

Description

`line_var "!y1 ... ym. f x1 ... xn = t"` returns the variable `"f"`.

Failure

Fails if the argument term is not of the specified form.

See also

`unwindLib.line_name`.

LIST_BETA_CONV

(Drule)

LIST_BETA_CONV : conv

Synopsis

Performs an iterated beta conversion.

Description

The conversion LIST_BETA_CONV maps terms of the form

$$"(\lambda x_1 x_2 \dots x_n. u) v_1 v_2 \dots v_n"$$

to the theorems of the form

$$|- (\lambda x_1 x_2 \dots x_n. u) v_1 v_2 \dots v_n = u[v_1/x_1][v_2/x_2] \dots [v_n/x_n]$$

where $u[v_i/x_i]$ denotes the result of substituting v_i for all free occurrences of x_i in u , after renaming sufficient bound variables to avoid variable capture.

Failure

LIST_BETA_CONV tm fails if tm does not have the form $"(\lambda x_1 \dots x_n. u) v_1 \dots v_n"$ for n greater than 0.

Example

```
- LIST_BETA_CONV (Term '(λx y. x+y) 1 2');
> val it = |- (λx y. x + y)1 2 = 1 + 2 : thm
```

See also

Thm.BETA_CONV, Conv.BETA_RULE, Tactic.BETA_TAC, Drule.RIGHT_BETA, Drule.RIGHT_LIST_BETA.

list_compare

(Lib)

list_compare : ('a * 'a -> order) -> 'a list * 'a list -> order

Synopsis

Lifts a comparison function to a lexicographic ordering on lists.

Description

An application `list_compare comp (L1,L2)` uses `comp` as a basis for comparing the lists `L1` and `L2` lexicographically, in left-to-right order. The returned value is one of `{LESS, EQUAL, GREATER}`.

Failure

If `comp` fails when applied to corresponding elements of `L1` and `L2`.

Example

```
- list_compare Int.compare ([1,2,3,4], [1,2,3,4]);
> val it = EQUAL : order

- list_compare Int.compare ([1,2,3,4], [1,2,3,4,5]);
> val it = LESS : order

- list_compare Int.compare ([1,2,3,4], [1,2,3,2]);
> val it = GREATER : order
```

LIST_CONJ	(Drule)
-----------	---------

LIST_CONJ : thm list -> thm

Synopsis

Conjoins the conclusions of a list of theorems.

Description

$$\frac{A1 \mid\text{-} t1 \dots An \mid\text{-} tn}{A1 \text{ u } \dots \text{ u } An \mid\text{-} t1 \wedge \dots \wedge tn} \text{ LIST_CONJ}$$

Failure

LIST_CONJ fails if applied to an empty list of theorems.

See also

Drule.BODY_CONJUNCTS, Thm.CONJ, Thm.CONJUNCT1, Thm.CONJUNCT2, Drule.CONJUNCTS, Drule.CONJ_PAIR, Tactic.CONJ_TAC.

LIST_CONV

(listLib)

LIST_CONV : conv

Synopsis

Proves theorems about list constants applied to NIL, CONS, SNOC, APPEND, FLAT and REVERSE.

Description

LIST_CONV takes a term of the form:

$$\text{CONST1 } \dots (\text{CONST2 } \dots) \dots$$

where CONST1 and CONST2 are operators on lists and CONST2 returns a list result. It can be one of NIL, CONS, SNOC, APPEND, FLAT or REVERSE. The form of the resulting theorem depends on CONST1 and CONST2. Some auxiliary information must be provided about CONST1. LIST_CONV maintains a database of such auxiliary information. It initially holds information about the constants in the system. However, additional information can be supplied by the user as new constants are defined. The main information that is needed is a theorem defining the constant in terms of FOLDR or FOLDL. The definition should have the form:

$$|- \text{CONST1 } \dots l \dots = \text{fold } f \ e \ l$$

where fold is either FOLDR or FOLDL, f is a function, e a base element and l a list variable. For example, a suitable theorem for SUM is

$$|- \text{SUM } l = \text{FOLDR } \$+ \ 0 \ l$$

Knowing this theorem and given the term --'SUM (CONS x l)'--, LIST_CONV returns the theorem:

$$|- \text{SUM } (\text{CONS } x \ l) = x + (\text{SUM } l)$$

Other auxiliary theorems that are needed concern the terms f and e found in the definition with respect to FOLDR or FOLDL. For example, knowing the theorem:

$$|- \text{MONOID } \$+ \ 0$$

and given the term --'SUM (APPEND l1 l2)'--, LIST_CONV returns the theorem

$$|- \text{SUM } (\text{APPEND } l1 \ l2) = (\text{SUM } l1) + (\text{SUM } l2)$$

The following table shows the form of the theorem returned and the auxiliary theorems needed if CONST1 is defined in terms of FOLDR.

CONST2	side conditions	tm2 in result - tm1 = tm2
=====	=====	=====
[]	NONE	e
[x]	NONE	f x e
CONS x l	NONE	f x (CONST1 l)
SNOC x l	e is a list variable	CONST1 (f x e) l
APPEND l1 l2	e is a list variable	CONST1 (CONST1 l1) l2
APPEND l1 l2	- FCOMM g f, - LEFT_ID g e	g (CONST1 l1) (CONST2 l2)
FLAT l1	- FCOMM g f, - LEFT_ID g e, - CONST3 l = FOLDR g e l	CONST3 (MAP CONST1 l)
REVERSE l	- COMM f, - ASSOC f	CONST1 l
REVERSE l	f == (\x l. h (g x) l) - COMM h, - ASSOC h	CONST1 l

The following table shows the form of the theorem returned and the auxiliary theorems needed if CONST1 is defined in terms of FOLDL.

CONST2	side conditions	tm2 in result - tm1 = tm2
=====	=====	=====
[]	NONE	e
[x]	NONE	f x e
SNOC x l	NONE	f x (CONST1 l)
CONS x l	e is a list variable	CONST1 (f x e) l
APPEND l1 l2	e is a list variable	CONST1 (CONST1 l1) l2
APPEND l1 l2	- FCOMM f g, - RIGHT_ID g e	g (CONST1 l1) (CONST2 l2)
FLAT l1	- FCOMM f g, - RIGHT_ID g e, - CONST3 l = FOLDR g e l	CONST3 (MAP CONST1 l)
REVERSE l	- COMM f, - ASSOC f	CONST1 l
REVERSE l	f == (\l x. h l (g x)) - COMM h, - ASSOC h	CONST1 l

|- MONOID f e can be used instead of |- FCOMM f f, |- LEFT_ID f or |- RIGHT_ID f.
|- ASSOC f can also be used in place of |- FCOMM f f.

Auxiliary theorems are held in a user-updatable database. In particular, definitions of constants in terms of FOLDR and FOLDL, and monoid, commutativity, associativity, left identity, right identity and binary function commutativity theorems are stored. The database can be updated by the user to allow LIST_CONV to prove theorems about new constants. This is done by calling `set_list_thm_database`. The database can be inspected by calling `list_thm_database`. The database initially holds FOLDR/L theorems

for the following system constants: APPEND, FLAT, LENGTH, NULL, REVERSE, MAP, FILTER, ALL_EL, SUM, SOME_EL, IS_EL, AND_EL, OR_EL, PREFIX, SUFFIX, SNOC and FLAT combined with REVERSE. It also holds auxiliary theorems about their step functions and base elements.

Example

```
- LIST_CONV (--'LENGTH ([]:'a list) '--);
|- LENGTH [] = 0

- LIST_CONV (--'APPEND (CONS h t) (l1:'a list) '--);
|- APPEND (CONS h t) l1 = CONS h (APPEND t l1)

- LIST_CONV (--'APPEND (l1:'a list) (CONS h t) '--);
|- APPEND l1 (CONS h t) = APPEND (SNOC h l1) t

- LIST_CONV (--'MAP (P:'a list -> 'a) (SNOC h t) '--);
|- MAP P (SNOC h t) = SNOC (P h) (MAP P t)

- LIST_CONV (--'SUM (FLAT l) '--);
|- SUM (FLAT l) = SUM (MAP SUM l)

- LIST_CONV (--'NULL (REVERSE (l:bool list)) '--);
|- NULL (REVERSE l) = NULL l
```

Failure

LIST_CONV *tm* fails if *tm* is not of the form described above. It also fails if no fold definition for CONST1 is held in the databases, or if the required auxiliary theorems, as described above, are not held in the databases.

See also

listLib.list_thm_database, listLib.PURE_LIST_CONV, listLib.set_list_thm_database, listLib.X_LIST_CONV.

<code>list_FOLD_CONV</code>	<code>(listLib)</code>
-----------------------------	------------------------

`list_FOLD_CONV : thm -> conv -> conv`

Synopsis

Computes by inference the result of applying a function to the elements of a list.

Description

Evaluating `list_FOLD_CONV fthm conv tm` returns a theorem

```
|- CONST x0' ... xi' ... xn' = tm'
```

The first argument `fthm` should be a theorem of the form

```
|- !x0 ... xi ... xn. CONST x0 ... xi ... xn = FOLD[LR] f e xi
```

where `FOLD[LR]` means either `FOLDL` or `FOLDR`. The last argument `tm` is a term of the following form:

```
CONST x0' ... xi' ... xn'
```

where `xi'` is a concrete list. `list_FOLD_CONV` first instantiates the input theorem using `tm`. It then calls either `FOLDL_CONV` or `FOLDR_CONV` with the user supplied conversion `conv` on the right-hand side.

Failure

`list_FOLD_CONV fthm conv tm` fails if `fthm` or `tm` is not of the form described above, or if they do not agree, or the call to `FOLDL_CONV` OR `FOLDR_CONV` fails.

Uses

This function is used to implement conversions for logical constants which can be expressed in terms of the fold operators. For example, the constant `SUM` can be expressed in terms of `FOLDR` as in the following theorem:

```
|- !l. SUM l = FOLDR $+ 0 l
```

The conversion for `SUM`, `SUM_CONV` can be implemented as

```
load_library_in_place num_lib;
val SUM_CONV =
  list_FOLD_CONV (theorem "list" "SUM_FOLDR") Num_lib.ADD_CONV;
```

Then, evaluating `SUM_CONV (--'SUM [0;1;2;3] '--)` will return the following theorem:

```
|- SUM [0;1;2;3] = 6
```

See also

`listLib.FOLDL_CONV`, `listLib.FOLDR_CONV`.

LIST_INDUCT_TAC	(listLib)
-----------------	-----------

LIST_INDUCT_TAC : tactic

Synopsis

Performs tactical proof by structural induction on lists.

Description

`LIST_INDUCT_TAC` reduces a goal `!l.P[l]`, where `l` ranges over lists, to two subgoals corresponding to the base and step cases in a proof by structural induction on `l`. The induction hypothesis appears among the assumptions of the subgoal for the step case. The specification of `LIST_INDUCT_TAC` is:

$$\frac{A \text{ ?- } !l. P}{\text{A |- P[NIL/l] \quad A u \{P[l'/l]\} \text{ ?- } !h. P[CONS h l'/l]} \quad \text{LIST_INDUCT_TAC}$$

where `l'` is a primed variant of `l` that does not appear free in the assumptions `A` (usually, `l'` is just `l`). When `LIST_INDUCT_TAC` is applied to a goal of the form `!l.P`, where `l` does not appear free in `P`, the subgoals are just `A ?- P` and `A u {P} ?- !h.P`.

Failure

`LIST_INDUCT_TAC g` fails unless the conclusion of the goal `g` has the form `!l.t`, where the variable `l` has type `(ty)list` for some type `ty`.

See also

`listLib.EQ_LENGTH_INDUCT_TAC`, `listLib.EQ_LENGTH_SNOC_INDUCT_TAC`,
`listLib.SNOC_INDUCT_TAC`.

`list_mk_abs`

(`boolSyntax`)

```
list_mk_abs : term list * term -> term
```

Synopsis

Iteratively constructs abstractions.

Description

`list_mk_abs([x1,...,xn],t)` returns the term `\x1 ... xn.t`.

Failure

Fails if the terms in the list are not variables.

See also

`boolSyntax.strip_abs`, `Term.mk_abs`.

list_mk_abs

(Term)

```
list_mk_abs : term list * term -> term
```

Synopsis

Performs a sequence of lambda binding operations.

Description

An application `list_mk_abs ([v1,...,vn], M)` yields the term `\v1 ... vn. M`. Free occurrences of `v1, ..., vn` in `M` become bound in the result.

Failure

Fails if if some `vi` ($1 \leq i \leq n$) is not a variable.

Example

```
- list_mk_abs ([mk_var("v1",bool),mk_var("v2",bool),mk_var("v3",bool)],
              Term 'v1 /\ v2 /\ v3');
> val it = '\v1 v2 v3. v1 /\ v2 /\ v3' : term
```

Comments

In the current implementation, `list_mk_abs` is more efficient than iteration of `mk_abs` for larger tasks.

See also

`Term.mk_abs`, `boolSyntax.list_mk_forall`, `boolSyntax.list_mk_exists`.

list_mk_anylet

(pairSyntax)

```
list_mk_anylet : (term * term) list list * term -> term
```

Synopsis

Construct arbitrary `let` terms.

Description

The invocation `list_mk_anylet ([[a1,b1],..., [an,bn]], ... [(u1,v1),..., (uk,vk)], body)` returns a term with surface syntax

```

let a1 = b1 and ... an = bn in
    ...                               in
let u1 = v1 and ... and uk = vk
  in body

```

Failure

If any binding pair (x,y) is such that x and y have different types.

Example

```

list_mk_anylet
  ([[('x:'a'', 'P:'a'')],
   [('(y:'a, z:ind)'', 'M:'a#ind'')],
   [('f (x:'a):bool'', 'N:bool''),
   ('g:bool->'a'', 'K (v:'a):bool->'a'')]], 'g (f (x:'a):bool):'a'');
> val it = 'let x = P in
           let (y,z) = M in
           let f x = N
           and g = K v
           in g (f x)'

```

Uses

Programming that involves manipulation of term syntax.

See also

`boolSyntax.dest_let`, `pairSyntax.mk_anylet`, `pairSyntax.strip_anylet`,
`pairSyntax.dest_anylet`.

<code>list_mk_binder</code>	<code>(Term)</code>
-----------------------------	---------------------

```
list_mk_binder : term option -> term list * term -> term
```

Synopsis

Performs a sequence of variable binding operations on a term

Description

An application `list_mk_binder (SOME c) ([v1,...,vn],M)` builds the term $c (\lambda v1. \dots (c (\lambda vn. M$
The term c should be a binder, that is, a constant that takes a lambda abstraction and

returns a bound term. Thus `list_mk_binder` implements Church's view that variable binding operations should be reduced to lambda-binding.

An application `list_mk_binder NONE ([v1,...,vn],M)` builds the term $\lambda v_1 \dots \lambda v_n. M$.

Failure

`list_mk_binder opt ([v1,...,vn],M)` fails if some v_i $1 \leq i \leq n$ is not a variable. It also fails if the constructed term $c (\lambda v_1. \dots (c (\lambda v_n. M) \dots))$ is not well typed.

Example

Repeated existential quantification is easy to code up using `list_mk_binder`. For testing, we make a list of boolean variables.

```
- fun upto b t acc = if b >= t then rev acc else upto (b+1) t (b::acc)

fun vlist n = map (C (curry mk_var) bool o concat "v" o int_to_string)
                (upto 0 n []);
val vars = vlist 100;

> val vars =
['v0', 'v1', 'v2', 'v3', 'v4', 'v5', 'v6', 'v7', 'v8', 'v9', 'v10', 'v11',
 'v12', 'v13', 'v14', 'v15', 'v16', 'v17', 'v18', 'v19', 'v20', 'v21',
 'v22', 'v23', 'v24', 'v25', 'v26', 'v27', 'v28', 'v29', 'v30', 'v31',
 'v32', 'v33', 'v34', 'v35', 'v36', 'v37', 'v38', 'v39', 'v40', 'v41',
 'v42', 'v43', 'v44', 'v45', 'v46', 'v47', 'v48', 'v49', 'v50', 'v51',
 'v52', 'v53', 'v54', 'v55', 'v56', 'v57', 'v58', 'v59', 'v60', 'v61',
 'v62', 'v63', 'v64', 'v65', 'v66', 'v67', 'v68', 'v69', 'v70', 'v71',
 'v72', 'v73', 'v74', 'v75', 'v76', 'v77', 'v78', 'v79', 'v80', 'v81',
 'v82', 'v83', 'v84', 'v85', 'v86', 'v87', 'v88', 'v89', 'v90', 'v91',
 'v92', 'v93', 'v94', 'v95', 'v96', 'v97', 'v98', 'v99'] : term list
```

Now we exercise `list_mk_binder`.

```
- val ex1_tm = list_mk_binder (SOME boolSyntax.existential)
                    (vars, list_mk_conj vars);

> val ex1_tm =
'?v0 v1 v2 v3 v4 v5 v6 v7 v8 v9 v10 v11 v12 v13 v14 v15 v16 v17 v18 v19 v20
 v21 v22 v23 v24 v25 v26 v27 v28 v29 v30 v31 v32 v33 v34 v35 v36 v37 v38
 v39 v40 v41 v42 v43 v44 v45 v46 v47 v48 v49 v50 v51 v52 v53 v54 v55 v56
 v57 v58 v59 v60 v61 v62 v63 v64 v65 v66 v67 v68 v69 v70 v71 v72 v73 v74
 v75 v76 v77 v78 v79 v80 v81 v82 v83 v84 v85 v86 v87 v88 v89 v90 v91 v92
 v93 v94 v95 v96 v97 v98 v99.
  v0 /\ v1 /\ v2 /\ v3 /\ v4 /\ v5 /\ v6 /\ v7 /\ v8 /\ v9 /\ v10 /\
```

```
v11 /\ v12 /\ v13 /\ v14 /\ v15 /\ v16 /\ v17 /\ v18 /\ v19 /\ v20 /\
v21 /\ v22 /\ v23 /\ v24 /\ v25 /\ v26 /\ v27 /\ v28 /\ v29 /\ v30 /\
v31 /\ v32 /\ v33 /\ v34 /\ v35 /\ v36 /\ v37 /\ v38 /\ v39 /\ v40 /\
v41 /\ v42 /\ v43 /\ v44 /\ v45 /\ v46 /\ v47 /\ v48 /\ v49 /\ v50 /\
v51 /\ v52 /\ v53 /\ v54 /\ v55 /\ v56 /\ v57 /\ v58 /\ v59 /\ v60 /\
v61 /\ v62 /\ v63 /\ v64 /\ v65 /\ v66 /\ v67 /\ v68 /\ v69 /\ v70 /\
v71 /\ v72 /\ v73 /\ v74 /\ v75 /\ v76 /\ v77 /\ v78 /\ v79 /\ v80 /\
v81 /\ v82 /\ v83 /\ v84 /\ v85 /\ v86 /\ v87 /\ v88 /\ v89 /\ v90 /\
v91 /\ v92 /\ v93 /\ v94 /\ v95 /\ v96 /\ v97 /\ v98 /\ v99' : term
```

Comments

Terms with many consecutive binders should be constructed using `list_mk_binder` and its instantiations `list_mk_abs`, `list_mk_forall`, and `list_mk_exists`. In the current implementation of HOL, iterating `mk_abs`, `mk_forall`, or `mk_exists` is far slower for terms with many consecutive binders.

See also

`Term.list_mk_abs`, `boolSyntax.list_mk_forall`, `boolSyntax.list_mk_exists`, `Term.strip_binder`.

<code>list_mk_comb</code>	<code>(Term)</code>
---------------------------	---------------------

```
list_mk_comb : term * term list -> term
```

Synopsis

Iteratively constructs combinations (function applications).

Description

`list_mk_comb(t, [t1, ..., tn])` returns `t t1 ... tn`.

Failure

Fails if the types of `t1, ..., tn` are not equal to the argument types of `t`. It is not necessary for all the arguments of `t` to be given. In particular the list of terms `t1, ..., tn` may be empty.

Example

```

- list_mk_comb(conditional,[T, mk_var("one",alpha), mk_var("two",alpha)]);
> val it = '(if T then one else two)' : term

- list_mk_comb(universal,[]);
> val it = '$!' : term

- try list_mk_comb(universal,[F]);

```

Exception raised at Term.list_mk_comb:
incompatible types

See also

boolSyntax.strip_comb, Term.mk_comb.

list_mk_conj	(boolSyntax)
--------------	--------------

```
list_mk_conj : term list -> term
```

Synopsis

Constructs the conjunction of a list of terms.

Description

list_mk_conj([t1,...,tn]) returns $t1 \wedge \dots \wedge tn$.

Failure

Fails if the list is empty or if the list has more than one element, one or more of which are not of type bool.

Example

```

- list_mk_conj [T,F,T];
> val it = 'T /\ F /\ T' : term

- try list_mk_conj [T,mk_var("x",alpha),F];

```

Exception raised at boolSyntax.mk_conj:
Non-boolean argument

```
- list_mk_conj [mk_var("x",alpha)];
> val it = 'x' : term
```

See also

`boolSyntax.strip_conj`, `boolSyntax.mk_conj`.

<code>list_mk_disj</code>	<code>(boolSyntax)</code>
---------------------------	---------------------------

```
list_mk_disj : term list -> term
```

Synopsis

Constructs the disjunction of a list of terms.

Description

`list_mk_disj([t1,...,tn])` returns $t1 \vee \dots \vee tn$.

Failure

Fails if the list is empty or if the list has more than one element, one or more of which are not of type `bool`.

Example

```
- list_mk_disj [T,F,T];
> val it = 'T \vee F \vee T' : term

- try list_mk_disj [T,mk_var("x",alpha),F];
```

```
Exception raised at boolSyntax.mk_disj:
Non-boolean argument
```

```
- list_mk_disj [mk_var("x",alpha)];
> val it = 'x' : term
```

See also

`boolSyntax.strip_disj`, `boolSyntax.mk_disj`.

list_mk_exists

(boolSyntax)

```
list_mk_exists : term list * term -> term
```

Synopsis

Iteratively constructs an existential quantification.

Description

list_mk_exists([x1,...,xn],t) returns $\exists x_1 \dots x_n. t$.

Failure

Fails if the terms in the list are not variables or if t is not of type `bool` and the list of terms is non-empty. If the list of terms is empty the type of t can be anything.

See also

boolSyntax.strip_exists, boolSyntax.mk_exists.

LIST_MK_EXISTS

(Drule)

```
LIST_MK_EXISTS : (term list -> thm -> thm)
```

Synopsis

Multiply existentially quantifies both sides of an equation using the given variables.

Description

When applied to a list of terms $[x_1; \dots; x_n]$, where the x_i are all variables, and a theorem $A \vdash t_1 = t_2$, the inference rule LIST_MK_EXISTS existentially quantifies both sides of the equation using the variables given, none of which should be free in the assumption list.

$$\frac{A \vdash t_1 = t_2}{A \vdash (\exists x_1 \dots x_n. t_1) = (\exists x_1 \dots x_n. t_2)} \text{ LIST_MK_EXISTS } ["x_1"; \dots; "x_n"]$$

Failure

Fails if any term in the list is not a variable or is free in the assumption list, or if the theorem is not equational.

See also

`Drule.EXISTS_EQ`, `Drule.MK_EXISTS`.

<code>list_mk_forall</code>	<code>(boolSyntax)</code>
-----------------------------	---------------------------

`list_mk_forall` : `term list * term -> term`

Synopsis

Iteratively constructs a universal quantification.

Description

`list_mk_forall([x1,...,xn],t)` returns `!x1 ... xn. t`.

Failure

Fails if the terms in the list are not variables or if `t` is not of type `bool` and the list of terms is non-empty. If the list of terms is empty the type of `t` can be anything.

See also

`boolSyntax.strip_forall`, `boolSyntax.mk_forall`.

<code>list_mk_fun</code>	<code>(boolSyntax)</code>
--------------------------	---------------------------

`list_mk_fun` : `hol_type list * hol_type -> hol_type`

Synopsis

Iteratively constructs function types.

Description

`list_mk_fun([ty1,...,tyn],ty)` returns `ty1 -> (... (tyn -> t) ...)`.

Failure

Never fails.

Example

```
- list_mk_fun ([alpha,bool],beta);
> val it = ':a -> bool -> 'b' : hol_type
```

See also

boolSyntax.strip_fun, Type.mk_type, Type.-->.

list_mk_ico mb

(boolSyntax)

```
term * term list -> term
```

Synopsis

Folds mk_ico**mb** over a series of arguments.

Description

A call to list_mk_ico**mb**(f, args) combines f with each of the elements of the list args in turn, moving from left to right. If args is empty, then the result is simply f. When args is non-empty, the growing application-term is created with successive calls to mk_ico**mb**, possibly causing type variables in any of the terms to become instantiated.

Failure

Fails if any of the underlying calls to mk_ico**mb** fails, which will occur if the type of the accumulating term (starting with f) is not of a function type, or if it has a domain type that can not be instantiated to equal the type of the next argument term.

Comments

list_mk_ico**mb** is to mk_ico**mb** what list_mk_co**mb** is to mk_co**mb**.

See also

Term.list_mk_co**mb**, Term.mk_co**mb**, boolSyntax.mk_ico**mb**.

list_mk_ico mb

(boolSyntax)

```
list_mk_icomb : term list * term -> term
```

Synopsis

Iteratively constructs implications.

Description

list_mk_ico**mb**([t1,...,tn], t) returns t1 ==> (... (tn ==> t)...

Failure

Fails if any of t_1, \dots, t_n are not of type `bool`. Also fails if the list of terms is non-empty and t is not of type `bool`. If the list of terms is empty the type of t can be anything.

Example

```
- list_mk_imp ([T,F],T);
> val it = 'T ==> F ==> T' : term

- try list_mk_imp ([T,F],mk_var("x",alpha));
evaluation failed      list_mk_imp

- list_mk_imp ([],mk_var("x",alpha));
> val it = 'x' : term
```

See also

`boolSyntax.strip_imp`, `boolSyntax.mk_imp`.

<code>list_mk_pabs</code>	<code>(pairSyntax)</code>
---------------------------	---------------------------

`list_mk_pabs : term list * term -> term`

Synopsis

Iteratively constructs paired abstractions.

Description

`list_mk_pabs([p1, ..., pn], t)` returns $\backslash p_1 \dots p_n. t$.

Failure

Fails with `list_mk_pabs` if the terms in the list are not paired structures of variables.

See also

`boolSyntax.list_mk_abs`, `pairSyntax.strip_pabs`, `pairSyntax.mk_pabs`.

<code>list_mk_pair</code>	<code>(pairSyntax)</code>
---------------------------	---------------------------

`list_mk_pair : term list -> term`

Synopsis

Constructs a tuple from a list of terms.

Description

`list_mk_pair([t1,...,tn])` returns the term $(t1, \dots, tn)$.

Failure

Fails if the list is empty.

Example

```
- pairSyntax.list_mk_pair [Term '1', T, Term '2'];
> val it = '(1,T,2)' : term

- pairSyntax.list_mk_pair [Term '1'];
> val it = '1' : term
```

See also

`pairSyntax.strip_pair`, `pairSyntax.mk_pair`.

LIST_MK_PEXISTS**(PairRules)**

LIST_MK_PEXISTS : (term list -> thm -> thm)

Synopsis

Multiply existentially quantifies both sides of an equation using the given pairs.

Description

When applied to a list of terms $[p1; \dots; pn]$, where the p_i are all paired structures of variables, and a theorem $A \vdash t1 = t2$, the inference rule LIST_MK_PEXISTS existentially quantifies both sides of the equation using the pairs given, none of the variables in the pairs should be free in the assumption list.

$$\frac{A \vdash t1 = t2}{A \vdash (?x1 \dots xn. t1) = (?x1 \dots xn. t2)} \quad \text{LIST_MK_PEXISTS } ["x1"; \dots; "xn"]$$

Failure

Fails if any term in the list is not a paired structure of variables, or if any variable is free in the assumption list, or if the theorem is not equational.

See also

Drule.LIST_MK_EXISTS, PairRules.PEXISTS_EQ, PairRules.MK_PEXISTS.

LIST_MK_PFORALL	(PairRules)
-----------------	-------------

LIST_MK_PFORALL : (term list -> thm -> thm)

Synopsis

Multiply universally quantifies both sides of an equation using the given pairs.

Description

When applied to a list of terms $[p_1; \dots; p_n]$, where the p_i are all paired structures of variables, and a theorem $A \vdash t_1 = t_2$, the inference rule LIST_MK_PFORALL universally quantifies both sides of the equation using the pairs given, none of the variables in the pairs should be free in the assumption list.

$$\frac{A \vdash t_1 = t_2}{A \vdash (!x_1 \dots x_n. t_1) = (!x_1 \dots x_n. t_2)} \quad \text{LIST_MK_PFORALL } ["x_1"; \dots; "x_n"]$$

Failure

Fails if any term in the list is not a paired structure of variables, or if any variable is free in the assumption list, or if the theorem is not equational.

See also

Drule.LIST_MK_EXISTS, PairRules.PFORALL_EQ, PairRules.MK_PFORALL.

list_mk_res_exists	(res_quanLib)
--------------------	---------------

list_mk_res_exists : ((term # term) list # term) -> term)

Synopsis

Iteratively constructs a restricted existential quantification.

Description

```
list_mk_res_exists([("x1", "P1"); ...; ("xn", "Pn")], "t")
```

returns "?x1::P1. ... ?xn::Pn. t".

Failure

Fails with `list_mk_res_exists` if the first terms x_i in the pairs are not a variable or if the second terms P_i in the pairs and t are not of type `:bool` if the list is non-empty. If the list is empty the type of t can be anything.

See also

`res_quanLib.strip_res_exists`, `res_quanLib.mk_res_exists`.

`list_mk_res_exists` (res_quanTools)

```
list_mk_res_exists : ((term # term) list # term) -> term
```

Synopsis

Iteratively constructs a restricted existential quantification.

Description

```
list_mk_res_exists([("x1", "P1"); ...; ("xn", "Pn")], "t")
```

returns "?x1::P1. ... ?xn::Pn. t".

Failure

Fails with `list_mk_res_exists` if the first terms x_i in the pairs are not a variable or if the second terms P_i in the pairs and t are not of type `:bool` if the list is non-empty. If the list is empty the type of t can be anything.

See also

`res_quanTools.strip_res_exists`, `res_quanTools.mk_res_exists`.

`list_mk_res_forall` (res_quanLib)

```
list_mk_res_forall : (term # term) list # term -> term
```

Synopsis

Iteratively constructs a restricted universal quantification.

Description

```
list_mk_res_forall([("x1", "P1"); ...; ("xn", "Pn")], "t")
```

returns " $!x1::P1. \dots !xn::Pn. t$ ".

Failure

Fails with `list_mk_res_forall` if the first terms x_i in the pairs are not a variable or if the second terms P_i in the pairs and t are not of type `" :bool"` if the list is non-empty. If the list is empty the type of t can be anything.

See also

`res_quantLib.strip_res_forall`, `res_quantLib.mk_res_forall`.

<code>list_mk_res_forall</code>	<code>(res_quantTools)</code>
---------------------------------	-------------------------------

```
list_mk_res_forall : ((term # term) list # term) -> term)
```

Synopsis

Iteratively constructs a restricted universal quantification.

Description

```
list_mk_res_forall([("x1", "P1"); ...; ("xn", "Pn")], "t")
```

returns " $!x1::P1. \dots !xn::Pn. t$ ".

Failure

Fails with `list_mk_res_forall` if the first terms x_i in the pairs are not a variable or if the second terms P_i in the pairs and t are not of type `" :bool"` if the list is non-empty. If the list is empty the type of t can be anything.

See also

`res_quantTools.strip_res_forall`, `res_quantTools.mk_res_forall`.

<code>LIST_MP</code>	<code>(Drule)</code>
----------------------	----------------------

```
LIST_MP : thm list -> thm -> thm
```

Synopsis

Performs a chain of Modus Ponens inferences.

Description

When applied to theorems $A_1 \vdash t_1, \dots, A_n \vdash t_n$ and a theorem which is a chain of implications with the successive antecedents the same as the conclusions of the theorems in the list (up to alpha-conversion), $A \vdash t_1 \implies \dots \implies t_n \implies t$, the LIST_MP inference rule performs a chain of MP inferences to deduce $A \cup A_1 \cup \dots \cup A_n \vdash t$.

$$\begin{array}{c}
 A_1 \vdash t_1 \dots A_n \vdash t_n \quad A \vdash t_1 \implies \dots \implies t_n \implies t \\
 \hline
 A \cup A_1 \cup \dots \cup A_n \vdash t
 \end{array}
 \quad \text{LIST_MP}$$

Failure

Fails unless the theorem is a chain of implications whose consequents are the same as the conclusions of the list of theorems (up to alpha-conversion), in sequence.

See also

Thm.EQ_MP, Drule.MATCH_MP, Tactic.MATCH_MP_TAC, Thm.MP, Tactic.MP_TAC.

LIST_PBETA_CONV

(PairRules)

LIST_PBETA_CONV : conv

Synopsis

Performs an iterated paired beta-conversion.

Description

The conversion LIST_PBETA_CONV maps terms of the form

$$(\lambda p_1 p_2 \dots p_n. t) q_1 q_2 \dots q_n$$

to the theorems of the form

$$\vdash (\lambda p_1 p_2 \dots p_n. t) q_1 q_2 \dots q_n = t[q_1/p_1][q_2/p_2] \dots [q_n/p_n]$$

where $t[q_i/p_i]$ denotes the result of substituting q_i for all free occurrences of p_i in t , after renaming sufficient bound variables to avoid variable capture.

Failure

LIST_PBETA_CONV t_m fails if t_m does not have the form $(\lambda p_1 \dots p_n. t) q_1 \dots q_n$ for n greater than 0.

Example

```
- LIST_PBETA_CONV (Term '(\\(a,b) (c,d) . a + b + c + d) (1,2) (3,4)');
> val it = |- \\(a,b) (c,d). a + b + c + d) (1,2) (3,4) = 1 + 2 + 3 + 4 : thm
```

See also

Drule.LIST_BETA_CONV, PairRules.PBETA_CONV, Conv.BETA_RULE, Tactic.BETA_TAC, PairRules.RIGHT_PBETA, PairRules.RIGHT_LIST_PBETA, PairRules.LEFT_PBETA, PairRules.LEFT_LIST_PBETA.

list_ss	(bossLib)
---------	-----------

```
list_ss : simpset
```

Synopsis

Simplification set for lists.

Description

The simplification set `list_ss` is a version of `arith_ss` enhanced for the theory of lists. The following rewrites are currently used to augment those already present from `arith_ss`:

```
|- (!l. APPEND [] l = l) /\
    !l1 l2 h. APPEND (h::l1) l2 = h::APPEND l1 l2
|- (!l1 l2 l3. (APPEND l1 l2 = APPEND l1 l3) = (l2 = l3)) /\
    !l1 l2 l3. (APPEND l2 l1 = APPEND l3 l1) = (l2 = l3)
|- (!l. EL 0 l = HD l) /\ !l n. EL (SUC n) l = EL n (TL l)
|- (!P. EVERY P [] = T) /\ !P h t. EVERY P (h::t) = P h /\ EVERY P t
|- (FLAT [] = []) /\ !h t. FLAT (h::t) = APPEND h (FLAT t)
|- (LENGTH [] = 0) /\ !h t. LENGTH (h::t) = SUC (LENGTH t)
|- (!f. MAP f [] = []) /\ !f h t. MAP f (h::t) = f h::MAP f t
|- (!f. MAP2 f [] [] = []) /\
    !f h1 t1 h2 t2.
    MAP2 f (h1::t1) (h2::t2) = f h1 h2::MAP2 f t1 t2
|- (!x. MEM x [] = F) /\ !x h t. MEM x (h::t) = (x = h) \\/ MEM x t
|- (NULL [] = T) /\ !h t. NULL (h::t) = F
|- (REVERSE [] = []) /\ !h t. REVERSE (h::t) = APPEND (REVERSE t) [h]
|- (SUM [] = 0) /\ !h t. SUM (h::t) = h + SUM t
|- !h t. HD (h::t) = h
|- !h t. TL (h::t) = t
```

```

|- !l1 l2 l3. APPEND l1 (APPEND l2 l3) = APPEND (APPEND l1 l2) l3
|- !l. ~NULL l ==> (HD l::TL l = l)
|- !a0 a1 a0' a1'. (a0::a1 = a0'::a1') = (a0 = a0') /\ (a1 = a1')
|- !l1 l2. LENGTH (APPEND l1 l2) = LENGTH l1 + LENGTH l2
|- !l f. LENGTH (MAP f l) = LENGTH l
|- !f l1 l2. MAP f (APPEND l1 l2) = APPEND (MAP f l1) (MAP f l2)
|- !a1 a0. ~(a0::a1 = [])
|- !a1 a0. ~([] = a0::a1)
|- !l f. ((MAP f l = []) = (l = [])) /\
          (([] = MAP f l) = (l = []))
|- !l. APPEND l [] = l
|- !l x. ~(l = x::l) /\ ~(x::l = l)
|- (!v f. case v f [] = v) /\
    !v f a0 a1. case v f (a0::a1) = f a0 a1
|- (!l1 l2. ([] = APPEND l1 l2) = (l1 = []) /\ (l2 = [])) /\
    !l1 l2. (APPEND l1 l2 = []) = (l1 = []) /\ (l2 = [])
|- (ZIP ([] []) = []) /\
    !x1 l1 x2 l2. ZIP (x1::l1,x2::l2) = (x1,x2)::ZIP (l1,l2)
|- (UNZIP [] = ([], [])) /\
    !x l. UNZIP (x::l) = (FST x::FST (UNZIP l),SND x::SND (UNZIP l))
|- !P l1 l2. EVERY P (APPEND l1 l2) = EVERY P l1 /\ EVERY P l2
|- !P l1 l2. EXISTS P (APPEND l1 l2) = EXISTS P l1 \/ EXISTS P l2
|- !e l1 l2. MEM e (APPEND l1 l2) = MEM e l1 \/ MEM e l2
|- (!x. LAST [x] = x) /\ !x y z. LAST (x::y::z) = LAST (y::z)
|- (!x. FRONT [x] = []) /\ !x y z. FRONT (x::y::z) = x::FRONT (y::z)
|- (!f e. FOLDL f e [] = e) /\
    !f e x l. FOLDL f e (x::l) = FOLDL f (f e x) l
|- (!f e. FOLDR f e [] = e) /\
    !f e x l. FOLDR f e (x::l) = f x (FOLDR f e l)

```

See also

BasicProvers.RW_TAC, BasicProvers.SRW_TAC, simpLib.SIMP_TAC, simpLib.SIMP_CONV, simpLib.SIMP_RULE, BasicProvers.bool_ss, bossLib.std_ss, bossLib.arith_ss.

list_thm_database	(listLib)
-------------------	-----------

```
list_thm_database: unit -> {{Aux_thms: thm list, Fold_thms: thm list}}
```

Synopsis

Returns the theorems known by `LIST_CONV`.

Description

The conversion `LIST_CONV` uses a database of theorems relating to system list constants. These theorems fall into two categories: definitions of list operators in terms of `FOLDR` and `FOLDL`; and auxiliary theorems about the base element and step functions in those definitions. `list_thm_database` provides a means of inspecting the database.

A call to `list_thm_database()` returns a pair of lists. The first element of the pair contains the known fold definitions. The second contains the known auxiliary theorems.

The following is an example of a fold definition in the database:

```
|- !l. SUM l = FOLDR $+ 0 l
```

Here `$+` is the step function and `0` is the base element of the definition. Definitions are initially held for the following system operators: `APPEND`, `FLAT`, `LENGTH`, `NULL`, `REVERSE`, `MAP`, `FILTER`, `ALL_EL`, `SUM`, `SOME_EL`, `IS_EL`, `AND_EL`, `OR_EL`, `PREFIX`, `SUFFIX`, `SNOC` and `FLAT` combined with `REVERSE`.

The following is an example of an auxiliary theorem:

```
|- MONOID $+ 0
```

Auxiliary theorems stored include monoid, commutativity, associativity, binary function commutativity, left identity and right identity theorems.

Failure

Never fails.

See also

`listLib.LIST_CONV`, `listLib.set_list_thm_database`, `listLib.X_LIST_CONV`.

<code>listDB</code>

<code>(DB)</code>

```
listDB : unit -> data list
```

Synopsis

All theorems, axioms, and definitions in the currently loaded theory segments.

Description

An invocation `listDB()` returns everything that has been stored in all theory segments currently loaded.

Example


```
- length (listDB());
> val it = 736 : int
```

See also

DB.thy, DB.theorems, DB.definitions, DB.axioms, DB.find, DB.match.

<div data-bbox="159 656 370 707" data-label="Text"> <p>LT_CONV</p> </div>	<div data-bbox="1011 654 1332 707" data-label="Text"> <p>(reduceLib)</p> </div>
---	---

LT_CONV : conv

Synopsis

Proves result of less-than ordering on two numerals.

Description

If m and n are both numerals (e.g. 0, 1, 2, 3,...), then LT_CONV " $m < n$ " returns the theorem:

$$\vdash (m < n) = T$$

if the natural number denoted by m is less than that denoted by n , or

$$\vdash (m < n) = F$$

otherwise.

Failure

LT_CONV tm fails unless tm is of the form " $m < n$ ", where m and n are numerals.

Example

```
#LT_CONV "0 < 12";;
|- 0 < 12 = T
```

```
#LT_CONV "13 < 13";;
|- 13 < 13 = F
```

```
#LT_CONV "25 < 12";;
|- 25 < 12 = F
```

map2**(Lib)**

```
map2 : ('a -> 'b -> 'c) -> 'a list -> 'b list -> 'c list
```

Synopsis

Maps a function over two lists to create one new list.

Description

`map2 f [x1,...,xn] [y1,...,yn]` returns `[f x1 y1,...,f xn yn]`.

Failure

Fails if the two lists are of different lengths. Also fails if any `f xi yi` fails.

Example

```
- map2 (curry op+) [1,2,3] [3,2,1];
> val it = [4, 4, 4] : int list
```

See also

`Lib.itlist`, `Lib.rev_itlist`, `Lib.itlist2`, `Lib.rev_itlist2`.

MAP2_CONV**(listLib)**

```
MAP2_CONV : conv -> conv
```

Synopsis

Compute the result of mapping a binary function down two lists.

Description

The function `MAP2_CONV` is a conversion for computing the result of mapping a binary function `f:ty1->ty2->ty3` down two lists `--'[l11;...;l1n]'` whose elements are of type `ty1` and `--'[l21;...;l2n]'` whose elements are of type `ty2`. The lengths of the two lists must be identical. The first argument to `MAP2_CONV` is expected to be a conversion that computes the result of applying the function `f` to a pair of corresponding elements of these lists. When applied to a term `--'f l1i l2i'`, this conversion should return a theorem of the form `|- (f l1i l2i) = ri`, where `ri` is the result of applying the function `f` to the elements `l1i` and `l2i`.

Given an appropriate `conv`, the conversion `MAP2_CONV conv` takes a term of the form `--'MAP2 f [l11;...;l12tn] [l21;...;l2n]'` and returns the theorem

```
|- MAP2 f [l11;...;l1n] [l21;...;l2n] = [r1;...;rn]
```

where `conv` (`--'f l1i l2i'--`) returns `|- (f l1i l2i) = ri` for `i` from 1 to `n`.

Example

The following is a very simple example in which the corresponding elements from the two lists are summed to form the resulting list:

```
- load_library_in_place num_lib;
- MAP2_CONV Num_lib.ADD_CONV (--'MAP2 $+ [1;2;3] [1;2;3]'--);
|- MAP2 $+ [1;2;3] [1;2;3] = [2;4;6]
```

Failure

`MAP2_CONV conv` fails if applied to a term not of the form described above. An application of `MAP2_CONV conv` to a term `--'MAP2 f [l11;...;l1n] [l21;...;l2n]'--` fails unless for all `i` where `1<=i<=n` evaluating `conv` (`--'f l1i l2i'--`) returns `|- (f l1i l2i) = ri` for some `ri`.

See also

`listLib.MAP_CONV`.

<div data-bbox="159 1220 397 1267" data-label="Text"> <p>MAP_CONV</p> </div>	<div data-bbox="1067 1218 1331 1267" data-label="Text"> <p>(listLib)</p> </div>
---	--

`MAP_CONV : conv -> conv`

Synopsis

Compute the result of mapping a function down a list.

Description

The function `MAP_CONV` is a parameterized conversion for computing the result of mapping a function `f : ty1 -> ty2` down a list `--'[t1;...;tn]'--` of elements of type `ty1`. The first argument to `MAP_CONV` is expected to be a conversion that computes the result of applying the function `f` to an element of this list. When applied to a term `--'f ti'--`, this conversion should return a theorem of the form `|- (f ti) = ri`, where `ri` is the result of applying the function `f` to the element `ti`.

Given an appropriate `conv`, the conversion `MAP_CONV conv` takes a term of the form `--'MAP f [t1;...;tn]'--` to the theorem

```
|- MAP f [t1;...;tn] = [r1;...;rn]
```

where `conv (--'f ti'--)` returns `|- (f ti) = ri` for i from 1 to n .

Example

The following is a very simple example in which no computation is done for applications of the function being mapped down a list:

```
- MAP_CONV ALL_CONV (--'MAP SUC [1;2;1;4]'--);
|- MAP SUC[1;2;1;4] = [SUC 1;SUC 2;SUC 1;SUC 4]
```

The result just contains applications of `SUC`, since the supplied conversion `ALL_CONV` does no evaluation.

We now construct a conversion that maps `SUC n` for any numeral n to the numeral standing for the successor of n :

```
- fun SUC_CONV tm =
  let val n = string_to_int(#Name(dest_const(rand tm)))
      val sucn = mk_const{{Name =int_to_string(n+1), Ty==(==' :num'==)}}
  in
    SYM (num_CONV sucn)
  end;
SUC_CONV = - : conv
```

The result is a conversion that inverts `num_CONV`:

```
- num_CONV (--'4'--);
|- 4 = SUC 3

- SUC_CONV (--'SUC 3'--);
|- SUC 3 = 4
```

The conversion `SUC_CONV` can then be used to compute the result of mapping the successor function down a list of numerals:

```
- MAP_CONV SUC_CONV (--'MAP SUC [1;2;1;4]'--);
|- MAP SUC[1;2;1;4] = [2;3;2;5]
```

Failure

`MAP_CONV conv` fails if applied to a term not of the form `--'MAP f [t1;...;tn]'--`. An application of `MAP_CONV conv` to a term `--'MAP f [t1;...;tn]'--` fails unless for all t_i in the list $[t_1; \dots; t_n]$, evaluating `conv (--'f ti'--)` returns `|- (f ti) = ri` for some r_i .

MAP EVERY**(Tactical)**

```
MAP EVERY : ((* -> tactic) -> * list -> tactic)
```

Synopsis

Sequentially applies all tactics given by mapping a function over a list.

Description

When applied to a tactic-producing function f and an operand list $[x_1; \dots; x_n]$, the elements of which have the same type as f 's domain type, `MAP EVERY` maps the function f over the list, producing a list of tactics, then applies these tactics in sequence as in the case of `EVERY`. The effect is:

```
MAP EVERY f [x1;...;xn] = (f x1) THEN ... THEN (f xn)
```

If the operand list is empty, then `MAP EVERY` has no effect.

Failure

The application of `MAP EVERY` to a function and operand list fails iff the function fails when applied to any element in the list. The resulting tactic fails iff any of the resulting tactics fails.

Example

A convenient way of doing case analysis over several boolean variables is:

```
MAP EVERY BOOL_CASES_TAC ["var1:bool";...;"varn:bool"]
```

See also

`Tactical.EVERY`, `Tactical.FIRST`, `Tactical.MAP_FIRST`, `Tactical.THEN`.

MAP FIRST**(Tactical)**

```
MAP FIRST : (('a -> tactic) -> 'a list -> tactic)
```

Synopsis

Applies first tactic that succeeds in a list given by mapping a function over a list.

Description

When applied to a tactic-producing function f and an operand list $[x_1, \dots, x_n]$, the elements of which have the same type as f 's domain type, `MAP_FIRST` maps the function f over the list, producing a list of tactics, then tries applying these tactics to the goal till one succeeds. If $f(x_m)$ is the first to succeed, then the overall effect is the same as applying $f(x_m)$. Thus:

$$\text{MAP_FIRST } f \ [x_1, \dots, x_n] = (f \ x_1) \ \text{ORELSE} \ \dots \ \text{ORELSE} \ (f \ x_n)$$
Failure

The application of `MAP_FIRST` to a function and tactic list fails iff the function does when applied to any of the elements of the list. The resulting tactic fails iff all the resulting tactics fail when applied to the goal.

See also

`Tactical.EVERY`, `Tactical.FIRST`, `Tactical.MAP_EVERY`, `Tactical.ORELSE`.

<code>mapfilter</code>	<code>(Lib)</code>
------------------------	--------------------

`mapfilter` : ('a -> 'b) -> 'a list -> 'b list

Synopsis

Applies a function to every element of a list, returning a list of results for those elements for which application succeeds.

Failure

If $f \ x$ raises `Interrupt` for some element x of l , then `mapfilter f l` fails.

Example

```
- mapfilter hd [[1,2,3],[4,5],[],[6,7,8],[]];
> val it = [1, 4, 6] : int list
```

See also

`Lib.filter`.

<code>match</code>	<code>(DB)</code>
--------------------	-------------------

`match` : string list -> term -> data list

Synopsis

Attempt to find matching theorems in the specified theories.

Description

An invocation `DB.match [s1,...,sn] M` collects all theorems, definitions, and axioms of the theories designated by `s1,...,sn` that have a subterm that matches `M`. If there are no matches, the empty list is returned.

The strings `s1,...,sn` should be a subset of the currently loaded theory segments. The string `"-"` may be used to designate the current theory segment. If the list of theories is empty, then all currently loaded theories are searched.

Failure

Never fails.

Example

```
- DB.match ["bool","pair"] (Term '(a = b) = c');
<<HOL message: inventing new type variable names: 'a'>>
> val it =
  [(("bool", "EQ_CLAUSES"),
    (|- !t.((T = t) = t) /\ ((t = T) = t) /\
      ((F = t) = ~t) /\ ((t = F) = ~t), Db.Thm)),
  (("bool", "EQ_EXPAND"),
    (|- !t1 t2. (t1 = t2) = t1 /\ t2 \/ ~t1 /\ ~t2, Db.Thm)),
  (("bool", "EQ_IMP_THM"),
    (|- !t1 t2. (t1 = t2) = (t1 ==> t2) /\ (t2 ==> t1), Db.Thm)),
  (("bool", "EQ_SYM_EQ"), (|- !x y. (x = y) = (y = x), Db.Thm)),
  (("bool", "FUN_EQ_THM"), (|- !f g. (f = g) = !x. f x = g x, Db.Thm)),
  (("bool", "OR_IMP_THM"), (|- !A B. (A = B \/ A) = B ==> A, Db.Thm)),
  (("bool", "REFL_CLAUSE"), (|- !x. (x = x) = T, Db.Thm)),
  (("pair", "CLOSED_PAIR_EQ"),
    (|- !x y a b. ((x,y) = (a,b)) = (x = a) /\ (y = b), Db.Thm)),
  (("pair", "CURRY_ONE_ONE_THM"),
    (|- (CURRY f = CURRY g) = (f = g), Db.Thm)),
  (("pair", "PAIR_EQ"), (|- ((x,y) = (a,b)) = (x = a) /\ (y = b), Db.Thm)),
  (("pair", "UNCURRY_ONE_ONE_THM"),
    (|- (UNCURRY f = UNCURRY g) = (f = g), Db.Thm))] :
  ((string * string) * (thm * class)) list
```

Comments

The notion of matching is a restricted version of higher-order matching.

Uses

For locating theorems when doing interactive proof.

See also

DB.matcher, DB.matchp, DB.find, DB.theorems, Db.thy, Db.listDB.

<div data-bbox="233 602 387 647" data-label="Text"><code>match</code></div>	<div data-bbox="1115 598 1410 647" data-label="Text"><code>(hol88Lib)</code></div>
---	--

```
match : term -> term -> (term * term) list * (hol_type * hol_type) list
```

Synopsis

Finds instantiations to match one term to another.

Description

When applied to two terms, `match_term` attempts to find a set of type and term instantiations for the first term (only) to make it equal the second. If it succeeds, it returns the instantiations in the form of a pair containing a hol88 term substitution and a hol88 type substitution. If the first term represents the conclusion of a theorem, the returned instantiations are of the appropriate form to be passed to `INST_TY_TERM`.

Failure

Fails if the term cannot be matched by one-way instantiation.

Comments

Note that `INST_TY_TERM` may still fail (when a variable that is instantiated occurs free in the theorem's assumptions).

Superseded by `Term.match_term`.

See also

`Term.match_term`.

<div data-bbox="233 1706 702 1756" data-label="Text"><code>MATCH_ABBREV_TAC</code></div>	<div data-bbox="1321 1704 1410 1756" data-label="Text"><code>(Q)</code></div>
--	---

```
Q.MATCH_ABBREV_TAC : term quotation -> tactic
```

Synopsis

Introduces abbreviations by matching a pattern against the goal statement.

Description

When applied to the goal $(as1, w)$, the tactic `Q.MATCH_ABBREV_TAC q` parses the quotation `q` in the context of the goal, producing a term to use as a pattern. The tactic then attempts a (first order) match of the pattern against the term w . Variables that occur in both the pattern and the goal are treated as “local constants”, and will not acquire instantiations.

For each variable v in the pattern that has not been treated as a local constant, there will be a instantiation term t , such that the substitution `pattern[v1 |-> t1, v2 |-> t2, ...]` produces w . The effect of the tactic is to then perform abbreviations in the goal, replacing each t with the corresponding v , and adding assumptions of the form `Abbrev(v = t)` to the goal.

Failure

`MATCH_ABBREV_TAC` fails if the pattern provided does not match the goal, or if variables from the goal are used in the pattern in ways that make the pattern fail to type-check.

Example

If the current goal is

```
?- (n + 10) * y <= 42315 /\ (!x y. x < y ==> f x < f y)
```

then applying the tactic `Q.MATCH_ABBREV_TAC 'X <= Y /\ P'` results in the goal

```
Abbrev(X = (n + 10) * y),
Abbrev(Y = 42315),
Abbrev(P = !x y. x < y ==> f x < f y)
  ?-
X <= Y /\ P
```

See also

`Q.ABBREV_TAC`, `Q.HO_MATCH_ABBREV_TAC`.

MATCH_ACCEPT_TAC	(Tactic)
------------------	----------

`MATCH_ACCEPT_TAC` : `thm_tactic`

Synopsis

Solves a goal which is an instance of the supplied theorem.

Description

When given a theorem $A' \vdash t$ and a goal $A \text{ ?- } t'$ where t can be matched to t' by instantiating variables which are either free or universally quantified at the outer level, including appropriate type instantiation, `MATCH_ACCEPT_TAC` completely solves the goal.

```
A ?- t'
===== MATCH_ACCEPT_TAC (A' |- t)
```

Unless A' is a subset of A , this is an invalid tactic.

Failure

Fails unless the theorem has a conclusion which is instantiable to match that of the goal.

Example

The following example shows variable and type instantiation at work. We can use the polymorphic list theorem `HD`:

```
HD = |- !h t. HD(CONS h t) = h
```

to solve the goal:

```
?- HD [1;2] = 1
```

simply by:

```
MATCH_ACCEPT_TAC HD
```

See also

`Tactic.ACCEPT_TAC`.

`MATCH_ASSUM_ABBREV_TAC` (Q)

```
Q.MATCH_ASSUM_ABBREV_TAC : term quotation -> tactic
```

Synopsis

Introduces abbreviations by matching a pattern against an assumption.

Description

When applied to the goal $(as1, w)$, the tactic `Q.MATCH_ASSUM_ABBREV_TAC q` parses the quotation q in the context of the goal, producing a term to use as a pattern. The tactic

then attempts a (first order) match of the pattern against each term in `as1`, stopping on the first matching assumption `a`. Variables that occur in both the pattern and the goal are treated as “local constants”, and will not acquire instantiations.

For each variable `v` in the pattern that has not been treated as a local constant, there will be an instantiation term `t`, such that the substitution `pattern[v1 |-> t1, v2 |-> t2, ...]` produces `a`. The effect of the tactic is to then perform abbreviations in the goal, replacing each `t` with the corresponding `v`, and adding assumptions of the form `Abbrev(v = t)` to the goal.

Failure

`MATCH_ABBREV_TAC` fails if the pattern provided does not match any assumption, or if variables from the goal are used in the pattern in ways that make the pattern fail to type-check.

Comments

This tactic improves on the following tedious workflow: `Q.PAT_ASSUM pat MP_TAC, Q.MATCH_ABBREV_TAC 'pat ==> X', Q.UNABBREV_TAC 'X', STRIP_TAC`.

See also

`Q.MATCH_ABBREV_TAC`, `Q.MATCH_ASSUM_RENAME_TAC`.

<code>MATCH_ASSUM_RENAME_TAC</code>

<code>(Q)</code>

`Q.MATCH_ASSUM_RENAME_TAC : term quotation -> string list -> tactic`

Synopsis

Replaces selected terms with new variables by matching a pattern against an assumption.

Description

When applied to the goal `(as1, w)`, the tactic `Q.MATCH_ASSUM_RENAME_TAC q ls` parses the quotation `q` in the context of the goal, producing a term to use as a pattern. The tactic then attempts a (first order) match of the pattern against each term in `as1`, stopping on the first matching assumption `a`.

For each variable `v` in the pattern, there will be an instantiation term `t`, such that the substitution `pattern[v1 |-> t1, v2 |-> t2, ...]` produces `a`. The effect of the tactic is to then replace each `t` with the corresponding `v`, yielding a new goal. The list `ls` is of exceptions: if a variable `v`'s name appears in `ls`, then no replacement of `v` for `t` is made.

Failure

`MATCH_ASSUM_RENAME_TAC` fails if the pattern provided does not match any assumption, or if variables from the goal are used in the pattern in ways that make the pattern fail to type-check.

Example

If the current goal is

```
(f x = Pair C'' C0') ?- (f C'' = f C0')
```

then applying the tactic `Q.MATCH_ASSUM_RENAME_TAC 'X = Pair c1 c2' ["X"]` results in the goal

```
(f x = Pair c1 c2) ?- (f c1 = f c2)
```

Comments

This tactic improves on the following tedious workflow: `Q.PAT_ASSUM pat MP_TAC, Q.MATCH_ABBREV_TAC 'pat ==> X', Q.UNABBREV_TAC 'X', markerLib.RM_ALL_ABBREVS_TAC, STRIP_TAC`.

See also

`Q.MATCH_RENAME_TAC`.

<div data-bbox="234 1256 474 1305" data-label="Text"><code>MATCH_MP</code></div>	<div data-bbox="1203 1256 1410 1305" data-label="Text"><code>(Drule)</code></div>
--	---

```
MATCH_MP : thm -> thm -> thm
```

Synopsis

Modus Ponens inference rule with automatic matching.

Description

When applied to theorems $A1 \vdash !x1...xn. t1 \implies t2$ and $A2 \vdash t1'$, the inference rule `MATCH_MP` matches $t1$ to $t1'$ by instantiating free or universally quantified variables in the first theorem (only), and returns a theorem $A1 \cup A2 \vdash !xa...xk. t2'$, where $t2'$ is a correspondingly instantiated version of $t2$. Polymorphic types are also instantiated if necessary.

Variables free in the consequent but not the antecedent of the first argument theorem will be replaced by variants if this is necessary to maintain the full generality of the theorem, and any which were universally quantified over in the first argument theorem will be universally quantified over in the result, and in the same order.

$$\frac{A1 \mid - !x1..xn. t1 ==> t2 \quad A2 \mid - t1'}{\text{MATCH_MP}} A1 \text{ u } A2 \mid - !xa..xk. t2'$$

Failure

Fails unless the first theorem is a (possibly repeatedly universally quantified) implication whose antecedent can be instantiated to match the conclusion of the second theorem, without instantiating any variables which are free in A1, the first theorem's assumption list.

Example

In this example, automatic renaming occurs to maintain the most general form of the theorem, and the variant corresponding to z is universally quantified over, since it was universally quantified over in the first argument theorem.

```
- val ith = (GENL [Term 'x:num', Term 'z:num']
             o DISCH_ALL
             o AP_TERM (Term '$+ (w + z)'))
  (ASSUME (Term 'x:num = y'));
> val ith = |- !x z. (x = y) ==> (w + z + x = w + z + y) : thm

- val th = ASSUME (Term 'w:num = z');
> val th = [w = z] |- w = z : thm

- MATCH_MP ith th;
> val it = [w = z] |- !z'. w' + z' + w = w' + z' + z : thm
```

See also

Thm.EQ_MP, Tactic.MATCH_MP_TAC, Thm.MP, Tactic.MP_TAC, ConseqConv.CONSEQ_REWRITE_CONV.

MATCH_MP_TAC

(Tactic)

MATCH_MP_TAC : thm_tactic

Synopsis

Reduces the goal using a supplied implication, with matching.

Description

When applied to a theorem of the form

$$A' \vdash !x_1 \dots x_n. s \implies !y_1 \dots y_m. t$$

`MATCH_MP_TAC` produces a tactic that reduces a goal whose conclusion t' is a substitution and/or type instance of t to the corresponding instance of s . Any variables free in s but not in t will be existentially quantified in the resulting subgoal:

$$\frac{A \text{ ?- } !v_1 \dots v_i. t'}{\text{===== MATCH_MP_TAC (A' \vdash !x_1 \dots x_n. s \implies !y_1 \dots y_m. t)} \\ A \text{ ?- } ?z_1 \dots z_p. s'}$$

where z_1, \dots, z_p are (type instances of) those variables among x_1, \dots, x_n that do not occur free in t . Note that this is not a valid tactic unless A' is a subset of A .

Failure

Fails unless the theorem is an (optionally universally quantified) implication whose consequent can be instantiated to match the goal. The generalized variables v_1, \dots, v_i must occur in s' in order for the conclusion t of the supplied theorem to match t' .

See also

`Thm.EQ_MP`, `Drule.MATCH_MP`, `Thm.MP`, `Tactic.MP_TAC`, `ConseqConv.CONSEQ_CONV_TAC`.

<code>MATCH_RENAME_TAC</code>	<code>(Q)</code>
-------------------------------	------------------

`Q.MATCH_RENAME_TAC` : `term quotation -> string list -> tactic`

Synopsis

Replaces selected terms with new variables by matching a pattern against the goal statement.

Description

When applied to the goal $(as1, w)$, the tactic `Q.MATCH_RENAME_TAC q ls` parses the quotation q in the context of the goal, producing a term to use as a pattern. The tactic then attempts a (first order) match of the pattern against the term w .

For each variable v in the pattern, there will be an instantiation term τ , such that the substitution `pattern[v1 |-> t1, v2 |-> t2, ...]` produces w . The effect of the tactic is to then replace each τ with the corresponding v , yielding a new goal. The list ls is of exceptions: if a variable v 's name appears in ls , then no replacement of v for τ is made.

Failure

`MATCH_RENAME_TAC` fails if the pattern provided does not match the goal, or if variables from the goal are used in the pattern in ways that make the pattern fail to type-check.

Example

If the current goal is

$$\text{?- (f x = Pair C'' C0') ==> (f C'' = f C0')}$$

then applying the tactic `Q.MATCH_RENAME_TAC '(f x = Pair c1 c2) ==> X' ["X"]` results in the goal

$$\text{?- (f x = Pair c1 c2) ==> (f c1 = f c2)}$$
Comments

This tactic is equivalent to first applying `Q.MATCH_ABBREV_TAC q`, then applying `Q.RM_ABBREV_TAC 'v'` for each `v` in `q` whose name is not in `ls`.

See also

`Q.MATCH_ABBREV_TAC`, `Q.MATCH_ASSUM_RENAME_TAC`.

<div data-bbox="158 1068 456 1120" data-label="Text"> <p><code>match_term</code></p> </div>	<div data-bbox="1155 1064 1329 1120" data-label="Text"> <p>(Term)</p> </div>
---	--

`match_term : term -> term -> (term,term) subst * (hol_type,hol_type) subst`

Synopsis

Finds instantiations to match one term to another.

Description

An application `match_term M N` attempts to find a set of type and term instantiations for `M` to make it alpha-convertible to `N`. If `match_term` succeeds, it returns the instantiations in the form of a pair containing a term substitution and a type substitution. In particular, if `match_term pat ob` succeeds in returning a value `(S,T)`, then

$$\text{aconv (subst S (inst T pat)) ob.}$$
Failure

Fails if the term cannot be matched by one-way instantiation.

Example

The following shows how `match_term` could be used to match the conclusion of a theorem to a term.

```

- val th = REFL (Term 'x:'a');
  val th = |- x = x : thm

- match_term (concl th) (Term '1 = 1');
  val it = ([{redex = 'x', residue = '1'}],
            [{redex = ':'a', residue = ':num'}])
    : term subst * hol_type subst

- INST_TY_TERM it th;
  val it = |- 1 = 1

```

Comments

For instantiating theorems `PART_MATCH` is usually easier to use.

See also

`Type.match_type`, `Drule.INST_TY_TERM`, `Drule.PART_MATCH`.

<div data-bbox="231 1090 555 1140" data-label="Text"> <p><code>match_term1</code></p> </div>	<div data-bbox="1230 1088 1409 1140" data-label="Text"> <p>(Term)</p> </div>
--	--

```

match_term1
  : hol_type list -> term set -> term -> term
  -> (term,term) subst * (hol_type,hol_type) subst

```

Synopsis

Match two terms while restricting some instantiations.

Description

An invocation `match_term1 avoid_tys avoid_tms pat ob (tmS,tyS)`, if it does not raise an exception, returns a pair of substitutions (S,T) such that

$$\text{aconv } (\text{subst } S \text{ (inst } T \text{ pat)}) \text{ ob.}$$

The arguments `avoid_tys` and `avoid_tms` specify type and term variables in `pat` that are not allowed to become redexes in S and T .

Failure

`match_term1` will fail if no S and T meeting the above requirements can be found. If a match (S,T) between `pat` and `ob` can be found, but elements of `avoid_tys` would appear

as redexes in T or elements of `avoid_tms` would appear as redexes in S, then `match_term1` will also fail.

Example

```
- val (S,T) = match_term1 [] empty_varset
      (Term '\x:'a. x = f (y:'b)')
      (Term '\a.    a = ~p');
> val S = [{redex = '(f :'b -> 'a)', residue = '$~'},
           {redex = '(y :'b)',      residue = '(p :bool)'}] : ...

      val T = [{redex = ':'b', residue = ':bool'},
               {redex = ':'a', residue = ':bool'}] : ...

- match_term1 [alpha] empty_varset (* forbid instantiation of 'a *)
  (Term '\x:'a. x = f (y:'b)')
  (Term '\a.    a = ~p');
! Uncaught exception:
! HOL_ERR

- match_term1 [] (HOLset.add(empty_varset,mk_var("y",beta)))
  (Term '\x:'a. x = f (y:'b)')
  (Term '\a.    a = ~p');
! Uncaught exception:
! HOL_ERR
```

See also

`Term.match_term`, `Term.raw_match`, `Term.subst`, `Term.inst`, `Type.match_typed`, `Type.type_subst`.

<div data-bbox="158 1563 454 1619" data-label="Text"> <h2 style="margin: 0;">match_type</h2> </div>	<div data-bbox="1155 1559 1332 1619" data-label="Text"> (Type) </div>
---	--

`match_type` : `hol_type -> hol_type -> hol_type subst`

Synopsis

Calculates a substitution `theta` such that instantiating the first argument with `theta` equals the second argument.

Description

If `match_type ty1 ty2` succeeds, then

```
type_subst (match_type ty1 ty2) ty1 = ty2
```

Failure

If no such substitution can be found.

Example

```
- match_type alpha (Type':num');
> val it = [{redex = ':'a', residue = ':num'}] : hol_type subst

- let val patt = Type':('a -> bool) -> 'b'
      val ty =   Type':(num -> bool) -> bool'
  in
      type_subst (match_type patt ty) patt = ty
  end;
> val it = true : bool

- match_type (alpha --> alpha)
              (ind   --> bool);
! Uncaught exception:
! HOL_ERR
```

See also

Term.match_term, Type.type_subst.

<pre>match_type1</pre>	<pre>(Type)</pre>
------------------------	-------------------

```
match_type1 : hol_type list -> hol_type -> hol_type
              -> (hol_type, hol_type) subst
```

Synopsis

Match types with restrictions.

Description

An invocation `match_type1 away pat ty` matches `pat` to `ty` in the same way as `match_type`, but prohibits any of the type variables in `away` from being instantiated. In effect, the

elements of `away`, although type variables, are treated as constants in `pat` during the matching process.

Failure

An invocation of `match_type1 away pat ty` will fail if `match_type pat ty` would fail. It will also fail if `match_type pat ty` would succeed giving a substitution $\{redex_1, residue_1\}, \dots, \{redex_n, residue_n\}$ where one or more of the `redex_i` are members of `away`.

Example

In the first example, we perform a normal match operation

```
- match_type1 [] (alpha --> beta --> gamma)
                (bool --> ind --> delta);
> val it = [{redex = ':'c', residue = ':'d'},
            {redex = ':'b', residue = ':ind'},
            {redex = ':'a', residue = ':bool'}] : ...
```

Now we require that `gamma`, although a type variable in the pattern, not be instantiable. In the first try, the match succeeds because `'c` is mapped only to itself. In the second, it fails because an association is made between `'c` and `'d`.

```
- match_type1 [gamma] (alpha --> beta --> gamma)
                  (bool --> ind --> gamma);
> val it = [{redex = ':'b', residue = ':ind'},
            {redex = ':'a', residue = ':bool'}] : ...

- match_type1 [gamma] (alpha --> beta --> gamma)
                  (bool --> ind --> delta);
! Uncaught exception:
! HOL_ERR
```

Comments

The use of `away` allows matching to take account of type variables that are 'frozen' (by occurring in the hypotheses of a theorem, for example). This allows certain fruitless proof attempts to be avoided at the matching stage.

See also

`Type.match_type`, `Term.match_term.`, `HolKernel.ho_match_term`, `Type.type_subst`.

matcher	(DB)
---	--

`matcher : (term -> term -> 'a) -> string list -> term -> data list`

Synopsis

All theory elements matching a given term.

Description

An invocation `matcher pm [thy1,...,thyn] M` collects all elements of the theory segments `thy1,...,thyn` that have a subterm `N` such that `pm M` does not fail (raise an exception) when applied to `N`. Thus `matcher` potentially traverses all subterms of all theorems in all the listed theories in its search for ‘matches’.

If the list of theory segments is empty, then all currently loaded segments are examined. The string `"-"` may be used to designate the current theory segment.

Failure

Never fails, but may return an empty list.

Example

```
- DB.matcher match_term ["relation"] (Term 'P \/\ Q');
> val it =
  [(("relation", "RC_def"), (|- !R x y. RC R x y = (x = y) \/\ R x y, Def)),
   (("relation", "RTC_CASES1"),
    (|- !R x y. RTC R x y = (x = y) \/\ ?u. R x u /\ RTC R u y, Thm)),
   (("relation", "RTC_CASES2"),
    (|- !R x y. RTC R x y = (x = y) \/\ ?u. RTC R x u /\ R u y, Thm)),
   (("relation", "RTC_TC_RC"),
    (|- !R x y. RTC R x y ==> RC R x y \/\ TC R x y, Thm)),
   (("relation", "TC_CASES1"),
    (|- !R x z. TC R x z ==> R x z \/\ ?y. R x y /\ TC R y z, Thm)),
   (("relation", "TC_CASES2"),
    (|- !R x z. TC R x z ==> R x z \/\ ?y. TC R x y /\ R y z, Thm))] :
  ((string * string) * (thm * class)) list

- DB.matcher (ho_match_term [] empty_varset) [] (Term '?x. P x \/\ Q x');
<<HOL message: inventing new type variable names: 'a>>
> val it =
  [(("arithmetic", "ODD_OR_EVEN"),
   (|- !n. ?m. (n = SUC (SUC 0) * m) \/\ (n = SUC (SUC 0) * m + 1), Thm)),
   (("bool", "EXISTS_OR_THM"),
   (|- !P Q. (?x. P x \/\ Q x) = (?x. P x) \/\ ?x. Q x, Thm)),
   (("bool", "LEFT_OR_EXISTS_THM"),
   (|- !P Q. (?x. P x) \/\ Q = ?x. P x \/\ Q, Thm)),
   (("bool", "RIGHT_OR_EXISTS_THM"),
```

```
(|- !P Q. P \\/ (?x. Q x) = ?x. P \\/ Q x, Thm)),
(("sum", "IS_SUM_REP"),
(|- !f.
  IS_SUM_REP f =
  ?v1 v2.
    (f = (\b x y. (x = v1) /\ b)) \\/ (f = (\b x y. (y = v2) /\ ~b)),
  Def))] : ((string * string) * (thm * class)) list
```

Comments

Usually, pm will be a pattern-matcher, but it need not be.

See also

DB.match, DB.apropos, DB.matchp, DB.find.

<div data-bbox="158 972 341 1023" data-label="Text"> <p>matchp</p> </div>	<div data-bbox="1212 967 1331 1019" data-label="Text"> <p>(DB)</p> </div>
---	---

matchp : (thm -> bool) -> string list -> data list

Synopsis

All theory elements satisfying a predicate.

Description

An invocation `matchp P [thy1,...,thyn]` collects all elements of the theory segments `thy1,...,thyn` that `P` holds of. If the list of theory segments is empty, then all currently loaded segments are examined. The string `"-"` may be used to designate the current theory segment.

Failure

Fails if `P` fails when applied to a theorem in one of the theories being searched.

Example

The following query returns all unconditional rewrite rules in the theory `pair`.

```
- matchp (is_eq o snd o strip_forall o concl) ["pair"];
> val it =
  [(("pair", "CLOSED_PAIR_EQ"),
    (|- !x y a b. ((x,y) = (a,b)) = (x = a) /\ (y = b), Thm)),
   (("pair", "COMMA_DEF"), (|- !x y. (x,y) = ABS_prod (MK_PAIR x y), Def)),
```

```

(("pair", "CURRY_DEF"), (|- !f x y. CURRY f x y = f (x,y), Def)),
(("pair", "CURRY_ONE_ONE_THM"), (|- (CURRY f = CURRY g) = (f = g), Thm)),
(("pair", "CURRY_UNCURRY_THM"), (|- !f. CURRY (UNCURRY f) = f, Thm)),
(("pair", "ELIM_PEXISTS"),
  (|- (?p. P (FST p) (SND p)) = ?p1 p2. P p1 p2, Thm)),
(("pair", "ELIM_PFORALL"),
  (|- (!p. P (FST p) (SND p)) = !p1 p2. P p1 p2, Thm)),
(("pair", "ELIM_UNCURRY"),
  (|- !f. UNCURRY f = (\x. f (FST x) (SND x)), Thm)),
(("pair", "EXISTS_PROD"), (|- (?p. P p) = ?p_1 p_2. P (p_1,p_2), Thm)),
(("pair", "FORALL_PROD"), (|- (!p. P p) = !p_1 p_2. P (p_1,p_2), Thm)),
(("pair", "FST"), (|- !x y. FST (x,y) = x, Thm)),
(("pair", "IS_PAIR_DEF"),
  (|- !P. IS_PAIR P = ?x y. P = MK_PAIR x y, Def)),
(("pair", "LAMBDA_PROD"),
  (|- !P. (\p. P p) = (\(p1,p2). P (p1,p2)), Thm)),
(("pair", "LET2_RAND"),
  (|- !P M N. P (let (x,y) = M in N x y) = (let (x,y) = M in P (N x y)),
  Thm)),
(("pair", "LET2_RATOR"),
  (|- !M N b. (let (x,y) = M in N x y) b = (let (x,y) = M in N x y b),
  Thm)),
(("pair", "LEX_DEF"),
  (|- !R1 R2. R1 LEX R2 = (\(s,t) (u,v). R1 s u /\ (s = u) /\ R2 t v),
  Def)),
(("pair", "MK_PAIR_DEF"),
  (|- !x y. MK_PAIR x y = (\a b. (a = x) /\ (b = y)), Def)),
(("pair", "PAIR"), (|- !x. (FST x,SND x) = x, Def)),
(("pair", "pair_case_def"), (|- case = UNCURRY, Def)),
(("pair", "pair_case_thm"), (|- case f (x,y) = f x y, Thm)),
(("pair", "PAIR_EQ"), (|- ((x,y) = (a,b)) = (x = a) /\ (y = b), Thm)),
(("pair", "PAIR_MAP"),
  (|- !f g p. (f ## g) p = (f (FST p),g (SND p)), Def)),
(("pair", "PAIR_MAP_THM"),
  (|- !f g x y. (f ## g) (x,y) = (f x,g y), Thm)),
(("pair", "PEXISTS_THM"), (|- !P. (?x y. P x y) = ?(x,y). P x y, Thm)),
(("pair", "PFORALL_THM"), (|- !P. (!x y. P x y) = !(x,y). P x y, Thm)),
(("pair", "RPROD_DEF"),
  (|- !R1 R2. RPROD R1 R2 = (\(s,t) (u,v). R1 s u /\ R2 t v), Def)),
(("pair", "SND"), (|- !x y. SND (x,y) = y, Thm)),

```

```

(("pair", "UNCURRY"), (|- !f v. UNCURRY f v = f (FST v) (SND v), Def)),
(("pair", "UNCURRY_CURRY_THM"), (|- !f. UNCURRY (CURRY f) = f, Thm)),
(("pair", "UNCURRY_DEF"), (|- !f x y. UNCURRY f (x,y) = f x y, Thm)),
(("pair", "UNCURRY_ONE_ONE_THM"),
  (|- (UNCURRY f = UNCURRY g) = (f = g), Thm)),
(("pair", "UNCURRY_VAR"),
  (|- !f v. UNCURRY f v = f (FST v) (SND v), Thm))]
: ((string * string) * (thm * class)) list

```

See also

DB.match, DB.matcher, DB.apropos, DB.find.

max_print_depth	(Globals)
-----------------	-----------

max_print_depth : int ref

Synopsis

Sets depth bound on prettyprinting.

Description

The reference variable `max_print_depth` is used to define the maximum depth of printing for the pretty printer. If the number of blocks (an internal notion used by the prettyprinter) becomes greater than the value set by `max_print_depth` then the blocks are abbreviated by the holophrast `....`. By default, the value of `max_print_depth` is `~1`. This is interpreted to mean ‘print everything’.

Failure

Never fails.

Example

To change the maximum depth setting to 10, the command will be:

```

- max_print_depth := 10;
> val it = () : unit

```

The theorem `numeralTheory.numeral_distrib` then prints as follows:

```

- numeralTheory.numeral_distrib;
> val it =
  |- (!n. 0 + n = n) /\ (!n. n + 0 = n) /\
    (!n m. NUMERAL n + NUMERAL m = NUMERAL (iZ (n + m))) /\
    (!n. 0 * n = 0) /\ (!n. n * 0 = 0) /\
    (!n m. ... .. * ... .. = NUMERAL (... * ...)) /\
    (!n. ... - ... = 0) /\ (!n. ... = ...) /\ (!... .. .) /\ ... /\ ...
: thm

```

measureInduct_on

(bossLib)

```
measureInduct_on : term quotation -> tactic
```

Synopsis

Perform complete induction with a supplied measure function.

Description

If q parses into a well-typed term M N , an invocation `measureInduct_on q` begins a proof by induction, using M to map N into a number. The term N should occur free in the current goal.

Failure

If M N does not parse into a term or if N does not occur free in the current goal.

Example

Suppose we wish to prove P (APPEND 11 12) by induction on the length of 11. Then `measureInduct_on 'LENGTH 11'` yields the goal

```
{ !y. LENGTH y < LENGTH 11 ==> P (APPEND y 12) } ?- P (APPEND 11 12)
```

See also

`bossLib.completeInduct_on`, `bossLib.Induct`, `bossLib.Induct_on`.

mem

(Lib)

```
mem : ''a -> ''a list -> bool
```


Synopsis

Tests whether a list contains a certain member.

Description

An invocation `mem x [x1, ..., xn]` returns `true` if some `xi` in the list is equal to `x`. Otherwise it returns `false`.

Failure

Never fails.

Comments

Note that the type of the members of the list must be an SML equality type. If set operations on a non-equality type are desired, use the ‘op_’ variants, which take an equality predicate as an extra argument.

A high-performance implementation of finite sets may be found in structure `HOLset`.

See also

`Lib.op_mem`, `Lib.insert`, `Lib.tryfind`, `Lib.exists`, `Lib.all`, `Lib.assoc`, `Lib.rev_assoc`.

merge

(Tag)

```
merge : tag -> tag -> tag
```

Synopsis

Combine two tags into one.

Description

When two theorems interact via inference, their tags are merged. This propagates to the new theorem the fact that either or both were constructed via shortcut.

Failure

Never fails.

Example

```
- Tag.merge (Tag.read "foo") (Tag.read "bar");
> val it = Kerneltypes.TAG(["bar", "foo"], []) : tag

- Tag.merge it (Tag.read "foo");
> val it = Kerneltypes.TAG(["bar", "foo"], []) : tag
```

Comments

Although it is not harmful to use this entrypoint, there is little reason to, since the merge operation is only used inside the HOL kernel.

See also

`Tag.read`, `Thm.mk_oracle_thm`, `Thm.tag`.

<code>MESG_outstream</code>	(Feedback)
-----------------------------	----------------------------

`MESG_outstream` : `TextIO.outstream` ref

Synopsis

Reference to output stream used when printing `HOL_MESG`

Description

The value of reference cell `MESG_outstream` controls where `HOL_MESG` prints its argument.

The default value of `MESG_outstream` is `TextIO.stdOut`.

Example

```
- val ostrm = TextIO.openOut "foo";
> val ostrm = <ostream> : ostream

- MESG_outstream := ostrm;
> val it = () : unit

- HOL_MESG "Nattering nabobs of negativity.";
> val it = () : unit

- TextIO.closeOut ostrm;
> val it = () : unit

- val istrm = TextIO.openIn "foo";
> val istrm = <instream> : instream

- print (TextIO.inputAll istrm);
<<HOL message: Nattering nabobs of negativity.>>
```

See also

Feedback, Feedback.HOL_MESG, Feedback.ERR_outstream, Feedback.WARNING_outstream, Feedback.emit_MESG.

<p>MESG_to_string</p>	<p>(Feedback)</p>
-----------------------	-------------------

MESG_to_string : (string -> string) ref

Synopsis

Alterable function for formatting HOL_MESG

Description

MESG_to_string is a reference to a function for formatting the argument to an application of HOL_MESG.

The default value of MESG_to_string is format_MESG.

Example

```

- fun alt_MESG_report s = String.concat["Dear HOL user: ", s, "\n"];

- MESG_to_string := alt_MESG_report;

- HOL_MESG "Hi there."

Dear HOL user: Hi there.
> val it = () : unit

```

See also

Feedback, Feedback.HOL_MESG, Feedback.format_MESG, Feedback.ERR_to_string, Feedback.WARNING_to_string.

<p>MESON_TAC</p>	<p>(mesonLib)</p>
------------------	-------------------

MESON_TAC : thm list -> tactic

Synopsis

Performs first order proof search to prove the goal, using the given theorems as additional assumptions in the search.

Description

MESON_TAC performs first order proof using the model elimination algorithm. This algorithm is semi-complete for pure first order logic. It makes special provision for handling polymorphic and higher-order values, and often this is sufficient. It does not handle conditional expressions at all, and these should be eliminated before MESON_TAC is applied.

MESON_TAC works by first converting the problem instance it is given into an internal format where it can do proof search efficiently, without having to do proof search at the level of HOL inference. If a proof is found, this is translated back into applications of HOL inference rules, proving the goal.

The feedback given by MESON_TAC is controlled by the level of the integer reference variable `mesonLib.chatting`. At level zero, nothing is printed. At the default level of one, a line of dots is printed out as the proof progresses. At all other values for this variable, MESON_TAC is most verbose. If the proof is progressing quickly then it is often worth waiting for it to go quite deep into its search. Once a proof slows down, it is not usually worth waiting for it after it has gone through a few (no more than five or six) levels. (At level one, a “level” is represented by the printing of a single dot.)

Failure

MESON_TAC fails if it searches to a depth equal to the contents of the reference variable `mesonLib.max_depth` (set to 30 by default, but changeable by the user) without finding a proof. Shouldn't fail otherwise.

Uses

MESON_TAC can only progress the goal to a successful proof of the (whole) goal or not at all. In this respect it differs from tactics such as simplification and rewriting. Its ability to solve existential goals and to make effective use of transitivity theorems make it a particularly powerful tactic.

Comments

The assumptions of a goal are ignored when MESON_TAC is applied. To include assumptions use `ASM_MESON_TAC`.

See also

`mesonLib.ASM_MESON_TAC`, `mesonLib.GEN_MESON_TAC`.

MK_ABS

(Drule)

MK_ABS : (thm -> thm)

Synopsis

Abstracts both sides of an equation.

Description

When applied to a theorem $A \vdash !x. t1 = t2$, whose conclusion is a universally quantified equation, MK_ABS returns the theorem $A \vdash \lambda x. t1 = \lambda x. t2$.

$$\frac{A \vdash !x. t1 = t2}{A \vdash (\lambda x. t1) = (\lambda x. t2)} \quad \text{MK_ABS}$$

Failure

Fails unless the theorem is a (singly) universally quantified equation.

See also

Thm.ABS, Drule.HALF_MK_ABS, Thm.MK_COMB, Drule.MK_EXISTS.

mk_abs

(Term)

mk_abs : term * term -> term

Synopsis

Constructs an abstraction.

Description

mk_abs (v, t) returns the lambda abstraction $\lambda v. t$. All free occurrences of v in t thereby become bound.

Failure

Fails if v is not a variable.

See also

Term.dest_abs, Term.is_abs, boolSyntax.list_mk_abs, Term.mk_var, Term.mk_const, Term.mk_comb.

mk_anylet**(pairSyntax)**

```
mk_anylet : (term * term) list * term -> term
```

Synopsis

Constructs arbitrary let terms.

Description

The invocation `mk_anylet ((a1,b1),..., (an,bn), N)` returns a term of the form ‘LET P Q’, which will prettyprint as `let a1 = b1 and ... and an = bn in N`. The internal representation is equal to

```
LET (... (LET (\an ... \a1. N) bn) ...) b1
```

Each a_i can be a varstruct (a single variable or a tuple of variables), or a function variable applied to a sequence of varstructs. In the usual case, only a single binding is made, i.e., `mk_anylet ((a,b), N)`, and the result is equal to `LET (\a. N) b`.

Failure

Fails if the type of any a_i is not equal to the type of the corresponding b_i .

Example

```
- strip_comb (mk_anylet ((Term'x', Term'M'), Term'N x'));
> val it = ('LET', ['\x. N x', 'M']) : term * term list

- mk_anylet ((('f (x:'a,y:'b):'c', 'M:'c'), ('g (z:'c) :'d', 'N:'d'),
              'g (f (a:'a,b:'b):'c):'d');
> val it = 'let f (x,y) = M and g z = N in g (f (a,b))' : term
```

Uses

Programming that involves manipulation of term syntax.

See also

`boolSyntax.mk_let`, `boolSyntax.dest_let`, `boolSyntax.is_let`,
`pairSyntax.list_mk_anylet`, `pairSyntax.dest_anylet`.

mk_arb**(boolSyntax)**

```
mk_arb : hol_type -> term
```

Synopsis

Creates a type instance of the ARB constant.

Description

For any HOL type `ty`, `mk_arb ty` creates a type instance of the ARB constant.

Failure

Never fails.

Comments

ARB is a constant of type `'a`. It is sometimes used for creating pseudo-partial functions.

See also

`boolSyntax.dest_arb`, `boolSyntax.is_arb`, `boolSyntax.arb`.

<code>mk_bool_case</code>

<code>(boolSyntax)</code>

```
mk_bool_case : term * term * term -> term
```

Synopsis

Constructs a case expression over `bool`.

Description

`mk_bool_case M1 M2 b` returns `bool_case M1 M2 b`. The prettyprinter displays this as `case b of T -> M1 || F -> M2`. The `bool_case` constant may be thought of as a pattern-matching version of the conditional.

Failure

Fails if `b` is not of type `bool`. Also fails if `M1` and `M2` do not have the same type.

Example

```
- mk_bool_case (Term'f x',Term'b:'b',Term'x:bool');
<<HOL message: inventing new type variable names: 'a, 'b>>

> val it = 'case x of T -> f x || F -> b' : term
```

See also

`boolSyntax.dest_bool_case`, `boolSyntax.is_bool_case`.

<code>mk_comb</code>	(Term)
----------------------	--------

```
mk_comb : term * term -> term
```

Synopsis

Constructs a combination (function application).

Description

`mk_comb (t1,t2)` returns the combination `t1 t2`.

Failure

Fails if `t1` does not have a function type, or if `t1` has a function type, but its domain does not equal the type of `t2`.

Example

```
- mk_comb (neg_tm,T);

> val it = '~T' : term

- mk_comb(T, T) handle e => Raise e;
```

```
Exception raised at Term.mk_comb:
incompatible types
```

See also

`Term.dest_comb`, `Term.is_comb`, `Term.list_mk_comb`, `Term.mk_var`, `Term.mk_const`, `Term.mk_abs`.

<code>MK_COMB</code>	(Thm)
----------------------	-------

```
MK_COMB : thm * thm -> thm
```

Synopsis

Proves equality of combinations constructed from equal functions and operands.

Description

When applied to theorems `A1 |- f = g` and `A2 |- x = y`, the inference rule `MK_COMB` returns the theorem `A1 u A2 |- f x = g y`.

$$\frac{A1 \mid- f = g \quad A2 \mid- x = y}{A1 \text{ u } A2 \mid- f \ x = g \ y} \text{ MK_COMB}$$

Failure

Fails unless both theorems are equational and f and g are functions whose domain types are the same as the types of x and y respectively.

See also

Thm.AP_TERM, Thm.AP_THM, Tactic.MK_COMB_TAC.

MK_COMB_TAC

(Tactic)

MK_COMB_TAC : tactic

Synopsis

Breaks an equality between applications into two equality goals: one for the functions, and other for the arguments.

Description

MK_COMB_TAC reduces a goal of the form $A \text{ ?- } f \ x = g \ y$ to the goals $A \text{ ?- } f = g$ and $A \text{ ?- } x = y$.

$$\frac{A \text{ ?- } f \ x = g \ y}{A \text{ ?- } f = g, \quad A \text{ ?- } x = y} \text{ MK_COMB_TAC}$$

Failure

Fails unless the goal is equational, with both sides being applications.

See also

Thm.MK_COMB, Thm.AP_TERM, Thm.AP_THM, Tactic.AP_THM_TAC.

mk_cond

(boolSyntax)

mk_cond : term * term * term -> term

Synopsis

Constructs a conditional term.

Description

`mk_cond(t,t1,t2)` constructs an application `COND t t1 t2`. This is rendered by the prettyprinter as `if t then t1 else t2`.

Failure

Fails if `t` is not of type `bool` or if `t1` and `t2` are of different types.

Comments

The prettyprinter can be trained to print `if t then t1 else t2` as `t => t1 | t2`.

See also

`boolSyntax.dest_cond`, `boolSyntax.is_cond`.

<code>mk_conj</code>	<code>(boolSyntax)</code>
----------------------	---------------------------

`mk_conj : term * term -> term`

Synopsis

Constructs a conjunction.

Description

`mk_conj(t1, t2)` returns the term `t1 /\ t2`.

Failure

Fails if `t1` and `t2` do not both have type `bool`.

See also

`boolSyntax.dest_conj`, `boolSyntax.is_conj`, `boolSyntax.list_mk_conj`, `boolSyntax.strip_conj`.

<code>mk_cons</code>	<code>(listSyntax)</code>
----------------------	---------------------------

`mk_cons : {hd :term, tl :term} -> term`

Synopsis

Constructs a CONS pair.

Description

`mk_cons{hd = t, tl = '[t1;...;tn]'` returns `'[t;t1;...;tn]'`.

Failure

Fails if `tl` is not a list or if `hd` is not of the same type as the elements of the list.

See also

`listSyntax.dest_cons`, `listSyntax.is_cons`, `listSyntax.mk_list`,
`listSyntax.dest_list`, `listSyntax.is_list`.

<code>mk_const</code>

(Term)

```
mk_const : string * hol_type -> term
```

Synopsis

Constructs a constant.

Description

If `n` is a string that has been previously declared to be a constant with type `ty` and `ty1` is an instance of `ty`, then `mk_const(n, ty1)` returns the specified instance of the constant.

(A type `ty1` is an 'instance' of a type `ty2` when `match_type ty2 ty1` does not fail.)

Note, however, that constants with the same name (and type) may be declared in different theories. If two theories having constants with the same name `n` are in the ancestry of the current theory, then `mk_const(n, ty)` will issue a warning before arbitrarily selecting which constant to construct. In such situations, `mk_thy_const` allows one to specify exactly which constant to use.

Failure

Fails if `n` is not the name of a known constant, or if `ty` is not an instance of the type that the constant has in the signature.

Example

```
- mk_const ("T", bool);
> val it = 'T' : term
```

```

- mk_const ("=", bool --> bool --> bool);
> val it = '$=' : term

- try mk_const ("test", bool);
Exception raised at Term.mk_const:
test not found

```

The following example shows a new constant being introduced that has the same name as the standard equality of HOL. Then we attempt to make an instance of that constant.

```

- new_constant ("=", bool --> bool --> bool);
> val it = () : unit

- mk_const("=", bool --> bool --> bool);
<<HOL warning: Term.mk_const: "=": more than one possibility>>

> val it = '$=' : term

```

See also

Term.mk_thy_const, Term.dest_const, Term.is_const, Term.mk_var, Term.mk_comb, Term.mk_abs, Type.match_type.

mk_disj	(boolSyntax)
---------	--------------

mk_disj : term * term -> term

Synopsis

Constructs a disjunction.

Description

If t_1 and t_2 are terms, both of type `bool`, then `mk_disj (t1, t2)` returns the term $t_1 \ \vee \ t_2$.

Failure

Fails if t_1 or t_2 does not have type `bool`.

See also

boolSyntax.dest_disj, boolSyntax.is_disj, boolSyntax.list_mk_disj, boolSyntax.strip_disj.

mk_eq**(boolSyntax)**

```
mk_eq : term * term -> term
```

Synopsis

Constructs an equation.

Description

mk_eq(t1, t2) returns the term $t1 = t2$.

Failure

Fails if the type of $t1$ is not equal to that of $t2$.

See also

boolSyntax.dest_eq, boolSyntax.is_eq.

mk_exists**(boolSyntax)**

```
mk_exists : term * term -> term
```

Synopsis

Term constructor for existential quantification.

Description

If v is a variable and t is a term of type `bool`, then `mk_exists (v,t)` returns the term $?v. t$.

Failure

Fails if v is not a variable or if t is not of type `bool`.

See also

boolSyntax.dest_exists, boolSyntax.is_exists, boolSyntax.list.mk_exists,
boolSyntax.strip_exists.

MK_EXISTS**(Drule)**

```
MK_EXISTS : (thm -> thm)
```

Synopsis

Existentially quantifies both sides of a universally quantified equational theorem.

Description

When applied to a theorem $A \vdash !x. t1 = t2$, the inference rule `MK_EXISTS` returns the theorem $A \vdash (?x. t1) = (?x. t2)$.

$$\frac{A \vdash !x. t1 = t2}{A \vdash (?x. t1) = (?x. t2)} \quad \text{MK_EXISTS}$$

Failure

Fails unless the theorem is a singly universally quantified equation.

See also

`Thm.AP_TERM`, `Drule.EXISTS_EQ`, `Thm.GEN`, `Drule.LIST_MK_EXISTS`, `Drule.MK_ABS`.

<code>mk_exists1</code>	<code>(boolSyntax)</code>
-------------------------	---------------------------

```
mk_exists1 : term * term -> term
```

Synopsis

Term constructor for unique existence.

Description

If v is a variable and t is a term of type `bool`, then `mk_exists1 (v,t)` returns the term `?!v. t`.

Failure

Fails if v is not a variable or if t is not of type `bool`.

See also

`boolSyntax.dest_exists1`, `boolSyntax.is_exists1`.

<code>mk_forall</code>	<code>(boolSyntax)</code>
------------------------	---------------------------

```
mk_forall : term * term -> term
```

Synopsis

Term constructor for universal quantification.

Description

If v is a variable and t is a term of type `bool`, then `mk_forall (v,t)` returns the term $\lambda v. t$.

Failure

Fails if v is not a variable or if t is not of type `bool`.

See also

`boolSyntax.dest_forall`, `boolSyntax.is_forall`, `boolSyntax.list.mk_forall`,
`boolSyntax.strip_forall`.

<code>mk_HOL_ERR</code>

(Feedback)

```
mk_HOL_ERR : string -> string -> string -> exn
```

Synopsis

Creates an application of `HOL_ERR`.

Description

`mk_HOL_ERR` provides a curried interface to the standard `HOL_ERR` exception; experience has shown that this is often more convenient.

Failure

Never fails.

Example

```
- mk_HOL_ERR "Module" "function" "message"
```

```
> val it = HOL_ERR : exn
```

```
- print(exn_to_string it);
```

```
Exception raised at Module.function:
```

```
message
```

```
> val it = () : unit
```

See also

Feedback, Feedback.HOL_ERR, Feedback.error_record.

<div data-bbox="233 488 474 537" data-label="Text"> <p><code>mk_icomb</code></p> </div>	<div data-bbox="1059 486 1412 542" data-label="Text"> <p><code>(boolSyntax)</code></p> </div>
--	---

```
term * term -> term
```

Synopsis

Forms an application term, possibly instantiating the function.

Description

A call to `mk_icomb(f,x)` checks to see if the term `f`, which must have function type, can have any of its type variables instantiated so as to make the domain of the function match the type of `x`. If so, then the call returns the application of the instantiated `f` to `x`.

Failure

Fails if there is no way to instantiate the function term to make its domain match the argument's type.

Example

Note how both the `S` combinator and the argument have type variables invented for them when the two quotations are parsed.

```
- val t = mk_icomb('S', '\n:num b. (n,b));
<<HOL message: inventing new type variable names: 'a, 'b, 'c>>
<<HOL message: inventing new type variable names: 'a>>
> val t = 'S (\n b. (n,b))' : term
```

The resulting term `t` has only the type variable `'a` left after instantiation.

```
- type_of t;
> val it = ':(num -> 'a) -> num -> num # 'a' : hol_type
```

This term can now be combined with an argument and the final type variable instantiated:

```
- mk_icomb(t, 'ODD');
> val it = 'S (\n b. (n,b)) ODD' : term

- type_of it;
> val it = ':num -> num # bool';
```


Attempting to use `mk_comb` above results in immediate error because it requires domain and arguments types to be identical:

```
- mk_comb('S', '\n:num b. (n,b)') handle e => Raise e;
<<HOL message: inventing new type variable names: 'a, 'b, 'c>>
<<HOL message: inventing new type variable names: 'a>>
```

```
Exception raised at Term.mk_comb:
incompatible types
! Uncaught exception:
! HOL_ERR
```

See also

`boolSyntax.list_mk_icoomb`, `Term.mk_comb`.

<div data-bbox="158 1005 341 1059" data-label="Text"> <p><code>mk_imp</code></p> </div>	<div data-bbox="984 1001 1331 1059" data-label="Text"> <p><code>(boolSyntax)</code></p> </div>
---	--

`mk_imp : term * term -> term`

Synopsis

Constructs an implication.

Description

If `t1` and `t2` are terms of type `bool`, then `mk_imp(t1,t2)` constructs the term `t1 ==> t2`.

Failure

Fails if `t1` and `t2` are not both of type `bool`.

See also

`boolSyntax.dest_imp`, `boolSyntax.dest_imp_only`, `boolSyntax.is_imp`,
`boolSyntax.is_imp_only`, `boolSyntax.list_mk_imp`.

<div data-bbox="158 1814 458 1865" data-label="Text"> <p><code>mk_istream</code></p> </div>	<div data-bbox="1182 1809 1331 1863" data-label="Text"> <p><code>(Lib)</code></p> </div>
---	--

`mk_istream : ('a -> 'a) -> 'a -> ('a -> 'b) -> ('a,'b) istream`

Synopsis

Create a stream.

Description

An application `mk_istream trans init proj` creates an imperative stream of elements. The stream is generated by applying `trans` to the state. The first element in the stream state is `init`. The value of the state is obtained by applying `proj`.

Failure

If an application of `trans` or `proj` fails when applied to the state.

Example

The following creates a stream of distinct strings.

```
- mk_istream (fn x => x+1) 0 (concat "gsym" o int_to_string);
> val it = <istream> : (int, string) istream
```

Comments

It is aesthetically unpleasant that the underlying implementation type is visible.

See any book on ML programming to see how functional streams are built.

See also

`Lib.next`, `Lib.state`, `Lib.reset`.

<code>mk_let</code>

<code>(boolSyntax)</code>

`mk_let : term * term -> term`

Synopsis

Constructs a `let` term.

Description

The invocation `mk_let (M,N)` returns the term `'LET M N'`. If `M` is of the form `\x.t` then the result will be pretty-printed as `let x = N in t`. Since `LET M N` is defined to be `M N`, one can think of a `let`-expression as a suspended beta-redex (if that helps).

Failure

Fails if the types of `M` and `N` are such that `LET M N` is not well-typed, i.e., the type of `M` must be a function type, and the type of `N` must equal the domain of the type of `M`.

Example

```
- mk_let(Term'\x. x \/\ x', Term'Q /\ R');
> val it = 'let x = Q /\ R in x \/\ x' : term
```

Comments

let expressions may be nested.

Pairing can also be used in the let syntax, provided pairTheory has been loaded. The library pairLib provides support for manipulating 'paired' lets.

See also

boolSyntax.dest_let, boolSyntax.is_let, pairSyntax.mk_anylet.

mk_list	(listSyntax)
---------	--------------

```
mk_list : {els : term list, ty : hol_type} -> term
```

Synopsis

Constructs an object-level (HOL) list from an ML list of terms.

Description

mk_list{els = [t1, ..., tn], ty = ty} returns [t1;...;tn]:ty list. The type argument is required so that empty lists can be constructed.

Failure

Fails if any term in the list is not of the type specified as the second argument.

See also

listSyntax.dest_list, listSyntax.is_list, listSyntax.mk_cons,
listSyntax.dest_cons, listSyntax.is_cons.

mk_neg	(boolSyntax)
--------	--------------

```
mk_neg : (term -> term)
```

Synopsis

Constructs a negation.

Description

`mk_neg "t"` returns `"~t"`.

Failure

Fails with `mk_neg` unless `t` is of type `bool`.

See also

`boolSyntax.dest_neg`, `boolSyntax.is_neg`.

<code>mk_numeral</code>	<code>(numSyntax)</code>
-------------------------	--------------------------

`mk_numeral : Arbnum.num -> term`

Synopsis

Convert ML bignum value to HOL numeral.

Description

An invocation `mk_numeral n`, where `n` is an ML value of type `Arbnum.num` returns the corresponding HOL term.

Example

```
- Arbnum.fromString "1234";
> val it = 1234 : num

- mk_numeral it;
> val it = ``1234`` : term
```

Failure

Never fails.

See also

`numSyntax.dest_numeral`, `numSyntax.is_numeral`.

<code>mk_oracle_thm</code>	<code>(Thm)</code>
----------------------------	--------------------

`mk_oracle_thm : string -> term list * term -> thm`

Synopsis

Construct a theorem without proof, and tag it.

Description

In principle, nearly every theorem of interest can be proved in HOL by using only the axioms and primitive rules of inference. The use of ML to orchestrate larger inference steps from the primitives, along with support in HOL for goal-directed proof, considerably eases the task of formal proof. Nearly every theorem of interest can therefore be produced as the end product of a chain of primitive inference steps, and HOL implementations strive to keep this purity.

However, it is occasionally useful to interface HOL with trusted external tools that also produce, in some sense, theorems that would be derivable in HOL. It is clearly a burden to require that HOL proofs accompany such theorems so that they can be (re-)derived in HOL. In order to support greater interoperation of proof tools, therefore, HOL provides the notion of a ‘tagged’ theorem.

A tagged theorem is manufactured by invoking `mk_oracle_thm tag (A,w)`, where `A` is a list of HOL terms of type `bool`, and `w` is also a HOL term of boolean type. No proof is done; the sequent is merely injected into the type of theorems, and the `tag` value is attached to it. The result is the theorem $A \vdash w$.

The `tag` value stays with the theorem, and it propagates in a hereditary fashion to any theorem derived from the tagged theorem. Thus, if one examines a theorem with `Thm.tag` and finds that it has no tag, then the theorem has been derived purely by proof steps in the HOL logic. Otherwise, shortcuts have been taken, and the external tools, also known as ‘oracles’, used to make the shortcuts are signified by the tags.

Failure

If some element of `A` does not have type `bool`, or `w` does not have type `bool`, or the tag string doesn’t represent a valid tag (which occurs if it is the string `"DISK_THM"`, or if it is a string containing unprintable characters).

Example

In the following, we construct a tag and then make a rogue rule of inference.

```
- val tag = "SimonSays";
> val tag = "SimonSays" : string

- val SimonThm = mk_oracle_thm tag;
> val SimonThm = fn : term list * term -> thm

- val th = SimonThm ([], Term '!x. x');;
> val th = |- !x. x : thm
```

```

- val th1 = SPEC F th;
> val th1 = |- F : thm

- (show_tags := true; th1);
> val it = [oracles: SimonSays] [axioms: ] [] |- F : thm

```

Tags accumulate in a manner similar to logical hypotheses.

```

- CONJ th1 th1;
> val it = [oracles: SimonSays] [axioms: ] [] |- F /\ F : thm

- val SerenaThm = mk_oracle_thm "Serena";
> val SerenaThm = fn : term list * term -> thm

- CONJ th1 (SerenaThm ([],T));
> val it = [oracles: Serena, SimonSays] [axioms: ] [] |- F /\ T : thm

```

Comments

It is impossible to detach a tag from a theorem.

See also

Thm.add_tag, Thm.mk_thm, Tag.read, Thm.tag.

MK_PABS	(PairRules)
---------	-------------

MK_PABS : (thm -> thm)

Synopsis

Abstracts both sides of an equation.

Description

When applied to a theorem $A \text{ |- } !p. t1 = t2$, whose conclusion is a paired universally quantified equation, MK_PABS returns the theorem $A \text{ |- } (\backslash p. t1) = (\backslash p. t2)$.

$$\begin{array}{l}
 A \text{ |- } !p. t1 = t2 \\
 \hline
 A \text{ |- } (\backslash p. t1) = (\backslash p. t2)
 \end{array}
 \quad \text{MK_PABS}$$

Failure

Fails unless the theorem is a (singly) paired universally quantified equation.

See also

Drule.MK_ABS, PairRules.PABS, PairRules.HALF_MK_PABS, PairRules.MK_PEXISTS.

mk_pabs

(pairSyntax)

mk_pabs : term * term -> term

Synopsis

Constructs a paired abstraction.

Description

If M is the tuple (v_1, \dots, v_n) , and N is an arbitrary term, then `mk_pabs (M,N)` returns the paired abstraction $\lambda(v_1, \dots, v_n).N$.

Failure

Fails unless M is an arbitrarily nested pair composed from variables, with no repetitions of variables.

See also

pairSyntax.dest_pabs, pairSyntax.is_pabs, Term.mk_abs.

MK_PAIR

(PairRules)

MK_PAIR : thm -> thm -> thm

Synopsis

Proves equality of pairs constructed from equal components.

Description

When applied to theorems $A_1 \vdash a = x$ and $A_2 \vdash b = y$, the inference rule `MK_PAIR` returns the theorem $A_1 \wedge A_2 \vdash (a,b) = (x,y)$.

$$\frac{A_1 \vdash a = x \quad A_2 \vdash b = y}{A_1 \wedge A_2 \vdash (a,b) = (x,y)} \text{ MK_PAIR}$$

Failure

Fails unless both theorems are equational.

<code>mk_pair</code>	<code>(pairSyntax)</code>
----------------------	---------------------------

`mk_pair : term * term -> term`

Synopsis

Constructs object-level pair from a pair of terms.

Description

`mk_pair (t1,t2)` returns `(t1,t2)`.

Failure

Never fails.

See also

`pairSyntax.dest_pair`, `pairSyntax.is_pair`, `pairSyntax.list_mk_pair`.

<code>MK_PEXISTS</code>	<code>(PairRules)</code>
-------------------------	--------------------------

`MK_PEXISTS : (thm -> thm)`

Synopsis

Existentially quantifies both sides of a universally quantified equational theorem.

Description

When applied to a theorem `A |- !p. t1 = t2`, the inference rule `MK_PEXISTS` returns the theorem `A |- (?x. t1) = (?x. t2)`.

$$\frac{A \text{ |- } !p. t1 = t2}{A \text{ |- } (?p. t1) = (?p. t2)} \quad \text{MK_PEXISTS}$$

Failure

Fails unless the theorem is a singly paired universally quantified equation.

See also

PairRules.PEXISTS_EQ, PairRules.PGEN, PairRules.LIST_MK_PEXISTS,
PairRules.MK_PABS.

MK_PFORALL

(PairRules)

MK_PFORALL : (thm -> thm)

Synopsis

Universally quantifies both sides of a universally quantified equational theorem.

Description

When applied to a theorem $A \vdash !p. t1 = t2$, the inference rule MK_PFORALL returns the theorem $A \vdash (!x. t1) = (!x. t2)$.

$$\frac{A \vdash !p. t1 = t2}{A \vdash (!p. t1) = (!p. t2)} \quad \text{MK_PFORALL}$$

Failure

Fails unless the theorem is a singly paired universally quantified equation.

See also

PairRules.PFORALL_EQ, PairRules.LIST_MK_PFORALL, PairRules.MK_PABS.

mk_primed_var

(Term)

mk_primed_var : string * hol_type -> term

Synopsis

Primes a variable name sufficiently to make it distinct from all constants.

Description

When applied to a record made from a string v and a type ty , the function `mk_primed_var` constructs a variable whose name consists of v followed by however many primes are necessary to make it distinct from any constants in the current theory.

Failure

Never fails.

Example

```
- new_theory "wombat";
> val it = () : unit

- mk_primed_var("x", bool);
> val it = 'x' : term

- new_constant("x", alpha);
> val it = () : unit

- mk_primed_var("x", bool);
> val it = 'x'' : term
```

See also

`Term.genvar`, `Term.variant`, `Globals.priming`.

<div data-bbox="231 1370 448 1429" data-label="Text"> <p><code>mk_prod</code></p> </div>	<div data-bbox="1059 1368 1414 1429" data-label="Text"> <p><code>(pairSyntax)</code></p> </div>
--	---

`mk_prod : hol_type * hol_type -> hol_type`

Synopsis

Constructs a product type from two constituent types.

Description

`mk_prod(ty1, ty2)` returns `ty1 # t2`.

Failure

Never fails.

See also

`pairSyntax.is_prod`, `pairSyntax.dest_prod`.

MK_PSELECT

(PairRules)

MK_PSELECT : (thm -> thm)

Synopsis

Quantifies both sides of a universally quantified equational theorem with the choice quantifier.

Description

When applied to a theorem $A \vdash !p. t1 = t2$, the inference rule MK_PSELECT returns the theorem $A \vdash (@x. t1) = (@x. t2)$.

$$\frac{A \vdash !p. t1 = t2}{A \vdash (@p. t1) = (@p. t2)} \quad \text{MK_PSELECT}$$

Failure

Fails unless the theorem is a singly paired universally quantified equation.

See also

PairRules.PSELECT EQ, PairRules.MK_PABS.

mk_ptree

(patriciaLib)

mk_ptree : term_ptree -> term

Synopsis

Term constructor for Patricia trees.

Description

The constructor `mk_ptree` will return a HOL term that corresponds with the supplied ML Patricia tree. The ML abstract data type `term_ptree` is defined in `patriciaLib`.

Failure

The conversion will fail if the terms stored in the supplied Patricia tree do not all have the same type.

Example

```

- mk_ptree (int_ptree_of_list [(1, 'T'), (2, '2')]);
Exception-
  HOL_ERR
  {message = "", origin_function = "mk_branch", origin_structure =
  "HolKernel"} raised

- mk_ptree (int_ptree_of_list [(1, '1'), (2, '2')]);
val it = 'Branch 0 0 (Leaf 1 1) (Leaf 2 2)': term

```

Comments

When working with large trees it is a good idea constrain term printing by setting `Globals.max_print_depth`.

See also

`patriciaLib.dest_ptree`, `patriciaLib.is_ptree`.

<code>mk_res_abstract</code>	<code>(res_quanLib)</code>
------------------------------	----------------------------

```
mk_res_abstract : (term # term # term) -> term
```

Synopsis

Term constructor for restricted abstraction.

Description

`mk_res_abstract("var", "P", "t")` returns `"\var :: P . t"`.

Failure

Fails with `mk_res_abstract` if the first term is not a variable or if `P` and `t` are not of type `" : bool"`.

See also

`res_quanLib.dest_res_abstract`, `res_quanLib.is_res_abstract`.

<code>mk_res_abstract</code>	<code>(res_quanTools)</code>
------------------------------	------------------------------

```
mk_res_abstract : ((term # term # term) -> term)
```

Synopsis

Term constructor for restricted abstraction.

Description

`mk_res_abstract("var", "P", "t")` returns `"\var :: P . t"`.

Failure

Fails with `mk_res_abstract` if the first term is not a variable or if `P` and `t` are not of type `" : bool "`.

See also

`res_quantools.dest_res_abstract`, `res_quantools.is_res_abstract`.

<code>mk_res_exists</code>	<code>(res_quantLib)</code>
----------------------------	-----------------------------

`mk_res_exists : ((term # term # term) -> term)`

Synopsis

Term constructor for restricted existential quantification.

Description

`mk_res_exists("var", "P", "t")` returns `"?var :: P . t"`.

Failure

Fails with `mk_res_exists` if the first term is not a variable or if `P` and `t` are not of type `" : bool "`.

See also

`res_quantLib.dest_res_exists`, `res_quantLib.is_res_exists`,
`res_quantLib.list.mk_res_exists`.

<code>mk_res_exists</code>	<code>(res_quantTools)</code>
----------------------------	-------------------------------

`mk_res_exists : ((term # term # term) -> term)`

Synopsis

Term constructor for restricted existential quantification.

Description

`mk_res_exists("var", "P", "t")` returns `"?var :: P . t"`.

Failure

Fails with `mk_res_exists` if the first term is not a variable or if `P` and `t` are not of type `":bool"`.

See also

`res_quantools.dest_res_exists`, `res_quantools.is_res_exists`,
`res_quantools.list_mk_res_exists`.

<code>mk_res_exists_unique</code>	<code>(res_quantLib)</code>
-----------------------------------	-----------------------------

`mk_res_exists_unique : (term # term # term) -> term`

Synopsis

Term constructor for restricted unique existential quantification.

Description

`mk_res_exists_unique ("var", "P", "t")` returns `"?!var :: P . t"`.

Failure

Fails with `mk_res_exists_unique` if the first term is not a variable or if `P` and `t` are not of type `":bool"`.

See also

`res_quantLib.dest_res_exists_unique`, `res_quantLib.is_res_exists_unique`.

<code>mk_res_forall</code>	<code>(res_quantLib)</code>
----------------------------	-----------------------------

`mk_res_forall : (term # term # term) -> term`

Synopsis

Term constructor for restricted universal quantification.

Description

`mk_res_forall("var", "P", "t")` returns `"!var :: P . t"`.

Failure

Fails with `mk_res_forall` if the first term is not a variable or if `P` and `t` are not of type `:bool`.

See also

`res_quanLib.dest_res_forall`, `res_quanLib.is_res_forall`,
`res_quanLib.list_mk_res_forall`.

<code>mk_res_forall</code>	<code>(res_quanTools)</code>
----------------------------	------------------------------

`mk_res_forall` : ((term # term # term) -> term)

Synopsis

Term constructor for restricted universal quantification.

Description

`mk_res_forall("var","P","t")` returns `!var :: P . t`.

Failure

Fails with `mk_res_forall` if the first term is not a variable or if `P` and `t` are not of type `:bool`.

See also

`res_quanTools.dest_res_forall`, `res_quanTools.is_res_forall`,
`res_quanTools.list_mk_res_forall`.

<code>mk_res_select</code>	<code>(res_quanLib)</code>
----------------------------	----------------------------

`mk_res_select` : (term # term # term) -> term

Synopsis

Term constructor for restricted choice quantification.

Description

`mk_res_select("var","P","t")` returns `@var :: P . t`.

Failure

Fails with `mk_res_select` if the first term is not a variable or if `P` and `t` are not of type `:bool`.

See also

`res_quanLib.dest_res_select`, `res_quanLib.is_res_select`.

<code>mk_res_select</code>	<code>(res_quanTools)</code>
----------------------------	------------------------------

```
mk_res_select : ((term # term # term) -> term)
```

Synopsis

Term constructor for restricted choice quantification.

Description

`mk_res_select("var", "P", "t")` returns `@var :: P . t`.

Failure

Fails with `mk_res_select` if the first term is not a variable or if `P` and `t` are not of type `:bool`.

See also

`res_quanTools.dest_res_select`, `res_quanTools.is_res_select`.

<code>mk_select</code>	<code>(boolSyntax)</code>
------------------------	---------------------------

```
mk_select : term * term -> term
```

Synopsis

Constructs a choice-term.

Description

If `v` is a variable and `t` is a term of type `bool`, then `mk_select (v,t)` returns `@var . t`.

Failure

Fails if `v` is not a variable or if `t` is not of type `bool`.

See also

boolSyntax.dest_select, boolSyntax.is_select.

mk_set**(Lib)**

```
mk_set : 'a list -> 'a list
```

Synopsis

Transforms a list into one with distinct elements.

Description

An invocation `mk_set list` returns a list consisting of the distinct members of `list`. In particular, the result list has no repeated elements.

Failure

Never fails.

Example

```
- mk_set [1,1,1,2,2,2,3,3,4];  
> val it = [1, 2, 3, 4] : int list
```

Comments

In some programming situations, it is convenient to implement sets by lists, in which case `mk_set` may be helpful. However, such an implementation is only suitable for small sets.

A high-performance implementation of finite sets may be found in structure `HOLset`.

ML equality types are used in the implementation of `mk_set` and its kin. This limits its applicability to types that allow equality. For other types, typically abstract ones, use the 'op_' variants.

See also

Lib.op_mk_set, Lib.mem, Lib.insert, Lib.union, Lib.U, Lib.set_diff,
Lib.subtract, Lib.intersect, Lib.null_intersection, Lib.set_eq.

mk_simpset**(simpLib)**

```
simpLib.mk_simpset : ssfrag list -> simpset
```

Synopsis

Creates a `simpset` by combining a list of `ssfrag` values.

Description

This function creates a `simpset` value by repeatedly adding (as per the `++` operator) `simpset` fragment values to the base `empty_ss`.

Failure

Never fails.

Uses

Creates `simpsets`, which are a necessary argument to any simplification function.

See also

`simpLib.++`, `simpLib.rewrites`, `simpLib.SIMP.CONV`.

<code>mk_state</code>	<code>(holCheckLib)</code>
-----------------------	----------------------------

```
mk_state : term -> (string,term) list -> term
```

Synopsis

Given the initial states and transition system of a `HolCheck` model, constructs a state tuple that can be used to specify `HolCheck` properites.

Description

`HolCheck` models atomic propositions in properties as functions on the state. Thus we need a representation of the state to specify properties. This function is used to create such a representative. Its return value is also passed to `holCheckLib.set_state` to ensure that the properties and the model use the same state tuple.

See also

`holCheckLib.holCheck`, `holCheckLib.set_state`.

<code>mk_thm</code>	<code>(Thm)</code>
---------------------	--------------------

```
mk_thm : term list * term -> thm
```

Synopsis

Creates an arbitrary theorem (dangerous!)

Description

The function `mk_thm` can be used to construct an arbitrary theorem. It is applied to a pair consisting of the desired assumption list (possibly empty) and conclusion. All the terms therein should be of type `bool`.

$$\text{mk_thm}([a_1, \dots, a_n], c) = (\{a_1, \dots, a_n\} \mid - c)$$

`mk_thm` is an application of `mk_oracle_thm`, and every application of it tags the resulting theorem with `MK_THM`.

Failure

Fails unless all the terms provided for assumptions and conclusion are of type `bool`.

Example

The following shows how to create a simple contradiction:

```
- val falsity = mk_thm([], boolSyntax.F);
> val falsity = |- F : thm

- Globals.show_tags := true;
> val it = () : unit

- falsity;
> val it = [oracles: MK_THM] [axioms: ] [] |- F : thm
```

Comments

Although `mk_thm` can be useful for experimentation or temporarily plugging gaps, its use should be avoided if at all possible in important proofs, because it can be used to create theorems leading to contradictions. The example above is a trivial case, but it is all too easy to create a contradiction by asserting ‘obviously sound’ theorems.

All theorems which are likely to be needed can be derived using only HOL’s inbuilt axioms and primitive inference rules, which are provably sound (see the DESCRIPTION). Basing all proofs, normally via derived rules and tactics, on just these axioms and inference rules gives proofs which are (apart from bugs in HOL or the underlying system) completely secure. This is one of the great strengths of HOL, and it is foolish to sacrifice it to save a little work.

Because of the way tags are propagated during proof, a theorem proved with the aid of `mk_thm` is detectable by examining its tag.

See also

Theory.new_axiom, Thm.mk_oracle_thm, Thm.tag, Globals.show_tags.

<code>mk_thy_const</code>	<code>(Term)</code>
---------------------------	---------------------

```
mk_thy_const : {Thy:string, Name:string, Ty:hol_type} -> term
```

Synopsis

Constructs a constant.

Description

If `n` is a string that has been previously declared to be a constant with type `ty` in theory `thy`, and `ty1` is an instance of `ty`, then `mk_thy_const{Name=n, Thy=thy, Ty=ty1}` returns the specified instance of the constant.

(A type `ty1` is an 'instance' of a type `ty2` when `match_type ty2 ty1` does not fail.)

Failure

Fails if `n` is not the name of a constant in theory `thy`, if `thy` is not in the ancestry of the current theory, or if `ty1` is not an instance of `ty`.

Example

```
- mk_thy_const {Name="T", Thy="bool", Ty=bool};
> val it = 'T' : term

- try mk_thy_const {Name = "bar", Thy="foo", Ty=bool};
Exception raised at Term.mk_thy_const:
"foo$bar" not found
```

See also

Term.dest_thy_const, Term.mk_const, Term.dest_const, Term.is_const, Term.mk_var, Term.mk_comb, Term.mk_abs, Type.match_type.

<code>mk_thy_type</code>	<code>(Type)</code>
--------------------------	---------------------

```
mk_thy_type
  : {Thy:string, Tyop:string, Args:hol_type list} -> hol_type
```

Synopsis

Constructs a type.

Description

If `s` is a string that has been previously declared to be a type with arity type `n` in theory `thy`, and the length of `ty1` is equal to `n`, then `mk_thy_type{Tyop=s, Thy=thy, Args=ty1}` returns the requested compound type.

Failure

Fails if `s` is not the name of a type in theory `thy`, if `thy` is not in the ancestry of the current theory, or if `n` is not the length of `ty1`.

Example

```
- mk_thy_type {Tyop="fun", Thy="min", Args = [alpha,bool]};
> val it = `:'a -> bool' : hol_type
```

```
- try mk_thy_type {Tyop="bar", Thy="foo", Args = []};
```

```
Exception raised at Type.mk_thy_type:
"foo$bar" not found
```

Comments

In general, `mk_thy_type` is to be preferred over `mk_type` because HOL provides a fresh namespace for each theory (`mk_type` is a holdover from a time when there was only one namespace shared by all theories).

See also

`Type.mk_type`, `Type.dest_thy_type`, `Term.mk_const`, `Term.mk_thy_const`.

<div data-bbox="158 1518 370 1574" data-label="Text"> <p><code>mk_type</code></p> </div>	<div data-bbox="1155 1514 1331 1574" data-label="Text"> <p>(Type)</p> </div>
--	--

```
mk_type : string * hol_type list -> hol_type
```

Synopsis

Constructs a compound type.

Description

`mk_type(tyop, [ty1, ..., tyn])` returns the HOL type `(ty1, ..., tyn)tyop`, provided `tyop` is the name of a known `n`-ary type constructor.

Failure

Fails if `tyop` is not the name of a known type, or if `tyop` is known, but the length of the list of argument types is not equal to the arity of `tyop`.

Example

```
- mk_type ("bool", []);
> val it = ':bool' : hol_type

- mk_type ("fun", [alpha, it]);
> val it = ': 'a -> bool' : hol_type
```

Comments

Note that type operators with the same name (and arity) may be declared in different theories. If two theories having type operators with the same name `s` are in the ancestry of the current theory, then `mk_type(s, ty1)` will issue a warning before arbitrarily selecting which type operator to use. In such situations, it is preferable to use `mk_thy_type` since it allows one to specify exactly which type operator to use.

See also

`Type.mk_thy_type`, `Type.dest_type`, `Type.mk_vartype`, `Type.-->`.

<code>mk_var</code>	(Term)
---------------------	--------

```
mk_var : string * hol_type -> term
```

Synopsis

Constructs a variable of given name and type.

Description

If `v` is a string and `ty` is a HOL type, then `mk_var(v, ty)` returns a HOL variable.

Failure

Never fails.

Comments

`mk_var` can be used to construct variables with names which are not acceptable to the term parser. In particular, a variable with the name of a known constant can be constructed using `mk_var`.

See also

Term.dest_var, Term.is_var, Term.mk_const, Term.mk_comb, Term.mk_abs.

mk_vartype**(Type)**

```
mk_vartype : string -> hol_type
```

Synopsis

Constructs a type variable of the given name.

Failure

Fails if the string does not begin with '.

Example

```
- mk_vartype "'giraffe";  
> val it = ':'giraffe' : hol_type
```

```
- try mk_vartype "test";
```

```
Exception raised at Type.mk_vartype:  
incorrect syntax
```

See also

Type.dest_vartype, Type.is_vartype, Type.mk_type.

mk_word_size**(wordsLib)**

```
mk_word_size : int -> unit
```

Synopsis

Adds a type abbreviation and theorems for a given word length.

Description

An invocation of `mk_word_size n` introduces a type abbreviation for words of length `n`. Theorems for `dimindex(:n)`, `dimword(:n)` and `INT_MIN(:n)` are generated and stored.

Example

```

- mk_word_size 128
> val it = () : unit
- ``:word128``
> val it = ``:bool[128]`` : hol_type
- theorem "dimword_128"
> val it = |- dimword (:128) = 340282366920938463463374607431768211456 : thm

```

Comments

The type abbreviation will only print when `type_pp.pp_array_types` is set to `false`.

See also

`Parse.type_abbrev`, `wordsLib.SIZES_CONV`, `wordsLib.SIZES_ss`.

<code>mlquote</code>	<code>(Lib)</code>
----------------------	--------------------

`mlquote` : `string -> string`

Synopsis

Put quotation marks around a string.

Description

Like `quote`, `mlquote` `s` puts quotation marks around a string. However, it also transforms the characters in a string so that, when printed, it would be a valid ML lexeme.

Failure

Never fails

Example

```

- print (quote "foo\nbar" ^ "\n");
"foo
bar"
> val it = () : unit

- print (mlquote "foo\nbar" ^ "\n");
"foo\nbar"
> val it = () : unit

```


See also

Lib.quote.

MOD_CONV

(reduceLib)

MOD_CONV : conv

Synopsis

Calculates by inference the remainder after dividing one numeral by another.

DescriptionIf m and n are numerals (e.g. 0, 1, 2, 3,...), then MOD_CONV "m MOD n" returns the theorem:

$$\vdash m \text{ MOD } n = s$$

where s is the numeral that denotes the remainder after dividing, with truncation, the natural number denoted by m by the natural number denoted by n .

Failure

MOD_CONV t_m fails unless t_m is of the form "m MOD n", where m and n are numerals, or if n denotes zero.

Example

```
#MOD_CONV "0 MOD 0";;
evaluation failed      MOD_CONV
```

```
#MOD_CONV "0 MOD 12";;
|- 0 MOD 12 = 0
```

```
#MOD_CONV "2 MOD 0";;
evaluation failed      MOD_CONV
```

```
#MOD_CONV "144 MOD 12";;
|- 144 MOD 12 = 0
```

```
#MOD_CONV "7 MOD 2";;
|- 7 MOD 2 = 1
```

<div data-bbox="231 349 531 405" data-label="Text"> <p><code>monitoring</code></p> </div>	<div data-bbox="1058 347 1410 405" data-label="Text"> <p><code>(computeLib)</code></p> </div>
---	---

`monitoring` : (term -> bool) option ref

Synopsis

Monitoring support for evaluation

Description

The reference variable `monitoring` provides a simple way to view the operation of `EVAL`, `EVAL_RULE`, and `EVAL_TAC`. The initial value of `monitoring` is `NONE`. If one wants to monitor the expansion of a function, defined with constant `c`, then setting `monitoring` to `SOME (same_const c)` will tell the system to print out the expansion of `c` by the evaluation entrypoints. To monitor the expansions of a collection of functions, defined with `c1, ..., cn`, then `monitoring` can be set to

```
SOME (fn x => same_const c1 x orelse ... orelse same_const cn x)
```

Failure

Never fails.

Example

```
- val [FACT] = decls "FACT";
> val FACT = 'FACT' : term

- computeLib.monitoring := SOME (same_const FACT);

- EVAL (Term 'FACT 4');
FACT 4 = (if 4 = 0 then 1 else 4 * FACT (PRE 4))
FACT 3 = (if 3 = 0 then 1 else 3 * FACT (PRE 3))
FACT 2 = (if 2 = 0 then 1 else 2 * FACT (PRE 2))
FACT 1 = (if 1 = 0 then 1 else 1 * FACT (PRE 1))
FACT 0 = (if 0 = 0 then 1 else 0 * FACT (PRE 0))
> val it = |- FACT 4 = 24 : thm
```

See also

`computeLib.RESTR.EVAL_CONV`, `Term.decls`.

MP

(Thm)

```
MP : thm -> thm -> thm
```

Synopsis

Implements the Modus Ponens inference rule.

Description

When applied to theorems $A1 \vdash t1 \implies t2$ and $A2 \vdash t1$, the inference rule MP returns the theorem $A1 \cup A2 \vdash t2$.

$$\frac{A1 \vdash t1 \implies t2 \quad A2 \vdash t1}{A1 \cup A2 \vdash t2} \text{ MP}$$

Failure

Fails unless the first theorem is an implication whose antecedent is the same as the conclusion of the second theorem (up to alpha-conversion).

See also

Thm.EQ_MP, Drule.LIST_MP, Drule.MATCH_MP, Tactic.MATCH_MP_TAC, Tactic.MP_TAC.

MP_TAC

(Tactic)

```
MP_TAC : thm_tactic
```

Synopsis

Reduces a goal to implication from a known theorem.

Description

When applied to the theorem $A' \vdash s$ and the goal $A \text{ ?- } t$, the tactic MP_TAC reduces the goal to $A \text{ ?- } s \implies t$. Unless A' is a subset of A , this is an invalid tactic.

$$\frac{A \text{ ?- } t}{\text{MP_TAC } (A' \vdash s)} A \text{ ?- } s \implies t$$

Failure

Never fails.

See also

Tactic.MATCH_MP_TAC, Thm.MP, Tactic.UNDISCH_TAC.

<div data-bbox="234 593 474 642" data-label="Text"> <p>MUL_CONV</p> </div>	<div data-bbox="1086 593 1414 642" data-label="Text"> <p>(reduceLib)</p> </div>
--	---

MUL_CONV : conv

Synopsis

Calculates by inference the product of two numerals.

Description

If m and n are numerals (e.g. 0, 1, 2, 3,...), then `MUL_CONV "m * n"` returns the theorem:

$$\vdash m * n = s$$

where s is the numeral that denotes the product of the natural numbers denoted by m and n .

Failure

`MUL_CONV tm` fails unless `tm` is of the form " $m * n$ ", where m and n are numerals.

Example

```
#MUL_CONV "0 * 12";;
|- 0 * 12 = 0
```

```
#MUL_CONV "1 * 1";;
|- 1 * 1 = 1
```

```
#MUL_CONV "6 * 11";;
|- 6 * 11 = 66
```

<div data-bbox="234 1823 504 1877" data-label="Text"> <p>NEG_DISCH</p> </div>	<div data-bbox="1203 1823 1414 1877" data-label="Text"> <p>(Drule)</p> </div>
---	---

NEG_DISCH : term -> thm -> thm

Synopsis

Discharges an assumption, transforming $\vdash s \implies F$ into $\vdash \sim s$.

Description

When applied to a term s and a theorem $A \vdash t$, the inference rule `NEG_DISCH` returns the theorem $A - \{s\} \vdash s \implies t$, or if t is just `F`, returns the theorem $A - \{s\} \vdash \sim s$.

$$\frac{A \vdash F}{A - \{s\} \vdash \sim s} \text{ NEG_DISCH } \text{ [special case]}$$

$$\frac{A \vdash t}{A - \{s\} \vdash s \implies t} \text{ NEG_DISCH } \text{ [general case]}$$

Failure

Fails unless the supplied term has type `bool`.

See also

`Thm.DISCH`, `Thm.NOT_ELIM`, `Thm.NOT_INTRO`.

NEGATE_CONV**(Arith)**

`NEGATE_CONV` : (`conv` -> `conv`)

Synopsis

Function for negating the operation of a conversion that proves a formula to be either true or false.

Description

This function negates the operation of a conversion that proves a formula to be either true or false. For example, if `conv` proves "`t`" to be equal to "`T`" then `NEGATE_CONV conv` will prove "`~t`" to be "`F`".

Failure

Fails if the application of the conversion to the negation of the formula does not yield either "`T`" or "`F`".

Example

```
#ARITH_CONV "!n. 0 <= n";;
|- (!n. 0 <= n) = T

#NEGATE_CONV ARITH_CONV "~(!n. 0 <= n)";;
|- ~(!n. 0 <= n) = F

#NEGATE_CONV ARITH_CONV "?n. ~(0 <= n)";;
|- (?n. ~0 <= n) = F
```

negation

(boolSyntax)

negation : term

Synopsis

Constant denoting logical negation.

DescriptionThe ML variable `boolSyntax.negation` is bound to the term `bool$~`.**See also**

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`, `boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let_tm`, `boolSyntax.arb`.

NEQ_CONV

(reduceLib)

NEQ_CONV : conv

Synopsis

Proves equality or inequality of two numerals.

Description

If m and n are both numerals (e.g. 0, 1, 2, 3,...), then `NEQ_CONV "m = n"` returns the theorem:

$\vdash (m = n) = T$

if m and n are identical, or

$\vdash (m = n) = F$

if m and n are distinct.

Failure

NEQ_CONV tm fails unless tm is of the form " $m = n$ ", where m and n are numerals.

Example

```
#NEQ_CONV "12 = 12";;
|- (12 = 12) = T
```

```
#NEQ_CONV "14 = 25";;
|- (14 = 25) = F
```

<div data-bbox="158 1128 427 1178" data-label="Text"> <p><code>new_axiom</code></p> </div>	<div data-bbox="1098 1124 1331 1182" data-label="Text"> <p>(Theory)</p> </div>
--	--

```
new_axiom : string * term -> thm
```

Synopsis

Install a new axiom in the current theory.

Description

If M is a term of type `bool`, a call `new_axiom(name,M)` creates a theorem

$\vdash tm$

and stores it away in the current theory segment under `name`.

Failure

Fails if the given term does not have type `bool`.

Example

```
- new_axiom("untrue", Term '!x. x = 1');
> val it = |- !x. x = 1 : thm
```

Comments

For most purposes, it is unnecessary to declare new axioms: all of classical mathematics can be derived by definitional extension alone. Proceeding by definition is not only more elegant, but also guarantees the consistency of the deductions made. However, there are certain entities which cannot be modelled in simple type theory without further axioms, such as higher transfinite ordinals.

See also

`Thm.mk_thm`, `Definition.new_definition`, `Definition.new_specification`.

new_binder

(boolSyntax)

```
new_binder : string * hol_type -> unit
```

Synopsis

Sets up a new binder in the current theory.

Description

A call `new_binder(bnd,ty)` declares a new binder `bnd` in the current theory. The type must be of the form $('a \rightarrow 'b) \rightarrow 'c$, because being a binder, `bnd` will apply to an abstraction; for example

```
!x:bool. (x=T) \/\ (x=F)
```

is actually a prettyprinting of

```
$! (\x. (x=T) \/\ (x=F))
```

Failure

Fails if the type does not correspond to the above pattern.

Example

```
- new_theory "anorak";
  () : unit

- new_binder ("!!", (bool-->bool)-->bool);;
  () : unit

- Term '!!x. T';
> val it = '!! x. T' : term
```


See also

Theory.constants, Theory.new_constant, boolSyntax.new_infix,
 Definition.new_definition, boolSyntax.new_infixl_definition,
 boolSyntax.new_infixr_definition, boolSyntax.new_binder_definition.

<div style="display: flex; justify-content: space-between;"> <code>new_binder_definition</code> <code>(boolSyntax)</code> </div>
--

```
new_binder_definition : string * term -> thm
```

Synopsis

Defines a new constant, giving it the syntactic status of a binder.

Description

The function `new_binder_definition` provides a facility for making definitional extensions to the current theory by introducing a constant definition. It takes a pair of arguments, consisting of the name under which the resulting theorem will be saved in the current theory segment and a term giving the desired definition. The value returned by `new_binder_definition` is a theorem which states the definition requested by the user.

Let v_1, \dots, v_n be syntactically distinct tuples constructed from the variables x_1, \dots, x_m . A binder is defined by evaluating

```
new_binder_definition (name, 'b v1 ... vn = t')
```

where b does not occur in t , all the free variables that occur in t are a subset of x_1, \dots, x_m , and the type of b has the form $(ty_1 \rightarrow ty_2) \rightarrow ty_3$. This declares b to be a new constant with the syntactic status of a binder in the current theory, and with the definitional theorem

$$\vdash !x_1 \dots x_n. b \ v_1 \ \dots \ v_n = t$$

as its specification. This constant specification for b is saved in the current theory under the name `name` and is returned as a theorem.

The equation supplied to `new_binder_definition` may optionally have any of its free variables universally quantified at the outermost level. The constant b has binder status only after the definition has been made.

Failure

`new_binder_definition` fails if t contains free variables that are not in any one of the variable structures v_1, \dots, v_n or if any variable occurs more than once in v_1, \dots, v_n . Failure also occurs if the type of b is not of the form appropriate for a binder, namely a

type of the form $(ty_1 \rightarrow ty_2) \rightarrow ty_3$. Finally, failure occurs if there is a type variable in v_1, \dots, v_n or t that does not occur in the type of b .

Example

The unique-existence quantifier `?!` is defined as follows.

```
- new_binder_definition
  ('EXISTS_UNIQUE_DEF',
   Term '$?! = \P:(*->bool). ($? P) /\ (!x y. ((P x) /\ (P y)) ==> (x=y))');

> val it = |- $?! = (\P. $? P /\ (!x y. P x /\ P y ==> (x = y))) : thm
```

Comments

It is a common practice among HOL users to write a `$` before the constant being defined as a binder to indicate that it will have a special syntactic status after the definition is made:

```
new_binder_definition(name, Term '$b = ...');
```

This use of `$` is not necessary; but after the definition has been made `$` must, of course, be used if the syntactic status of `b` needs to be suppressed.

See also

`Definition.new_definition`, `boolSyntax.new_infixl_definition`,
`boolSyntax.new_infixr_definition`, `Prim_rec.new_recursive_definition`,
`TotalDefn.Define`.

<code>new_constant</code>	(Theory)
---------------------------	----------

```
new_constant : string * hol_type -> unit
```

Synopsis

Declares a new constant in the current theory.

Description

A call `new_constant(n, ty)` installs a new constant named `n` in the current theory. Note that `new_constant` does not specify a value for the constant, just a name and type. The constant may have a polymorphic type, which can be used in arbitrary instantiations.

Failure

Never fails, but issues a warning if the name is not a valid constant name. It will overwrite an existing constant with the same name in the current theory.

See also

Theory.constants, boolSyntax.new_infix, boolSyntax.new_binder, Definition.new_definition, Definition.new_type_definition, Definition.new_specification, Theory.new_axiom, boolSyntax.new_infixl_definition, boolSyntax.new_infixr_definition, boolSyntax.new_binder_definition.

<div data-bbox="159 790 569 842" data-label="Text"> <p><code>new_definition</code></p> </div>	<div data-bbox="984 790 1331 842" data-label="Text"> <p>(Definition)</p> </div>
---	---

```
new_definition : string * term -> thm
```

Synopsis

Declare a new constant and install a definitional axiom in the current theory.

Description

The function `new_definition` provides a facility for definitional extensions to the current theory. It takes a pair argument consisting of the name under which the resulting definition will be saved in the current theory segment, and a term giving the desired definition. The value returned by `new_definition` is a theorem which states the definition requested by the user.

Let v_1, \dots, v_n be tuples of distinct variables, containing the variables x_1, \dots, x_m . Evaluating `new_definition (name, c v_1 ... v_n = t)`, where c is not already a constant, declares the sequent $(\{\}, \backslash v_1 \dots v_n. t)$ to be a definition in the current theory, and declares c to be a new constant in the current theory with this definition as its specification. This constant specification is returned as a theorem with the form

$$\vdash !x_1 \dots x_m. c v_1 \dots v_n = t$$

and is saved in the current theory under `name`. Optionally, the definitional term argument may have any of its variables universally quantified.

Failure

`new_definition` fails if t contains free variables that are not in x_1, \dots, x_m (this is equivalent to requiring $\backslash v_1 \dots v_n. t$ to be a closed term). Failure also occurs if any variable occurs more than once in v_1, \dots, v_n . Finally, failure occurs if there is a type variable in v_1, \dots, v_n or t that does not occur in the type of c .

Example

A NAND relation can be defined as follows.

```

- new_definition (
  "NAND2",
  Term'NAND2 (in_1,in_2) out = !t:num. out t = ~(in_1 t /\ in_2 t)');

> val it =
  |- !in_1 in_2 out.
      NAND2 (in_1,in_2) out = !t. out t = ~(in_1 t /\ in_2 t)
  : thm

```

See also

Definition.new_specification, boolSyntax.new_binder_definition,
 boolSyntax.new_infixl_definition, boolSyntax.new_infixr_definition,
 Prim_rec.new_recursive_definition, TotalDefn.Define.

new_infix**(boolSyntax)**

```
new_infix : string * hol_type * int -> unit
```

Synopsis

Declares a new infix constant in the current theory.

Description

A call `new_infix ("i", ty, n)` makes `i` a right associative infix constant in the current theory. It has binding strength of `n`, the larger this number, the more tightly the infix will attempt to “grab” arguments to its left and right. Note that the call to `new_infix` does not specify the value of the constant. The constant may have a polymorphic type, which may be arbitrarily instantiated. Like any other infix or binder, its special parse status may be suppressed by preceding it with a dollar sign.

Comments

Infixes defined with `new_infix` associate to the right, i.e., `A <op> B <op> C` is equivalent to `A op (B <op> C)`. Some standard infixes, with their precedences and associativities in the system are:

\$,	----> 50	RIGHT
\$=	----> 100	NONASSOC
\$==>	----> 200	RIGHT
\$\	----> 300	RIGHT
\$/\	----> 400	RIGHT
\$>, \$<	----> 450	RIGHT
\$>=, \$<=	----> 450	RIGHT
+\$, \$-	----> 500	LEFT
*\$, \$DIV	----> 600	LEFT
\$MOD	----> 650	LEFT
\$EXP	----> 700	RIGHT
\$o	----> 800	RIGHT

Note that the arithmetic operators `+`, `-`, `*`, `DIV` and `MOD` are left associative in `hol98` releases from `Taupo` onwards. Non-associative infixes (`=` above, for example) will cause parse errors if an attempt is made to group them (e.g., `x = y = z`).

Failure

Fails if the name is not a valid constant name.

Example

The following shows the use of the infix and the prefix form of an infix constant. It also shows binding resolution between infixes of different precedence.

```
- new_infix("orelse", Type':bool->bool->bool', 50);
val it = () : unit

- Term'T \/ T orelse F';
val it = 'T \/ T orelse F' : term

- --'$orelse T F'--;
val it = 'T orelse F' : term

- dest_comb (--'T \/ T orelse F'--);
> val it = ('$orelse (T \/ T)', 'F') : term * term
```

See also

`Parse.add_infix`, `Theory.constants`, `Theory.new_constant`, `boolSyntax.new_binder`, `Definition.new_definition`, `boolSyntax.new_binder_definition`.

<code>new_infixl_definition</code>	<code>(boolSyntax)</code>
------------------------------------	---------------------------

```
new_infixl_definition : string * term * int -> thm
```

Synopsis

Declares a new left associative infix constant and installs a definition in the current theory.

Description

The function `new_infix_definition` provides a facility for definitional extensions to the current theory. It takes a triple consisting of the name under which the resulting definition will be saved in the current theory segment, a term giving the desired definition and an integer giving the precedence of the infix. The value returned by `new_infix_definition` is a theorem which states the definition requested by the user.

Let v_1 and v_2 be tuples of distinct variables, containing the variables x_1, \dots, x_m . Evaluating `new_infix_definition (name, ix v_1 v_2 = t)` declares the sequent $(\{\}, \backslash v_1 v_2. t)$ to be a definition in the current theory, and declares `ix` to be a new constant in the current theory with this definition as its specification. This constant specification is returned as a theorem with the form

$$\vdash !x_1 \dots x_m. v_1 \text{ ix } v_2 = t$$

and is saved in the current theory under (the name) `name`. Optionally, the definitional term argument may have any of its variables universally quantified. The constant `ix` has infix status only after the infix declaration has been processed. It is therefore necessary to use the constant in normal prefix position when making the definition.

Failure

`new_infixl_definition` fails if t contains free variables that are not in either of the variable structures v_1 and v_2 (this is equivalent to requiring $\backslash v_1 v_2. t$ to be a closed term); or if any variable occurs more than once in v_1, v_2 . It also fails if the precedence level chosen for the infix is already home to parsing rules of a different form of fixity (infixes associating in a different way, or suffixes, prefixes etc). Finally, failure occurs if there is a type variable in v_1, \dots, v_n or t that does not occur in the type of `ix`.

Example

The `nand` function can be defined as follows.

```
- new_infix_definition
  ("nand", --'$nand in_1 in_2 = ~(in_1 /\ in_2)'--, 500);;
> val it = |- !in_1 in_2. in_1 nand in_2 = ~(in_1 /\ in_2) : thm
```

Comments

It is a common practice among HOL users to write a \$ before the constant being defined as an infix to indicate that after the definition is made, it will have a special syntactic status; ie. to write:

```
new_infixl_definition("ix_DEF", Term '$ix m n = ...')
```

This use of \$ is not necessary; but after the definition has been made \$ must, of course, be used if the syntactic status needs to be suppressed.

In releases of hol98 past Taupo 1, `new_infixl_definition` and its sister `new_infixr_definition` replace the old `new_infix_definition`, which has been superseded. Its behaviour was to define a right associative infix, so can be freely replaced by `new_infixr_definition`.

See also

`boolSyntax.new_binder_definition`, `Definition.new_definition`,
`Definition.new_specification`, `boolSyntax.new_infixr_definition`,
`Prim_rec.new_recursive_definition`, `TotalDefn.Define`.

<code>new_infixr_definition</code>	<code>(boolSyntax)</code>
------------------------------------	---------------------------

```
new_infixr_definition : string * term * int -> thm
```

Synopsis

Declares a new right associative infix constant and installs a definition in the current theory.

Description

The function `new_infixr_definition` has exactly the same effect as `new_infixl_definition` except that the infix constant defined will associate to the right.

See also

`Definition.new_definition`, `Definition.new_specification`, `boolSyntax.new_infix`,
`boolSyntax.new_infixl_definition`.

<code>new_recursive_definition</code>	<code>(Prim_rec)</code>
---------------------------------------	-------------------------

```
new_recursive_definition : {name:string, def:term, rec_axiom:thm} -> thm
```

Synopsis

Defines a primitive recursive function over a concrete recursive type.

Description

`new_recursive_definition` provides a facility for defining primitive recursive functions on arbitrary concrete recursive types. `name` is a name under which the resulting definition will be saved in the current theory segment. `def` is a term giving the desired primitive recursive function definition. `rec_axiom` is the primitive recursion theorem for the concrete type in question; this must be a theorem obtained from `define_type`. The value returned by `new_recursive_definition` is a theorem which states the primitive recursive definition requested by the user. This theorem is derived by formal proof from an instance of the general primitive recursion theorem given as the second argument.

A theorem `th` of the form returned by `define_type` is a primitive recursion theorem for an automatically-defined concrete type `ty`. Let `C1`, ..., `Cn` be the constructors of this type, and let '`(Ci vs)`' represent a (curried) application of the *i*th constructor to a sequence of variables. Then a curried primitive recursive function `fn` over `ty` can be specified by a conjunction of (optionally universally-quantified) clauses of the form:

$$\begin{aligned} \text{fn } v_1 \dots (C_1 \text{ vs}_1) \dots v_m &= \text{body}_1 \quad \wedge \\ \text{fn } v_1 \dots (C_2 \text{ vs}_2) \dots v_m &= \text{body}_2 \quad \wedge \\ &\vdots \\ \text{fn } v_1 \dots (C_n \text{ vs}_n) \dots v_m &= \text{body}_n \end{aligned}$$

where the variables `v1`, ..., `vm`, `vs` are distinct in each clause, and where in the *i*th clause `fn` appears (free) in `bodyi` only as part of an application of the form:

$$\text{fn } t_1 \dots v \dots t_m$$

in which the variable `v` of type `ty` also occurs among the variables `vsi`.

If `tm` is a conjunction of clauses, as described above, then evaluating:

$$\text{new_recursive_definition}\{\text{name}=\text{name}, \text{rec_axiom}=\text{th}, \text{def}=\text{tm}\}$$

automatically proves the existence of a function `fn` that satisfies the defining equations supplied as the fourth argument, and then declares a new constant in the current theory with this definition as its specification. This constant specification is returned as a theorem and is saved in the current theory segment under the name `name`.

`new_recursive_definition` also allows the supplied definition to omit clauses for any number of constructors. If a defining equation for the *i*th constructor is omitted, then the value of `fn` at that constructor:

$$\text{fn } v_1 \dots (C_i \text{ vs}_i) \dots v_n$$

is left unspecified (`fn`, however, is still a total function).

Failure

A call to `new_recursive_definition` fails if the supplied theorem is not a primitive recursion theorem of the form returned by `define_type`; if the term argument supplied is not a well-formed primitive recursive definition; or if any other condition for making a constant specification is violated (see the failure conditions for `new_specification`).

Example

Given the following primitive recursion theorem for labelled binary trees:

```
|- !f0 f1.
    ?! fn.
    (!x. fn(LEAF x) = f0 x) /\
    (!b1 b2. fn(NODE b1 b2) = f1(fn b1)(fn b2)b1 b2)
```

`new_recursive_definition` can be used to define primitive recursive functions over binary trees. Suppose the value of `th` is this theorem. Then a recursive function `Leaves`, which computes the number of leaves in a binary tree, can be defined recursively as shown below:

```
- val Leaves = new_recursive_definition
  {name = "Leaves",
   rec_axiom = th,
   def= --'(Leaves (LEAF (x:'a)) = 1) /\
           (Leaves (NODE t1 t2) = (Leaves t1) + (Leaves t2))'--};
> val Leaves =
  |- (!x. Leaves (LEAF x) = 1) /\
    !t1 t2. Leaves (NODE t1 t2) = Leaves t1 + Leaves t2 : thm
```

The result is a theorem which states that the constant `Leaves` satisfies the primitive-recursive defining equations supplied by the user.

The function defined using `new_recursive_definition` need not, in fact, be recursive. Here is the definition of a predicate `IsLeaf`, which is true of binary trees which are leaves, but is false of the internal nodes in a binary tree:

```
- val IsLeaf = new_recursive_definition
  {name = "IsLeaf",
   rec_axiom = th,
   def = --'(IsLeaf (NODE t1 t2) = F) /\
           (IsLeaf (LEAF (x:'a)) = T)'--};
> val IsLeaf = |- (!t1 t2. IsLeaf (NODE t1 t2) = F) /\
    !x. IsLeaf (LEAF x) = T : thm
```

Note that the equations defining a (recursive or non-recursive) function on binary trees by cases can be given in either order. Here, the `NODE` case is given first, and the `LEAF` case second. The reverse order was used in the above definition of `Leaves`.

`new_recursive_definition` also allows the user to partially specify the value of a function defined on a concrete type, by allowing defining equations for some of the constructors to be omitted. Here, for example, is the definition of a function `Label` which extracts the label from a leaf node. The value of `Label` applied to an internal node is left unspecified:

```
- val Label = new_recursive_definition
    {name = "Label",
     rec_axiom = th,
     def = --'Label (LEAF (x:'a)) = x'--};
> val Label = |- !x. Label (LEAF x) = x : thm
```

Curried functions can also be defined, and the recursion can be on any argument. The next definition defines an infix function `<<` which expresses the idea that one tree is a proper subtree of another.

```
- val _ = set_fixity ("<<", Infixl 231);

- val Subtree = new_recursive_definition
    {name = "Subtree",
     rec_axiom = th,
     def = --'($<< (t:'a bintree) (LEAF (x:'a)) = F) /\
              ($<< t (NODE t1 t2) = (t = t1) \/\
                                   (t = t2) \/\
                                   ($<< t t1) \/\
                                   ($<< t t2))'--};

> val Subtree =
    |- (!t x. t << LEAF x = F) /\
       !t t1 t2.
       t << NODE t1 t2 = (t = t1) \/\ (t = t2) \/\
                        (t << t1) \/\ (t << t2) : thm
```

Note that the fixity of the identifier `<<` is set independently of the definition.

See also

`bossLib.Hol_datatype`, `Prim_rec.prove_rec_fn_exists`, `TotalDefn.Define`, `Parse.set_fixity`.

<div data-bbox="159 349 655 405" data-label="Text"> <p><code>new_specification</code></p> </div>	<div data-bbox="984 347 1329 398" data-label="Text"> <p>(Definition)</p> </div>
--	---

```
new_specification : string * string list * thm -> thm
```

Synopsis

Introduce a constant or constants satisfying a given property.

Description

The ML function `new_specification` implements the primitive rule of constant specification for the HOL logic. Evaluating:

```
new_specification (name, ["c1", ..., "cn"], |- ?x1...xn. t)
```

simultaneously introduces new constants named `c1, ..., cn` satisfying the property:

```
|- t[c1, ..., cn/x1, ..., xn]
```

This theorem is stored, with name `name`, as a definition in the current theory segment. It is also returned by the call to `new_specification`

Failure

`new_specification` fails if the theorem argument has assumptions or free variables. It also fails if the supplied constant names `c1, ..., cn` are not distinct. It also fails if the length of the existential prefix of the theorem is not at least `n`. Finally, failure occurs if some `ci` does not contain all the type variables that occur in the term `?x1...xn. t`.

Uses

`new_specification` can be used to introduce constants that satisfy a given property without having to make explicit equational constant definitions for them. For example, the built-in constants `MOD` and `DIV` are defined in the system by first proving the theorem:

```
th |- ?MOD DIV.
      !n. 0 < n ==> !k. (k = (DIV k n * n) + MOD k n) /\ MOD k n < n
```

and then making the constant specification:

```
new_specification ("DIVISION", ["MOD", "DIV"], th)
```

This introduces the constants `MOD` and `DIV` with the defining property shown above.

Comments

The introduced constants have a prefix parsing status. To alter this, use `set_fixity`. Typical fixity values are `Prefix n`, `Binder n`, `Infixl n`, `Infixr n`, `Suffix n`, `TruePrefix n` or `Closefix`.

See also

Definition.new_definition, boolSyntax.new_binder_definition,
 boolSyntax.new_infixl_definition, boolSyntax.new_infixr_definition,
 TotalDefn.Define, Parse.set_fixity.

new_theory**(Theory)**

```
new_theory : string -> unit
```

Synopsis

Creates a new theory segment.

Description

A theory consists of a hierarchy of named parts called ‘theory segments’. All theory segments have a ‘theory’ of the same name associated with them consisting of the theory segment itself together with the contents of all its ancestors. Each axiom, definition, specification and theorem belongs to a particular theory segment.

Calling `new_theory thy` creates a new, and empty, theory segment having name `thy`. The theory segment which was current before the call becomes a parent of the new theory segment. The new theory therefore consists of the current theory extended with the new theory segment. The new theory segment replaces its parent as the current theory segment. The parent segment is exported to disk.

In the interests of interactive usability, the behaviour of `new_theory` has some special cases. First, if `new_theory thy` is called in a situation where the current theory segment is already called `thy`, then this is interpreted as the user wanting to restart the current segment. In that case, the current segment is wiped clean (types and constants declared in it are removed from the signature, and all definitions, theorems and axioms are deleted) but is otherwise unchanged (it keeps the same parents, for example).

Second, if the current theory segment is empty and named "scratch", then `new_theory thy` creates a new theory segment the parents of which are the parents of "scratch". (This situation is almost never visible to users.)

Failure

A call `new_theory thy` fails if the name `thy` is unsuitable for use as a filename. In particular, it should be an alphanumeric identifier.

Failure also occurs if `thy` is the name of a currently loaded theory segment. In general, all theory names, whether loaded or not, should be distinct. Moreover, the names should be distinct even when case distinctions are ignored.

Example

In the following, we follow a standard progression: start HOL up and declare a new theory segment.

```

- current_theory();
> val it = "scratch" : string

- parents "-";
> val it = ["list", "option"] : string list

- new_theory "foo";
<<HOL message: Created theory "foo">>
> val it = () : unit

- parents "-";
> val it = ["list", "option"] : string list

```

Next we make a definition, prove and store a theorem, and then change our mind about the name of the defined constant. Restarting the current theory keeps the static theory context fixed but clears the current segment so that we have a clean slate to work from.

```

- val def = new_definition("foo", Term 'foo x = x + x');
> val def = |- !x. foo x = x + x : thm

val thm = Q.store_thm("foo_thm", 'foo x = 2 * x',
                    RW_TAC arith_ss [def]);
> val thm = |- foo x = 2 * x : thm

- new_theory "foo";
<<HOL message: Restarting theory "foo">>
> val it = () : unit

val def = new_definition("twice", Term 'twice x = x + x');
> val def = |- !x. twice x = x + x : thm

- curr_defs();
> val it = [("twice", |- !x. twice x = x + x)]
           : (string * thm) list

```

Comments

The theory file in which the data of the new theory segment is ultimately stored will have name `thyTheory` in the directory in which `export_theory` is called.

Uses

Modularizing large formalizations. By splitting a formalization effort into theory segments by use of `new_theory`, the work required if definitions, etc., need to be changed is minimized. Only the associated segment and its descendants need be redefined.

See also

`Theory.current_theory`, `Theory.new_axiom`, `Theory.parents`, `boolSyntax.new_binder`, `Theory.new_constant`, `Definition.new_definition`, `boolSyntax.new_infix`, `Definition.new_specification`, `Theory.new_type`, `DB.print_theory`, `Theory.save_thm`, `Theory.export_theory`, `Theory.after_new_theory`.

<code>new_type</code>	<code>(Theory)</code>
-----------------------	-----------------------

```
new_type : string * int -> unit
```

Synopsis

Declares a new type or type constructor.

Description

A call `new_type(t,n)` declares a new n -ary type constructor called t in the current theory segment. If n is zero, this is just a new base type.

Failure

Never fails, but issues a warning if the name is not a valid type name. It will overwrite an existing type operator with the same name in the current theory.

Example

A non-definitional version of ZF set theory might declare a new type `set` and start using it as follows:

```
- new_theory"ZF";
<<HOL message: Created theory "ZF">>
> val it = () : unit

- new_type("set", 0);;
> val it = () : unit

- new_constant ("mem", Type' :set->set->bool');
> val it = () : unit
```

```
- new_axiom("EXT", Term'(!z. mem z x = mem z y) ==> (x = y)');
> val it = |- (!z. mem z x = mem z y) ==> (x = y) : thm
```

See also

Theory.types, Theory.new_constant, Theory.new_axiom.

new_type_definition (Definition)

```
new_type_definition : string * thm -> thm
```

Synopsis

Defines a new type constant or type operator.

Description

The ML function `new_type_definition` implements the primitive HOL rule of definition for introducing new type constants or type operators into the logic. If t is a term of type $ty \rightarrow \text{bool}$ containing n distinct type variables, then evaluating:

```
new_type_definition (tyop, |- ?x. t x)
```

results in `tyop` being declared as a new n -ary type operator in the current theory and returned by the call to `new_type_definition`. This new type operator is characterized by a definitional axiom of the form:

```
|- ?rep:( 'a, ..., 'n)op->tyop. TYPE_DEFINITION t rep
```

which is stored as a definition in the current theory segment under the automatically-generated name `op_TY_DEF`. The arguments to the new type operator occur in the order given by an alphabetic ordering of the name of the corresponding type variables. The constant `TYPE_DEFINITION` in this axiomatic characterization of `tyop` is defined by:

```
|- TYPE_DEFINITION (P: 'a->bool) (rep: 'b->'a) =
  (!x' x''. (rep x' = rep x'') ==> (x' = x'')) /\
  (!x. P x = (?x'. x = rep x'))
```

Thus `|- ?rep. TYPE_DEFINITION P rep` asserts that there is a bijection between the newly defined type $('a, \dots, 'n)tyop$ and the set of values of type `ty` that satisfy `P`.

Failure

Executing `new_type_definition(tyop,th)` fails if `th` is not an assumption-free theorem of the form $\vdash \ ?x. \ t \ x$. Failure also occurs if the type of `t` is not of the form `ty->bool`.

Example

In this example, a type containing three elements is defined. The predicate defining the type is over the type `bool # bool`.

```
app load ["PairedLambda", "Q"]; open PairedLambda pairTheory;

- val tyax =
  new_type_definition ("three",
    Q.prove('?p. (\(x,y). ~(x /\ y)) p',
      Q.EXISTS_TAC '(F,F)' THEN GEN_BETA_TAC THEN REWRITE_TAC []));

> val tyax = \|- ?rep. TYPE_DEFINITION (\(x,y). ~(x /\ y)) rep : thm
```

Comments

Usually, once a type has been defined, maps between the representation type and the new type need to be proved. This may be accomplished using `define_new_type_bijections`. In the example, the two functions are named `abs3` and `rep3`.

```
- val three_bij = define_new_type_bijections
  {name="three_tybij", ABS="abs3", REP="rep3", tyax=tyax};

> val three_bij =
  \|- (!a. abs3 (rep3 a) = a) /\
    (!r. (\(x,y). ~(x /\ y)) r = (rep3 (abs3 r) = r))
```

Properties of the maps may be conveniently proved with `prove_abs_fn_one_one`, `prove_abs_fn_onto`, `prove_rep_fn_one_one`, and `prove_rep_fn_onto`. In this case, we need only `prove_abs_fn_one_one`.

```
- val abs_11 = GEN_BETA_RULE (prove_abs_fn_one_one three_bij);

> val abs_11 =
  \|- !r r'.
    ~(FST r /\ SND r) ==>
    ~(FST r' /\ SND r') ==>
    ((abs3 r = abs3 r') = (r = r')) : thm
```

Now we address how to define constants designating the three elements of our example type. We will use `new_specification` to create these constants (say `e1`, `e2`, and `e3`) and their characterizing property, which is


```
~(e1 = e2) /\ ~(e2 = e3) /\ ~(e3 = e1)
```

A simple lemma stating that the abstraction function doesn't confuse any of the representations is required:

```
- val abs_distinct =
  REWRITE_RULE (PAIR_EQ::pair_rws)
  (LIST_CONJ (map (C Q.SPECL abs_11)
    [[ '(F,F)', '(F,T)',
      '(F,T)', '(T,F)',
      '(T,F)', '(F,F)' ] ]));

> val abs_distinct =
  |- ~(abs3 (F,F) = abs3 (F,T)) /\
    ~(abs3 (F,T) = abs3 (T,F)) /\
    ~(abs3 (T,F) = abs3 (F,F)) : thm
```

Finally, we can introduce the constants and their property.

```
- val THREE = new_specification
  ("THREE", ["e1", "e2", "e3"],
  PROVE [abs_distinct]
  (Term '?x y z:three. ~(x=y) /\ ~(y=z) /\ ~(z=x)'));

> val THREE = |- ~(e1 = e2) /\ ~(e2 = e3) /\ ~(e3 = e1) : thm
```

See also

Drule.define_new_type_bijections, Prim_rec.prove_abs_fn_one_one,
Prim_rec.prove_abs_fn_onto, Drule.prove_rep_fn_one_one, Drule.prove_rep_fn_onto,
Definition.new_specification.

next	(Lib)
------	-------

```
next : ('a,'b) istream -> ('a,'b) istream
```

Synopsis

Move to the next element in the stream.

Description

An application `next istrm` moves to the next element in the stream.

Failure

If the transition function supplied when building the stream fails on the current state.

Example

```
- val istrm = mk_istream (fn x => x+1) 0 (concat "gsym" o int_to_string);
> val it = <istream> : (int, string) istream

- next istrm;
> val it = <istream> : (int, string) istream
```

Comments

Perhaps the type of `next` should be `('a,'b) istream -> unit`.

See also

`Lib.mk_istream`, `Lib.state`, `Lib.reset`.

NO_CONV	(Conv)
---------	--------

NO_CONV : conv

Synopsis

Conversion that always fails.

Failure

NO_CONV always fails.

See also

`Conv.ALL_CONV`.

NO_TAC	(Tactical)
--------	------------

NO_TAC : tactic

Synopsis

Tactic which always fails.

Description

Whatever goal it is applied to, NO_TAC always fails with string 'NO_TAC'.

Failure

Always fails.

See also

Tactical.ALL_TAC, Thm_cont.ALL_THEN, Tactical.FAIL_TAC, Thm_cont.NO_THEN.

NO_THEN	(Thm_cont)
---------	------------

NO_THEN : thm_tactical

Synopsis

Theorem-tactical which always fails.

Description

When applied to a theorem-tactic and a theorem, the theorem-tactical NO_THEN always fails with string 'NO_THEN'.

Failure

Always fails when applied to a theorem-tactic and a theorem (note that it never gets as far as being applied to a goal!)

Uses

Writing compound tactics or tacticals.

See also

Tactical.ALL_TAC, Thm_cont.ALL_THEN, Tactical.FAIL_TAC, Tactical.NO_TAC.

non_presburger_subterms	(Arith)
-------------------------	---------

non_presburger_subterms : (term -> term list)

Synopsis

Computes the subterms of a term that are not in the Presburger subset of arithmetic.

Description

This function computes a list of subterms of a term that are not in the Presburger subset of natural number arithmetic. All numeric variables in the term are included in the result. Presburger natural arithmetic is the subset of arithmetic formulae made up from natural number constants, numeric variables, addition, multiplication by a constant, the natural number relations $<$, $<=$, $=$, $>=$, $>$ and the logical connectives \sim , \wedge , \vee , \implies , $=$ (if-and-only-if), $!$ ('forall') and $?$ ('there exists').

Products of two expressions which both contain variables are not included in the subset, so such products will appear in the result list. However, the function `SUC` which is not normally included in a specification of Presburger arithmetic is allowed in this HOL implementation. This function also considers subtraction and the predecessor function, `PRE`, to be part of the subset.

Failure

Never fails.

Example

```
#non_presburger_subterms "!m n p. m < (2 * n) /\ (n + n) <= p ==> m < SUC p";;
["m"; "n"; "p"] : term list
```

```
#non_presburger_subterms "!m n p q. m < (n * p) /\ (n * p) < q ==> m < q";;
["m"; "n * p"; "q"] : term list
```

```
#non_presburger_subterms "(m + n) - m = f n";;
["m"; "n"; "f n"] : term list
```

See also

`Arith.INSTANCE.T_CONV`, `Arith.is_presburger`.

<pre>non_type_definitions</pre>	<pre>(EmitTeX)</pre>
---------------------------------	----------------------

```
non_type_definitions : string -> (string * thm) list
```

Synopsis

A versions of `definitions` that attempts to filter out definitions created by `Hol_datatype`.

Description

An invocation `non_type_definitions thy`, where `thy` is the name of a currently loaded theory segment, will return a list of the definitions stored in that theory. Each definition is paired with its name in the result.

Failure

Never fails. If `thy` is not the name of a currently loaded theory segment, the empty list is returned.

Example

```
- new_theory "example";
<<HOL message: Created theory "example">>
> val it = () : unit
- val _ = Hol_datatype 'example = First | Second';
<<HOL message: Defined type: "example">>
- val example_def = Define
  '(example First = Second) /\ (example Second = First)';
Definition has been stored under "example_def".
> val example_def = |- (example First = Second) /\ (example Second = First) :
  thm

- definitions "example";
> val it =
  [("example_TY_DEF", |- ?rep. TYPE_DEFINITION (\n. n < 2) rep),
   ("example_BIJ",
    |- (!a. num2example (example2num a) = a) /\
       !r. (\n. n < 2) r = (example2num (num2example r) = r)),
   ("First", |- First = num2example 0),
   ("Second", |- Second = num2example 1),
   ("example_size_def", |- !x. example_size x = 0),
   ("example_case",
    |- !v0 v1 x.
       (case x of First -> v0 || Second -> v1) =
       (\m. (if m = 0 then v0 else v1)) (example2num x)),
   ("example_def", |- (example First = Second) /\ (example Second = First))]
  : (string * thm) list

- EmitTeX.non_type_definitions "example";
> val it =
  [("example_def", |- (example First = Second) /\ (example Second = First))]
  : (string * thm) list
```

See also

DB.definitions, bossLib.Hol_datatype.

non_type_theorems

(EmitTeX)

```
non_type_theorems : string -> (string * thm) list
```

Synopsis

A versions of theorems that attempts to filter out theorems created by Hol_datatype.

Description

An invocation `non_type_theorems thy`, where `thy` is the name of a currently loaded theory segment, will return a list of the theorems stored in that theory. Axioms and definitions are excluded. Each theorem is paired with its name in the result.

Failure

Never fails. If `thy` is not the name of a currently loaded theory segment, the empty list is returned.

Example

```
- new_theory "example";
<<HOL message: Created theory "example">>
> val it = () : unit
- val _ = Hol_datatype 'example = First | Second';
<<HOL message: Defined type: "example">>
- val example_def = Define
  '(example First = Second) /\ (example Second = First)';
Definition has been stored under "example_def".
> val example_def = |- (example First = Second) /\ (example Second = First) :
  thm
- save_thm("example_thm",
  METIS_PROVE [example_def, theorem "example_nchotomy"]
  ' '!x. example (example x) = x ' ');
metis: r[+0+5]+0+0+0+0+6+2+2+1+0+1+1#
> val it = |- !x. example (example x) = x : thm

- theorems "example";
```

```

> val it =
  [("num2example_example2num", |- !a. num2example (example2num a) = a),
   ("example2num_num2example",
    |- !r. r < 2 = (example2num (num2example r) = r)),
   ("num2example_11",
    |- !r r'.
      r < 2 ==> r' < 2 ==> ((num2example r = num2example r') = (r = r'))),
   ("example2num_11", |- !a a'. (example2num a = example2num a') = (a = a')),
   ("num2example_ONTO", |- !a. ?r. (a = num2example r) /\ r < 2),
   ("example2num_ONTO", |- !r. r < 2 = ?a. r = example2num a),
   ("num2example_thm",
    |- (num2example 0 = First) /\ (num2example 1 = Second)),
   ("example2num_thm",
    |- (example2num First = 0) /\ (example2num Second = 1)),
   ("example_EQ_example",
    |- !a a'. (a = a') = (example2num a = example2num a')),
   ("example_case_def",
    |- (!v0 v1. (case First of First -> v0 || Second -> v1) = v0) /\
      !v0 v1. (case Second of First -> v0 || Second -> v1) = v1),
   ("datatype_example", |- DATATYPE (example First Second)),
   ("example_distinct", |- ~(First = Second)),
   ("example_case_cong",
    |- !M M' v0 v1.
      (M = M') /\ ((M' = First) ==> (v0 = v0')) /\
      ((M' = Second) ==> (v1 = v1')) ==>
      ((case M of First -> v0 || Second -> v1) =
       case M' of First -> v0' || Second -> v1')),
   ("example_nchotomy", |- !a. (a = First) \/ (a = Second)),
   ("example_Axiom", |- !x0 x1. ?f. (f First = x0) /\ (f Second = x1)),
   ("example_induction", |- !P. P First /\ P Second ==> !a. P a),
   ("example_thm", |- !x. example (example x) = x)] : (string * thm) list

- EmitTeX.non_type_theorems "example";
> val it = [("example_thm", |- !x. example (example x) = x)] :
  (string * thm) list

```

See also

DB.theorems, bossLib.Hol.datatype.

norm_subst	(Term)
-------------------	---------------

```
norm_subst : (hol_type,hol_type) subst
            -> (term,term) subst -> (term,term)subst
```

Synopsis

Instantiate term substitution by a type substitution.

Description

The substitutions coming from `raw_match` need to be normalized before they can be applied by inference rules like `INST_TY_TERM`. An invocation `raw_match avoid_tys avoid_tms pat ob A` returns a pair of substitutions $(S, (T, Id))$. The `Id` component can be ignored. The `S` component is a substitution for term variables, but it has to be instantiated by `T` in order to be suitable for use by `INST_TY_TERM`. In this case, one uses `norm_subst T S`. Thus a suitable input for `INST_TY_TERM` would be $(norm_subst\ T\ S, T)$.

Failure

Never fails.

Example

```
- val (S,(T,_)) = raw_match [] empty_varset
      (Term '\x:'a. x = f (y:'b)')
      (Term '\a.    a = ~p') ([], ([], []));
> val S = [{redex = '(f :'b -> 'a)', residue = '$~'},
           {redex = '(y :'b)',      residue = '(p :bool)'}] : ...

      val T = [{redex = ':'b', residue = ':bool'},
              {redex = ':'a', residue = ':bool'}] : ...

- norm_subst T S;
> val it =
  [{redex = '(y :bool)', residue = '(p :bool)'},
   {redex = '(f :bool -> bool)', residue = '$~'}]
  : {redex : term, residue : term} list
```

Comments

Higher level matching routines, like `match_term` and `match_term1` already return normalized substitutions.

See also

`Term.raw_match`, `Term.match_term`, `Term.match_term1`.

NOT_CONV

(reduceLib)

NOT_CONV : conv

Synopsis

Simplifies certain boolean negation expressions.

Description

If `tm` corresponds to one of the forms given below, where `t` is an arbitrary term of type `bool`, then `NOT_CONV tm` returns the corresponding theorem.

```

NOT_CONV "~F" = |- ~F = T
NOT_CONV "~T" = |- ~T = F
NOT_CONV "~~t" = |- ~~t = t

```

Failure

`NOT_CONV tm` fails unless `tm` has one of the forms indicated above.

Example

```

#NOT_CONV "~~~~T";;
|- ~~~~T = ~T

```

```

#NOT_CONV "~~T";;
|- ~~T = T

```

```

#NOT_CONV "~T";;
|- ~T = F

```

NOT_ELIM

(Thm)

NOT_ELIM : thm -> thm

Synopsis

Transforms $A \vdash \sim t$ into $A \vdash t \implies F$.

Description

When applied to a theorem $A \vdash \sim t$, the inference rule NOT_ELIM returns the theorem $A \vdash t \implies F$.

$$\frac{A \vdash \sim t}{A \vdash t \implies F} \text{ NOT_ELIM}$$

Failure

Fails unless the theorem has a negated conclusion.

See also

Drule.IMP_ELIM, Thm.NOT_INTRO.

<p>NOT_EQ_SYM</p>

<p>(Drule)</p>

NOT_EQ_SYM : (thm -> thm)

Synopsis

Swaps left-hand and right-hand sides of a negated equation.

Description

When applied to a theorem $A \vdash \sim(t_1 = t_2)$, the inference rule NOT_EQ_SYM returns the theorem $A \vdash \sim(t_2 = t_1)$.

$$\frac{A \vdash \sim(t_1 = t_2)}{A \vdash \sim(t_2 = t_1)} \text{ NOT_EQ_SYM}$$

Failure

Fails unless the theorem's conclusion is a negated equation.

See also

Conv.DEPTH_CONV, Thm.REFL, Thm.SYM.

NOT_EXISTS_CONV

(Conv)

NOT_EXISTS_CONV : conv

Synopsis

Moves negation inwards through an existential quantification.

Description

When applied to a term of the form $\sim(?x.P)$, the conversion NOT_EXISTS_CONV returns the theorem:

$$\vdash \sim(?x.P) = !x.\sim P$$

Failure

Fails if applied to a term not of the form $\sim(?x.P)$.

See also

Conv.EXISTS_NOT_CONV, Conv.FORALL_NOT_CONV, Conv.NOT_FORALL_CONV.

NOT_FORALL_CONV

(Conv)

NOT_FORALL_CONV : conv

Synopsis

Moves negation inwards through a universal quantification.

Description

When applied to a term of the form $\sim(!x.P)$, the conversion NOT_FORALL_CONV returns the theorem:

$$\vdash \sim(!x.P) = ?x.\sim P$$

It is irrelevant whether x occurs free in P .

Failure

Fails if applied to a term not of the form $\sim(!x.P)$.

See also

`Conv.EXISTS_NOT_CONV`, `Conv.FORALL_NOT_CONV`, `Conv.NOT_EXISTS_CONV`.

NOT_INTRO	(Thm)
------------------	--------------

`NOT_INTRO` : (thm -> thm)

Synopsis

Transforms $\vdash t \implies F$ into $\vdash \sim t$.

Description

When applied to a theorem $A \vdash t \implies F$, the inference rule `NOT_INTRO` returns the theorem $A \vdash \sim t$.

$$\frac{A \vdash t \implies F}{A \vdash \sim t} \text{ NOT_INTRO}$$

Failure

Fails unless the theorem has an implicative conclusion with F as the consequent.

See also

`Drule.IMP_ELIM`, `Thm.NOT_ELIM`.

NOT_PEXISTS_CONV	(PairRules)
-------------------------	--------------------

`NOT_PEXISTS_CONV` : conv

Synopsis

Moves negation inwards through a paired existential quantification.

Description

When applied to a term of the form $\sim(?p. t)$, the conversion `NOT_PEXISTS_CONV` returns the theorem:

$$\vdash \sim(?p. t) = (!p. \sim t)$$

Failure

Fails if applied to a term not of the form $\sim(?p. t)$.

See also

Conv.NOT_EXISTS_CONV, PairRules.PEXISTS_NOT_CONV, PairRules.PFORALL_NOT_CONV, PairRules.NOT_PFORALL_CONV.

NOT_PFORALL_CONV	(PairRules)
------------------	-------------

NOT_PFORALL_CONV : conv

Synopsis

Moves negation inwards through a paired universal quantification.

Description

When applied to a term of the form $\sim(!p. t)$, the conversion NOT_PFORALL_CONV returns the theorem:

$$\vdash \sim(!p. t) = (?p. \sim t)$$

It is irrelevant whether any variables in p occur free in t .

Failure

Fails if applied to a term not of the form $\sim(!p. t)$.

See also

Conv.NOT_FORALL_CONV, PairRules.PEXISTS_NOT_CONV, PairRules.PFORALL_NOT_CONV, PairRules.NOT_PEXISTS_CONV.

notify_word_length_guesses	(wordsLib)
----------------------------	------------

notify_word_length_guesses : bool ref

Synopsis

Controls notification of word length guesses.

Description

When the reference `notify_word_length_guesses` is true a HOL message is printed (in interactive sessions) when the function `inst_word_lengths` instantiates types in a term.

Example

```

- load "wordsLib";
...
- wordsLib.notify_word_length_guesses := false;
> val it = () : unit
- wordsLib.inst_word_lengths '(7 >< 5) a @@ (4 >< 0) a'';
<<HOL message: inventing new type variable names: 'a, 'b, 'c, 'd>>
> val it = '(7 >< 5) a @@ (4 >< 0) a'' : term
- type_of it;
> val it = ':bool[8]'' : hol_type

```

Comments

By default `notify_word_length_guesses` is true.

See also

`wordsLib.guess_lengths`, `wordsLib.inst_word_lengths`.

NTAC	(Tactic)
-------------	-----------------

```
NTAC : int -> tactic -> tactic
```

Synopsis

Apply tactic a specified number of times.

Description

An invocation `NTAC n tac` applies the tactic `tac` exactly `n` times. If `n <= 0` then the goal is unchanged.

Failure

Fails if `tac` fails.

Example

Suppose we have the following goal:

```
?- x = y
```

We apply a tactic for symmetry of equality 3 times:

```
NTAC 3 (PURE_ONCE_REWRITE_TAC [EQ_SYM_EQ])
```

and obtain

```
?- y = x
```

Uses

Controlling iterated application tactics.

See also

`Rewrite.PURE_ONCE_REWRITE_TAC`, `Tactical.REPEAT`, `Conv.REPEATC`.

<div data-bbox="159 703 341 752" data-label="Text"> <p>Ntimes</p> </div>	<div data-bbox="1125 703 1331 754" data-label="Text"> <p>(Drule)</p> </div>
--	---

```
Ntimes : thm -> int -> thm
```

Synopsis

Rewriting control

Description

When used as an argument to the rewriter or simplifier, `Ntimes th n` is a directive saying that `th` should be used at most `n` times in the rewriting process. This is useful for controlling looping rewrites.

Failure

Never fails.

Example

Suppose factorial was defined as follows:

```
- val fact_def = Define 'fact n = if n=0 then 1 else n * fact (n-1)';
Equations stored under "fact_def".
Induction stored under "fact_ind".
> val fact_def = |- fact n = (if n = 0 then 1 else n * fact (n - 1)) : thm
```

The theorem `fact_def` is a looping rewrite since the recursive call `fac (n-1)` matches the left-hand side of `fact_def`. Thus, a naive application of the simplifier will loop:

```
- SIMP_CONV arith_ss [fact_def] 'fact 6';
(* looping *)
> Interrupted.
```

In order to expand the definition of `fact_def` three times, the following invocation can be made

```
- SIMP_CONV arith_ss [Ntimes Fact_def 3] ‘‘fact 6’’;
> val it = |- fact 6 = 6 * (5 * (4 * fact 3)) : thm
```

Comments

Use of `Ntimes` does not compose well. For example,

```
tac1 THENL [SIMP_TAC std_ss [Ntimes th 1],
            SIMP_TAC std_ss [Ntimes th 1]]
```

is not equivalent in behaviour to

```
tac1 THEN SIMP_TAC std_ss [Ntimes th 1].
```

In the first call two rewrites using `th` can occur; in the second, only one can occur.

See also

`Drule.Once`, `Tactical.THEN`, `simpLib.SIMP_TAC`, `bossLib.RW_TAC`, `Rewrite.REWRITE_TAC`.

<code>null_intersection</code>	<code>(Lib)</code>
--------------------------------	--------------------

```
null_intersection : 'a list -> 'a list -> bool
```

Synopsis

Tells if two lists have no common elements.

Description

An invocation `null_intersection l1 l2` is equivalent to `null(intersect l1 l2)`, but is more efficient in the case where the intersection is not empty.

Failure

Never fails.

Example

```
- null_intersection [1,2,3,4] [5,6,7,8];
> val it = true : bool

- null_intersection [1,2,3,4] [8,5,3];
> val it = false : bool
```


Comments

A high-performance implementation of finite sets may be found in structure `HOLset`.

See also

`Lib.intersect`, `Lib.union`, `Lib.U`, `Lib.mk_set`, `Lib.mem`, `Lib.insert`, `Lib.set_eq`, `Lib.set_diff`.

<div data-bbox="159 642 399 694" data-label="Text"> <p><code>num_CONV</code></p> </div>	<div data-bbox="1096 642 1331 694" data-label="Text"> <p><code>(numLib)</code></p> </div>
---	---

`num_CONV` : conv

Synopsis

Equates a non-zero numeral with the form `SUC x` for some `x`.

Example

```
- num_CONV ``1203``;
> val it = |- 1203 = SUC 1202 : thm
```

Failure

Fails if the argument term is not a numeral of type ```:num```, or if the argument is ```0```.

See also

`numLib.SUC_TO_NUMERAL_DEFN_CONV`.

<div data-bbox="159 1494 769 1545" data-label="Text"> <p><code>NUM_DEPTH_CONSEQ_CONV</code></p> </div>	<div data-bbox="983 1494 1331 1550" data-label="Text"> <p><code>(ConseqConv)</code></p> </div>
--	--

`NUM_DEPTH_CONSEQ_CONV` : `directed_conseq_conv -> int -> directed_conseq_conv`

Synopsis

Applies a consequence conversion at most a given number of times to the sub-terms of a term, in bottom-up order.

Description

While `DEPTH_CONSEQ_CONV c tm` applies `c` repeatedly, `NUM_DEPTH_CONSEQ_CONV c n tm` applies it at most `n`-times.

See also

Conv.DEPTH_CONV, ConseqConv.ONCE_DEPTH_CONSEQ_CONV,
 ConseqConv.DEPTH_CONSEQ_CONV, ConseqConv.DEPTH_STRENGTHEN_CONSEQ_CONV.

`occs_in``(pairSyntax)`

```
occs_in : (term -> term -> bool)
```

Synopsis

Occurrence check for bound variables.

Description

When applied to two terms p and t , where p is a paired structure of variables, the function `occs_in` returns `true` if and of the constituent variables of p occurs free in t , and `false` otherwise.

Failure

Fails if p is not a paired structure of variables.

See also

Term.free_in, hol88Lib.frees, hol88Lib.frees1, thm_frees.

`Once``(Drule)`

```
Once : thm -> thm
```

Synopsis

Rewriting control

Description

When used as an argument to the rewriter or simplifier, `Once th` is a directive saying that th should be used at most once in the rewriting process. This is useful for controlling looping rewrites.

Failure

Never fails.

Example

Suppose factorial was defined as follows:

```

- val fact_def = Define 'fact n = if n=0 then 1 else n * fact (n-1)';
Equations stored under "fact_def".
Induction stored under "fact_ind".
> val fact_def = |- fact n = (if n = 0 then 1 else n * fact (n - 1)) : thm

```

The theorem `fact_def` is a looping rewrite since the recursive call `fac (n-1)` matches the left-hand side of `fact_def`. Thus, a naive application of the simplifier will loop:

```

- SIMP_CONV arith_ss [fact_def] 'fact 6';
(* looping *)
> Interrupted.

```

In order to expand the definition of `fact_def`, the following invocation can be made

```

- SIMP_CONV arith_ss [Once fact_def] 'fact 6';
> val it = |- fact 6 = 6 * fact 5 : thm

```

Comments

Use of `Once` does not compose well. For example,

```

tac1 THENL [SIMP_TAC std_ss [Once th],
            SIMP_TAC std_ss [Once th]]

```

is not equivalent in behaviour to

```

tac1 THEN SIMP_TAC std_ss [Once th].

```

In the first call two rewrites using `th` can occur; in the second, only one can occur.

See also

`Drule.Ntimes`, `Tactical.THEN`, `simpLib.SIMP_TAC`, `bossLib.RW_TAC`, `Rewrite.ONCE_REWRITE_TAC`.

ONCE_ASM_REWRITE_RULE

(Rewrite)

`ONCE_ASM_REWRITE_RULE` : (thm list -> thm -> thm)

Synopsis

Rewrites a theorem once including built-in rewrites and the theorem's assumptions.

Description

ONCE_ASM_REWRITE_RULE applies all possible rewrites in one step over the subterms in the conclusion of the theorem, but stops after rewriting at most once at each subterm. This strategy is specified as for ONCE_DEPTH_CONV. For more details see ASM_REWRITE_RULE, which does search recursively (to any depth) for matching subterms. The general strategy for rewriting theorems is described under GEN_REWRITE_RULE.

Failure

Never fails.

Uses

This tactic is used when rewriting with the hypotheses of a theorem (as well as a given list of theorems and `basic_rewrites`), when more than one pass is not required or would result in divergence.

See also

Rewrite.ASM_REWRITE_RULE, Rewrite.FILTER_ASM_REWRITE_RULE,
 Rewrite.FILTER_ONCE_ASM_REWRITE_RULE, Rewrite.GEN_REWRITE_RULE,
 Conv.ONCE_DEPTH_CONV, Rewrite.ONCE_REWRITE_RULE, Rewrite.PURE_ASM_REWRITE_RULE,
 Rewrite.PURE_ONCE_ASM_REWRITE_RULE, Rewrite.PURE_REWRITE_RULE,
 Rewrite.REWRITE_RULE.

ONCE_ASM_REWRITE_TAC	(Rewrite)
----------------------	-----------

ONCE_ASM_REWRITE_TAC : (thm list -> tactic)

Synopsis

Rewrites a goal once including built-in rewrites and the goal's assumptions.

Description

ONCE_ASM_REWRITE_TAC behaves in the same way as ASM_REWRITE_TAC, but makes one pass only through the term of the goal. The order in which the given theorems are applied is an implementation matter and the user should not depend on any ordering. See GEN_REWRITE_TAC for more information on rewriting a goal in HOL.

Failure

ONCE_ASM_REWRITE_TAC does not fail and, unlike ASM_REWRITE_TAC, does not diverge. The resulting tactic may not be valid, if the rewrites performed add new assumptions to the theorem eventually proved.

Example

The use of `ONCE_ASM_REWRITE_TAC` to control the amount of rewriting performed is illustrated below:

```
- ONCE_ASM_REWRITE_TAC []
  ([Term '(a:'a) = b', Term '(b:'a) = c'], Term 'P (a:'a): bool');

> val it = (((['a = b', 'b = c'], 'P b'), fn)
  : (term list * term) list * (thm list -> thm)

- (ONCE_ASM_REWRITE_TAC [] THEN ONCE_ASM_REWRITE_TAC [])
  ([Term '(a:'a) = b', Term '(b:'a) = c'], Term 'P (a:'a): bool');

> val it = (((['a = b', 'b = c'], 'P c'), fn)
  : (term list * term) list * (thm list -> thm)
```

Uses

`ONCE_ASM_REWRITE_TAC` can be applied once or iterated as required to give the effect of `ASM_REWRITE_TAC`, either to avoid divergence or to save inference steps.

See also

`Rewrite.ASM_REWRITE_TAC`, `Rewrite.FILTER_ASM_REWRITE_TAC`,
`Rewrite.FILTER_ONCE_ASM_REWRITE_TAC`, `Rewrite.GEN_REWRITE_TAC`,
`Rewrite.ONCE_ASM_REWRITE_TAC`, `Rewrite.ONCE_REWRITE_TAC`,
`Rewrite.PURE_ASM_REWRITE_TAC`, `Rewrite.PURE_ONCE_ASM_REWRITE_TAC`,
`Rewrite.PURE_ONCE_REWRITE_TAC`, `Rewrite.PURE_REWRITE_TAC`, `Rewrite.REWRITE_TAC`,
`Tactic.SUBST_TAC`.

<div data-bbox="161 1525 798 1579" data-label="Text"> <p><code>ONCE_DEPTH_CONSEQ_CONV</code></p> </div>	<div data-bbox="984 1525 1331 1583" data-label="Text"> <p><code>(ConseqConv)</code></p> </div>
---	--

`ONCE_DEPTH_CONSEQ_CONV` : `directed_conseq_conv -> directed_conseq_conv`

Synopsis

Applies a consequence conversion at most once to a sub-terms of a term.

Description

While `DEPTH_CONSEQ_CONV c tm` applies `c` repeatedly, `ONCE_DEPTH_CONSEQ_CONV c tm` applies `c` at most once.

See also

Conv.DEPTH_CONV, ConseqConv.NUM_DEPTH_CONSEQ_CONV, ConseqConv.DEPTH_CONSEQ_CONV, ConseqConv.DEPTH_STRENGTHEN_CONSEQ_CONV.

ONCE_DEPTH_CONV

(Conv)

ONCE_DEPTH_CONV : (conv -> conv)

Synopsis

Applies a conversion once to the first suitable sub-term(s) encountered in top-down order.

Description

ONCE_DEPTH_CONV c tm applies the conversion c once to the first subterm or subterms encountered in a top-down ‘parallel’ search of the term tm for which c succeeds. If the conversion c fails on all subterms of tm , the theorem returned is $\vdash tm = tm$.

Failure

Never fails.

Example

The following example shows how ONCE_DEPTH_CONV applies a conversion to only the first suitable subterm(s) found in a top-down search:

```
- ONCE_DEPTH_CONV BETA_CONV (Term '(\x. (\y. y + x) 1) 2');
> val it = |- (\x. (\y. y + x)1)2 = (\y. y + 2) 1 : thm
```

Here, there are two beta-redexes in the input term. One of these occurs within the other, so BETA_CONV is applied only to the outermost one.

Note that the supplied conversion is applied by ONCE_DEPTH_CONV to all independent subterms at which it succeeds. That is, the conversion is applied to every suitable subterm not contained in some other subterm for which the conversions also succeeds, as illustrated by the following example:

```
- ONCE_DEPTH_CONV numLib.num_CONV (Term '(\x. (\y. y + x) 1) 2');
> val it = |- (\x. (\y. y + x)1)2 = (\x. (\y. y + x)(SUC 0))(SUC 1) : thm
```

Here num_CONV is applied to both 1 and 2, since neither term occurs within a larger subterm for which the conversion num_CONV succeeds.

Uses

ONCE_DEPTH_CONV is frequently used when there is only one subterm to which the desired conversion applies. This can be much faster than using other functions that attempt to apply a conversion to all subterms of a term (e.g. DEPTH_CONV). If, for example, the current goal in a goal-directed proof contains only one beta-redex, and one wishes to apply BETA_CONV to it, then the tactic

```
CONV_TAC (ONCE_DEPTH_CONV BETA_CONV)
```

may, depending on where the beta-redex occurs, be much faster than

```
CONV_TAC (TOP_DEPTH_CONV BETA_CONV)
```

ONCE_DEPTH_CONV *c* may also be used when the supplied conversion *c* never fails, in which case using a conversion such as DEPTH_CONV *c*, which applies *c* repeatedly would never terminate.

Comments

The implementation of this function uses failure to avoid rebuilding unchanged subterms. That is to say, during execution the exception `QConv.UNCHANGED` may be generated and later trapped. The behaviour of the function is dependent on this use of failure. So, if the conversion given as an argument happens to generate the same exception, the operation of ONCE_DEPTH_CONV will be unpredictable.

See also

`Conv.DEPTH_CONV`, `Conv.REDEPTH_CONV`, `Conv.TOP_DEPTH_CONV`.

ONCE_REWRITE_CONV	(Rewrite)
-------------------	-----------

```
ONCE_REWRITE_CONV : (thm list -> conv)
```

Synopsis

Rewrites a term, including built-in tautologies in the list of rewrites.

Description

ONCE_REWRITE_CONV searches for matching subterms and applies rewrites once at each subterm, in the manner specified for ONCE_DEPTH_CONV. The rewrites which are used are obtained from the given list of theorems and the set of tautologies stored in `basic_rewrites`. See GEN_REWRITE_CONV for the general method of using theorems to rewrite a term.

Failure

ONCE_REWRITE_CONV does not fail; it does not diverge.

Uses

ONCE_REWRITE_CONV can be used to rewrite a term when recursive rewriting is not desired.

See also

Rewrite.GEN_REWRITE_CONV, Rewrite.PURE_ONCE_REWRITE_CONV,
Rewrite.PURE_REWRITE_CONV, Rewrite.REWRITE_CONV.

ONCE_REWRITE_RULE	(Rewrite)
-------------------	-----------

ONCE_REWRITE_RULE : (thm list -> thm -> thm)

Synopsis

Rewrites a theorem, including built-in tautologies in the list of rewrites.

Description

ONCE_REWRITE_RULE searches for matching subterms and applies rewrites once at each subterm, in the manner specified for ONCE_DEPTH_CONV. The rewrites which are used are obtained from the given list of theorems and the set of tautologies stored in `basic_rewrites`. See `GEN_REWRITE_RULE` for the general method of using theorems to rewrite an object theorem.

Failure

ONCE_REWRITE_RULE does not fail; it does not diverge.

Uses

ONCE_REWRITE_RULE can be used to rewrite a theorem when recursive rewriting is not desired.

See also

Rewrite.ASM_REWRITE_RULE, Rewrite.GEN_REWRITE_RULE,
Rewrite.ONCE_ASM_REWRITE_RULE, Rewrite.PURE_ONCE_REWRITE_RULE,
Rewrite.PURE_REWRITE_RULE, Rewrite.REWRITE_RULE.

ONCE_REWRITE_TAC	(Rewrite)
------------------	-----------

ONCE_REWRITE_TAC : thm list -> tactic

Synopsis

Rewrites a goal only once with `basic_rewrites` and the supplied list of theorems.

Description

A set of equational rewrites is generated from the theorems supplied by the user and the set of basic tautologies, and these are used to rewrite the goal at all subterms at which a match is found in one pass over the term part of the goal. The result is returned without recursively applying the rewrite theorems to it. The order in which the given theorems are applied is an implementation matter and the user should not depend on any ordering. More details about rewriting can be found under `GEN_REWRITE_TAC`.

Failure

`ONCE_REWRITE_TAC` does not fail and does not diverge. It results in an invalid tactic if any of the applied rewrites introduces new assumptions to the theorem eventually proved.

Example

Given a theorem list:

```
th1 = [ |- a = b, |- b = c, |- c = a]
```

the tactic `ONCE_REWRITE_TAC th1` can be iterated as required without diverging:

```
- ONCE_REWRITE_TAC th1 ([], Term 'P (a:'a) :bool');
> val it = ([[[]], 'P b']), fn)
  : (term list * term) list * (thm list -> thm)

- (ONCE_REWRITE_TAC th1 THEN ONCE_REWRITE_TAC th1)
  ([], Term 'P a');
> val it = ([[[]], 'P c']), fn)
  : (term list * term) list * (thm list -> thm)

- (NTAC 3 (ONCE_REWRITE_TAC th1)) ([], Term 'P a');
> val it = ([[[]], 'P a']), fn)
  : (term list * term) list * (thm list -> thm)
```

Uses

`ONCE_REWRITE_TAC` can be used iteratively to rewrite when recursive rewriting would diverge. It can also be used to save inference steps.

See also

`Rewrite.ASM_REWRITE_TAC`, `Drule.Once`, `Rewrite.ONCE_ASM_REWRITE_TAC`,
`Rewrite.PURE_ASM_REWRITE_TAC`, `Rewrite.PURE_ONCE_REWRITE_TAC`,
`Rewrite.PURE_REWRITE_TAC`, `Rewrite.REWRITE_TAC`, `Tactic.SUBST_TAC`.

op_arity

(Type)

```
op_arity : {Thy:string, Tyop:string} -> int option
```

Synopsis

Return the arity of a type operator.

Description

An invocation `op_arity{Tyop,Thy}` returns `NONE` if the given record does not identify a type operator in the current type signature. Otherwise, it returns `SOME n`, where `n` identifies the number of arguments the specified type operator takes.

Failure

Never fails.

Example

```
- op_arity{Tyop="fun", Thy="min"};
> val it = SOME 2 : int option

- op_arity{Tyop="foo", Thy="min"};
> val it = NONE : int option
```

See also

`Type.decls`.

op_insert

(Lib)

```
op_insert ('a -> 'a -> bool) -> 'a -> 'a list -> 'a list
```

Synopsis

Add an element to a list if it is not already there.

Description

If there exists an element `y` in `list`, such that `eq x y`, then `insert eq x list` equals `list`. Otherwise, `x` is added to `list`.

Failure

Never fails.

Example

```
- op_insert (fn x => fn y => x = y mod 2) 1 [3,2];
> val it = [3, 2] : int list

- op_insert aconv (Term '\x. x /\ y')
                  [T, Term '\z. z /\ y', F];
> val it = ['T', '\z. z /\ y', 'F'] : term list

- op_insert aconv (Term '\x. x /\ y')
                  [T, Term '\z. z /\ a', F];
> val it = ['\x. x /\ y', 'T', '\z. z /\ a', 'F'] : term list
```

Comments

There is no requirement that eq be recognizable as a kind of equality (it could be implemented by an order relation, for example).

One should not write code that depends on the arrangement of elements in the result.

A high-performance implementation of finite sets may be found in structure HOLset.

See also

Lib.insert, Lib.op_mem, Lib.op_union, Lib.op_mk_set, Lib.op_U, Lib.op_intersect, Lib.op_set_diff.

op_intersect	(Lib)
--------------	-------

```
op_intersect : ('a -> 'a -> bool) -> 'a list -> 'a list -> 'a list
```

Synopsis

Computes the intersection of two 'sets'.

Description

op_intersect eq l1 l2 returns a list consisting of those elements of l1 that are eq to some element in l2.

Failure

Fails if an application of eq fails.

Example

```
- op_intersect aconv [Term '\x:bool.x', Term '\x y. x /\ y']
                    [Term '\y:bool.y', Term '\x y. x /\ z'];
> val it = ['\x. x'] : term list
```

Comments

The order of items in the list returned by `op_intersect` is not dependable.

A high-performance implementation of finite sets may be found in structure `HOLset`.

There is no requirement that `eq` be recognizable as a kind of equality (it could be implemented by an order relation, for example).

See also

`Lib.intersect`, `Lib.op_mem`, `Lib.op_insert`, `Lib.op_mk_set`, `Lib.op_union`, `Lib.op_U`, `Lib.op_set_diff`.

<div data-bbox="236 940 418 992" data-label="Text"> <p><code>op_mem</code></p> </div>	<div data-bbox="1260 936 1412 987" data-label="Text"> <p>(Lib)</p> </div>
---	---

```
op_mem : ('a -> 'a -> bool) -> 'a -> 'a list -> bool
```

Synopsis

Tests whether a list contains a certain element.

Description

An invocation `op_mem eq x [x1, ..., xn]` returns `true` if, for some x_i in the list, `eq x_i x` evaluates to `true`. Otherwise it returns `false`.

Failure

Only fails if an application of `eq` fails.

Example

```
- op_mem aconv (Term '\x. x /\ y') [T, Term '\z. z /\ y', F];
> val it = true : bool
```

Comments

A high-performance implementation of finite sets may be found in structure `HOLset`.

See also

`Lib.mem`, `Lib.op_insert`, `Lib.tryfind`, `Lib.exists`, `Lib.all`, `Lib.assoc`, `Lib.rev_assoc`, `Lib.assoc1`, `Lib.assoc2`, `Lib.op_union`, `Lib.op_mk_set`, `Lib.op_U`, `Lib.op_intersect`, `Lib.op_set_diff`.

op_mk_set

(Lib)

```
op_mk_set : ('a -> 'a -> bool) -> 'a list -> 'a list
```

Synopsis

Transforms a list into one with elements that are distinct modulo the supplied relation.

Description

An invocation `op_mk_set eq list` returns a list consisting of the `eq`-distinct members of `list`. In particular, the result list will not contain elements `x` and `y` at different positions such that `eq x y` evaluates to `true`.

Failure

If an application of `eq` fails when applied to two elements of `list`.

Example

```
- op_mk_set aconv [Term '\x y. x /\ y',
                  Term '\y x. y /\ x',
                  Term '\z a. z /\ a'];
> val it = ['\z a. z /\ a'] : term list
```

Comments

The order of items in the list returned by `op_mk_set` is not dependable.

A high-performance implementation of finite sets may be found in structure `HOLset`.

There is no requirement that `eq` be recognizable as a kind of equality (it could be implemented by an order relation, for example).

See also

`Lib.mk_set`, `Lib.op_mem`, `Lib.op_insert`, `Lib.op_union`, `Lib.op_U`, `Lib.op_intersect`, `Lib.op_set_diff`.

op_set_diff

(Lib)

```
op_set_diff : ('a -> 'a -> bool) -> 'a list -> 'a list -> 'a list
```

Synopsis

Computes the set-theoretic difference of two ‘sets’, modulo a supplied relation.

Description

`op_set_diff eq l1 l2` returns a list consisting of those elements of `l1` that are not `eq` to some element of `l2`.

Failure

Fails if an application of `eq` fails.

Example

```
- op_set_diff (fn x => fn y => x mod 2 = y mod 2) [1,2,3] [4,5,6];
> val it = [] : int list

- op_set_diff (fn x => fn y => x mod 2 = y mod 2) [1,2,3] [2,4,6,8];
> val it = [1, 3] : int list
```

Comments

The order in which the elements occur in the resulting list should not be depended upon.

A high-performance implementation of finite sets may be found in structure `HOLset`.

See also

`Lib.set_diff`, `Lib.op_mem`, `Lib.op_insert`, `Lib.op_union`, `Lib.op_U`, `Lib.op_mk_set`, `Lib.op_intersect`.

<div data-bbox="236 1451 362 1507" data-label="Text"><code>op_U</code></div>	<div data-bbox="1260 1449 1412 1503" data-label="Text"><code>(Lib)</code></div>
--	---

```
op_U : ('a -> 'a -> bool) -> 'a list list -> 'a list
```

Synopsis

Takes the union of a list of sets, modulo the supplied relation.

Description

An application `op_U eq [l1, ..., ln]` is equivalent to `op_union eq l1 (... (op_union eq ln-1, l1 ...)`. Thus, every element that occurs in one of the lists will appear in the result. However, if there are two elements `x` and `y` from different lists such that `eq x y`, then only one of `x` and `y` will appear in the result.

Failure

If an application of `eq` fails when applied to two elements from the lists.

Example

```
- op_U (fn x => fn y => x mod 2 = y mod 2)
      [[1,2,3], [4,5,6], [2,4,6,8,10]];
> val it = [5, 2, 4, 6, 8, 10] : int list
```

Comments

The order in which the elements occur in the resulting list should not be depended upon.

A high-performance implementation of finite sets may be found in structure `HOLset`.

There is no requirement that `eq` be recognizable as a kind of equality (it could be implemented by an order relation, for example).

See also

`Lib.U`, `Lib.op_mem`, `Lib.op_insert`, `Lib.op_union`, `Lib.op_mk_set`, `Lib.op_intersect`, `Lib.op_set_diff`.

<div data-bbox="161 1193 314 1240" data-label="Text"><code>union</code></div>	<div data-bbox="1182 1189 1331 1240" data-label="Text"><code>(Lib)</code></div>
---	---

```
union : ('a -> 'a -> bool) -> 'a list -> 'a list -> 'a list
```

Synopsis

Computes the union of two ‘sets’.

Description

If `l1` and `l2` are both ‘sets’ (lists with no repeated members), `union eq l1 l2` returns the set union of `l1` and `l2`, using `eq` as the implementation of element equality. If one or both of `l1` and `l2` have repeated elements, there may be repeated elements in the result.

Failure

If some application of `eq` fails.

Example

```
- op_union (fn x => fn y => x mod 2 = y mod 2) [1,2,3] [5,4,7];
> val it = [5, 4, 7] : int list
```

Comments

Do not make the assumption that the order of items in the list returned by `op_union` is fixed. Later implementations may use different algorithms, and return a different concrete result while still meeting the specification.

There is no requirement that `eq` be recognizable as a kind of equality (it could be implemented by an order relation, for example).

A high-performance implementation of finite sets may be found in structure `HOLset`.

See also

`Lib.union`, `Lib.op_mem`, `Lib.op_insert`, `Lib.op_mk_set`, `Lib.op_U`, `Lib.op_intersect`, `Lib.op_set_diff`.

OR_CONV	(reduceLib)
----------------	--------------------

`OR_CONV` : `conv`

Synopsis

Simplifies certain boolean disjunction expressions.

Description

If `tm` corresponds to one of the forms given below, where `t` is an arbitrary term of type `bool`, then `OR_CONV tm` returns the corresponding theorem. Note that in the last case the disjuncts need only be alpha-equivalent rather than strictly identical.

```
OR_CONV "T \\/ t" = |- T \\/ t = T
OR_CONV "t \\/ T" = |- t \\/ T = T
OR_CONV "F \\/ t" = |- F \\/ t = t
OR_CONV "t \\/ F" = |- t \\/ F = t
OR_CONV "t \\/ t" = |- t \\/ t = t
```

Failure

`OR_CONV tm` fails unless `tm` has one of the forms indicated above.

Example

```
#OR_CONV "F \\/ T";;
|- F \\/ T = T

#OR_CONV "X \\/ F";;
```



```
|- X \/\ F = X
```

```
#OR_CONV "(!n. n + 1 = SUC n) \/\ (!m. m + 1 = SUC m)";;
```

```
|- (!n. n + 1 = SUC n) \/\ (!m. m + 1 = SUC m) = (!n. n + 1 = SUC n)
```

OR_EL_CONV	(listLib)
-------------------	------------------

```
OR_EL_CONV : conv
```

Synopsis

Computes by inference the result of taking the disjunction of the elements of a boolean list.

Description

For any object language list of the form `--'[x1;x2;...;xn]'--`, where x_1, x_2, \dots, x_n are boolean expressions, the result of evaluating

```
OR_EL_CONV (--'OR_EL [x1;x2;...;xn]'--)
```

is the theorem

```
|- OR_EL [x1;x2;...;xn] = b
```

where b is either the boolean constant that denotes the disjunction of the elements of the list, or a disjunction of those x_i that are not boolean constants.

Example

```
- OR_EL_CONV (--'OR_EL [T;F;F;T]'--);
```

```
|- OR_EL [T;F;F;T] = T
```

```
- OR_EL_CONV (--'OR_EL [F;F;F]'--);
```

```
|- OR_EL [F;F;F] = F
```

```
- OR_EL_CONV (--'OR_EL [F;x;y]'--);
```

```
|- OR_EL [F; x; y] = x \/\ y
```

```
- OR_EL_CONV (--'OR_EL [x;T;y]'--);
```

```
|- OR_EL [x; T; y] = T
```

Failure

`OR_EL_CONV` tm fails if tm is not of the form described above.

<code>OR_EXISTS_CONV</code>	<code>(Conv)</code>
-----------------------------	---------------------

`OR_EXISTS_CONV` : `conv`

Synopsis

Moves an existential quantification outwards through a disjunction.

Description

When applied to a term of the form $(?x.P) \vee (?x.Q)$, the conversion `OR_EXISTS_CONV` returns the theorem:

$$\vdash (?x.P) \vee (?x.Q) = (?x. P \vee Q)$$

Failure

Fails if applied to a term not of the form $(?x.P) \vee (?x.Q)$.

See also

`Conv.EXISTS_OR_CONV`, `Conv.LEFT_OR_EXISTS_CONV`, `Conv.RIGHT_OR_EXISTS_CONV`.

<code>OR_FORALL_CONV</code>	<code>(Conv)</code>
-----------------------------	---------------------

`OR_FORALL_CONV` : `conv`

Synopsis

Moves a universal quantification outwards through a disjunction.

Description

When applied to a term of the form $(!x.P) \vee (!x.Q)$, where x is free in neither P nor Q , `OR_FORALL_CONV` returns the theorem:

$$\vdash (!x. P) \vee (!x. Q) = (!x. P \vee Q)$$

Failure

OR_FORALL_CONV fails if it is applied to a term not of the form $(!x.P) \ \vee \ (!x.Q)$, or if it is applied to a term $(!x.P) \ \vee \ (!x.Q)$ in which the variable x is free in either P or Q .

See also

Conv.FORALL_OR_CONV, Conv.LEFT_OR_FORALL_CONV, Conv.RIGHT_OR_FORALL_CONV.

OR_PEXISTS_CONV

(PairRules)

OR_PEXISTS_CONV : conv

Synopsis

Moves a paired existential quantification outwards through a disjunction.

Description

When applied to a term of the form $(?p. t) \ \vee \ (?p. u)$, the conversion OR_PEXISTS_CONV returns the theorem:

$$\vdash (?p. t) \ \vee \ (?p. u) = (?p. t \ \vee \ u)$$

Failure

Fails if applied to a term not of the form $(?p. t) \ \vee \ (?p. u)$.

See also

Conv.OR_EXISTS_CONV, PairRules.PEXISTS_OR_CONV, PairRules.LEFT_OR_PEXISTS_CONV, PairRules.RIGHT_OR_PEXISTS_CONV.

OR_PFORALL_CONV

(PairRules)

OR_PFORALL_CONV : conv

Synopsis

Moves a paired universal quantification outwards through a disjunction.

Description

When applied to a term of the form $(!p. t) \ \vee \ (!p. u)$, where no variables from p are free in either t nor u , OR_PFORALL_CONV returns the theorem:

$$\vdash (!p. t) \vee (!p. u) = (!p. t \vee u)$$

Failure

OR_PFORALL_CONV fails if it is applied to a term not of the form $(!p. t) \vee (!p. u)$, or if it is applied to a term $(!p. t) \vee (!p. u)$ in which the variables from p are free in either t or u .

See also

Conv.OR_FORALL_CONV, PairRules.PFORALL_OR_CONV, PairRules.LEFT_OR_PFORALL_CONV, PairRules.RIGHT_OR_PFORALL_CONV.

ORELSE	(Tactical)
--------	------------

```
op ORELSE : tactic * tactic -> tactic
```

Synopsis

Applies first tactic, and if it fails, applies the second instead.

Description

If $T1$ and $T2$ are tactics, $T1$ ORELSE $T2$ is a tactic which applies $T1$ to a goal, and if it fails, applies $T2$ to the goal instead.

Failure

The application of ORELSE to a pair of tactics never fails. The resulting tactic fails if both $T1$ and $T2$ fail when applied to the relevant goal.

See also

Tactical.EVERY, Tactical.FIRST, Tactical.THEN.

ORELSE_CONSEQ_CONV	(ConseqConv)
--------------------	--------------

```
ORELSE_CONSEQ_CONV : (conseq_conv -> conseq_conv -> conseq_conv)
```

Synopsis

Applies the first of two consequence conversions that succeeds.

See also

Conv.ORELSEC, ConseqConv.FIRST_CONSEQ_CONV.

<div data-bbox="161 486 454 535" data-label="Text"> <p>ORELSE_TCL</p> </div>	<div data-bbox="1038 483 1331 535" data-label="Text"> <p>(Thm_cont)</p> </div>
--	--

\$ORELSE_TCL : (thm_tactical -> thm_tactical -> thm_tactical)

Synopsis

Applies a theorem-tactical, and if it fails, tries a second.

Description

When applied to two theorem-tacticals, `tt11` and `tt12`, a theorem-tactic `ttac`, and a theorem `th`, if `tt11 ttac th` succeeds, that gives the result. If it fails, the result is `tt12 ttac th`, which may itself fail.

Failure

ORELSE_TCL fails if both the theorem-tacticals fail when applied to the given theorem-tactic and theorem.

See also

Thm_cont.EVERY_TCL, Thm_cont.FIRST_TCL, Thm_cont.THEN_TCL.

<div data-bbox="161 1348 370 1400" data-label="Text"> <p>ORELSEC</p> </div>	<div data-bbox="1155 1346 1331 1402" data-label="Text"> <p>(Conv)</p> </div>
---	--

op ORELSEC : (conv -> conv -> conv)

Synopsis

Applies the first of two conversions that succeeds.

Description

`(c1 ORELSEC c2) 't'` returns the result of applying the conversion `c1` to the term `'t'` if this succeeds. Otherwise `(c1 ORELSEC c2) 't'` returns the result of applying the conversion `c2` to the term `'t'`. If either conversion raises the UNCHANGED exception when applied, this is passed on to ORELSEC's caller.

Failure

`(c1 ORELSEC c2) 't'` fails if both `c1` and `c2` fail when applied to `'t'`.

See also

Conv.FIRST_CONV.

<div style="display: flex; justify-content: space-between;"> output_words_as (wordsLib) </div>
--

```
output_words_as : (int * num -> radix) -> unit
```

Synopsis

Controls pretty-printing of word literals.

Description

A call to `output_words_as f` makes function `f` determine the output base for word literals. The function `f` takes a word-length/word-value pair and returns the required output radix.

Example

The default setting is:

```
output_words_as
  (fn (l, v) =>
    if Arbnun.<=(Arbnun.fromHexString "10000", v) then
      StringCvt.HEX
    else
      StringCvt.DEC);
```

The `l = 0` case is used for word literals with non-numeric index types.

```
- wordsLib.output_words_as
  (fn (l,_) => if l = 0 then StringCvt.HEX else StringCvt.DEC);
- ``32w``;
<<HOL message: inventing new type variable names: 'a>>
> val it = ``0x20w`` : term
- ``32w:word5``;
> val it = ``32w`` : term
```

Comments

Printing and parsing in octal is controlled by the reference `base_tokens.allow_octal_input`. Pretty-printing for word literals can be turned off with a call to `wordsLib.output_words_as_dec`.

See also

Parse.add_user_printer, wordsLib.output_words_as_dec,
wordsLib.output_words_as_bin, wordsLib.output_words_as_oct,
wordsLib.output_words_as_hex.

output_words_as_bin

(wordsLib)

output_words_as_bin : unit -> unit

Synopsis

Makes word literals pretty-print as binary.

Description

A call to output_words_as_bin will make word literals output in binary format.

Example

```
- wordsLib.output_words_as_bin();  
- EVAL '$FCP ODD : word8';  
> val it = |- $FCP ODD = 0b10101010w : thm
```

See also

wordsLib.output_words_as, wordsLib.remove_word_printer,
wordsLib.output_words_as_dec, wordsLib.output_words_as_oct,
wordsLib.output_words_as_hex.

output_words_as_dec

(wordsLib)

output_words_as_dec : unit -> unit

Synopsis

Makes word literals pretty-print as decimal.

Description

A call to output_words_as_dec will make word literals output in decimal format.

Example

```

- ‘‘0x100000w’’;
<<HOL message: inventing new type variable names: 'a>>
> val it = ‘‘0x100000w’’ : term
- wordsLib.output_words_as_dec();
- ‘‘0x100000w’’;
<<HOL message: inventing new type variable names: 'a>>
> val it = ‘‘1048576w’’ : term

```

See also

wordsLib.output_words_as, wordsLib.remove_word_printer,
 wordsLib.output_words_as_dec, wordsLib.output_words_as_bin,
 wordsLib.output_words_as_oct.

output_words_as_hex	(wordsLib)
---------------------	------------

output_words_as_hex : unit -> unit

Synopsis

Makes word literals pretty-print as hexadecimal.

Description

A call to output_words_as_hex will make word literals output in hexadecimal format.

Example

```

- wordsLib.output_words_as_hex();
- EVAL ‘‘44w : word32 << 3’’
> val it = |- 0x2Cw << 3 = 0x160w : thm

```

See also

wordsLib.output_words_as, wordsLib.remove_word_printer,
 wordsLib.output_words_as_dec, wordsLib.output_words_as_bin,
 wordsLib.output_words_as_oct.

output_words_as_oct	(wordsLib)
---------------------	------------

output_words_as_oct : unit -> unit

Synopsis

Makes word literals pretty-print as octal.

Description

A call to `output_words_as_oct` will make word literals output in octal format.

Example

```

- '032w:word5';
> val it = '32w' : term
- wordsLib.output_words_as_oct();
- '032w:word5';
> val it = '032w' : term
- wordsLib.output_words_as_dec();
- '032w:word5';
> val it = '26w' : term

```

Comments

Printing and parsing in octal is controlled by the reference `base_tokens.allow_octal_input`. A call to `output_words_as_oct` sets this value to true.

See also

`wordsLib.output_words_as`, `wordsLib.remove_word_printer`, `wordsLib.output_words_as_dec`, `wordsLib.output_words_as_bin`, `wordsLib.output_words_as_hex`.

overload_on

(Parse)

```
Parse.overload_on : string * term -> unit
```

Synopsis

Establishes a term as one of the overloading possibilities for a string.

Description

Calling `overload_on(name, tm)` establishes `tm` as a possible resolution of the overloaded name. The call to `overload_on` also ensures that `tm` is the first in the list of possible resolutions chosen when a string might be parsed into a term in more than one way, and this is the only effect if this combination is already recorded as a possible overloading.

When printing, this call causes `tm` to be seen as the operator name. The string name may prompt further pretty-printing if it is involved in any of the relevant grammar's rules for concrete syntax.

If `tm` is an abstraction, then the parser will perform beta-reductions if the term is the function part of a redex position.

Failure

Never fails.

Example

We define the equivalent of intersection over predicates:

```
- val inter = new_definition("inter", Term`inter p q x = p x /\ q x`);
<<HOL message: inventing new type variable names: 'a.>>
> val inter = |- !p q x. inter p q x = p x /\ q x : thm
```

We overload on our new intersection constant, and can be sure that in ambiguous situations, it will be preferred:

```
- overload_on ("/\\", Term`inter`);
<<HOL message: inventing new type variable names: 'a.>>
> val it = () : unit
- Term`p /\ q`;
<<HOL message: more than one resolution of overloading was possible.>>
<<HOL message: inventing new type variable names: 'a.>>
> val it = `p /\ q` : term
- type_of it;
> val it = `:'a -> bool` : hol_type
```

Note that the original constant is considered overloaded to itself, so that our one call to `overload_on` now allows for two possibilities whenever the identifier `/\` is seen. In order to make normal conjunction the preferred choice, we can call `overload_on` with the original constant:

```
- overload_on ("/\\", Term`bool$/\`);
> val it = () : unit
- Term`p /\ q`;
<<HOL message: more than one resolution of overloading was possible.>>
> val it = `p /\ q` : term
- type_of it;
> val it = `:bool` : hol_type
```

Note that in order to specify the original conjunction constant, we used the qualified identifier syntax, with the \$. If we'd used just `/\`, the overloading would have ensured that this was parsed as `inter`. Instead of the qualified identifier syntax, we could have also constrained the type of conjunction explicitly so that the original constant would be the only possibility. Thus:

```
- overload_on ("/\\", Term '/\ :bool->bool->bool');
> val it = () : unit
```

The ability to overload to abstractions allows the use of simple symbols for “complicated” effects, without needing to actually define new constants.

```
- overload_on ("|<", Term '\x y. ~(x < y)');
> val it = () : unit
```

```
- set_fixity "|<" (Infix(NONASSOC, 450));
> val it = () : unit
```

```
- val t = Term 'p |< q';
> val t = 'p |< q' : term
```

```
- dest_neg t;
> Val it = 'p < q' : term
```

This facility is used to provide symbols for “is-not-equal” (`<>`), and “is-not-a-member” (`NOTIN`).

Comments

Overloading with abandon can lead to input that is very hard to make sense of, and so should be used with caution. There is a temporary version of this function: `temp_overload_on`.

See also

`Parse.clear_overloads_on`, `Parse.set_fixity`.

p

(proofManagerLib)

p : unit -> proof

Synopsis

Prints the top levels of the subgoal package goal stack.

Description

The function `p` is part of the subgoal package. For a description of the subgoal package, see `set_goal`.

Failure

Never fails.

Uses

Examining the proof state during an interactive proof session.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`, `proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`, `proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`, `proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

P_FUN_EQ_CONV	(PairRules)
----------------------	--------------------

`P_FUN_EQ_CONV` : (term -> conv)

Synopsis

Performs extensionality conversion for functions (function equality).

Description

The conversion `P_FUN_EQ_CONV` embodies the fact that two functions are equal precisely when they give the same results for all values to which they can be applied. For any paired variable structure "`p`" and equation "`f = g`", where `p` is of type `ty1` and `f` and `g` are functions of type `ty1->ty2`, a call to `P_FUN_EQ_CONV "p" "f = g"` returns the theorem:

$$\vdash (f = g) = (!p. f p = g p)$$

Failure

`P_FUN_EQ_CONV p tm` fails if `p` is not a paired structure of variables or if `tm` is not an equation `f = g` where `f` and `g` are functions. Furthermore, if `f` and `g` are functions of type `ty1->ty2`, then the pair `x` must have type `ty1`; otherwise the conversion fails. Finally, failure also occurs if any of the variables in `p` is free in either `f` or `g`.

See also

Conv.FUN_EQ_CONV, PairRules.PEXT.

P_PCHOOSE_TAC	(PairRules)
---------------	-------------

P_PCHOOSE_TAC : (term -> thm_tactic)

Synopsis

Assumes a theorem, with existentially quantified pair replaced by a given witness.

Description

P_PCHOOSE_TAC expects a pair q and theorem with a paired existentially quantified conclusion. When applied to a goal, it adds a new assumption obtained by introducing the pair q as a witness for the pair p whose existence is asserted in the theorem.

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \quad P_CHOOSE_TAC \text{ "q" (A1 |- ?p. u)} \\ A \text{ u } \{u[q/p]\} \text{ ?- } t \quad \quad \quad \text{("y" not free anywhere)} \end{array}$$
Failure

Fails if the theorem's conclusion is not a paired existential quantification, or if the first argument is not a paired structure of variables. Failures may arise in the tactic-generating function. An invalid tactic is produced if the introduced variable is free in u or t , or if the theorem has any hypothesis which is not alpha-convertible to an assumption of the goal.

See also

Tactic.X_CHOOSE_TAC, PairRules.PCHOOSE, PairRules.PCHOOSE_THEN, PairRules.P_PCHOOSE_THEN.

P_PCHOOSE_THEN	(PairRules)
----------------	-------------

P_PCHOOSE_THEN : (term -> thm_tactical)

Synopsis

Replaces existentially quantified pair with given witness, and passes it to a theorem-tactic.

Description

`P_PCHOOSE_THEN` expects a pair `q`, a tactic-generating function `f:thm->tactic`, and a theorem of the form $(A1 \mid - ?p. u)$ as arguments. A new theorem is created by introducing the given pair `q` as a witness for the pair `p` whose existence is asserted in the original theorem, $(u[q/p] \mid - u[q/p])$. If the tactic-generating function `f` applied to this theorem produces results as follows when applied to a goal $(A \text{ ?- } u)$:

```
A ?- t
===== f ({u[q/p]} | - u[q/p])
A ?- t1
```

then applying `(P_PCHOOSE_THEN "q" f (A1 | - ?p. u))` to the goal $(A \text{ ?- } t)$ produces the subgoal:

```
A ?- t
===== P_PCHOOSE_THEN "q" f (A1 | - ?p. u)
A ?- t1      ("q" not free anywhere)
```

Failure

Fails if the theorem's conclusion is not existentially quantified, or if the first argument is not a paired structure of variables. Failures may arise in the tactic-generating function. An invalid tactic is produced if the introduced variable is free in `u` or `t`, or if the theorem has any hypothesis which is not alpha-convertible to an assumption of the goal.

See also

`Thm.cont.X_CHOOSE_THEN`, `PairRules.P_CHOOSE`, `PairRules.P_CHOOSE_THEN`, `PairRules.P_P_CHOOSE_TAC`.

<div data-bbox="234 1529 531 1579" data-label="Text"> <p><code>P_PGEN_TAC</code></p> </div>	<div data-bbox="1086 1529 1410 1579" data-label="Text"> <p><code>(PairRules)</code></p> </div>
---	--

`P_PGEN_TAC` : (term -> tactic)

Synopsis

Specializes a goal with the given paired structure of variables.

Description

When applied to a paired structure of variables `p'`, and a goal $A \text{ ?- } !p. t$, the tactic `P_PGEN_TAC` returns the goal $A \text{ ?- } t[p'/p]$.

$$\begin{array}{l} A \text{ ?- } !p. t \\ \text{=====} \quad \text{P_PGEN_TAC "p'"} \\ A \text{ ?- } t[p'/x] \end{array}$$

Failure

Fails unless the goal's conclusion is a paired universal quantification and the term a paired structure of variables of the appropriate type. It also fails if any of the variables of the supplied structure occurs free in either the assumptions or (initial) conclusion of the goal.

See also

Tactic.X_GEN_TAC, PairRules.FILTER_PGEN_TAC, PairRules.PGEN, PairRules.PGENL, PairRules.PSPEC, PairRules.PSPECL, PairRules.PSPEC_ALL, PairRules.PSPEC_TAC.

<div data-bbox="159 940 568 992" data-label="Text"> <p>P_PSKOLEM_CONV</p> </div>	<div data-bbox="1011 940 1331 992" data-label="Text"> <p>(PairRules)</p> </div>
--	---

P_PSKOLEM_CONV : (term -> conv)

Synopsis

Introduces a user-supplied Skolem function.

Description

P_PSKOLEM_CONV takes two arguments. The first is a variable f , which must range over functions of the appropriate type, and the second is a term of the form $!p_1 \dots p_n. ?q. t$ (where p_i and q may be pairs). Given these arguments, P_PSKOLEM_CONV returns the theorem:

$$\vdash (!p_1 \dots p_n. ?q. t) = (?f. !p_1 \dots p_n. tm[f p_1 \dots p_n/q])$$

which expresses the fact that a skolem function f of the universally quantified variables $p_1 \dots p_n$ may be introduced in place of the the existentially quantified pair p .

Failure

P_PSKOLEM_CONV f tm fails if f is not a variable, or if the input term tm is not a term of the form $!p_1 \dots p_n. ?q. t$, or if the variable f is free in tm , or if the type of f does not match its intended use as an n -place curried function from the pairs $p_1 \dots p_n$ to a value having the same type as p .

See also

Conv.X_SKOLEM_CONV, PairRules.PSKOLEM_CONV.

PABS	(PairRules)
------	-------------

PABS : (term -> thm -> thm)

Synopsis

Paired abstraction of both sides of an equation.

Description

$$\frac{A \mid\text{- } t_1 = t_2}{A \mid\text{- } (\backslash p.t_1) = (\backslash p.t_2)} \quad \text{ABS "p"} \quad [\text{Where } p \text{ is not free in } A]$$

Failure

If the theorem is not an equation, or if any variable in the paired structure of variables p occurs free in the assumptions A .

EXAMPLE

```
- PABS (Term '(x:'a,y:'b)') (REFL (Term '(x:'a,y:'b)'));
> val it = |- (\(x,y). (x,y)) = (\(x,y). (x,y)) : thm
```

See also

Thm.ABS, PairRules.PABS_CONV, PairRules.PETA_CONV, PairRules.PEXT, PairRules.MK_PABS.

PABS_CONV	(PairRules)
-----------	-------------

PABS_CONV : conv -> conv

Synopsis

Applies a conversion to the body of a paired abstraction.

Description

If c is a conversion that maps a term t to the theorem $\mid\text{- } t = t'$, then the conversion $\text{PABS_CONV } c$ maps abstractions of the form $\backslash p.t$ to theorems of the form:

$$\mid\text{- } (\backslash p.t) = (\backslash p.t')$$

That is, `ABS_CONV c "\p.t` applies `p` to the body of the paired abstraction `"\p.t`.

Failure

`PABS_CONV c tm` fails if `tm` is not a paired abstraction or if `tm` has the form `"\p.t` but the conversion `c` fails when applied to the term `t`. The function returned by `ABS_CONV p` may also fail if the ML function `c:term->thm` is not, in fact, a conversion (i.e. a function that maps a term `t` to a theorem `|- t = t'`).

Example

```
- PABS_CONV SYM_CONV (Term '(x,y). (1,2) = (x,y)');
> val it = |- (\(x,y). (1,2) = (x,y)) = (\(x,y). (x,y) = (1,2)) : thm
```

See also

`Conv.ABS_CONV`, `PairRules.PSUB_CONV`.

paconv

(pairSyntax)

```
paconv : (term -> term -> bool)
```

Synopsis

Tests for alpha-equivalence of terms.

Description

When applied to a pair of terms `t1` and `t2`, `paconv` returns true if the terms are alpha-equivalent.

Failure

Never fails.

Comments

`paconv` is implemented as `curry (can (uncurry PALPHA))`.

See also

`PairRules.PALPHA`, `Term.aconv`.

pair

(Lib)

```
pair : 'a -> 'b -> 'a * 'b
```

Synopsis

Makes two values into a pair.

Description

`pair x y` returns (x, y) .

Failure

Never fails.

See also

`Lib.rpair`, `Lib.swap`, `Lib.fst`, `Lib.snd`, `Lib.pair_of_list`, `Lib.triple`,
`Lib.quadruple`, `Lib.curry`, `Lib.uncurry`.

<code>PAIR_CONV</code>	<code>(PairRules)</code>
------------------------	--------------------------

`PAIR_CONV` : $(\text{conv} \rightarrow \text{conv})$

Synopsis

Applies a conversion to all the components of a pair structure.

Description

For any conversion c , the function returned by `PAIR_CONV c` is a conversion that applies c to all the components of a pair. If the term t is not a pair, then `PAIR_CONV c t` applies c to t . If the term t is the pair (t_1, t_2) then `PAIR c t` recursively applies `PAIR_CONV c` to t_1 and t_2 .

Failure

The conversion returned by `PAIR_CONV c` will fail for the pair structure t if the conversion c would fail for any of the components of t .

See also

`Conv.RAND_CONV`, `Conv.RATOR_CONV`.

<code>pair_of_list</code>	<code>(Lib)</code>
---------------------------	--------------------

`pair_of_list` : $'a \text{ list} \rightarrow 'a * 'a$

Synopsis

Turns a two-element list into a pair.

Description

`pair_of_list [x, y]` returns (x, y) .

Failure

Fails if applied to a list that is not of length 2.

See also

`Lib.singleton_of_list`, `Lib.triple_of_list`, `Lib.quadruple_of_list`.

<p>PAIRED_BETA_CONV</p>	<p>(PairedLambda)</p>
-------------------------	-----------------------

PAIRED_BETA_CONV : conv

Synopsis

Performs generalized beta conversion for tupled beta-redexes.

Description

The conversion PAIRED_BETA_CONV implements beta-reduction for certain applications of tupled lambda abstractions called ‘tupled beta-redexes’. Tupled lambda abstractions have the form $\lambda\langle vs \rangle. tm$, where $\langle vs \rangle$ is an arbitrarily-nested tuple of variables called a ‘varstruct’. For the purposes of PAIRED_BETA_CONV, the syntax of varstructs is given by:

$$\langle vs \rangle ::= (v1, v2) \mid (\langle vs \rangle, v) \mid (v, \langle vs \rangle) \mid (\langle vs \rangle, \langle vs \rangle)$$

where v , $v1$, and $v2$ range over variables. A tupled beta-redex is an application of the form $(\lambda\langle vs \rangle. tm) t$, where the term t is a nested tuple of values having the same structure as the varstruct $\langle vs \rangle$. For example, the term:

$$(\lambda((a,b), (c,d)). a + b + c + d) ((1,2), (3,4))$$

is a tupled beta-redex, but the term:

$$(\lambda((a,b), (c,d)). a + b + c + d) ((1,2), p)$$

is not, since p is not a pair of terms.

Given a tupled beta-redex $(\lambda\langle vs \rangle. tm) t$, the conversion PAIRED_BETA_CONV performs generalized beta-reduction and returns the theorem

$$\vdash (\lambda\langle vs \rangle. tm) t = t[t1, \dots, tn/v1, \dots, vn]$$

where t_i is the subterm of the tuple t that corresponds to the variable v_i in the varstruct $\langle vs \rangle$. In the simplest case, the varstruct $\langle vs \rangle$ is flat, as in the term:

$$(\backslash(v_1, \dots, v_n).t) (t_1, \dots, t_n)$$

When applied to a term of this form, `PAIRED_BETA_CONV` returns:

$$\vdash (\backslash(v_1, \dots, v_n).t) (t_1, \dots, t_n) = t[t_1, \dots, t_n/v_1, \dots, v_n]$$

As with ordinary beta-conversion, bound variables may be renamed to prevent free variable capture. That is, the term $t[t_1, \dots, t_n/v_1, \dots, v_n]$ in this theorem is the result of substituting t_i for v_i in parallel in t , with suitable renaming of variables to prevent free variables in t_1, \dots, t_n becoming bound in the result.

Failure

`PAIRED_BETA_CONV tm` fails if t_m is not a tupled beta-redex, as described above. Note that ordinary beta-redexes are specifically excluded: `PAIRED_BETA_CONV` fails when applied to $(\backslash v.t)u$. For these beta-redexes, use `BETA_CONV`, or `GEN_BETA_CONV`.

Example

The following is a typical use of the conversion:

```
- PairedLambda.PAIRED_BETA_CONV
  (Term '(\\((a,b),(c,d)). a + b + c + d) ((1,2),(3,4))');
> val it = \\- \\((a,b),c,d). a+b+c+d ((1,2),3,4) = 1+2+3+4 : thm
```

Note that the term to which the tupled lambda abstraction is applied must have the same structure as the varstruct. For example, the following succeeds:

```
- PairedLambda.PAIRED_BETA_CONV
  (Term '(\\((a,b),p). a + b) ((1,2),(3+5,4))');
> val it = \\- \\((a,b),p). a + b((1,2),3 + 5,4) = 1 + 2 : thm
```

but the following call fails:

```
- PairedLambda.PAIRED_BETA_CONV
  (Term '(\\((a,b),(c,d)). a + b + c + d) ((1,2),p)');
! Uncaught exception:
! HOL_ERR
```

because p is not a pair.

See also

`Thm.BETA_CONV`, `Conv.BETA_RULE`, `Tactic.BETA_TAC`, `Drule.LIST_BETA_CONV`, `Drule.RIGHT_BETA`, `Drule.RIGHT_LIST_BETA`.

PAIRED_ETA_CONV (PairedLambda)

PAIRED_ETA_CONV : conv

Synopsis

Performs generalized eta conversion for tupled eta-redexes.

Description

The conversion PAIRED_ETA_CONV generalizes ETA_CONV to eta-redexes with tupled abstractions.

$$\begin{aligned} & \text{PAIRED_ETA_CONV } \lambda(v1..(..)..vn). f (v1..(..)..vn) \\ & = |- \lambda(v1..(..)..vn). f (v1..(..)..vn) = f \end{aligned}$$

Failure

Fails unless the given term is a paired eta-redex as illustrated above.

Comments

Note that this result cannot be achieved by ordinary eta-reduction because the tupled abstraction is a surface syntax for a term which does not correspond to a normal pattern for eta reduction. Taking the term apart reveals the true form of a paired eta redex:

```
- dest_comb (Term '(x:num,y:num). FST (x,y)')
> val it = ('UNCURRY', '\x y. FST (x,y)') : term * term
```

Example

The following is a typical use of the conversion:

```
val SELECT_PAIR_EQ = Q.prove
  ('@(x:'a,y:'b). (a,b) = (x,y)) = (a,b)',
  CONV_TAC (ONCE_DEPTH_CONV PairedLambda.PAIRED_ETA_CONV) THEN
  ACCEPT_TAC (SYM (MATCH_MP SELECT_AX (REFL (Term '(a:'a,b:'b)'))));
```

See also

Drule.ETA_CONV.

PALPHA (PairRules)

PALPHA : term -> term -> thm

Synopsis

Proves equality of paired alpha-equivalent terms.

Description

When applied to a pair of terms t_1 and t_1' which are alpha-equivalent, ALPHA returns the theorem $\vdash t_1 = t_1'$.

```
----- PALPHA "t1" "t1'"
  \vdash t1 = t1'
```

The difference between PALPHA and ALPHA is that PALPHA is prepared to consider pair structures of different structure to be alpha-equivalent. In its most trivial case this means that PALPHA can consider a variable and a pair to alpha-equivalent.

Failure

Fails unless the terms provided are alpha-equivalent.

Example

```
- PALPHA (Term '\(x:'a,y:'a). (x,y)') (Term '\xy:'a#'a. xy');
> val it = \vdash (\(x,y). (x,y)) = (\xy. xy) : thm
```

Comments

Alpha-converting a paired abstraction to a nonpaired abstraction can introduce instances of the terms FST and SND. A paired abstraction and a nonpaired abstraction will be considered equivalent by PALPHA if the nonpaired abstraction contains all those instances of FST and SND present in the paired abstraction, plus the minimum additional instances of FST and SND. For example:

```
- PALPHA
  (Term '\(x:'a,y:'b). (f x y (x,y)):'c')
  (Term '\xy:'a#'b. (f (FST xy) (SND xy) xy):'c');
> val it = \vdash (\(x,y). f x y (x,y)) = (\xy. f (FST xy) (SND xy) xy) : thm

- PALPHA
  (Term '\(x:'a,y:'b). (f x y (x,y)):'c')
  (Term '\xy:'a#'b. (f (FST xy) (SND xy) (FST xy, SND xy)):'c')
  handle e => Raise e;
```

```
Exception raised at ??.failwith:
PALPHA
! Uncaught exception:
! HOL_ERR
```

See also

Thm.ALPHA, Term.aconv, PairRules.PALPHA_CONV, PairRules.GEN_PALPHA_CONV.

PALPHA_CONV	(PairRules)
--------------------	--------------------

PALPHA_CONV : term -> conv

Synopsis

Renames the bound variables of a paired lambda-abstraction.

Description

If q is a variable of type ty and $\lambda p.t$ is a paired abstraction in which the bound pair p also has type ty , then `ALPHA_CONV q "\p.t"` returns the theorem:

$$\vdash (\lambda p.t) = (\lambda q'. t[q'/p])$$

where the pair $q':ty$ is a primed variant of q chosen so that none of its components are free in $\lambda p.t$. The pairs p and q need not have the same structure, but they must be of the same type.

Example

PALPHA_CONV renames the variables in a bound pair:

```
- PALPHA_CONV
  (Term '((w:'a,x:'a),(y:'a,z:'a))')
  (Term '\((a:'a,b:'a),(c:'a,d:'a)). (f a b c d):'a');
> val it = \- (\((a,b),c,d). f a b c d) = (\((w,x),y,z). f w x y z) : thm
```

The new bound pair and the old bound pair need not have the same structure.

```
- PALPHA_CONV
  (Term '((wx:'a#'a),(y:'a,z:'a))')
  (Term '\((a:'a,b:'a),(c:'a,d:'a)). (f a b c d):'a');
> val it = \- (\((a,b),c,d). f a b c d) =
  (\(wx,y,z). f (FST wx) (SND wx) y z) : thm
```

PALPHA_CONV recognises subpairs of a pair as variables and preserves structure accordingly.

```
- PALPHA_CONV
  (Term '((wx:'a#'a),(y:'a,z:'a))')
  (Term '\((a:'a,b:'a),(c:'a,d:'a)). (f (a,b) c d):'a');
> val it = \- (\((a,b),c,d). f (a,b) c d) = (\(wx,y,z). f wx y z) : thm
```

Comments

PALPHA_CONV will only ever add the terms FST and SND, i.e., it will never remove them. This means that while $\lambda(x,y). x + y$ can be converted to $\lambda xy. (FST\ xy) + (SND\ xy)$, it can not be converted back again.

Failure

PALPHA_CONV $q\ tm$ fails if q is not a variable, if tm is not an abstraction, or if q is a variable and tm is the lambda abstraction $\lambda p.t$ but the types of p and q differ.

See also

Drule.ALPHA_CONV, PairRules.PALPHA, PairRules.GEN_PALPHA_CONV.

parents

(Theory)

```
parents : string -> string list
```

Synopsis

Lists the parent theories of a named theory.

Description

If s is the name of the current theory or an ancestor of the current theory, the call `parents s` returns a list of strings that identify the parent theories of s . The shorthand `"-"` may be used to denote the name of the current theory segment.

Failure

Fails if the named theory is not an ancestor of the current theory.

Example

```
- parents "bool";
> val it = ["min"] : string list

- parents "min";
> val it = [] : string list

- current_theory();
> val it = "scratch" : string

- parents "-";
> val it = ["list", "option"] : string list
```


See also

Theory.ancestry, Theory.current_theory.

parse_from_grammars

(Parse)

```
parse_from_grammars :
  (type_grammar.grammar * term_grammar.grammar) ->
  ((hol_type frag list -> hol_type) * (term frag list -> term))
```

Synopsis

Returns parsing functions based on the supplied grammars.

Description

When given a pair consisting of a type and a term grammar, this function returns parsing functions that use those grammars to turn strings (strictly, quotations) into types and terms respectively.

Failure

Can't fail immediately. However, when the precedence matrix for the term parser is built on first application of the term parser, this may generate precedence conflict errors depending on the rules in the grammar.

Example

First the user loads `arithmeticTheory` to augment the built-in grammar with the ability to lex numerals and deal with symbols such as `+` and `-`:

```
- load "arithmeticTheory";
> val it = () : unit
- val t = Term'2 + 3';
> val t = '2 + 3' : term
```

Then the `parse_from_grammars` function is used to make the values `Type` and `Term` use the grammar present in the simpler theory of booleans. Using this function fails to parse numerals or even the `+` infix:

```
- val (Type,Term) = parse_from_grammars boolTheory.bool_grammars;
> val Type = fn : hol_type frag list -> hol_type
  val Term = fn : term frag list -> term
- Term'2 + 3';
```

```

<<HOL message: No numerals currently allowed.>>
! Uncaught exception:
! HOL_ERR <poly>
- Term'x + y';
<<HOL message: inventing new type variable names: 'a, 'b.>>
> val it = 'x $+ y' : term

```

But, as the last example above also demonstrates, the installed pretty-printer is still dependent on the global grammar, and the global value of `Term` can still be accessed through the `Parse` structure:

```

- t;
> val it = '2 + 3' : term

- Parse.Term'2 + 3';
> val it = '2 + 3' : term

```

Uses

This function is used to ensure that library code has access to a term parser that is a known quantity. In particular, it is not good form to have library code that depends on the default parsers `Term` and `Type`. When the library is loaded, which may happen at any stage, these global values may be such that the parsing causes quite unexpected results or failures.

See also

`Parse.add_rule`, `Parse.print_from_grammars`, `Parse.Term`.

<code>parse_in_context</code>	<code>(Parse)</code>
-------------------------------	----------------------

`Parse.parse_in_context` : `term list -> term quotation -> term`

Synopsis

Parses a quotation into a term, using the terms as typing context.

Description

Where the `Term` function parses a quotation in isolation of all possible contexts (except inasmuch as the global grammar provides a form of context), this function uses the additional parameter, a list of terms, to help in giving variables in the quotation types.

Thus, `Term 'x'` will either guess the type `'' : 'a''` for this quotation, or refuse to parse it at all, depending on the value of the `guessing_tyvars` flag. The `parse_in_context` function, in contrast, will attempt to find a type for `x` from the list of free variables.

If the quotation already provides enough context in itself to determine a type for a variable, then the context is not consulted, and a conflicting type there for a given variable is ignored.

Failure

Fails if the quotation doesn't make syntactic sense, or if the assignment of context types to otherwise unconstrained variables in the quotation causes overloading resolution to fail. The latter would happen if the variable `x` was given boolean type in the context, if `+` was overloaded to be over either `:num` or `:int`, and if the quotation was `x + y`.

Example

<< There should be an example here >>

Uses

Used in many of the `Q` module's variants of the standard tactics in order to have a goal provide contextual information to the parsing of arguments to tactics.

See also

`Parse.Term`.

PART_MATCH

(Drule)

`PART_MATCH : (term -> term) -> thm -> term -> thm`

Synopsis

Instantiates a theorem by matching part of it to a term.

Description

When applied to a 'selector' function of type `term -> term`, a theorem and a term:

```
PART_MATCH fn (A |- !x1...xn. t) tm
```

the function `PART_MATCH` applies `fn` to `t`' (the result of specializing universally quantified variables in the conclusion of the theorem), and attempts to match the resulting term to the argument term `tm`. If it succeeds, the appropriately instantiated version of the theorem is returned.

Failure

Fails if the selector function `fn` fails when applied to the instantiated theorem, or if the match fails with the term it has provided.

Example

Suppose that we have the following theorem:

```
th = |- !x. x==>x
```

then the following:

```
PART_MATCH (fst o dest_imp) th "T"
```

results in the theorem:

```
|- T ==> T
```

because the selector function picks the antecedent of the implication (the inbuilt specialization gets rid of the universal quantifier), and matches it to `T`.

See also

`Thm.INST_TYPE`, `Drule.INST_TY_TERM`, `Term.match_term`.

PART_PMATCH	(PairRules)
--------------------	--------------------

```
PART_PMATCH : ((term -> term) -> thm -> term -> thm)
```

Synopsis

Instantiates a theorem by matching part of it to a term.

Description

When applied to a ‘selector’ function of type `term -> term`, a theorem and a term:

```
PART_MATCH fn (A |- !p1...pn. t) tm
```

the function `PART_PMATCH` applies `fn` to `t` (the result of specializing universally quantified pairs in the conclusion of the theorem), and attempts to match the resulting term to the argument term `tm`. If it succeeds, the appropriately instantiated version of the theorem is returned.

Failure

Fails if the selector function `fn` fails when applied to the instantiated theorem, or if the match fails with the term it has provided.

See also

Drule.PART_MATCH.

partial**(Lib)**

```
partial : exn -> ('a -> 'b option) -> 'a -> 'b
```

Synopsis

Converts a total function to a partial function.

Description

In ML, there are two main ways for a function to signal that it has been called on an element outside of its intended domain of application: exceptions and options. The function `partial` maps a function returning an element in an option type to one that may raise an exception. Thus, if `f x` returns `NONE`, then `partial e f x` results in the exception `e` being raised. If `f x` returns `SOME y`, then `partial e f x` returns `y`.

The function `partial` has an inverse `total`. Generally speaking, `(partial err o total) f` equals `f`, provided that `err` is the only exception that `f` raises. Similarly, `(total o partial err) f` is equal to `f`.

Failure

When application of the second argument to the third argument returns `NONE`.

Example

```
- Int.fromString "foo";
> val it = NONE : int option

- partial (Fail "not convertible") Int.fromString "foo";
! Uncaught exception:
! Fail "not convertible"

- (total o partial (Fail "not convertible")) Int.fromString "foo";
> val it = NONE : int option
```

See also

Lib.total.

<code>partition</code>	<code>(Lib)</code>
------------------------	--------------------

```
partition : ('a -> bool) -> 'a list -> 'a list * 'a list
```

Synopsis

Split a list by a predicate

Description

An invocation `partition P l` divides `l` into a pair of lists `(l1,l2)`. `P` holds of each element of `l1`, and `P` does not hold of any element of `l2`.

Failure

If applying `P` to any element of `l` results in failure.

Example

```
- partition (fn i => i mod 2 = 0) [1,2,3,4,5,6,7,8,9];
> val it = ([2, 4, 6, 8], [1, 3, 5, 7, 9]) : int list * int list

- partition (fn _ => true) [1,2,3];
> val it = ([1, 2, 3], []) : int list * int list

- partition (fn _ => raise Fail "") ([]:int list);
> val it = ([], []) : int list * int list

- partition (fn _ => raise Fail "") [1];
! Uncaught exception:
! Fail ""
```

See also

`Lib.split_after`, `Lib.pluck`.

<code>PAT_ASSUM</code>	<code>(Tactical)</code>
------------------------	-------------------------

```
PAT_ASSUM : term -> thm_tactic -> tactic
```

Synopsis

Finds the first assumption that matches the term argument, applies the theorem tactic to it, and removes this assumption.

Description

The tactic

```
PAT_ASSUM tm ttac ([A1, ..., An], g)
```

finds the first A_i which matches tm using higher-order pattern matching in the sense of `ho_match_term`. Unless there is just one match otherwise, free variables in the pattern that are also free in the assumptions or the goal must not be bound by the match. In effect, these variables are being treated as local constants.

Failure

Fails if the term doesn't match any of the assumptions, or if the theorem-tactic fails when applied to the first assumption that does match the term.

Example

The tactic

```
PAT_ASSUM (Term 'x:num = y') SUBST_ALL_TAC
```

searches the assumptions for an equality over numbers and causes its right hand side to be substituted for its left hand side throughout the goal and assumptions. It also removes the equality from the assumption list. Trying to use `FIRST_ASSUM` above (i.e., replacing `PAT_ASSUM` with `FIRST_ASSUM` and dropping the term argument entirely) would require that the desired equality was the first such on the list of assumptions, and would leave an equality on the assumption list of the form $x = x$.

If one is trying to solve the goal

```
{ !x. f x = g (x + 1), !x. g x = f0 (f x) } ?- f x = g y
```

rewriting with the assumptions directly will cause a loop. Instead, one might want to rewrite with the formula for f . This can be done in an assumption-order-independent way with

```
PAT_ASSUM (Term '!x. f x = f' x') (fn th => REWRITE_TAC [th])
```

This use of the tactic exploits higher order matching to match the RHS of the assumption, and the fact that f is effectively a local constant in the goal to find the correct assumption.

See also

`Tactical.ASSUM_LIST`, `Tactical.EVERY`, `Tactical.EVERY_ASSUM`, `Tactical.FIRST`, `Tactical.MAP EVERY`, `Tactical.MAP_FIRST`, `Thm.cont.UNDISCH.THEN`, `Term.match_term`.

PBETA_CONV

(PairRules)

PBETA_CONV : conv

Synopsis

Performs a general beta-conversion.

DescriptionThe conversion PBETA_CONV maps a paired beta-redex " $(\lambda p.t)_q$ " to the theorem

$$\vdash (\lambda p.t)_q = t[q/p]$$

where $u[q/p]$ denotes the result of substituting q for all free occurrences of p in t , after renaming sufficient bound variables to avoid variable capture. Unlike PAIRED_BETA_CONV, PBETA_CONV does not require that the structure of the argument match the structure of the pair bound by the abstraction. However, if the structure of the argument does match the structure of the pair bound by the abstraction, then PAIRED_BETA_CONV will do the job much faster.

FailurePBETA_CONV tm fails if tm is not a paired beta-redex.**Example**

PBETA_CONV will reduce applications with arbitrary structure.

```
- PBETA_CONV
  (Term '(\\((a:'a,b:'a),(c:'a,d:'a)). f a b c d) ((w,x),(y,z)):'a');
> val it = \\((a,b),c,d). f a b c d) ((w,x),y,z) = f w x y z : thm
```

PBETA_CONV does not require the structure of the argument and the bound pair to match.

```
- PBETA_CONV
  (Term '(\\((a:'a,b:'a),(c:'a,d:'a)). f a b c d) ((w,x),yz)):'a');
> val it = \\((a,b),c,d). f a b c d) ((w,x),yz) =
  f w x (FST yz) (SND yz) : thm
```

PBETA_CONV regards component pairs of the bound pair as variables in their own right and preserves structure accordingly:

```
- PBETA_CONV
  (Term '(\\((a:'a,b:'a),(c:'a,d:'a)). f (a,b) (c,d)) (wx,(y,z)):'a');
> val it = \\((a,b),c,d). f (a,b) (c,d)) (wx,y,z) = f wx (y,z) : thm
```


See also

Thm.BETA_CONV, PairedLambda.PAIRED_BETA_CONV, PairRules.PBETA_RULE,
 PairRules.PBETA_TAC, PairRules.LIST_PBETA_CONV, PairRules.RIGHT_PBETA,
 PairRules.RIGHT_LIST_PBETA, PairRules.LEFT_PBETA, PairRules.LEFT_LIST_PBETA.

PBETA_RULE

(PairRules)

PBETA_RULE : (thm -> thm)

Synopsis

Beta-reduces all the paired beta-redexes in the conclusion of a theorem.

Description

When applied to a theorem $A \vdash \tau$, the inference rule PBETA_RULE beta-reduces all beta-redexes, at any depth, in the conclusion τ . Variables are renamed where necessary to avoid free variable capture.

$$\frac{A \vdash \dots((\lambda p. s1) s2)\dots}{A \vdash \dots(s1[s2/p])\dots} \text{ BETA_RULE}$$

Failure

Never fails, but will have no effect if there are no paired beta-redexes.

See also

Conv.BETA_RULE, PairRules.PBETA_CONV, PairRules.PBETA_TAC,
 PairRules.RIGHT_PBETA, PairRules.LEFT_PBETA.

PBETA_TAC

(PairRules)

PBETA_TAC : tactic

Synopsis

Beta-reduces all the paired beta-redexes in the conclusion of a goal.

Description

When applied to a goal $A \text{ ?- } \tau$, the tactic PBETA_TAC produces a new goal which results from beta-reducing all paired beta-redexes, at any depth, in τ . Variables are renamed where necessary to avoid free variable capture.

$$\frac{A \text{ ?- } \dots((\backslash p. s1) s2)\dots}{\text{PBETA_TAC}} A \text{ ?- } \dots(s1[s2/p])\dots$$
Failure

Never fails, but will have no effect if there are no paired beta-redexes.

See also

Tactic.BETA_TAC, PairRules.PBETA_CONV, PairRules.PBETA_RULE.

pbody

(pairSyntax)

pbody : (term -> term)

Synopsis

Returns the body of a paired abstraction.

Description

pbody "\pair. t" returns "t".

Failure

Fails unless the term is a paired abstraction.

See also

Term.body, pairSyntax.dest_pabs.

PCHOOSE

(PairRules)

PCHOOSE : term * thm -> thm -> thm

Synopsis

Eliminates paired existential quantification using deduction from a particular witness.

Description

When applied to a term-theorem pair $(q, A1 \text{ |- } ?p. s)$ and a second theorem of the form $A2 \text{ u } \{s[q/p]\} \text{ |- } t$, the inference rule PCHOOSE produces the theorem $A1 \text{ u } A2 \text{ |- } t$.

$$\frac{A1 \mid - ?p. s \quad A2 \text{ u } \{s[q/p]\} \mid - t}{A1 \text{ u } A2 \mid - t} \quad \text{PCHOOSE ("q", (A1 \mid - ?q. s))}$$

Where no variable in the paired variable structure q is free in $A1$, $A2$ or t .

Failure

Fails unless the terms and theorems correspond as indicated above; in particular q must have the same type as the pair existentially quantified over, and must not contain any variable free in $A1$, $A2$ or t .

See also

Thm.CHOOSE, PairRules.PCHOOSE_TAC, PairRules.PEXISTS, PairRules.PEXISTS_TAC, PairRules.PSELECT_ELIM.

PCHOOSE_TAC

(PairRules)

PCHOOSE_TAC : thm_tactic

Synopsis

Adds the body of a paired existentially quantified theorem to the assumptions of a goal.

Description

When applied to a theorem $A' \mid - ?p. t$ and a goal, `CHOOSE_TAC` adds $t[p'/p]$ to the assumptions of the goal, where p' is a variant of the pair p which has no components free in the assumption list; normally p' is just p .

$$\frac{A \text{ ?- } u}{A \text{ u } \{t[p'/p]\} \text{ ?- } u} \quad \text{CHOOSE_TAC (A' \mid - ?q. t)}$$

Unless A' is a subset of A , this is not a valid tactic.

Failure

Fails unless the given theorem is a paired existential quantification.

See also

Tactic.CHOOSE_TAC, PairRules.PCHOOSE_THEN, PairRules.P_PCHOOSE_TAC.

PCHOOSE_THEN

(PairRules)

PCHOOSE_THEN : thm_tactical

Synopsis

Applies a tactic generated from the body of paired existentially quantified theorem.

Description

When applied to a theorem-tactic `ttac`, a paired existentially quantified theorem:

$$A' \mid- ?p. t$$

and a goal, `CHOOSE_THEN` applies the tactic `ttac (t[p'/p] \mid- t[p'/p])` to the goal, where `p'` is a variant of the pair `p` chosen to have no components free in the assumption list of the goal. Thus if:

$$\begin{array}{l} A \text{ ?- } s1 \\ \text{=====} \quad \text{ttac (t[q'/q] \mid- t[q'/q])} \\ B \text{ ?- } s2 \end{array}$$

then

$$\begin{array}{l} A \text{ ?- } s1 \\ \text{=====} \quad \text{CHOOSE_THEN ttac (A' \mid- ?q. t)} \\ B \text{ ?- } s2 \end{array}$$

This is invalid unless `A'` is a subset of `A`.

Failure

Fails unless the given theorem is a paired existential quantification, or if the resulting tactic fails when applied to the goal.

See also

`Thm_cont.CHOOSE_THEN`, `PairRules.PCHOOSE_TAC`, `PairRules.P_PCHOOSE_THEN`.

PETA_CONV

(PairRules)

PETA_CONV : conv

Synopsis

Performs a top-level paired eta-conversion.

Description

PETA_CONV maps an eta-redex $\lambda p. \tau p$, where none of variables in the paired structure of variables p occurs free in τ , to the theorem $\vdash (\lambda p. \tau p) = \tau$.

Failure

Fails if the input term is not a paired eta-redex.

PEXISTENCE

(PairRules)

PEXISTENCE : (thm -> thm)

Synopsis

Deduces paired existence from paired unique existence.

Description

When applied to a theorem with a paired unique-existentially quantified conclusion, EXISTENCE returns the same theorem with normal paired existential quantification over the same pair.

$$\begin{array}{l} A \vdash \exists! p. \tau \\ \text{-----} \quad \text{PEXISTENCE} \\ A \vdash \exists p. \tau \end{array}$$
Failure

Fails unless the conclusion of the theorem is a paired unique-existential quantification.

See also

Conv.EXISTENCE, PairRules.PEXISTS_UNIQUE_CONV.

PEXISTS

(PairRules)

PEXISTS : term * term -> thm -> thm)

Synopsis

Introduces paired existential quantification given a particular witness.

Description

When applied to a pair of terms and a theorem, where the first term a paired existentially quantified pattern indicating the desired form of the result, and the second a witness whose substitution for the quantified pair gives a term which is the same as the conclusion of the theorem, PEXISTS gives the desired theorem.

$$\begin{array}{l} A \mid\!-\ t[q/p] \\ \hline \text{PEXISTS ("?p. t", "q")} \\ A \mid\!-\ ?p. t \end{array}$$

Failure

Fails unless the substituted pattern is the same as the conclusion of the theorem.

Example

The following examples illustrate the various uses of PEXISTS:

```
- PEXISTS (Term'?x. x + 2 = x + 2', Term'1') (REFL (Term'1 + 2'));
> val it = | - ?x. x + 2 = x + 2 : thm

- PEXISTS (Term'?y. 1 + y = 1 + y', Term'2') (REFL (Term'1 + 2'));
> val it = | - ?y. 1 + y = 1 + y : thm

- PEXISTS (Term'?(x,y). x + y = x + y', Term'(1,2)') (REFL (Term'1 + 2'));
> val it = | - ?(x,y). x + y = x + y : thm

- PEXISTS (Term'?(a:'a,b:'a). (a,b) = (a,b)', Term'ab:'a#'a')
          (REFL (Term 'ab:'a#'a'));
> val it = | - ?(a,b). (a,b) = (a,b) : thm
```

See also

Thm.EXISTS, PairRules.PCHOOSE, PairRules.PEXISTS_TAC.

PEXISTS_AND_CONV

(PairRules)

PEXISTS_AND_CONV : conv

Synopsis

Moves a paired existential quantification inwards through a conjunction.

Description

When applied to a term of the form $?p. t \wedge u$, where variables in p are not free in both t and u , `PEXISTS_AND_CONV` returns a theorem of one of three forms, depending on occurrences of variables from p in t and u . If p contains variables free in t but none in u , then the theorem:

$$\vdash (?p. t \wedge u) = (?p. t) \wedge u$$

is returned. If p contains variables free in u but none in t , then the result is:

$$\vdash (?p. t \wedge u) = t \wedge (?x. u)$$

And if p does not contain any variable free in either t nor u , then the result is:

$$\vdash (?p. t \wedge u) = (?x. t) \wedge (?x. u)$$

Failure

`PEXISTS_AND_CONV` fails if it is applied to a term not of the form $?p. t \wedge u$, or if it is applied to a term $?p. t \wedge u$ in which variables in p are free in both t and u .

See also

`Conv.EXISTS_AND_CONV`, `PairRules.AND_PEXISTS_CONV`,
`PairRules.LEFT_AND_PEXISTS_CONV`, `PairRules.RIGHT_AND_PEXISTS_CONV`.

<div data-bbox="161 1426 512 1476" data-label="Text"> <p><code>PEXISTS_CONV</code></p> </div>	<div data-bbox="1011 1426 1331 1476" data-label="Text"> <p><code>(PairRules)</code></p> </div>
---	--

`PEXISTS_CONV` : `conv`

Synopsis

Eliminates paired existential quantifier by introducing a paired choice-term.

Description

The conversion `PEXISTS_CONV` expects a boolean term of the form $(?p. t[p])$, where p may be a paired structure or variables, and converts it to the form $(t [@p. t[p]])$.

$$\text{----- PEXISTS_CONV "(?p. t[p])"} \\ (\vdash (?p. t[p]) = (t [@p. t[p]]))$$

Failure

Fails if applied to a term that is not a paired existential quantification.

See also

PairRules.PSELECT_RULE, PairRules.PSELECT_CONV, PairRules.PEXISTS_RULE,
PairRules.PSELECT_INTRO, PairRules.PSELECT_ELIM.

PEXISTS_EQ	(PairRules)
------------	-------------

PEXISTS_EQ : (term -> thm -> thm)

Synopsis

Existentially quantifies both sides of an equational theorem.

Description

When applied to a paired structure of variables p and a theorem whose conclusion is equational:

$$A \vdash t_1 = t_2$$

the inference rule PEXISTS_EQ returns the theorem:

$$A \vdash (?p. t_1) = (?p. t_2)$$

provided the none of the variables in p is not free in any of the assumptions.

$$\frac{A \vdash t_1 = t_2}{A \vdash (?p. t_1) = (?p. t_2)} \quad \text{PEXISTS_EQ "p"} \quad [\text{where } p \text{ is not free in } A]$$

Failure

Fails unless the theorem is equational with both sides having type `bool`, or if the term is not a paired structure of variables, or if any variable in the pair to be quantified over is free in any of the assumptions.

See also

Drule.EXISTS_EQ, PairRules.PEXISTS_IMP, PairRules.PFORALL_EQ,
PairRules.MK_PEXISTS, PairRules.PSELECT_EQ.

PEXISTS_IMP

(PairRules)

PEXISTS_IMP : (term -> thm -> thm)

Synopsis

Existentially quantifies both the antecedent and consequent of an implication.

Description

When applied to a paired structure of variables p and a theorem $A \vdash t1 \implies t2$, the inference rule PEXISTS_IMP returns the theorem $A \vdash (?p. t1) \implies (?p. t2)$, provided no variable in p is free in the assumptions.

$$\frac{A \vdash t1 \implies t2}{A \vdash (?x. t1) \implies (?x. t2)} \text{ EXISTS_IMP "x" } \quad [\text{where } x \text{ is not free in } A]$$
Failure

Fails if the theorem is not implicative, or if the term is not a paired structure of variables, or if any variable in the pair is free in the assumption list.

See also

Drule.EXISTS_IMP, PairRules.PEXISTS_EQ.

PEXISTS_IMP_CONV

(PairRules)

PEXISTS_IMP_CONV : conv

Synopsis

Moves a paired existential quantification inwards through an implication.

Description

When applied to a term of the form $?p. t \implies u$, where variables from p are not free in both t and u , PEXISTS_IMP_CONV returns a theorem of one of three forms, depending on occurrences of variable from p in t and u . If variables from p are free in t but none are in u , then the theorem:

$$\vdash (?p. t \implies u) = (!p. t) \implies u$$

is returned. If variables from p are free in u but none are in t , then the result is:

$$\vdash (\lambda p. t \implies u) = t \implies (\lambda p. u)$$

And if no variable from p is free in either t nor u , then the result is:

$$\vdash (\lambda p. t \implies u) = (\lambda p. t) \implies (\lambda p. u)$$

Failure

PEXISTS_IMP_CONV fails if it is applied to a term not of the form $\lambda p. t \implies u$, or if it is applied to a term $\lambda p. t \implies u$ in which the variables from p are free in both t and u .

See also

Conv.EXISTS_IMP_CONV, PairRules.LEFT_IMP_PFORALL_CONV,
PairRules.RIGHT_IMP_PEXISTS_CONV.

PEXISTS_NOT_CONV	(PairRules)
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PEXISTS_NOT_CONV : conv

Synopsis

Moves a paired existential quantification inwards through a negation.

Description

When applied to a term of the form $\lambda p. \sim t$, the conversion PEXISTS_NOT_CONV returns the theorem:

$$\vdash (\lambda p. \sim t) = \sim(\lambda p. t)$$

Failure

Fails if applied to a term not of the form $\lambda p. \sim t$.

See also

Conv.EXISTS_NOT_CONV, PairRules.PFORALL_NOT_CONV, PairRules.NOT_PEXISTS_CONV,
PairRules.NOT_PFORALL_CONV.

PEXISTS_OR_CONV	(PairRules)
-----------------	-------------

PEXISTS_OR_CONV : conv

Synopsis

Moves a paired existential quantification inwards through a disjunction.

Description

When applied to a term of the form $?p. t \vee u$, the conversion `PEXISTS_OR_CONV` returns the theorem:

$$\vdash (?p. t \vee u) = (?p. t) \vee (?p. u)$$

Failure

Fails if applied to a term not of the form $?p. t \vee u$.

See also

`Conv.EXISTS_OR_CONV`, `PairRules.OR_PEXISTS_CONV`, `PairRules.LEFT_OR_PEXISTS_CONV`, `PairRules.RIGHT_OR_PEXISTS_CONV`.

<div data-bbox="159 1034 513 1086" data-label="Text"> <p>PEXISTS_RULE</p> </div>	<div data-bbox="1011 1034 1332 1086" data-label="Text"> <p>(PairRules)</p> </div>
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`PEXISTS_RULE` : (thm -> thm)

Synopsis

Introduces a paired existential quantification in place of a paired choice.

Description

The inference rule `PEXISTS_RULE` expects a theorem asserting that $(@p. t)$ denotes a pair for which t holds. The equivalent assertion that there exists a p for which t holds is returned.

$$\frac{A \vdash t[(@p. t)/p]}{A \vdash ?p. t} \text{ PEXISTS_RULE}$$

Failure

Fails if applied to a theorem the conclusion of which is not of the form $(t[(@p. t)/p])$.

See also

`PairRules.PEXISTS_CONV`, `PairRules.PSELECT_RULE`, `PairRules.PSELECT_CONV`, `PairRules.PSELECT_INTRO`, `PairRules.PSELECT_ELIM`.

PEXISTS_TAC	(PairRules)
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PEXISTS_TAC : (term -> tactic)

Synopsis

Reduces paired existentially quantified goal to one involving a specific witness.

Description

When applied to a term q and a goal $?p. t$, the tactic PEXISTS_TAC reduces the goal to $t[q/p]$.

$$\begin{array}{l} A \text{ ?- } ?p. t \\ \text{=====} \quad \text{PEXISTS_TAC "q"} \\ A \text{ ?- } t[q/p] \end{array}$$

Failure

Fails unless the goal's conclusion is a paired existential quantification and the term supplied has the same type as the quantified pair in the goal.

Example

The goal:

$$\text{?- } ?(x,y). (x,y)=(1,2)$$

can be solved by:

$$\text{PEXISTS_TAC "(1,2)" THEN REFL_TAC}$$

See also

Tactic.EXISTS_TAC, PairRules.PEXISTS.

PEXISTS_UNIQUE_CONV	(PairRules)
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PEXISTS_UNIQUE_CONV : conv

Synopsis

Expands with the definition of paired unique existence.

Description

Given a term of the form " $\exists! p. t[p]$ ", the conversion `PEXISTS_UNIQUE_CONV` proves that this assertion is equivalent to the conjunction of two statements, namely that there exists at least one pair p such that $t[p]$, and that there is at most one value p for which $t[p]$ holds. The theorem returned is:

$$\vdash (\exists! p. t[p]) = (\exists p. t[p]) \wedge (\forall p p'. t[p] \wedge t[p'] \implies (p = p'))$$

where p' is a primed variant of the pair p none of the components of which appear free in the input term. Note that the quantified pair p need not in fact appear free in the body of the input term. For example, `PEXISTS_UNIQUE_CONV "!(x,y). T"` returns the theorem:

$$\vdash (\exists!(x,y). T) = (\exists(x,y). T) \wedge (\forall(x,y) (x',y'). T \wedge T \implies ((x,y) = (x',y')))$$

Failure

`PEXISTS_UNIQUE_CONV tm` fails if tm does not have the form " $\exists! p.t$ ".

See also

`Conv.EXISTS_UNIQUE_CONV`, `PairRules.PEXISTENCE`.

PEXT	(PairRules)
------	-------------

`PEXT : (thm -> thm)`

Synopsis

Derives equality of functions from extensional equivalence.

Description

When applied to a theorem $A \vdash \exists! p. t1\ p = t2\ p$, the inference rule `PEXT` returns the theorem $A \vdash t1 = t2$.

$$\frac{A \vdash \exists! p. t1\ p = t2\ p}{A \vdash t1 = t2} \text{ PEXT} \quad [\text{where } p \text{ is not free in } t1 \text{ or } t2]$$

Failure

Fails if the theorem does not have the form indicated above, or if any of the component variables in the paired variable structure p is free either of the functions $t1$ or $t2$.

Example

```
- PEXT (ASSUME (Term '(x,y). ((f:('a#'a)->'a) (x,y)) = (g (x,y))'));
> val it = [...] |- f = g : thm
```

See also

Drule.EXT, Thm.AP_THM, PairRules.PETA_CONV, Conv.FUN_EQ_CONV,
PairRules.P_FUN_EQ_CONV.

PFORALL_AND_CONV

(PairRules)

PFORALL_AND_CONV : conv

Synopsis

Moves a paired universal quantification inwards through a conjunction.

Description

When applied to a term of the form $!p. t \wedge u$, the conversion PFORALL_AND_CONV returns the theorem:

$$|- (!p. t \wedge u) = (!p. t) \wedge (!p. u)$$

Failure

Fails if applied to a term not of the form $!p. t \wedge u$.

See also

Conv.FORALL_AND_CONV, PairRules.AND_PFORALL_CONV,
PairRules.LEFT_AND_PFORALL_CONV, PairRules.RIGHT_AND_PFORALL_CONV.

PFORALL_EQ

(PairRules)

PFORALL_EQ : (term -> thm -> thm)

Synopsis

Universally quantifies both sides of an equational theorem.

Description

When applied to a paired structure of variables p and a theorem

$$A \vdash t1 = t2$$

whose conclusion is an equation between boolean terms:

$$\text{Pforall_EQ}$$

returns the theorem:

$$A \vdash (!p. t1) = (!p. t2)$$

unless any of the variables in p is free in any of the assumptions.

$$\frac{A \vdash t1 = t2}{A \vdash (!p. t1) = (!p. t2)} \quad \text{Pforall_EQ "p"} \quad [\text{where } p \text{ is not free in } A]$$

Failure

Fails if the theorem is not an equation between boolean terms, or if the supplied term is not a paired structure of variables, or if any of the variables in the supplied pair is free in any of the assumptions.

See also

`Drule.FORALL_EQ`, `PairRules.PEXISTS_EQ`, `PairRules.PSELECT_EQ`.

Pforall_imp_conv

(PairRules)

Pforall_imp_conv : conv

Synopsis

Moves a paired universal quantification inwards through an implication.

Description

When applied to a term of the form $!p. t ==> u$, where variables from p are not free in both t and u , `Pforall_imp_conv` returns a theorem of one of three forms, depending on occurrences of the variables from p in t and u . If variables from p are free in t but none are in u , then the theorem:

$$\vdash (!p. t ==> u) = (?p. t) ==> u$$

is returned. If variables from p are free in u but none are in t , then the result is:

$$\vdash (!p. t ==> u) = t ==> (!p. u)$$

And if no variable from p is free in either t nor u , then the result is:

$$\vdash (!p. t ==> u) = (?p. t) ==> (!p. u)$$

Failure

`PFORALL_IMP_CONV` fails if it is applied to a term not of the form $!p. t ==> u$, or if it is applied to a term $!p. t ==> u$ in which variables from p are free in both t and u .

See also

`Conv.FORALL_IMP_CONV`, `PairRules.LEFT_IMP_PEXISTS_CONV`,
`PairRules.RIGHT_IMP_PFORALL_CONV`.

<code>PFORALL_NOT_CONV</code>

<code>(PairRules)</code>

`PFORALL_NOT_CONV` : `conv`

Synopsis

Moves a paired universal quantification inwards through a negation.

Description

When applied to a term of the form $!p. \sim t$, the conversion `PFORALL_NOT_CONV` returns the theorem:

$$\vdash (!p. \sim t) = \sim(?p. t)$$

Failure

Fails if applied to a term not of the form $!p. \sim t$.

See also

`Conv.FORALL_NOT_CONV`, `PairRules.PEXISTS_NOT_CONV`, `PairRules.NOT_PEXISTS_CONV`,
`PairRules.NOT_PFORALL_CONV`.

<code>PFORALL_OR_CONV</code>

<code>(PairRules)</code>

`PFORALL_OR_CONV` : `conv`

Synopsis

Moves a paired universal quantification inwards through a disjunction.

Description

When applied to a term of the form $!p. t \ \vee \ u$, where no variable in p is free in both t and u , PFORALL_OR_CONV returns a theorem of one of three forms, depending on occurrences of the variables from p in t and u . If variables from p are free in t but not in u , then the theorem:

$$\vdash (!p. t \ \vee \ u) = (!p. t) \ \vee \ u$$

is returned. If variables from p are free in u but none are free in t , then the result is:

$$\vdash (!p. t \ \vee \ u) = t \ \vee \ (!t. u)$$

And if no variable from p is free in either t nor u , then the result is:

$$\vdash (!p. t \ \vee \ u) = (!p. t) \ \vee \ (!p. u)$$

Failure

PFORALL_OR_CONV fails if it is applied to a term not of the form $!p. t \ \vee \ u$, or if it is applied to a term $!p. t \ \vee \ u$ in which variables from p are free in both t and u .

See also

Conv.FORALL_OR_CONV, PairRules.OR_PFORALL_CONV, PairRules.LEFT_OR_PFORALL_CONV, PairRules.RIGHT_OR_PFORALL_CONV.

PGEN	(PairRules)
------	-------------

PGEN : (term -> thm -> thm)

Synopsis

Generalizes the conclusion of a theorem.

Description

When applied to a paired structure of variables p and a theorem $A \ \vdash \ t$, the inference rule PGEN returns the theorem $A \ \vdash \ !p. t$, provided that no variable in p occurs free in the assumptions A . There is no compulsion that the variables of p should be free in t .

$$\frac{A \ \vdash \ t}{A \ \vdash \ !p. t} \quad \text{PGEN "p"} \quad \text{[where } p \text{ does not occur free in } A\text{]}$$

Failure

Fails if p is not a paired structure of variables, or if any variable in p is free in the assumptions.

See also

Thm.GEN, PairRules.PGENL, PairRules.PGEN_TAC, PairRules.PSPEC, PairRules.PSPECL, PairRules.PSPEC_ALL, PairRules.PSPEC_TAC.

<div data-bbox="234 694 474 745" data-label="Text"> <p>PGEN_TAC</p> </div>	<div data-bbox="1086 694 1412 745" data-label="Text"> <p>(PairRules)</p> </div>
--	---

PGEN_TAC : tactic

Synopsis

Strips the outermost paired universal quantifier from the conclusion of a goal.

Description

When applied to a goal $A \text{ ?- } !p. t$, the tactic PGEN_TAC reduces it to $A \text{ ?- } t[p'/p]$ where p' is a variant of the paired variable structure p chosen to avoid clashing with any variables free in the goal's assumption list. Normally p' is just p .

$$\begin{array}{l} A \text{ ?- } !p. t \\ \text{===== PGEN_TAC} \\ A \text{ ?- } t[p'/p] \end{array}$$
Failure

Fails unless the goal's conclusion is a paired universal quantification.

See also

Tactic.GEN_TAC, PairRules.FILTER_PGEN_TAC, PairRules.PGEN, PairRules.PGENL, PairRules.PSPEC, PairRules.PSPECL, PairRules.PSPEC_ALL, PairRules.PSPEC_TAC, PairRules.PSTRIP_TAC, PairRules.P_PGEN_TAC.

<div data-bbox="234 1812 389 1861" data-label="Text"> <p>PGENL</p> </div>	<div data-bbox="1086 1812 1412 1861" data-label="Text"> <p>(PairRules)</p> </div>
---	---

PGENL : (term list -> thm -> thm)

Synopsis

Generalizes zero or more pairs in the conclusion of a theorem.

Description

When applied to a list of paired variable structures $[p_1; \dots; p_n]$ and a theorem $A \vdash t$, the inference rule `PGENL` returns the theorem $A \vdash !p_1 \dots p_n. t$, provided none of the constituent variables from any of the pairs p_i occur free in the assumptions.

$$\frac{A \vdash t}{A \vdash !p_1 \dots p_n. t} \text{PGENL } "[p_1; \dots; p_n]" \quad [\text{where no } p_i \text{ is free in } A]$$

Failure

Fails unless all the terms in the list are paired structures of variables, none of the variables from which are free in the assumption list.

See also

`Thm.GENL`, `PairRules.PGEN`, `PairRules.PGEN_TAC`, `PairRules.PSPEC`, `PairRules.PSPECL`, `PairRules.PSPEC_ALL`, `PairRules.PSPEC_TAC`.

pluck

(Lib)

```
pluck : ('a -> bool) -> 'a list -> 'a * 'a list
```

Synopsis

Pull an element out of a list.

Description

An invocation `pluck P [x1, ..., xk, ..., xn]` returns a pair $(x_k, [x_1, \dots, x_{k-1}, x_{k+1}, \dots, x_n])$, where x_k has been lifted out of the list without disturbing the relative positions of the other elements. For this to happen, $P \ x_k$ must hold, and $P \ x_i$ must not have held for x_1, \dots, x_{k-1} .

Failure

If the input list is empty. Also fails if P holds of no member of the list. Also fails if an application of P fails.

Example

```
- val (x,rst) = pluck (fn x => x mod 2 = 0) [1,2,3];
> val x = 2 : int
   val rst = [1, 3] : int list
```

See also

Lib.first, Lib.filter, Lib.mapfilter, Lib.assoc1, Lib.assoc2, Lib.assoc, Lib.rev_assoc.

++	(bossLib)
-----------	------------------

```
op ++ : simpset * ssfrag -> simpset
```

Synopsis

Infix operator for augmenting simpsets with `ssfrag` values.

Description

The `++` function combines its two arguments and creates a new simpset. This is a way of creating simpsets that are tailored to the particular simplification task at hand.

Failure

Never fails.

Example

Here we add the `UNWIND_ss` `ssfrag` value to the `pure_ss` simpset to exploit the former's point-wise elimination conversions.

```
- SIMP_CONV (pureSimps.pure_ss ++ boolSimps.UNWIND_ss) []
   (Term '!x. x ==> (?y. P(x,y) /\ (y = 5))');

> val it = |- (!x. x ==> (?y. P (x,y) /\ (y = 5))) = P (T,5) : thm
```

See also

simpLib.mk_simpset, simpLib.rewrites, simpLib.SIMP_CONV, pureSimps.pure_ss.

PMATCH_MP	(PairRules)
------------------	--------------------

```
PMATCH_MP : (thm -> thm -> thm)
```

Synopsis

Modus Ponens inference rule with automatic matching.

Description

When applied to theorems $A1 \vdash !p1...pn. t1 ==> t2$ and $A2 \vdash t1'$, the inference rule `PMATCH_MP` matches $t1$ to $t1'$ by instantiating free or paired universally quantified variables in the first theorem (only), and returns a theorem $A1 \cup A2 \vdash !pa..pk. t2'$, where $t2'$ is a correspondingly instantiated version of $t2$. Polymorphic types are also instantiated if necessary.

Variables free in the consequent but not the antecedent of the first argument theorem will be replaced by variants if this is necessary to maintain the full generality of the theorem, and any pairs which were universally quantified over in the first argument theorem will be universally quantified over in the result, and in the same order.

$$\frac{A1 \vdash !p1..pn. t1 ==> t2 \quad A2 \vdash t1'}{\text{MATCH_MP} \quad A1 \cup A2 \vdash !pa..pk. t2'}$$

Failure

Fails unless the first theorem is a (possibly repeatedly paired universally quantified) implication whose antecedent can be instantiated to match the conclusion of the second theorem, without instantiating any variables which are free in $A1$, the first theorem's assumption list.

See also

`Drule.MATCH_MP`.

<div style="display: flex; justify-content: space-between;"> PMATCH_MP_TAC (PairRules) </div>

`PMATCH_MP_TAC` : `thm_tactic`

Synopsis

Reduces the goal using a supplied implication, with matching.

Description

When applied to a theorem of the form

$$A' \vdash !p1...pn. s ==> !q1...qm. t$$

PMATCH_MP_TAC produces a tactic that reduces a goal whose conclusion τ' is a substitution and/or type instance of τ to the corresponding instance of s . Any variables free in s but not in τ will be existentially quantified in the resulting subgoal:

$$\frac{A \text{ ?- } !u_1 \dots u_i. \tau'}{\text{PMATCH_MP_TAC } (A' \text{ |- } !p_1 \dots p_n. s \implies !q_1 \dots q_m. \tau)} A \text{ ?- } ?w_1 \dots w_p. s'$$

where w_1, \dots, w_p are (type instances of) those pairs among p_1, \dots, p_n having variables that do not occur free in τ . Note that this is not a valid tactic unless A' is a subset of A .

Failure

Fails unless the theorem is an (optionally paired universally quantified) implication whose consequent can be instantiated to match the goal. The generalized pairs u_1, \dots, u_i must occur in s' in order for the conclusion τ of the supplied theorem to match τ' .

See also

Tactic.MATCH_MP_TAC.

polymorphic

(Type)

```
polymorphic : hol_type -> bool
```

Synopsis

Checks if there is a type variable in a type

Description

An invocation `polymorphic ty` checks to see if `ty` has an occurrence of any type variable. It is equivalent in functionality to `not o null o type_vars`, but may be more efficient in some situations, since it can stop processing once it finds one type variable.

Failure

Never fails.

Example

```
- polymorphic (bool --> alpha --> ind);
> val it = true : bool
```

Comments

`polymorphic` is also equivalent to `exists_tyvar (K true)`, and no faster.

See also

`Type.type_vars`, `Type.type_var_in`, `Type.exists_tyvar`.

POP_ASSUM

(Tactical)

```
POP_ASSUM : thm_tactic -> tactic
```

Synopsis

Applies tactic generated from the first element of a goal's assumption list.

Description

When applied to a theorem-tactic and a goal, `POP_ASSUM` applies the theorem-tactic to the ASSUMED first element of the assumption list, and applies the resulting tactic to the goal without the first assumption in its assumption list:

$$\text{POP_ASSUM } f \text{ } (\{A_1, \dots, A_n\} \text{ ?- } t) = f \text{ } (A_1 \text{ |- } A_1) \text{ } (\{A_2, \dots, A_n\} \text{ ?- } t)$$

Failure

Fails if the assumption list of the goal is empty, or the theorem-tactic fails when applied to the popped assumption, or if the resulting tactic fails when applied to the goal (with depleted assumption list).

Comments

It is possible simply to use the theorem `ASSUME A1` as required rather than use `POP_ASSUM`; this will also maintain `A1` in the assumption list, which is generally useful. In addition, this approach can equally well be applied to assumptions other than the first.

There are admittedly times when `POP_ASSUM` is convenient, but it is most unwise to use it if there is more than one assumption in the assumption list, since this introduces a dependency on the ordering, which is vulnerable to changes in the HOL system.

Another point to consider is that if the relevant assumption has been obtained by `DISCH_TAC`, it is often cleaner to use `DISCH_THEN` with a theorem-tactic. For example, instead of:

```
DISCH_TAC THEN POP_ASSUM (\th. SUBST1_TAC (SYM th))
```

one might use

```
DISCH_THEN (SUBST1_TAC o SYM)
```

Example

The goal:

```
{4 = SUC x} ?- x = 3
```

can be solved by:

```
POP_ASSUM
  (fn th => REWRITE_TAC[REWRITE_RULE[num_CONV (Term'4', INV_SUC_EQ) th]])
```

Uses

Making more delicate use of an assumption than rewriting or resolution using it.

See also

Tactical.ASSUM_LIST, Tactical.EVERY_ASSUM, Tactic.IMP_RES_TAC,
Tactical.POP_ASSUM_LIST, Rewrite.REWRITE_TAC.

POP_ASSUM_LIST	(Tactical)
----------------	------------

```
POP_ASSUM_LIST : (thm list -> tactic) -> tactic
```

Synopsis

Generates a tactic from the assumptions, discards the assumptions and applies the tactic.

Description

When applied to a function and a goal, POP_ASSUM_LIST applies the function to a list of theorems corresponding to the ASSUMED assumptions of the goal, then applies the resulting tactic to the goal with an empty assumption list.

```
POP_ASSUM_LIST f ({A1,...,An} ?- t) = f [A1 |- A1, ..., An |- An] (?- t)
```

Failure

Fails if the function fails when applied to the list of ASSUMED assumptions, or if the resulting tactic fails when applied to the goal with no assumptions.

Comments

There is nothing magical about `POP_ASSUM_LIST`: the same effect can be achieved by using `ASSUME a` explicitly wherever the assumption `a` is used. If `POP_ASSUM_LIST` is used, it is unwise to select elements by number from the ASSUMED-assumption list, since this introduces a dependency on ordering.

Example

Suppose we have a goal of the following form:

```
{a /\ b, c, (d /\ e) /\ f} ?- t
```

Then we can split the conjunctions in the assumption list apart by applying the tactic:

```
POP_ASSUM_LIST (MAP EVERY STRIP_ASSUME_TAC)
```

which results in the new goal:

```
{a, b, c, d, e, f} ?- t
```

Uses

Making more delicate use of the assumption list than simply rewriting or using resolution.

See also

`Tactical.ASSUM_LIST`, `Tactical.EVERY_ASSUM`, `Tactic.IMP_RES_TAC`,
`Tactical.POP_ASSUM`, `Rewrite.REWRITE_TAC`.

pp_tag

(Tag)

```
pp_tag : ppstream -> tag -> unit
```

Synopsis

Prettyprinter for tags.

Description

An invocation `pp_tag ppstrm t` will place a representation of tag `t` on prettyprinting stream `ppstrm`.

Failure

Never fails.

Example

```

- val ppstrm = PP.mk_ppstream (Portable.defaultConsumer());
> val ppstrm = <ppstream> : ppstream

- Tag.pp_tag ppstrm (Tag.read "fooble");
> val it = () : unit

- (PP.flush_ppstream ppstrm; print "\n");
[oracles: fooble] [axioms: ]
> val it = () : unit

```

Comments

In MoscowML, `Meta.installPP` will install `pp_tag` in the top-level loop.

`pp_term_without_overloads_on` (Parse)

```

Parse.pp_term_without_overloads_on :
  string list -> Portable.ppstream -> term -> unit

```

Synopsis

Printing function for terms without using overload mappings of certain tokens.

Description

The call `pp_term_without_overloads_on ls` returns a printing function to print terms without using any overload mappings of the tokens in `ls`, using the system's standard pretty-printing stream type.

Example

```

> val termpp = pp_term_without_overloads_on ["+"];
val termpp = fn: ppstream -> term -> unit
> val _ = Portable.pprint termpp 'x + y' before print"\n";
arithmetic$+ x y
>

```

Failure

Should never fail.

See also

Parse.pp_term_without_overloads, Parse.print_term_without_overloads_on,
Parse.term_without_overloads_on_to_string, Parse.print_from_grammars.

PRE_CONV

(reduceLib)

```
PRE_CONV : conv
```

Synopsis

Calculates by inference the predecessor of a numeral.

Description

If n is a numeral (e.g. 0, 1, 2, 3,...), then `PRE_CONV "PRE n"` returns the theorem:

$$\vdash \text{PRE } n = s$$

where s is the numeral that denotes the predecessor of the natural number denoted by n .

Failure

`PRE_CONV tm` fails unless `tm` is of the form `"PRE n"`, where n is a numeral.

Example

```
#PRE_CONV "PRE 0";;  
|- PRE 0 = 0
```

```
#PRE_CONV "PRE 1";;  
|- PRE 1 = 0
```

```
#PRE_CONV "PRE 22";;  
|- PRE 22 = 21
```

prefer_form_with_tok

(Parse)

```
prefer_form_with_tok : {term_name : string, tok : string} -> unit
```

Synopsis

Sets a grammar rule's preferred flag, causing it to be preferentially printed.

Description

A call to `prefer_form_with_tok` causes the parsing/pretty-printing rule specified by the `term_name-tok` combination to be the preferred rule for pretty-printing purposes. This change affects the global grammar.

Failure

Never fails.

Example

The initially preferred rule for conditional expressions causes them to print using the `if-then-else` syntax. If the user prefers the “traditional” syntax with `=>|`, this change can be brought about as follows:

```

- prefer_form_with_tok {term_name = "COND", tok = ">="};
> val it = () : unit

- Term'if p then q else r';
<<HOL message: inventing new type variable names: 'a.>>
> val it = 'p => q | r' : term

```

Comments

As the example above demonstrates, using this function does not affect the parser at all.

There is a companion `temp_prefer_form_with_tok` function, which has the same effect on the global grammar, but which does not cause this effect to persist when the current theory is exported.

`prefer_int`

`(intLib)`

```
intLib.prefer_int : unit -> unit
```

Synopsis

Makes the parser favour integer possibilities in ambiguous terms.

Description

Calling `prefer_int()` causes the global grammar to be altered so that the standard arithmetic operator symbols (`+`, `*`, etc.), as well as numerals, are given integral types

if possible. This effect is brought about through the application of multiple calls to `temp_overload_on`, so that the “arithmetic symbols” need not have been previously mapping to integral possibilities at all (as would be the situation after a call to `deprecate_int`).

Failure

Never fails.

See also

`intLib.deprecate_int`, `Parse.overload_on`.

<pre>PRENEX_CONV</pre>	<pre>(Arith)</pre>
------------------------	--------------------

`PRENEX_CONV` : `conv`

Synopsis

Puts a formula into prenex normal form.

Description

This function puts a formula into prenex normal form, and in the process splits any Boolean equalities (if-and-only-if) into two implications. If there is a Boolean-valued subterm present as the condition of a conditional, the subterm will be put in prenex normal form, but quantifiers will not be moved out of the condition. Some renaming of variables may take place.

Failure

Never fails.

Example

```
#PRENEX_CONV "!m n. (m <= n) ==> !p. (m < SUC(n + p))";;
|- (!m n. m <= n ==> (!p. m < (SUC(n + p)))) =
  (!m n p. m <= n ==> m < (SUC(n + p)))

#PRENEX_CONV "!p. (!m. m >= p) = (p = 0)";;
|- (!p. (!m. m >= p) = (p = 0)) =
  (!p m. ?m'. (m' >= p ==> (p = 0)) /\ ((p = 0) ==> m >= p))

#PRENEX_CONV "!m. (((m = 0) ==> (!n. m <= n)) => 0 | m) + m = m";;
|- (!m. (((m = 0) ==> (!n. m <= n)) => 0 | m) + m = m) =
  (!m. ((!n. (m = 0) ==> m <= n) => 0 | m) + m = m)
```

Uses

Useful as a preprocessor to decision procedures which require their argument formula to be in prenex normal form.

See also

`Arith.is_prenex`.

<code>prim_mk_const</code>	<code>(Term)</code>
----------------------------	---------------------

```
prim_mk_const : {Thy:string, Name:string} -> term
```

Synopsis

Build a constant.

Description

If `Name` is the name of a previously declared constant in theory `Thy`, then `prim_mk_const {Thy,Name}` will return the specified constant.

Failure

If `Name` is not the name of a constant declared in theory `Thy`.

Example

```
- prim_mk_const {Thy="min", Name="="};
> val it = '$=' : term

- type_of it;
> val it = ': 'a -> 'a -> bool' : hol_type
```

Comments

The difference between `mk_thy_const` (and `mk_const`) and `prim_mk_const` is that `mk_thy_const` and `mk_const` will create type instances of polymorphic constants, while `prim_mk_const` merely returns the originally declared constant.

See also

`Term.mk_thy_const`.

prim_variant	(Term)
--------------	--------

```
prim_variant : term list -> term -> term
```

Synopsis

Rename a variable to be different from any in a list.

Description

The function `prim_variant` is exactly the same as `variant`, except that it doesn't rename away from constants.

Failure

`prim_variant l t` fails if any term in the list `l` is not a variable or if `t` is not a variable.

Example

```
- variant [] (mk_var("T",bool));
> val it = 'T' : term

- prim_variant [] (mk_var("T",bool));
> val it = 'T' : term
```

Comments

The extra amount of renaming that `variant` does is useful when generating new constant names (even though it returns a variable) inside high-level definition mechanisms. Otherwise, `prim_variant` seems preferable.

See also

`Term.variant`, `Term.mk_var`, `Term.genvar`, `Term.mk_primed_var`.

prime	(Lib)
-------	-------

```
prime : string -> string
```

Synopsis

Attach a prime mark to a string.

Description

A call `prime s` is equal to `s ^ ""`.

Failure

Never fails.

See also

`Term.variant`.

<code>priming</code>	<code>(Globals)</code>
----------------------	------------------------

`priming` : string option ref

Synopsis

Controls how variables get renamed.

Description

The flag `Globals.priming` controls how certain system function perform renaming of variables. When `priming` has the value `NONE`, renaming is achieved by concatenation of primes (`'`). When `priming` has the value `SOME s`, renaming is achieved by incrementing a counter.

The default value of `priming` is `NONE`.

Example

```
- mk_primed_var ("T",bool);
> val it = 'T' : term

- with_flag (priming,SOME "_") mk_primed_var ("T",bool);
> val it = 'T_1' : term
```

Comments

Proofs should be re-run in the same priming regime as they were originally performed in, since different styles of renaming can break proofs.

See also

`Term.variant`, `Term.subst`, `Term.inst`, `Term.mk_primed_var`, `Lib.with_flag`.


```
print_backend_term_without_overloads_on
(Parse)
```

```
Parse.print_backend_term_without_overloads_on : string list -> term -> unit
```

Synopsis

Prints a term to the screen (standard out), using current backend information, without using overload mappings of certain tokens.

Description

The call `print_backend_term_without_overloads_on ls t` prints `t` to the screen, as appropriate for the current backend, without using any overloads on tokens in `ls`.

If the current backend is a color-capable terminal, for example, the printed string will contain escape codes for coloring free and bound variables, which should then be interpreted by the terminal as colors.

Failure

Should never fail.

See also

`Parse.print_term_without_overloads_on`,
`Parse.print_backend_term_without_overloads`,
`Parse.term_without_overloads_on_to_backend_string`, `Parse.clear_overloads_on`,
`Parse.print_backend_term`.

```
print_datatypes (EmitTeX)
```

```
print_datatypes : string -> unit
```

Synopsis

Prints datatype declarations for the named theory to the screen (standard out).

Description

An invocation of `print_datatypes thy`, where `thy` is the name of a currently loaded theory segment, will print the datatype declarations made in that theory.

Failure

Never fails. If `thy` is not the name of a currently loaded theory segment then no output will be produced.

Example

```
- new_theory "example";
<<HOL message: Created theory "example">>
> val it = () : unit
- val _ = Hol_datatype `example = First | Second`;
<<HOL message: Defined type: "example">>
- EmitTeX.print_datatypes "example";
example = First | Second
> val it = () : unit
```

See also

`EmitTeX.datatype_thm_to_string`, `bossLib.Hol_datatype`.

<code>print_from_grammars</code>	<code>(Parse)</code>
----------------------------------	----------------------

```
print_from_grammars :
  (type_grammar.grammar * term_grammar.grammar) ->
  ((Portable.ppstream -> hol_type -> unit) *
   (Portable.ppstream -> term -> unit))
```

Synopsis

Returns printing functions based on the supplied grammars.

Description

When given a pair consisting of a type and term grammar (such a pair is exported with every theory, under the name `<thy>_grammars`), this function returns printing functions that use those grammars to render terms and types using the system's standard pretty-printing stream type.

Failure

Never fails.

Example

With `arithmeticTheory` loaded, arithmetic expressions and numerals print pleasingly:

```

- load "arithmeticTheory";
> val it = () : unit

- ``3 + x * 4``;
> val it = ``3 + x * 4`` : term

```

The printing of these terms is controlled by the global grammar, which is augmented when the theory of arithmetic is loaded. Printing functions based on the grammar of the base theory `bool` can be defined:

```

- val (typepp, termpp) = print_from_grammars bool_grammars
> val typepp = fn : ppstream -> hol_type -> unit
    val termpp = fn : ppstream -> term -> unit

```

These functions can then be used to print arithmetic terms (note that neither the global parser nor printer are disturbed by this activity), using the `Portable.pprint` function:

```

- Portable.pprint termpp ``3 + x * 4``;
arithmetic$+
  (arithmetic$NUMERAL
    (arithmetic$BIT1 (arithmetic$BIT1 arithmetic$ZERO)))
  (arithmetic$* x
    (arithmetic$NUMERAL
      (arithmetic$BIT2 (arithmetic$BIT1 arithmetic$ZERO))))
> val it = () : unit

```

Not only have the fixities of `+` and `*` been ignored, but the constants in the term, belonging to `arithmeticTheory`, are all printed in “long identifier” form because the grammars from `boolTheory` don’t know about them.

Uses

Printing terms with early grammars such as `bool_grammars` can remove layers of potentially confusing pretty-printing, including complicated concrete syntax and overloading, and even the underlying representation of numerals.

See also

`Parse.parse_from_grammars`, `Parse.print_term_by_grammar`, `Parse.Term`.

`print_term`

(Parse)

`Parse.print_term` : term -> unit

Synopsis

Prints a term to the screen (standard out).

Description

The function `print_term` prints a term to the screen. It first converts the term into a string, and then outputs that string to the standard output stream.

The conversion to the string is done by `term_to_string`. The term is printed using the pretty-printing information contained in the global grammar.

Failure

Should never fail.

See also

`Parse.term_to_string`.

```
print_term_as_tex
```

```
(EmitTeX)
```

```
print_term_as_tex : term -> unit
```

Synopsis

Prints a term as LaTeX.

Description

An invocation of `print_term_as_tex tm` will print the term `tm`, replacing various character patterns (e.g. `/\` and `\/`) with LaTeX commands. The translation is controlled by the string to string function `EmitTeX.hol_to_tex`.

Failure

Should never fail.

Example

```
- EmitTeX.print_term_as_tex ‘\l h. {x | l <= x /\ x <= h}‘ before print "\n";
  \HOLTokenLambda{}l h. \HOLTokenLeftbrace{}x | l \HOLTokenLeq{} x \HOLTokenConj{} x
> val it = () : unit
```

Comments

The LaTeX style file `holtexbasic.sty` (or `holtex.sty`) should be used and the output should be pasted into a Verbatim environment.

See also

EmitTeX.print_type_as_tex, EmitTeX.print_theorem_as_tex,
 EmitTeX.print_theory_as_tex, EmitTeX.print_theories_as_tex_doc,
 EmitTeX.tex_theory.

<code>print_term_by_grammar</code> (Parse)

```
print_term_by_grammar :
  (type_grammar.grammar * term_grammar.grammar) -> term -> unit
```

Synopsis

Prints a term to standard out, using grammars to specify how.

Description

Where `print_term` uses the (implicit) global grammars to control the printing of its term argument, the `print_term_by_grammar` uses user-supplied grammars. These can control the printing of concrete syntax (operator fixities and precedence) and the degree of constant overloading.

Failure

Never fails.

See also

`Parse.print_from_grammars`.

<code>print_term_without_overloads_on</code> (Parse)

```
Parse.print_term_without_overloads_on : string list -> term -> unit
```

Synopsis

Prints a term to the screen (standard out), without using overload mappings of certain tokens.

Description

The call `print_term_without_overloads_on ls t` prints `t` to the screen without using any overloads on tokens in `ls`.

Example

```
> val _ = print_term_without_overloads_on ["+"] ``x + y`` before print "\n";
arithmetic$+ x y
>
```

Failure

Should never fail.

See also

`Parse.print_backend_term_without_overloads_on`,
`Parse.print_term_without_overloads`, `Parse.term_without_overloads_on_to_string`,
`Parse.clear_overloads_on`, `Parse.print_term`.

<code>print_theorem_as_tex</code>	<code>(EmitTeX)</code>
-----------------------------------	------------------------

```
print_theorem_as_tex : thm -> unit
```

Synopsis

Prints a theorem as LaTeX.

Description

An invocation of `print_theorem_as_tex thm` will print the term `thm`, replacing various character patterns (e.g. `/\` and `\/`) with LaTeX commands. The translation is controlled by the string to string function `EmitTeX.hol_to_tex`. If the theorem is for a datatype then the function `datatype_thm_to_string` is used to produce the original declaration.

Failure

Should never fail.

Example

```
- EmitTeX.print_theorem_as_tex listTheory.CONNS before print "\n";
\HOLTokenTurnstile{} \HOLTokenForall{}1. \HOLTokenNeg{}NULL 1 \HOLTokenImp{} (HD 1
> val it = () : unit
- EmitTeX.print_theorem_as_tex listTheory.datatype_list before print "\n";
list = [] | CONS of \HOLTokenQuote{}a \HOLTokenImp{} \HOLTokenQuote{}a list
> val it = () : unit
```

Comments

The LaTeX style file `holtexbasic.sty` (or `holtex.sty`) should be used and the output should be pasted into a `Verbatim` environment.

See also

`EmitTeX.print_term_as_tex`, `EmitTeX.print_type_as_tex`,
`EmitTeX.print_theory_as_tex`, `EmitTeX.print_theories_as_tex_doc`,
`EmitTeX.tex_theory`.

`print_theories_as_tex_doc` (EmitTeX)

```
print_theories_as_tex_doc : string list -> string -> unit
```

Synopsis

Emits theories as LaTeX commands and creates a document template.

Description

An invocation of `print_theories_as_tex_doc thys name` will export the named theories `thys` as a collection of LaTeX commands and it will also generate a document, whose file name is given by `name`, that presents all of the theories. The theories are exported with `print_theory_as_tex`.

Failure

Will fail if there is a system error when trying to write the files. It will not overwrite the file name, however, the theories may be overwritten.

Example

The invocation

```
- EmitTeX.print_theories_as_tex_doc ["arithmetic", "list", "words"] "report";
> val it = () : unit
```

will generate four files "HOLarithmetic.tex", "HOLlist.tex", "HOLwords.tex" and "report.tex".

The document can be built as follows:

```
$ cp $HOLHOME/src/emit/holtex.sty .
$ pdflatex report
$ makeindex report
$ pdflatex report
```

See also

`EmitTeX.print_term_as_tex`, `EmitTeX.print_type_as_tex`,
`EmitTeX.print_theorem_as_tex`, `EmitTeX.print_theory_as_tex`, `EmitTeX.tex_theory`.

<code>print_theory</code>	(DB)
---------------------------	------

```
print_theory : string -> unit
```

Synopsis

Print a theory on the standard output.

Description

An invocation `print_theory s` will display the contents of the theory segment `s` on the standard output. The string `"-"` may be used to denote the current theory segment.

Failure

If `s` is not the name of a loaded theory.

Example

```
- print_theory "combin";
Theory: combin
```

Parents:

```
  bool
```

Term constants:

```
C      : ('a -> 'b -> 'c) -> 'b -> 'a -> 'c
I      : 'a -> 'a
K      : 'a -> 'b -> 'a
S      : ('a -> 'b -> 'c) -> ('a -> 'b) -> 'a -> 'c
W      : ('a -> 'a -> 'b) -> 'a -> 'b
o      : ('c -> 'b) -> ('a -> 'c) -> 'a -> 'b
```

Definitions:

```
K_DEF  |- K = (\x y. x)
S_DEF  |- S = (\f g x. f x (g x))
I_DEF  |- I = S K K
C_DEF  |- combin$C = (\f x y. f y x)
```



```

W_DEF  |- W = (\f x. f x x)
o_DEF  |- !f g. f o g = (\x. f (g x))

```

Theorems:

```

o_THM  |- !f g x. (f o g) x = f (g x)
o_ASSOC |- !f g h. f o g o h = (f o g) o h
K_THM  |- !x y. K x y = x
S_THM  |- !f g x. S f g x = f x (g x)
C_THM  |- !f x y. combin$C f x y = f y x
W_THM  |- !f x. W f x = f x x
I_THM  |- !x. I x = x
I_o_ID |- !f. (I o f = f) /\ (f o I = f)

```

```
> val it = () : unit
```

See also

DB.dest_theory, DB.thy.

```
print_theory_as_tex
```

```
(EmitTeX)
```

```
print_theory_as_tex : string -> unit
```

Synopsis

Emits a theory as LaTeX commands.

Description

An invocation of `print_theory_as_tex thy` will export the named theory as a collection of LaTeX commands. The output file is named "HOLthy.tex", where `thy` is the named theory. The prefix "HOL" can be changed by setting `holPrefix`. The file is stored in the directory `emitTeXDir`. By default the current working directory is used.

The LaTeX file will contain commands for displaying the theory's datatypes, definitions and theorems.

Failure

Will fail if there is a system error when trying to write the file. If the theory is not loaded then a message will be printed and an empty file will be created.

Example

The list theory is exported with:

```
- EmitTeX.print_theory_as_tex "list";
> val it = () : unit
```

The resulting file can be included in a LaTeX document with

```
\input{HOLlist}
```

Some examples of the available LaTeX commands are listed below:

```
\HOLlistDatatypeslist
\HOLlistDefinitionsALLXXDISTINCT
\HOLlistTheoremsALLXXDISTINCTXXFILTER
```

Underscores in HOL names are replaced by "XX"; quotes become "YY" and numerals are expanded out e.g. "1" becomes "One".

Complete listings of the datatypes, definitions and theorems are displayed with:

```
\HOLlistDatatypes
\HOLlistDefinitions
\HOLlistTheorems
```

The date the theory was build can be displayed with:

```
\HOLlistDate
```

The generated LaTeX will reflect the output of `Parse.thm_to_string`, which is under the control of the user. For example, the line width can be changed by setting `Globals.linewidth`.

The Verbatim display environment is used, however, "boxed" versions can be constructed. For example,

```
\BUseVerbatim{HOLlistDatatypeslist}
```

can be used inside tables and figures.

Comments

The LaTeX style file `holtexbasic.sty` (or `holtex.sty`) should be used. These style files can be modified by the user. For example, the font can be changed to Helvetica with

```
\fvset{fontfamily=helvetica}
```

However, note that this will adversely effect the alignment of the output.

See also

```
EmitTeX.print_term_as_tex, EmitTeX.print_type_as_tex,
EmitTeX.print_theorem_as_tex, EmitTeX.print_theories_as_tex_doc,
EmitTeX.tex_theory.
```

<pre>print_type_as_tex</pre>	<pre>(EmitTeX)</pre>
------------------------------	----------------------

```
print_type_as_tex : hol_type -> unit
```

Synopsis

Prints a type as LaTeX.

Description

An invocation of `print_type_as_tex ty` will print the type `ty`, replacing various character patterns (e.g. `#` and `->`) with LaTeX commands. The translation is controlled by the string to string function `EmitTeX.hol_to_tex`.

Failure

Should never fail.

Example

```
- EmitTeX.print_type_as_tex ``:bool # bool -> num`` before print "\n";
:bool \HOLTokenProd{} bool \HOLTokenMap{} num
> val it = () : unit
```

Comments

The LaTeX style file `holtexbasic.sty` (or `holtex.sty`) should be used and the output should be pasted into a `Verbatim` environment.

See also

`EmitTeX.print_term_as_tex`, `EmitTeX.print_theorem_as_tex`,
`EmitTeX.print_theory_as_tex`, `EmitTeX.print_theories_as_tex_doc`,
`EmitTeX.tex_theory`.

<pre>PROVE</pre>	<pre>(BasicProvers)</pre>
------------------	---------------------------

```
PROVE : thm list -> term -> thm
```

Synopsis

Prove a theorem with use of supplied lemmas.

Description

`bossLib.PROVE` is identical to `BasicProvers.PROVE`.

See also

`bossLib.PROVE`.

<div data-bbox="234 593 389 640" data-label="Text"> <p>PROVE</p> </div>	<div data-bbox="1145 593 1412 640" data-label="Text"> <p>(bossLib)</p> </div>
--	--

```
PROVE : thm list -> term -> thm
```

Synopsis

Prove a theorem with use of supplied lemmas.

Description

An invocation `PROVE th1 M` attempts to prove `M` using an automated reasoner supplied with the lemmas in `th1`. The automated reasoner performs a first order proof search. It currently provides some support for polymorphism and higher-order values (lambda terms).

Failure

If the proof search fails, or if `M` does not have type `bool`.

Example

```
- PROVE [] (concl SKOLEM_THM);
Meson search level: .....
> val it = |- !P. (!x. ?y. P x y) = ?f. !x. P x (f x) : thm

- let open arithmeticTheory
  in
    PROVE [ADD_ASSOC, ADD_SYM, ADD_CLAUSES]
      (Term 'x + 0 + y + z = y + (z + x)')
  end;
Meson search level: .....
> val it = |- x + 0 + y + z = y + (z + x) : thm
```

Comments

Some output (a row of dots) is currently generated as `PROVE` works. If the frequency of dot emission becomes slow, that is a sign that the term is not likely to be proved with the current lemmas.

Unlike `MESON_TAC`, `PROVE` can handle terms with conditionals.

See also

`bossLib.PROVE_TAC`, `mesonLib.MESON_TAC`, `mesonLib.ASM_MESON_TAC`.

prove

(Tactical)

```
prove : term * tactic -> thm
```

Synopsis

Attempts to prove a boolean term using the supplied tactic.

Description

When applied to a term-tactic pair (tm, tac) , the function `prove` attempts to prove the goal $?- tm$, that is, the term tm with no assumptions, using the tactic tac . If `prove` succeeds, it returns the corresponding theorem $A \vdash tm$, where the assumption list A may not be empty if the tactic is invalid; `prove` has no inbuilt validity-checking.

Failure

Fails if the term is not of type `bool` (and so cannot possibly be the conclusion of a theorem), or if the tactic cannot solve the goal.

See also

`Tactical.TAC_PROOF`.

prove_abs_fn_one_one

(Drule)

```
prove_abs_fn_one_one : thm -> thm
```

Synopsis

Proves that a type abstraction function is one-to-one (injective).

Description

If th is a theorem of the form returned by the function `define_new_type_bijections`:

$$\vdash (!a. \text{abs}(\text{rep } a) = a) \wedge (!r. P \ r = (\text{rep}(\text{abs } r) = r))$$

then `prove_abs_fn_one_one th` proves from this theorem that the function `abs` is one-to-one for values that satisfy `P`, returning the theorem:

$$\text{|- !r r'. P r ==> P r' ==> ((abs r = abs r') = (r = r'))}$$

Failure

Fails if applied to a theorem not of the form shown above.

See also

`Definition.new_type_definition`, `Drule.define_new_type_bijections`,
`Prim_rec.prove_abs_fn_onto`, `Drule.prove_rep_fn_one_one`, `Drule.prove_rep_fn_onto`.

`prove_abs_fn_one_one` (Prim_rec)

`prove_abs_fn_one_one : thm -> thm`

Synopsis

Proves that a type abstraction function is one-to-one (injective).

Description

If `th` is a theorem of the form returned by the function `define_new_type_bijections`:

$$\text{|- (!a. abs(rep a) = a) /\ (!r. P r = (rep(abs r) = r))}$$

then `prove_abs_fn_one_one th` proves from this theorem that the function `abs` is one-to-one for values that satisfy `P`, returning the theorem:

$$\text{|- !r r'. P r ==> P r' ==> ((abs r = abs r') = (r = r'))}$$

Failure

Fails if applied to a theorem not of the form shown above.

See also

`Definition.new_type_definition`, `Drule.define_new_type_bijections`,
`Prim_rec.prove_abs_fn_onto`, `Drule.prove_rep_fn_one_one`, `Drule.prove_rep_fn_onto`.

`prove_abs_fn_onto` (Drule)

`prove_abs_fn_onto : thm -> thm`

Synopsis

Proves that a type abstraction function is onto (surjective).

Description

If `th` is a theorem of the form returned by the function `define_new_type_bijections`:

$$\vdash (\!a. \text{abs}(\text{rep } a) = a) \wedge (\!r. P \ r = (\text{rep}(\text{abs } r) = r))$$

then `prove_abs_fn_onto th` proves from this theorem that the function `abs` is onto, returning the theorem:

$$\vdash \!a. \ ?r. (a = \text{abs } r) \wedge P \ r$$

Failure

Fails if applied to a theorem not of the form shown above.

See also

`Definition.new_type_definition`, `Drule.define_new_type_bijections`,
`Prim_rec.prove_abs_fn_one_one`, `Drule.prove_rep_fn_one_one`,
`Drule.prove_rep_fn_onto`.

<code>prove_abs_fn_onto</code>

<code>(Prim_rec)</code>

```
prove_abs_fn_onto : thm -> thm
```

Synopsis

Proves that a type abstraction function is onto (surjective).

Description

If `th` is a theorem of the form returned by the function `define_new_type_bijections`:

$$\vdash (\!a. \text{abs}(\text{rep } a) = a) \wedge (\!r. P \ r = (\text{rep}(\text{abs } r) = r))$$

then `prove_abs_fn_onto th` proves from this theorem that the function `abs` is onto, returning the theorem:

$$\vdash \!a. \ ?r. (a = \text{abs } r) \wedge P \ r$$

Failure

Fails if applied to a theorem not of the form shown above.

See also

Definition.new_type_definition, Drule.define_new_type_bijections,
Prim_rec.prove_abs_fn_one_one, Drule.prove_rep_fn_one_one,
Drule.prove_rep_fn_onto.

<code>prove_cases_thm</code>	<code>(Prim_rec)</code>
------------------------------	-------------------------

```
prove_cases_thm : (thm -> thm)
```

Synopsis

Proves a structural cases theorem for an automatically-defined concrete type.

Description

`prove_cases_thm` takes as its argument a structural induction theorem, in the form returned by `prove_induction_thm` for an automatically-defined concrete type. When applied to such a theorem, `prove_cases_thm` automatically proves and returns a theorem which states that every value the concrete type in question is denoted by the value returned by some constructor of the type.

Failure

Fails if the argument is not a theorem of the form returned by `prove_induction_thm`

Example

Given the following structural induction theorem for labelled binary trees:

$$\begin{aligned} &|- !P. (!x. P(\text{LEAF } x)) \wedge (!b1\ b2. P\ b1 \wedge P\ b2 \implies P(\text{NODE } b1\ b2)) \implies \\ & \quad (!b. P\ b) \end{aligned}$$

`prove_cases_thm` proves and returns the theorem:

$$|- !b. (?x. b = \text{LEAF } x) \vee (?b1\ b2. b = \text{NODE } b1\ b2)$$

This states that every labelled binary tree `b` is either a leaf node with a label `x` or a tree with two subtrees `b1` and `b2`.

See also

Prim_rec.INDUCT_THEN, Prim_rec.new_recursive_definition,
Prim_rec.prove_constructors_distinct, Prim_rec.prove_constructors_one_one,
Prim_rec.prove_induction_thm, Prim_rec.prove_rec_fn_exists.


```
prove_constructors_distinct      (Prim_rec)
```

```
prove_constructors_distinct : (thm -> thm)
```

Synopsis

Proves that the constructors of an automatically-defined concrete type yield distinct values.

Description

`prove_constructors_distinct` takes as its argument a primitive recursion theorem, in the form returned by `define_type` for an automatically-defined concrete type. When applied to such a theorem, `prove_constructors_distinct` automatically proves and returns a theorem which states that distinct constructors of the concrete type in question yield distinct values of this type.

Failure

Fails if the argument is not a theorem of the form returned by `define_type`, or if the concrete type in question has only one constructor.

Example

Given the following primitive recursion theorem for labelled binary trees:

```
|- !f0 f1.
    ?! fn.
    (!x. fn(LEAF x) = f0 x) /\
    (!b1 b2. fn(NODE b1 b2) = f1(fn b1)(fn b2)b1 b2)
```

`prove_constructors_distinct` proves and returns the theorem:

```
|- !x b1 b2. ~(LEAF x = NODE b1 b2)
```

This states that leaf nodes are different from internal nodes. When the concrete type in question has more than two constructors, the resulting theorem is just conjunction of inequalities of this kind.

See also

`Prim_rec.INDUCT.THEN`, `Prim_rec.new_recursive_definition`,
`Prim_rec.prove_cases_thm`, `Prim_rec.prove_constructors_one_one`,
`Prim_rec.prove_induction_thm`, `Prim_rec.prove_rec_fn_exists`.

`prove_constructors_one_one` (Prim_rec)

`prove_constructors_one_one` : (thm -> thm)

Synopsis

Proves that the constructors of an automatically-defined concrete type are injective.

Description

`prove_constructors_one_one` takes as its argument a primitive recursion theorem, in the form returned by `define_type` for an automatically-defined concrete type. When applied to such a theorem, `prove_constructors_one_one` automatically proves and returns a theorem which states that the constructors of the concrete type in question are injective (one-to-one). The resulting theorem covers only those constructors that take arguments (i.e. that are not just constant values).

Failure

Fails if the argument is not a theorem of the form returned by `define_type`, or if all the constructors of the concrete type in question are simply constants of that type.

Example

Given the following primitive recursion theorem for labelled binary trees:

```
|- !f0 f1.
  ?! fn.
  (!x. fn(LEAF x) = f0 x) /\
  (!b1 b2. fn(NODE b1 b2) = f1(fn b1)(fn b2)b1 b2)
```

`prove_constructors_one_one` proves and returns the theorem:

```
|- (!x x'. (LEAF x = LEAF x') = (x = x')) /\
  (!b1 b2 b1' b2'.
  (NODE b1 b2 = NODE b1' b2') = (b1 = b1') /\ (b2 = b2'))
```

This states that the constructors `LEAF` and `NODE` are both injective.

See also

`Prim_rec.INDUCT_THEN`, `Prim_rec.new_recursive_definition`,
`Prim_rec.prove_cases_thm`, `Prim_rec.prove_constructors_distinct`,
`Prim_rec.prove_induction_thm`, `Prim_rec.prove_rec_fn_exists`.

PROVE_HYP	(Drule)
-----------	---------

PROVE_HYP : thm -> thm -> thm

Synopsis

Eliminates a provable assumption from a theorem.

Description

When applied to two theorems, PROVE_HYP returns a theorem having the conclusion of the second. The new hypotheses are the union of the two hypothesis sets (first deleting, however, the conclusion of the first theorem from the hypotheses of the second).

$$\frac{A1 \mid- t1 \quad A2 \mid- t2}{A1 \text{ u } (A2 - \{t1\}) \mid- t2} \text{ PROVE_HYP}$$

Failure

Never fails.

Comments

This is the Cut rule. It is not necessary for the conclusion of the first theorem to be the same as an assumption of the second, but PROVE_HYP is otherwise of doubtful value.

See also

Thm.DISCH, Thm.MP, Drule.UNDISCH.

prove_induction_thm	(Prim_rec)
---------------------	------------

prove_induction_thm : (thm -> thm)

Synopsis

Derives structural induction for an automatically-defined concrete type.

Description

prove_induction_thm takes as its argument a primitive recursion theorem, in the form returned by define_type for an automatically-defined concrete type. When applied to

such a theorem, `prove_induction_thm` automatically proves and returns a theorem that states a structural induction principle for the concrete type described by the argument theorem. The theorem returned by `prove_induction_thm` is in a form suitable for use with the general structural induction tactic `INDUCT_THEN`.

Failure

Fails if the argument is not a theorem of the form returned by `define_type`.

Example

Given the following primitive recursion theorem for labelled binary trees:

```
|- !f0 f1.
    ?! fn.
    (!x. fn(LEAF x) = f0 x) /\
    (!b1 b2. fn(NODE b1 b2) = f1(fn b1)(fn b2)b1 b2)
```

`prove_induction_thm` proves and returns the theorem:

```
|- !P. (!x. P(LEAF x)) /\ (!b1 b2. P b1 /\ P b2 ==> P(NODE b1 b2)) ==>
    (!b. P b)
```

This theorem states the principle of structural induction on labelled binary trees: if a predicate `P` is true of all leaf nodes, and if whenever it is true of two subtrees `b1` and `b2` it is also true of the tree `NODE b1 b2`, then `P` is true of all labelled binary trees.

See also

`Prim_rec.INDUCT_THEN`, `Prim_rec.new_recursive_definition`,
`Prim_rec.prove_cases_thm`, `Prim_rec.prove_constructors_distinct`,
`Prim_rec.prove_constructors_one_one`, `Prim_rec.prove_rec_fn_exists`.

`prove_model`

`(holCheckLib)`

```
prove_model : model -> model
```

Synopsis

Attempts to discharge all assumptions to the `term_bdd`'s and theorems in the results list of the `HolCheck` model.

Description

`HolCheck` uses postponed proof verification to speed up the model checking work-flow. Any success theorems and `term_bdd`'s thus end up with several undischarged assumptions. The idea is that the time-consuming proof verification can be postponed to a later time, when the user is otherwise occupied (e.g. asleep).

Failure

Fails if not called in the same HOL session that generated the results. This is because the required proof tactics are accumulated in memory as closures. Moscow ML (in which HOL is implemented) cannot persist closures.

Comments

Other than the failure scenario documented above, a failure in the proof verification points to a bug in the HolCheck proof verification machinery; it does not invalidate the result.

See also

`holCheckLib.holCheck`, `holCheckLib.get_results`.

`prove_rec_fn_exists` (Prim_rec)

```
prove_rec_fn_exists : thm -> term -> thm
```

Synopsis

Proves the existence of a primitive recursive function over a concrete recursive type.

Description

`prove_rec_fn_exists` is a version of `new_recursive_definition` which proves only that the required function exists; it does not make a constant specification. The first argument is a primitive recursion theorem of the form generated by `Hol_datatype`, and the second is a user-supplied primitive recursive function definition. The theorem which is returned asserts the existence of the recursively-defined function in question (if it is primitive recursive over the type characterized by the theorem given as the first argument). See the entry for `new_recursive_definition` for details.

Failure

As for `new_recursive_definition`.

Example

Given the following primitive recursion theorem for labelled binary trees:

```
|- !f0 f1.
    ?fn.
      (!a. fn (LEAF a) = f0 a) /\
      !a0 a1. fn (NODE a0 a1) = f1 a0 a1 (fn a0) (fn a1) : thm
```

`prove_rec_fn_exists` can be used to prove the existence of primitive recursive functions over binary trees. Suppose the value of `th` is this theorem. Then the existence of a recursive function `Leaves`, which computes the number of leaves in a binary tree, can be proved as shown below:

```
- prove_rec_fn_exists th
  ‘‘(Leaves (LEAF (x:'a)) = 1) /\
    (Leaves (NODE t1 t2) = (Leaves t1) + (Leaves t2))’’;
> val it =
  |- ?Leaves.
    (!x. Leaves (LEAF x) = 1) /\
    !t1 t2. Leaves (NODE t1 t2) = Leaves t1 + Leaves t2 : thm
```

The result should be compared with the example given under `new_recursive_definition`.

See also

`bossLib.Hol_datatype`, `Prim_rec.new_recursive_definition`.

`prove_rep_fn_one_one` (Drule)

```
prove_rep_fn_one_one : thm -> thm
```

Synopsis

Proves that a type representation function is one-to-one (injective).

Description

If `th` is a theorem of the form returned by the function `define_new_type_bijections`:

```
|- (!a. abs(rep a) = a) /\ (!r. P r = (rep(abs r) = r))
```

then `prove_rep_fn_one_one th` proves from this theorem that the function `rep` is one-to-one, returning the theorem:

```
|- !a a'. (rep a = rep a') = (a = a')
```

Failure

Fails if applied to a theorem not of the form shown above.

See also

`Definition.new_type_definition`, `Drule.define_new_type_bijections`,
`Prim_rec.prove_abs_fn_one_one`, `Prim_rec.prove_abs_fn_onto`,
`Drule.prove_rep_fn_onto`.

<pre>prove_rep_fn_onto</pre>	<pre>(Drule)</pre>
------------------------------	--------------------

```
prove_rep_fn_onto : thm -> thm
```

Synopsis

Proves that a type representation function is onto (surjective).

Description

If `th` is a theorem of the form returned by the function `define_new_type_bijections`:

$$\text{|- } (!a. \text{abs}(\text{rep } a) = a) \wedge (!r. P \ r = (\text{rep}(\text{abs } r) = r))$$

then `prove_rep_fn_onto th` proves from this theorem that the function `rep` is onto the set of values that satisfy `P`, returning the theorem:

$$\text{|- } !r. P \ r = (?a. r = \text{rep } a)$$

Failure

Fails if applied to a theorem not of the form shown above.

See also

`Definition.new_type_definition`, `Drule.define_new_type_bijections`,
`Prim_rec.prove_abs_fn_one_one`, `Prim_rec.prove_abs_fn_onto`,
`Drule.prove_rep_fn_one_one`.

<pre>PROVE_TAC</pre>	<pre>(BasicProvers)</pre>
----------------------	---------------------------

```
PROVE_TAC : thm list -> tactic
```

Synopsis

Solve a goal with use of hypotheses and supplied lemmas.

Description

`bossLib.PROVE_TAC` is identical to `BasicProvers.PROVE_TAC`.

See also

`bossLib.PROVE_TAC`.

PROVE_TAC	(bossLib)
------------------	------------------

PROVE_TAC : thm list -> tactic

Synopsis

Solve a goal with use of hypotheses and supplied lemmas.

Description

An invocation `PROVE_TAC th1` attempts to solve the goal it is applied to by executing a proof procedure that is semi-complete for pure first order logic. The assumptions of the goal and the theorems in `th1` are used. The procedure makes special provision for handling polymorphic and higher-order values (lambda terms). It also handles conditional expressions.

Failure

PROVE_TAC fails if it searches to a depth equal to the contents of the reference variable `mesonLib.max_depth` (set to 30 by default, but changeable by the user) without finding a proof.

Comments

PROVE_TAC can only progress the goal to a successful proof of the goal or not at all. In this respect it differs from tactics such as simplification and rewriting. Its ability to solve existential goals and to make effective use of transitivity theorems make it a particularly powerful tactic.

See also

`bossLib.PROVE`, `mesonLib.MESON_TAC`, `mesonLib.ASM_MESON_TAC`, `mesonLib.GEN_MESON_TAC`.

PRUNE_CONV	(unwindLib)
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PRUNE_CONV : conv

Synopsis

Prunes all hidden variables.

Description

PRUNE_CONV "?l1 ... lr. t1 /\ ... /\ eqn1 /\ ... /\ eqnr /\ ... /\ tp" returns a theorem of the form:

$$\vdash (?l1 \dots lr. t1 \wedge \dots \wedge eqn1 \wedge \dots \wedge eqnr \wedge \dots \wedge tp) = (t1 \wedge \dots \wedge tp)$$

where each $eqni$ has the form " $!y1 \dots ym. li \ x1 \dots xn = b$ " and li does not appear free in any of the other conjuncts or in b . The conversion works if one or more of the $eqni$'s are not present, that is if li is not free in any of the conjuncts, but does not work if li appears free in more than one of the conjuncts. p may be zero, that is, all the conjuncts may be $eqni$'s. In this case the result will be simply \top (true). Also, for each $eqni$, m and n may be zero.

Failure

Fails if the argument term is not of the specified form or if any of the li 's are free in more than one of the conjuncts or if the equation for any li is recursive.

Example

```
#PRUNE_CONV
# "?l2 l1.
#  (!x:num). l1 x = F) /\ (!x. l2 x = ~(out x)) /\ (!x:num). out x = T";;
|- (?l2 l1. (!x. l1 x = F) /\ (!x. l2 x = ~out x) /\ (!x. out x = T)) =
  (!x. out x = T)
```

See also

`unwindLib.PRUNE_ONCE_CONV`, `unwindLib.PRUNE_ONE_CONV`, `unwindLib.PRUNE_SOME_CONV`, `unwindLib.PRUNE_SOME_RIGHT_RULE`, `unwindLib.PRUNE_RIGHT_RULE`.

PRUNE_ONCE_CONV

(unwindLib)

PRUNE_ONCE_CONV : conv

Synopsis

Prunes one hidden variable.

Description

`PRUNE_ONCE_CONV "?l. t1 /\ ... /\ ti /\ eq /\ t(i+1) /\ ... /\ tp"` returns a theorem of the form:

$$\vdash (?l. t1 \wedge \dots \wedge ti \wedge eq \wedge t(i+1) \wedge \dots \wedge tp) = (t1 \wedge \dots \wedge ti \wedge t(i+1) \wedge \dots \wedge tp)$$

where eq has the form " $!y_1 \dots y_m. l \ x_1 \dots x_n = b$ " and l does not appear free in the t_i 's or in b . The conversion works if eq is not present, that is if l is not free in any of the conjuncts, but does not work if l appears free in more than one of the conjuncts. Each of m , n and p may be zero.

Failure

Fails if the argument term is not of the specified form or if l is free in more than one of the conjuncts or if the equation for l is recursive.

Example

```
#PRUNE_ONCE_CONV "?l2. (!x:num). l1 x = F) /\ (!x. l2 x = ~(l1 x))";;
|- (?l2. (!x. l1 x = F) /\ (!x. l2 x = ~l1 x)) = (!x. l1 x = F)
```

See also

`unwindLib.PRUNE_ONE_CONV`, `unwindLib.PRUNE_SOME_CONV`, `unwindLib.PRUNE_CONV`,
`unwindLib.PRUNE_SOME_RIGHT_RULE`, `unwindLib.PRUNE_RIGHT_RULE`.

PRUNE_ONE_CONV

(unwindLib)

`PRUNE_ONE_CONV : (string -> conv)`

Synopsis

Prunes a specified hidden variable.

Description

`PRUNE_ONE_CONV 'lj'` when applied to the term:

$$"?l_1 \dots l_j \dots l_r. t_1 \wedge \dots \wedge t_i \wedge eq \wedge t_{(i+1)} \wedge \dots \wedge t_p"$$

returns a theorem of the form:

$$|- (?l_1 \dots l_j \dots l_r. t_1 \wedge \dots \wedge t_i \wedge eq \wedge t_{(i+1)} \wedge \dots \wedge t_p) =$$

$$(?l_1 \dots l_{(j-1)} l_{(j+1)} \dots l_r. t_1 \wedge \dots \wedge t_i \wedge t_{(i+1)} \wedge \dots \wedge t_p)$$

where eq has the form " $!y_1 \dots y_m. l_j \ x_1 \dots x_n = b$ " and l_j does not appear free in the t_i 's or in b . The conversion works if eq is not present, that is if l_j is not free in any of the conjuncts, but does not work if l_j appears free in more than one of the conjuncts. Each of m , n and p may be zero.

If there is more than one line with the specified name (but with different types), the one that appears outermost in the existential quantifications is pruned.

Failure

Fails if the argument term is not of the specified form or if l_j is free in more than one of the conjuncts or if the equation for l_j is recursive. The function also fails if the specified line is not one of the existentially quantified lines.

Example

```
#PRUNE_ONE_CONV 'l2' "?l2 l1. (!(x:num). l1 x = F) /\ (!x. l2 x = ~(l1 x))";;
|- (?l2 l1. (!x. l1 x = F) /\ (!x. l2 x = ~l1 x)) = (?l1. !x. l1 x = F)
```

```
#PRUNE_ONE_CONV 'l1' "?l2 l1. (!(x:num). l1 x = F) /\ (!x. l2 x = ~(l1 x))";;
evaluation failed      PRUNE_ONE_CONV
```

See also

`unwindLib.PRUNE_ONCE_CONV`, `unwindLib.PRUNE_SOME_CONV`, `unwindLib.PRUNE_CONV`,
`unwindLib.PRUNE_SOME_RIGHT_RULE`, `unwindLib.PRUNE_RIGHT_RULE`.

PRUNE_RIGHT_RULE

(unwindLib)

`PRUNE_RIGHT_RULE` : (thm -> thm)

Synopsis

Prunes all hidden variables.

Description

`PRUNE_RIGHT_RULE` behaves as follows:

$$\frac{A \text{ |- } !z_1 \dots z_r. \quad t = ?l_1 \dots l_r. t_1 \wedge \dots \wedge eqn_1 \wedge \dots \wedge eqn_r \wedge \dots \wedge t_p}{A \text{ |- } !z_1 \dots z_r. t = t_1 \wedge \dots \wedge t_p}$$

where each eqn_i has the form " $!y_1 \dots y_m. l_i x_1 \dots x_n = b$ " and l_i does not appear free in any of the other conjuncts or in b . The rule works if one or more of the eqn_i 's are not present, that is if l_i is not free in any of the conjuncts, but does not work if l_i appears free in more than one of the conjuncts. p may be zero, that is, all the conjuncts may be eqn_i 's. In this case the result will be simply \top (true). Also, for each eqn_i , m and n may be zero.

Failure

Fails if the argument theorem is not of the specified form or if any of the l_i 's are free in more than one of the conjuncts or if the equation for any l_i is recursive.

Example

```
#PRUNE_RIGHT_RULE
# (ASSUME
#   "(in:num->bool) (out:num->bool).
#   DEV (in,out) =
#     (?l1:num->bool) l2.
#     (!x. l1 x = F) /\ (!x. l2 x = ~(in x)) /\ (!x. out x = ~(in x))");;
. |- !in out. DEV(in,out) = (!x. out x = ~in x)
```

See also

unwindLib.PRUNE_SOME_RIGHT_RULE, unwindLib.PRUNE_ONCE_CONV,
unwindLib.PRUNE_ONE_CONV, unwindLib.PRUNE_SOME_CONV, unwindLib.PRUNE_CONV.

PRUNE_SOME_CONV

(unwindLib)

PRUNE_SOME_CONV : (string list -> conv)

Synopsis

Prunes several hidden variables.

Description

PRUNE_SOME_CONV [l_{i1} ;...; l_{ik}] when applied to the term:

" $?l_1 \dots l_r. t_1 \wedge \dots \wedge eq_{n1} \wedge \dots \wedge eq_{nk} \wedge \dots \wedge t_p$ "

returns a theorem of the form:

$$|- (?l_1 \dots l_r. t_1 \wedge \dots \wedge eq_{n1} \wedge \dots \wedge eq_{nk} \wedge \dots \wedge t_p) =$$

$$(?l_{i(k+1)} \dots l_{ir}. t_1 \wedge \dots \wedge t_p)$$

where for $1 \leq j \leq k$, each eq_{nj} has the form:

" $!y_1 \dots y_m. l_{ij} x_1 \dots x_n = b$ "

and l_{ij} does not appear free in any of the other conjuncts or in b . The l_i 's are related by the equation:

$$\{\{l_{i1}, \dots, l_{ik}\}\} \cup \{\{l_{i(k+1)}, \dots, l_{ir}\}\} = \{\{l_1, \dots, l_r\}\}$$

The conversion works if one or more of the eq_{nij} 's are not present, that is if l_{ij} is not free in any of the conjuncts, but does not work if l_{ij} appears free in more than one of the conjuncts. p may be zero, that is, all the conjuncts may be eq_{nij} 's. In this case the body of the result will be \top (true). Also, for each eq_{nij} , m and n may be zero.

If there is more than one line with a specified name (but with different types), the one that appears outermost in the existential quantifications is pruned. If such a line name is mentioned twice in the list, the two outermost occurrences of lines with that name will be pruned, and so on.

Failure

Fails if the argument term is not of the specified form or if any of the l_{ij} 's are free in more than one of the conjuncts or if the equation for any l_{ij} is recursive. The function also fails if any of the specified lines are not one of the existentially quantified lines.

Example

```
#PRUNE_SOME_CONV ['l1'; 'l2']
# "?l3 l2 l1.
# (!x:num). l1 x = F) /\ (!x. l2 x = ~(l3 x)) /\ (!x:num). l3 x = T";;
|- (?l3 l2 l1. (!x. l1 x = F) /\ (!x. l2 x = ~l3 x) /\ (!x. l3 x = T)) =
    (?l3. !x. l3 x = T)
```

See also

`unwindLib.PRUNE_ONCE_CONV`, `unwindLib.PRUNE_ONE_CONV`, `unwindLib.PRUNE_CONV`,
`unwindLib.PRUNE_SOME_RIGHT_RULE`, `unwindLib.PRUNE_RIGHT_RULE`.

PRUNE_SOME_RIGHT_RULE

(unwindLib)

PRUNE_SOME_RIGHT_RULE : (string list -> thm -> thm)

Synopsis

Prunes several hidden variables.

Description

PRUNE_SOME_RIGHT_RULE ['l11'; ...; 'lik'] behaves as follows:

$$\begin{array}{l}
 A \mid- !z_1 \dots z_r. \\
 \quad t = ?l_1 \dots l_r. t_1 \wedge \dots \wedge eq_{n1} \wedge \dots \wedge eq_{nk} \wedge \dots \wedge t_p \\
 \hline
 A \mid- !z_1 \dots z_r. t = ?l_{i(k+1)} \dots l_{ir}. t_1 \wedge \dots \wedge t_p
 \end{array}$$

where for $1 \leq j \leq k$, each eq_{nij} has the form:

$$"!y_1 \dots y_m. l_{ij} x_1 \dots x_n = b"$$

and l_{ij} does not appear free in any of the other conjuncts or in b . The l_i 's are related by the equation:

$$\{\{l_{i1}, \dots, l_{ik}\}\} \cup \{\{l_{i(k+1)}, \dots, l_{ir}\}\} = \{\{l_1, \dots, l_r\}\}$$

The rule works if one or more of the eq_{nij} 's are not present, that is if l_{ij} is not free in any of the conjuncts, but does not work if l_{ij} appears free in more than one of the conjuncts. p may be zero, that is, all the conjuncts may be eq_{nij} 's. In this case the conjunction will be transformed to \top (true). Also, for each eq_{nij} , m and n may be zero.

If there is more than one line with a specified name (but with different types), the one that appears outermost in the existential quantifications is pruned. If such a line name is mentioned twice in the list, the two outermost occurrences of lines with that name will be pruned, and so on.

Failure

Fails if the argument theorem is not of the specified form or if any of the l_{ij} 's are free in more than one of the conjuncts or if the equation for any l_{ij} is recursive. The function also fails if any of the specified lines are not one of the existentially quantified lines.

Example

```
#PRUNE_SOME_RIGHT_RULE ['l1'; 'l2']
# (ASSUME
#   "(in:num->bool) (out:num->bool).
#   DEV (in,out) =
#     ?(l1:num->bool) l2.
#     (!x. l1 x = F) /\ (!x. l2 x = ~(in x)) /\ (!x. out x = ~(in x))");;
. |- !in out. DEV(in,out) = (!x. out x = ~in x)
```

See also

`unwindLib.PRUNE_RIGHT_RULE`, `unwindLib.PRUNE_ONCE_CONV`, `unwindLib.PRUNE_ONE_CONV`, `unwindLib.PRUNE_SOME_CONV`, `unwindLib.PRUNE_CONV`.

PSELECT_CONV

(PairRules)

PSELECT_CONV : conv

Synopsis

Eliminates a paired epsilon term by introducing a existential quantifier.

Description

The conversion PSELECT_CONV expects a boolean term of the form " $\tau[@p.\tau[p]/p]$ ", which asserts that the epsilon term $@p.\tau[p]$ denotes a pair, p say, for which $\tau[p]$ holds. This assertion is equivalent to saying that there exists such a pair, and PSELECT_CONV applied to a term of this form returns the theorem $\vdash \tau[@p.\tau[p]/p] = ?p.\tau[p]$.

Failure

Fails if applied to a term that is not of the form " $p[@p.\tau[p]/p]$ ".

See also

Conv.SELECT_CONV, PairRules.PSELECT_ELIM, PairRules.PSELECT_INTRO, PairRules.PSELECT_RULE.

PSELECT_ELIM

(PairRules)

PSELECT_ELIM : thm -> term * thm -> thm

Synopsis

Eliminates a paired epsilon term, using deduction from a particular instance.

Description

PSELECT_ELIM expects two arguments, a theorem $th1$, and a pair $(p,th2) : term * thm$. The conclusion of $th1$ must have the form $P(\$@ P)$, which asserts that the epsilon term $@ P$ denotes some value at which P holds. The paired variable structure p appears only in the assumption $P p$ of the theorem $th2$. The conclusion of the resulting theorem matches that of $th2$, and the hypotheses include the union of all hypotheses of the premises excepting $P p$.

$$\frac{A1 \vdash P(\$@ P) \quad A2 \cup \{P p\} \vdash t}{A1 \cup A2 \vdash t} \text{ PSELECT_ELIM } th1 (p, th2)$$

where p is not free in $A2$. If p appears in the conclusion of $th2$, the epsilon term will NOT be eliminated, and the conclusion will be $t [P/p]$.

Failure

Fails if the first theorem is not of the form $A1 \mid- P(P)$, or if any of the variables from the variable structure p occur free in any other assumption of $th2$.

See also

`Drule.SELECT_ELIM`, `PairRules.PCHOOSE`, `PairRules.PSELECT_CONV`,
`PairRules.PSELECT_INTRO`, `PairRules.PSELECT_RULE`.

PSELECT_EQ	(PairRules)
------------	-------------

`PSELECT_EQ` : (term -> thm -> thm)

Synopsis

Applies epsilon abstraction to both terms of an equation.

Description

When applied to a paired structure of variables p and a theorem whose conclusion is equational:

$$A \mid- t1 = t2$$

the inference rule `PSELECT_EQ` returns the theorem:

$$A \mid- (@p. t1) = (@p. t2)$$

provided no variable in p is free in the assumptions.

$$\frac{A \mid- t1 = t2}{A \mid- (@p. t1) = (@p. t2)} \quad \text{SELECT_EQ "p"} \quad [\text{where } p \text{ is not free in } A]$$

Failure

Fails if the conclusion of the theorem is not an equation, or if p is not a paired structure of variables, or if any variable in p is free in A .

See also

`Drule.SELECT_EQ`, `PairRules.PFORALL_EQ`, `PairRules.PEXISTS_EQ`.

PSELECT_INTRO

(PairRules)

PSELECT_INTRO : (thm -> thm)

Synopsis

Introduces an epsilon term.

Description

PSELECT_INTRO takes a theorem with an applicative conclusion, say $P\ x$, and returns a theorem with the epsilon term $\$@ P$ in place of the original operand x .

$$\frac{A \mid- P\ x}{A \mid- P(\$@ P)} \quad \text{PSELECT_INTRO}$$

The returned theorem asserts that $\$@ P$ denotes some value at which P holds.

Failure

Fails if the conclusion of the theorem is not an application.

Comments

This function is exactly the same as SELECT_INTRO, it is duplicated in the pair library for completeness.

See also

Drule.SELECT_INTRO, PairRules.PEXISTS, PairRules.PSELECT_CONV, PairRules.PSELECT_ELIM, PairRules.PSELECT_RULE.

PSELECT_RULE

(PairRules)

PSELECT_RULE : (thm -> thm)

Synopsis

Introduces a paired epsilon term in place of a paired existential quantifier.

Description

The inference rule PSELECT_RULE expects a theorem asserting the existence of a pair p such that τ holds. The equivalent assertion that the epsilon term $@p.\tau$ denotes a pair p for which τ holds is returned as a theorem.

$$\frac{A \vdash ?p. t}{A \vdash t[(\lambda p.t)/p]} \quad \text{PSELECT_RULE}$$
Failure

Fails if applied to a theorem the conclusion of which is not a paired existential quantifier.

See also

Drule.SELECT_RULE, PairRules.PCHOOSE, PairRules.PSELECT_CONV, PairRules.PEXISTS_CONV, PairRules.PSELECT_ELIM, PairRules.PSELECT_INTRO.

<div data-bbox="234 788 587 840" data-label="Text"> <p>PSKOLEM_CONV</p> </div>	<div data-bbox="1086 788 1410 840" data-label="Text"> <p>(PairRules)</p> </div>
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PSKOLEM_CONV : conv

Synopsis

Proves the existence of a pair of Skolem functions.

Description

When applied to an argument of the form $!p_1 \dots p_n. ?q. tm$, the conversion PSKOLEM_CONV returns the theorem:

$$\vdash (!p_1 \dots p_n. ?q. tm) = (?q'. !p_1 \dots p_n. tm[q' p_1 \dots p_n/yq])$$

where q' is a primed variant of the pair q not free in the input term.

Failure

PSKOLEM_CONV tm fails if tm is not a term of the form $!p_1 \dots p_n. ?q. tm$.

Example

Both q and any p_i may be a paired structure of variables:

```
- PSKOLEM_CONV
  (Term '(x11:'a,x12:'a) (x21:'a,x22:'a).
    ?(y1:'a,y2:'a). tm x11 x12 x21 x21 y1 y2');

> val it =
  |- (! (x11,x12) (x21,x22). ?(y1,y2). tm x11 x12 x21 x21 y1 y2) =
    ?(y1,y2).
      ! (x11,x12) (x21,x22).
        tm x11 x12 x21 x21 (y1 (x11,x12) (x21,x22)) (y2 (x11,x12) (x21,x22))
    : thm
```

See also

Conv.SKOLEM_CONV, PairRules.P_PSKOLEM_CONV.

PSPEC	(PairRules)
-------	-------------

PSPEC : (term -> thm -> thm)

Synopsis

Specializes the conclusion of a theorem.

Description

When applied to a term q and a theorem $A \vdash !p. t$, then PSPEC returns the theorem $A \vdash t[q/p]$. If necessary, variables will be renamed prior to the specialization to ensure that q is free for p in t , that is, no variables free in q become bound after substitution.

$$\frac{A \vdash !p. t}{A \vdash t[q/p]} \text{ PSPEC "q"}$$
Failure

Fails if the theorem's conclusion is not a paired universal quantification, or if p and q have different types.

Example

PSPEC specialised paired quantifications.

```
- PSPEC (Term '(1,2)') (ASSUME (Term '! (x,y). (x + y) = (y + x)'));
> val it = [...] |- 1 + 2 = 2 + 1 : thm
```

PSPEC treats paired structures of variables as variables and preserves structure accordingly.

```
- PSPEC (Term 'x:'a#'a') (ASSUME (Term '! (x:'a,y:'a). (x,y) = (x,y)'));
> val it = [...] |- x = x : thm
```

See also

Thm.SPEC, PairRules.IPSPEC, PairRules.PSPECL, PairRules.PSPEC_ALL, PairRules.PGEN, PairRules.PGENL.

PSPEC_ALL	(PairRules)
-----------	-------------

PSPEC_ALL : (thm -> thm)

Synopsis

Specializes the conclusion of a theorem with its own quantified pairs.

Description

When applied to a theorem $A \vdash !p_1 \dots p_n. t$, the inference rule PSPEC_ALL returns the theorem $A \vdash t[p_1'/p_1] \dots [p_n'/p_n]$ where the p_i' are distinct variants of the corresponding p_i , chosen to avoid clashes with any variables free in the assumption list and with the names of constants. Normally p_i' is just p_i , in which case PSPEC_ALL simply removes all universal quantifiers.

$$\frac{A \vdash !p_1 \dots p_n. t}{A \vdash t[p_1'/x_1] \dots [p_n'/x_n]} \text{ PSPEC_ALL}$$

Failure

Never fails.

See also

Drule.SPEC_ALL, PairRules.PGEN, PairRules.PGENL, PairRules.PGEN_TAC, PairRules.PSPEC, PairRules.PSPEC_L, PairRules.PSPEC_TAC.

PSPEC_PAIR	(PairRules)
------------	-------------

PSPEC_PAIR : thm -> term * thm

Synopsis

Specializes the conclusion of a theorem, returning the chosen variant.

Description

When applied to a theorem $A \vdash !p. t$, the inference rule PSPEC_PAIR returns the term q' and the theorem $A \vdash t[q'/p]$, where q' is a variant of p chosen to avoid free variable capture.

$$\frac{A \mid - !p. \tau}{A \mid - \tau[q'/q]} \text{ PSPEC_PAIR}$$

Failure

Fails unless the theorem's conclusion is a paired universal quantification.

Comments

This rule is very similar to plain PSPEC, except that it returns the variant chosen, which may be useful information under some circumstances.

See also

Drule.SPEC_VAR, PairRules.PGEN, PairRules.PGENL, PairRules.PGEN_TAC, PairRules.PSPEC, PairRules.PSPECL, PairRules.PSPEC_ALL.

PSPEC_TAC

(PairRules)

PSPEC_TAC : term * term -> tactic

Synopsis

Generalizes a goal.

Description

When applied to a pair of terms (q,p), where p is a paired structure of variables and a goal $A \text{ ?- } \tau$, the tactic PSPEC_TAC generalizes the goal to $A \text{ ?- } !p. \tau[p/q]$, that is, all components of q are turned into the corresponding components of p.

$$\frac{A \text{ ?- } \tau}{A \text{ ?- } !x. \tau[p/q]} \text{ PSPEC_TAC } (q,p)$$

Failure

Fails unless p is a paired structure of variables with the same type as q.

Example

```

- g '1 + 2 = 2 + 1';
> val it =
  Proof manager status: 1 proof.
  1. Incomplete:
    Initial goal:
    1 + 2 = 2 + 1

- e (PSPEC_TAC (Term '(1,2)', Term '(x:num,y:num)'));
OK..
1 subgoal:
> val it =
  !(x,y). x + y = y + x

  : proof

```

Uses

Removing unnecessary speciality in a goal, particularly as a prelude to an inductive proof.

See also

PairRules.PGEN, PairRules.PGENL, PairRules.PGEN_TAC, PairRules.PSPEC, PairRules.PSPECL, PairRules.PSPEC_ALL, PairRules.PSTRIP_TAC.

PSPECL	(PairRules)
--------	-------------

PSPECL : (term list -> thm -> thm)

Synopsis

Specializes zero or more pairs in the conclusion of a theorem.

Description

When applied to a term list $[q_1; \dots; q_n]$ and a theorem $A \vdash !p_1 \dots p_n. t$, the inference rule SPECL returns the theorem $A \vdash t[q_1/p_1] \dots [q_n/p_n]$, where the substitutions are made sequentially left-to-right in the same way as for PSPEC.

$$\frac{A \vdash !p_1 \dots p_n. t}{A \vdash t[q_1/p_1] \dots [q_n/p_n]} \text{ SPECL } "[q_1; \dots; q_n]"$$

It is permissible for the term-list to be empty, in which case the application of PSPECL has no effect.

Failure

Fails unless each of the terms is of the same type as that of the appropriate quantified variable in the original theorem. Fails if the list of terms is longer than the number of quantified pairs in the theorem.

See also

Drule.SPECL, PairRules.PGEN, PairRules.PGENL, PairRules.PGEN_TAC, PairRules.PSPEC, PairRules.PSPEC_ALL, PairRules.PSPEC_TAC.

<div data-bbox="161 831 655 882" data-label="Text"> <p>PSTRIP_ASSUME_TAC</p> </div>	<div data-bbox="1011 831 1331 882" data-label="Text"> <p>(PairRules)</p> </div>
--	--

PSTRIP_ASSUME_TAC : thm_tactic

Synopsis

Splits a theorem into a list of theorems and then adds them to the assumptions.

Description

Given a theorem *th* and a goal (A, t) , PSTRIP_ASSUME_TAC *th* splits *th* into a list of theorems. This is done by recursively breaking conjunctions into separate conjuncts, cases-splitting disjunctions, and eliminating paired existential quantifiers by choosing arbitrary variables. Schematically, the following rules are applied:

$$\frac{A \text{ ?- } t}{\text{PSTRIP_ASSUME_TAC } (A' \text{ |- } v1 \wedge \dots \wedge vn)} A \text{ u } \{v1, \dots, vn\} \text{ ?- } t$$

$$\frac{A \text{ ?- } t}{\text{PSTRIP_ASSUME_TAC } (A' \text{ |- } v1 \vee \dots \vee vn)} A \text{ u } \{v1\} \text{ ?- } t \dots A \text{ u } \{vn\} \text{ ?- } t$$

$$\frac{A \text{ ?- } t}{\text{PSTRIP_ASSUME_TAC } (A' \text{ |- } ?p. v)} A \text{ u } \{v[p'/p]\} \text{ ?- } t$$

where *p'* is a variant of the pair *p*.

If the conclusion of *th* is not a conjunction, a disjunction or a paired existentially quantified term, the whole theorem *th* is added to the assumptions.

As assumptions are generated, they are examined to see if they solve the goal (either by being alpha-equivalent to the conclusion of the goal or by deriving a contradiction).

The assumptions of the theorem being split are not added to the assumptions of the goal(s), but they are recorded in the proof. This means that if A' is not a subset of the assumptions A of the goal (up to alpha-conversion), `PSTRIP_ASSUME_TAC (A' | -v)` results in an invalid tactic.

Failure

Never fails.

Uses

`PSTRIP_ASSUME_TAC` is used when applying a previously proved theorem to solve a goal, or when enriching its assumptions so that resolution, rewriting with assumptions and other operations involving assumptions have more to work with.

See also

`PairRules.PSTRIP_THM_THEN`, `PairRules.PSTRIP_ASSUME_TAC`,
`PairRules.PSTRIP_GOAL_THEN`, `PairRules.PSTRIP_TAC`.

PSTRIP_GOAL_THEN	(PairRules)
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`PSTRIP_GOAL_THEN : (thm_tactic -> tactic)`

Synopsis

Splits a goal by eliminating one outermost connective, applying the given theorem-tactic to the antecedents of implications.

Description

Given a theorem-tactic `ttac` and a goal (A, τ) , `PSTRIP_GOAL_THEN` removes one outermost occurrence of one of the connectives `!`, `==>`, `~` or `&` from the conclusion of the goal τ . If τ is a universally quantified term, then `PSTRIP_GOAL_THEN` strips off the quantifier. Note that `PSTRIP_GOAL_THEN` will strip off paired universal quantifications.

$$\begin{array}{l} A \text{ ?- } !p. u \\ \text{=====} \text{ PSTRIP_GOAL_THEN ttac} \\ A \text{ ?- } u[p'/p] \end{array}$$

where p' is a primed variant that contains no variables that appear free in the assumptions A . If τ is a conjunction, then `PSTRIP_GOAL_THEN` simply splits the conjunction into two subgoals:

$$\begin{array}{l} A \text{ ?- } v \wedge w \\ \text{===== PSTRIP_GOAL_THEN ttac} \\ A \text{ ?- } v \quad A \text{ ?- } w \end{array}$$

If t is an implication " $u \implies v$ " and if:

$$\begin{array}{l} A \text{ ?- } v \\ \text{===== ttac (u |- u)} \\ A' \text{ ?- } v' \end{array}$$

then:

$$\begin{array}{l} A \text{ ?- } u \implies v \\ \text{===== PSTRIP_GOAL_THEN ttac} \\ A' \text{ ?- } v' \end{array}$$

Finally, a negation $\sim t$ is treated as the implication $t \implies F$.

Failure

PSTRIP_GOAL_THEN ttac (A,t) fails if t is not a paired universally quantified term, an implication, a negation or a conjunction. Failure also occurs if the application of ttac fails, after stripping the goal.

Uses

PSTRIP_GOAL_THEN is used when manipulating intermediate results (obtained by stripping outer connectives from a goal) directly, rather than as assumptions.

See also

PairRules.PGEN_TAC, Tactic.STRIP_GOAL_THEN, PairRules.FILTER_PSTRIP_THEN, PairRules.PSTRIP_TAC, PairRules.FILTER_PSTRIP_TAC.

PSTRIP_TAC

(PairRules)

PSTRIP_TAC : tactic

Synopsis

Splits a goal by eliminating one outermost connective.

Description

Given a goal (A,t), PSTRIP_TAC removes one outermost occurrence of one of the connectives $!$, \implies , \sim or \wedge from the conclusion of the goal t . If t is a universally quantified term, then STRIP_TAC strips off the quantifier. Note that PSTRIP_TAC will strip off paired quantifications.

$$\begin{array}{l} A \text{ ?- } !p. u \\ \hline \text{PSTRIP_TAC} \\ A \text{ ?- } u[p'/p] \end{array}$$

where p' is a primed variant of the pair p that does not contain any variables that appear free in the assumptions A . If t is a conjunction, then `PSTRIP_TAC` simply splits the conjunction into two subgoals:

$$\begin{array}{l} A \text{ ?- } v \wedge w \\ \hline \text{PSTRIP_TAC} \\ A \text{ ?- } v \quad A \text{ ?- } w \end{array}$$

If t is an implication, `PSTRIP_TAC` moves the antecedent into the assumptions, stripping conjunctions, disjunctions and existential quantifiers according to the following rules:

$$\begin{array}{l} A \text{ ?- } v_1 \wedge \dots \wedge v_n \implies v \\ \hline A \text{ u } \{v_1, \dots, v_n\} \text{ ?- } v \end{array} \qquad \begin{array}{l} A \text{ ?- } v_1 \vee \dots \vee v_n \implies v \\ \hline A \text{ u } \{v_1\} \text{ ?- } v \dots A \text{ u } \{v_n\} \text{ ?- } v \end{array}$$

$$\begin{array}{l} A \text{ ?- } (?p. w) \implies v \\ \hline A \text{ u } \{w[p'/p]\} \text{ ?- } v \end{array}$$

where p' is a primed variant of the pair p that does not appear free in A . Finally, a negation $\sim t$ is treated as the implication $t \implies F$.

Failure

`PSTRIP_TAC (A, t)` fails if t is not a paired universally quantified term, an implication, a negation or a conjunction.

Uses

When trying to solve a goal, often the best thing to do first is `REPEAT PSTRIP_TAC` to split the goal up into manageable pieces.

See also

`PairRules.PGEN_TAC`, `PairRules.PSTRIP_GOAL_THEN`, `PairRules.FILTER_PSTRIP_THEN`, `Tactic.STRIP_TAC`, `PairRules.FILTER_PSTRIP_TAC`.

PSTRIP_THM_THEN

(PairRules)

`PSTRIP_THM_THEN` : `thm_tactical`

Synopsis

PSTRIP_THM_THEN applies the given theorem-tactic using the result of stripping off one outer connective from the given theorem.

Description

Given a theorem-tactic $ttac$, a theorem th whose conclusion is a conjunction, a disjunction or a paired existentially quantified term, and a goal (A, t) , STRIP_THM_THEN $ttac$ th first strips apart the conclusion of th , next applies $ttac$ to the theorem(s) resulting from the stripping and then applies the resulting tactic to the goal.

In particular, when stripping a conjunctive theorem $A' \vdash u \wedge v$, the tactic

$$ttac(u|-u) \text{ THEN } ttac(v|-v)$$

resulting from applying $ttac$ to the conjuncts, is applied to the goal. When stripping a disjunctive theorem $A' \vdash u \vee v$, the tactics resulting from applying $ttac$ to the disjuncts, are applied to split the goal into two cases. That is, if

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t1 \end{array} \quad ttac(u|-u) \quad \text{and} \quad \begin{array}{l} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t2 \end{array} \quad ttac(v|-v)$$

then:

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t1 \quad A \text{ ?- } t2 \end{array} \quad \text{PSTRIP_THM_THEN } ttac(A' \vdash u \vee v)$$

When stripping a paired existentially quantified theorem $A' \vdash \exists p. u$, the tactic resulting from applying $ttac$ to the body of the paired existential quantification, $ttac(u|-u)$, is applied to the goal. That is, if:

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t1 \end{array} \quad ttac(u|-u)$$

then:

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t1 \end{array} \quad \text{PSTRIP_THM_THEN } ttac(A' \vdash \exists p. u)$$

The assumptions of the theorem being split are not added to the assumptions of the goal(s) but are recorded in the proof. If A' is not a subset of the assumptions A of the goal (up to alpha-conversion), PSTRIP_THM_THEN $ttac$ th results in an invalid tactic.

Failure

PSTRIP_THM_THEN *ttac th* fails if the conclusion of *th* is not a conjunction, a disjunction or a paired existentially quantification. Failure also occurs if the application of *ttac* fails, after stripping the outer connective from the conclusion of *th*.

Uses

PSTRIP_THM_THEN is used to enrich the assumptions of a goal with a stripped version of a previously-proved theorem.

See also

Thm_cont.STRIP_THM_THEN, PairRules.PSTRIP_ASSUME_TAC, PairRules.PSTRIP_GOAL_THEN, PairRules.PSTRIP_TAC.

<div data-bbox="234 878 730 929" data-label="Text"> <p>PSTRUCT_CASES_TAC</p> </div>	<div data-bbox="1086 878 1412 929" data-label="Text"> <p>(PairRules)</p> </div>
---	---

PSTRUCT_CASES_TAC : thm_tactic

Synopsis

Performs very general structural case analysis.

Description

When it is applied to a theorem of the form:

$$th = A' \mid - ?p11\dots p1m. (x=t1) \wedge (B11 \wedge \dots \wedge B1k) \vee \dots \vee \\ ?pn1\dots pnp. (x=tn) \wedge (Bn1 \wedge \dots \wedge Bnp)$$

in which there may be no paired existential quantifiers where a ‘vector’ of them is shown above, PSTRUCT_CASES_TAC *th* splits a goal $A \text{ ?- } s$ into *n* subgoals as follows:

$$A \text{ ?- } s$$

=====

$$A \cup \{B11, \dots, B1k\} \text{ ?- } s[t1/x] \quad \dots \quad A \cup \{Bn1, \dots, Bnp\} \text{ ?- } s[tn/x]$$

that is, performs a case split over the possible constructions (the *t_i*) of a term, providing as assumptions the given constraints, having split conjoined constraints into separate assumptions. Note that unless *A'* is a subset of *A*, this is an invalid tactic.

Failure

Fails unless the theorem has the above form, namely a conjunction of (possibly multiply paired existentially quantified) terms which assert the equality of the same variable *x* and the given terms.

Uses

Generating a case split from the axioms specifying a structure.

See also

Tactic.STRUCT_CASES_TAC.

<div data-bbox="161 600 426 649" data-label="Text"> <p>PSUB_CONV</p> </div>	<div data-bbox="1011 600 1331 649" data-label="Text"> <p>(PairRules)</p> </div>
---	---

PSUB_CONV : (conv -> conv)

Synopsis

Applies a conversion to the top-level subterms of a term.

Description

For any conversion c , the function returned by `PSUB_CONV c` is a conversion that applies c to all the top-level subterms of a term. If the conversion c maps t to $\vdash t = t'$, then `SUB_CONV c` maps a paired abstraction $\backslash p.t$ to the theorem:

$$\vdash (\backslash p.t) = (\backslash p.t')$$

That is, `PSUB_CONV c` $\backslash p.t$ applies c to the body of the paired abstraction $\backslash p.t$. If c is a conversion that maps t_1 to the theorem $\vdash t_1 = t_1'$ and t_2 to the theorem $\vdash t_2 = t_2'$, then the conversion `PSUB_CONV c` maps an application $t_1 t_2$ to the theorem:

$$\vdash (t_1 t_2) = (t_1' t_2')$$

That is, `PSUB_CONV c` $t_1 t_2$ applies c to both the operator t_1 and the operand t_2 of the application $t_1 t_2$. Finally, for any conversion c , the function returned by `PSUB_CONV c` acts as the identity conversion on variables and constants. That is, if t is a variable or constant, then `PSUB_CONV c` t returns $\vdash t = t$.

Failure

`PSUB_CONV c tm` fails if tm is a paired abstraction $\backslash p.t$ and the conversion c fails when applied to t , or if tm is an application $t_1 t_2$ and the conversion c fails when applied to either t_1 or t_2 . The function returned by `PSUB_CONV c` may also fail if the ML function $c : \text{term} \rightarrow \text{thm}$ is not, in fact, a conversion (i.e. a function that maps a term t to a theorem $\vdash t = t'$).

See also

Conv.SUB_CONV, PairRules.PABS_CONV, Conv.RAND_CONV, Conv.RATOR_CONV.

Psyntax

Psyntax : Psyntax_sig

Synopsis

A structure that provides a tuple-style environment for term manipulation.

Description

Each function in the Psyntax structure has a corresponding “record version” in the Rsyntax structure, and vice versa. One can flip-flop between the two structures by opening one and then the other. One can also use long identifiers in order to use both syntaxes at once.

Failure

Never fails.

Example

The following shows how to open the Psyntax structure and the functions that subsequently become available in the top level environment. Documentation for each of these functions is available online.

```
- open Psyntax;
```

This command results in the following functions entering the top-level name-space. Term creation functions:

```
val mk_var = fn : string * hol_type -> term
val mk_const = fn : string * hol_type -> term
val mk_comb = fn : term * term -> term
val mk_abs = fn : term * term -> term
val mk_primed_var = fn : string * hol_type -> term
val mk_eq = fn : term * term -> term
val mk_imp = fn : term * term -> term
val mk_select = fn : term * term -> term
val mk_forall = fn : term * term -> term
val mk_exists = fn : term * term -> term
val mk_conj = fn : term * term -> term
val mk_disj = fn : term * term -> term
val mk_cond = fn : term * term * term -> term
val mk_let = fn : term * term -> term
```

Term “destructor” functions (i.e., those functions that pull a term apart, and reveal some of its internal structure):

```

val dest_var = fn : term -> string * hol_type
val dest_const = fn : term -> string * hol_type
val dest_comb = fn : term -> term * term
val dest_abs = fn : term -> term * term
val dest_eq = fn : term -> term * term
val dest_imp = fn : term -> term * term
val dest_select = fn : term -> term * term
val dest_forall = fn : term -> term * term
val dest_exists = fn : term -> term * term
val dest_conj = fn : term -> term * term
val dest_disj = fn : term -> term * term
val dest_cond = fn : term -> term * term * term
val dest_let = fn : term -> term * term

```

The lambda datatype for taking terms apart, which is the range of the `dest_term` function.

```

datatype lambda =
  VAR of string * hol_type
  | CONST of {Name : string, Thy : string, Ty : hol_type}
  | COMB of term * term
  | LAMB of term * term
val dest_term : term -> lambda

```

See also

Rsyntax.

<div data-bbox="159 1516 454 1565" data-label="Text">PTAUT_CONV</div>	<div data-bbox="1067 1516 1331 1565" data-label="Text">(tautLib)</div>
---	--

PTAUT_CONV : conv

Synopsis

Tautology checker. Proves closed propositional formulae true or false.

Description

Given a term of the form " $\forall x_1 \dots x_n. t$ " where t contains only Boolean constants, Boolean-valued variables, Boolean equalities, implications, conjunctions, disjunctions, negations and Boolean-valued conditionals, and all the variables in t appear

in $x_1 \dots x_n$, the conversion `PTAUT_CONV` proves the term to be either true or false, that is, one of the following theorems is returned:

```
|- (!x1 ... xn. t) = T
|- (!x1 ... xn. t) = F
```

This conversion also accepts propositional terms that are not fully universally quantified. However, for such a term, the conversion will only succeed if the term is valid.

Failure

Fails if the term is not of the form " $!x_1 \dots x_n. f[x_1, \dots, x_n]$ " where $f[x_1, \dots, x_n]$ is a propositional formula (except that the variables do not have to be universally quantified if the term is valid).

Example

```
#PTAUT_CONV ‘‘!x y z w. (((x \ / ~y) ==> z) /\ (z ==> ~w) /\ w) ==> y’’;
|- (!x y z w. (x \ / ~y ==> z) /\ (z ==> ~w) /\ w ==> y) = T
```

```
#PTAUT_CONV ‘‘(((x \ / ~y) ==> z) /\ (z ==> ~w) /\ w) ==> y’’;
|- (x \ / ~y ==> z) /\ (z ==> ~w) /\ w ==> y = T
```

```
#PTAUT_CONV ‘‘!x. x = T’’;
|- (!x. x = T) = F
```

```
#PTAUT_CONV ‘‘x = T’’;
Uncaught exception:
HOL_ERR
```

See also

`tautLib.PTAUT_PROVE`, `tautLib.PTAUT_TAC`, `tautLib.TAUT_CONV`.

PTAUT_PROVE

(`tautLib`)

`PTAUT_PROVE` : term -> thm

Synopsis

Tautology checker. Proves propositional formulae.

Description

Given a term that contains only Boolean constants, Boolean-valued variables, Boolean equalities, implications, conjunctions, disjunctions, negations and Boolean-valued conditionals, PTAUT_PROVE returns the term as a theorem if it is valid. The variables in the term may be universally quantified.

Failure

Fails if the term is not a valid propositional formula.

Example

```
#PTAUT_PROVE ‘‘!x y z w. (((x \ / ~y) ==> z) /\ (z ==> ~w) /\ w) ==> y’’;
|- !x y z w. (x \ / ~y ==> z) /\ (z ==> ~w) /\ w ==> y
```

```
#PTAUT_PROVE ‘‘(((x \ / ~y) ==> z) /\ (z ==> ~w) /\ w) ==> y’’;
|- (x \ / ~y ==> z) /\ (z ==> ~w) /\ w ==> y
```

```
#PTAUT_PROVE ‘‘!x. x = T’’;
```

Uncaught exception:

HOL_ERR

```
#PTAUT_PROVE ‘‘x = T’’;
```

Uncaught exception:

HOL_ERR

See also

tautLib.PTAUT_CONV, tautLib.PTAUT_TAC, tautLib.TAUT_PROVE.

PTAUT_TAC	(tautLib)
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PTAUT_TAC : tactic

Synopsis

Tautology checker. Proves propositional goals.

Description

Given a goal with a conclusion that contains only Boolean constants, Boolean-valued variables, Boolean equalities, implications, conjunctions, disjunctions, negations and

Boolean-valued conditionals, this tactic will prove the goal if it is valid. If all the variables in the conclusion are universally quantified, this tactic will also reduce an invalid goal to false.

Failure

Fails if the conclusion of the goal is not of the form $!x_1 \dots x_n. f[x_1, \dots, x_n]$ where $f[x_1, \dots, x_n]$ is a propositional formula (except that the variables do not have to be universally quantified if the goal is valid).

See also

`tautLib.PTAUT_CONV`, `tautLib.PTAUT_PROVE`, `tautLib.TAUT_TAC`.

PTREE_ADD_CONV

(`patriciaLib`)

`PTREE_ADD_CONV` : `conv`

Synopsis

Conversion for evaluating applications of `patricia$ADD`.

Description

The conversion `PTREE_ADD_CONV` evaluates terms of the form `t |+ (m,n)` where `t` is a well-formed Patricia tree (correctly constructed using `patricia$Empty`, `patricia$Leaf` and `patricia$Branch`) and `m` is a natural number literal.

Failure

The conversion will fail if the supplied term is not a suitable application of `patricia$ADD`.

Example

```
- patriciaLib.PTREE_ADD_CONV ‘‘Empty |+ (3, x:num)’‘;
> val it = |- <{}> |+ (3,x) = Leaf 3 x: thm

- DEPTH_CONV patriciaLib.PTREE_ADD_CONV ‘‘Empty |+ (3, 2) |+ (2,1)’‘;
> val it = |- <{}> |+ (3,2) |+ (2,1) = Branch 0 0 (Leaf 3 2) (Leaf 2 1): thm
```

See also

`patriciaLib.PTREE_CONV`.

PTREE_CONV

(patriciaLib)

PTREE_CONV : conv

Synopsis

Conversion for evaluating Patricia tree operations.

Description

The conversion PTREE_CONV evaluates Patricia tree operations such as ADD, ADD_LIST, REMOVE, SIZE, PEEK and FIND. These evaluations work for constants that are defined using Define_mk_ptree. When adding to, or removing from, a Patricia tree a new constant will be defined after patriciaLib.ptree_new_defn_depth operations. By default ptree_new_defn_depth is ~1, which means that new constants are never defined.

Example

Consider the following Patricia tree:

```
val ptree = Define_mk_ptree "ptree" (int_ptree_of_list [(1, '1'), (2, '2')]);
<<HOL message: Saved IS_PTREE theorem for new constant "ptree">>
val ptree = |- ptree = Branch 0 0 (Leaf 1 1) (Leaf 2 2): thm
```

Adding a list of updates expands into applications of ADD:

```
> real_time PTREE_CONV 'ptree |++ [(3,3); (4,4); (5,5); (6,6); (7,7)]';
realtime: 0.000s
val it =
  |- ptree |++ [(3,3); (4,4); (5,5); (6,6); (7,7)] =
  ptree |+ (3,3) |+ (4,4) |+ (5,5) |+ (6,6) |+ (7,7):
  thm
```

However, setting ptree_new_defn_depth will cause new definitions to be made:

```
> ptree_new_defn_depth := 2;
val it = (): unit
> real_time PTREE_CONV 'ptree |++ [(3,3); (4,4); (5,5); (6,6); (7,7)]';
<<HOL message: Defined new ptree: ptree1>>
<<HOL message: Defined new ptree: ptree2>>
realtime: 0.006s
val it = |- ptree |++ [(3,3); (4,4); (5,5); (6,6); (7,7)] = ptree2 |+ (7,7):
  thm
```

New definitions will also be made when removing elements:

```
> real_time PTREE_CONV ‘‘ptree2 \\ 6 \\ 5‘‘;
<<HOL message: Defined new ptree: ptree3>>
realtime: 0.001s
val it = |- ptree2 \\ 6 \\ 5 = ptree3: thm
```

Here, the conversion is not smart enough to work out that `ptree3` is the same as `ptree1`.

```
> (DEPTH_CONV PTREE_DEFN_CONV THENC EVAL) ‘‘ptree1 = ptree3‘‘;
val it = |- (ptree1 = ptree3) T: thm
```

Look-up behaves as expected:

```
> real_time PTREE_CONV ‘‘ptree1 ’ 2‘‘;
realtime: 0.001s
val it = |- ptree1 ’ 2 = SOME 2: thm
> real_time PTREE_CONV ‘‘ptree1 ’ 5‘‘;
realtime: 0.001s
val it = |- ptree1 ’ 5 = NONE: thm
```

Comments

The conversion `PTREE_CONV` is automatically added to the standard `compset`. Thus, `EVAL` will have the same behaviour when `patriciaLib` is loaded.

Run-times should be respectable when working with large Patricia trees. However, this is predicated on the assumption that relatively small numbers of updates are made following an initial application of `Define_mk_ptree`. In this sense, the Patricia tree development is best suited to situations where users require fast "read-only" look-up; where the work of building the look-up tree can be performed outside of the logic (i.e. in ML).

See also

`patriciaLib.Define_mk_ptree`, `patriciaLib.PTREE_DEFN_CONV`.

PTREE_DEFN_CONV	(patriciaLib)
-----------------	---------------

`PTREE_DEFN_CONV` : `conv`

Synopsis

Conversion for evaluating applications of `ADD` and `REMOVE` to Patricia tree constants.

Description

Given a constant c defined using `Define_mk_ptree`, the conversion `PTREE_DEFN_CONV` will evaluate term of the form $c, c \mid+ (k,x)$ and $c \mid\mid k$ where k is a natural number literal.

Example

```
- val ptree = Define_mk_ptree "ptree" (int_ptree_of_list [(1, '1'), (2, '2')]);
<<HOL message: Saved IS_PTREE theorem for new constant "ptree">>
val ptree = |- ptree = Branch 0 0 (Leaf 1 1) (Leaf 2 2): thm

- PTREE_DEFN_CONV 'ptree \ 1';
val it = |- ptree \ 1 = Leaf 2 2: thm

- PTREE_DEFN_CONV 'ptree \+ (3,3)';
val it =
  |- ptree \+ (3,3) =
  Branch 0 0 (Branch 1 1 (Leaf 3 3) (Leaf 1 1)) (Leaf 2 2):
  thm
```

Comments

The conversion `PTREE_DEFN_CONV` has limited uses and is mostly used internally by the conversion `PTREE_CONV`.

See also

`patriciaLib.Define_mk_ptree`, `patriciaLib.PTREE_CONV`.

PTREE_DEPTH_CONV	(patriciaLib)
------------------	---------------

`PTREE_DEPTH_CONV` : conv

Synopsis

Conversion for evaluating applications of `patricia$DEPTH`.

Description

The conversion `PTREE_DEPTH_CONV` evaluates terms of the form `DEPTH t` where t is a well-formed Patricia tree (constructed by `patricia$Empty`, `patricia$Leaf` and `patricia$Branch`).

Failure

The conversion will fail if the supplied term is not a suitable application of `patricia$DEPTH`.

Example

```

- patriciaLib.PTREE_DEPTH_CONV ‘‘DEPTH Empty‘‘;
> val it = |- DEPTH <{}> = 0: thm

- patriciaLib.PTREE_DEPTH_CONV ‘‘DEPTH (Branch 0 0 (Leaf 3 2) (Leaf 2 1))‘‘;
> val it = |- DEPTH (Branch 0 0 (Leaf 3 2) (Leaf 2 1)) = 2: thm

```

See also

patriciaLib.PTREE_CONV.

PTREE_EVERY_LEAF_CONV (patriciaLib)

PTREE_EVERY_LEAF_CONV : conv

Synopsis

Conversion for evaluating applications of `patricia$EVERY_LEAF`.

Description

The conversion `PTREE_EVERY_LEAF_CONV` evaluates terms of the form `EVERY_LEAF P t` where `t` is a well-formed Patricia tree (constructed by `patricia$Empty`, `patricia$Leaf` and `patricia$Branch`) and `P` is predicate.

Failure

The conversion will fail if the supplied term is not a suitable application of `patricia$EVERY_LEAF`.

Example

```

- patriciaLib.PTREE_EVERY_LEAF_CONV ‘‘EVERY_LEAF (=) Empty‘‘;
> val it = |- EVERY_LEAF $= <{}> <=> T: thm

- patriciaLib.PTREE_EVERY_LEAF_CONV ‘‘EVERY_LEAF (\x y. (x < 3) ==> (y = 1)) (Branch
> val it =
  |- EVERY_LEAF (\x y. x < 3 ==> (y = 1))
    (Branch 0 0 (Leaf 3 2) (Leaf 2 1)) <=> T:
  thm

- patriciaLib.PTREE_EVERY_LEAF_CONV ‘‘EVERY_LEAF (\x y. x < 2) (Branch 0 0 (Leaf 3
> val it =
  |- EVERY_LEAF (\x y. x < 2) (Branch 0 0 (Leaf 3 2) (Leaf 2 1)) <=> F:
  thm

```

See also

patriciaLib.PTREE_CONV.

PTREE_EXISTS_LEAF_CONV	(patriciaLib)
------------------------	---------------

PTREE_EXISTS_LEAF_CONV : conv

Synopsis

Conversion for evaluating applications of patricia\$EXISTS_LEAF.

Description

The conversion PTREE_EXISTS_LEAF_CONV evaluates terms of the form EXISTS_LEAF P t where t is a well-formed Patricia tree (constructed by patricia\$Empty, patricia\$Leaf and patricia\$Branch) and P is predicate.

Failure

The conversion will fail if the supplied term is not a suitable application of patricia\$EXISTS_LEAF.

Example

```

- patriciaLib.PTREE_EXISTS_LEAF_CONV 'EXISTS_LEAF (=) Empty';
> val it = |- EXISTS_LEAF $= <{}> <=> F: thm

- patriciaLib.PTREE_EXISTS_LEAF_CONV 'EXISTS_LEAF (\x y. y = 2) (Branch 0 0 (Leaf 3 2))';
> val it =
  |- EXISTS_LEAF (\x y. y = 2) (Branch 0 0 (Leaf 3 2) (Leaf 2 1)) <=> T:
  thm

- patriciaLib.PTREE_EXISTS_LEAF_CONV 'EXISTS_LEAF (\x y. y = 3) (Branch 0 0 (Leaf 3 2))';
> val it =
  |- EXISTS_LEAF (\x y. y = 3) (Branch 0 0 (Leaf 3 2) (Leaf 2 1)) <=> F:
  thm

```

See also

patriciaLib.PTREE_CONV.

PTREE_IN_PTREE_CONV	(patriciaLib)
---------------------	---------------

PTREE_IN_PTREE_CONV : conv

Synopsis

Conversion for evaluating applications of `patricia$IN_PTREE`.

Description

The conversion `PTREE_IN_PTREE_CONV` evaluates terms of the form `n IN_PTREE t` where `t` is a well-formed unit Patricia tree (constructed by `patricia$Empty`, `patricia$Leaf` and `patricia$Branch`) and `n` is a natural number literal.

Failure

The conversion will fail if the supplied term is not a suitable application of `patricia$IN_PTREE`.

Example

```
- patriciaLib.PTREE_IN_PTREE_CONV ‘‘1 IN_PTREE Empty‘‘;
> val it = |- 1 IN_PTREE <{}> <=> F: thm
```

```
- patriciaLib.PTREE_IN_PTREE_CONV ‘‘3 IN_PTREE (Branch 0 0 (Leaf 3 ()) (Leaf 2 ()))‘‘;
> val it = |- 3 IN_PTREE Branch 0 0 (Leaf 3 ()) (Leaf 2 ()) <=> T: thm
```

See also

`patriciaLib.PTREE_CONV`.

`PTREE_INSERT_PTREE_CONV` (patriciaLib)

`PTREE_INSERT_PTREE_CONV` : conv

Synopsis

Conversion for evaluating applications of `patricia$INSERT_PTREE`.

Description

The conversion `PTREE_INSERT_PTREE_CONV` evaluates terms of the form `m INSERT_PTREE_PTREE t` where `t` is a well-formed unit Patricia tree (correctly constructed using `patricia$Empty`, `patricia$Leaf` and `patricia$Branch`) and `m` is a natural number literal.

Failure

The conversion will fail if the supplied term is not a suitable application of `patricia$INSERT_PTREE`.

Example


```

- patriciaLib.PTREE_INSERT_PTREE_CONV ‘‘2 INSERT_PTREE Empty‘‘;
> val it = |- <{2}> = Leaf 2 (): thm

- DEPTH_CONV patriciaLib.PTREE_INSERT_PTREE_CONV ‘‘3 INSERT_PTREE 2 INSERT_PTREE Empty‘‘;
> val it = |- <{3; 2}> = Branch 0 0 (Leaf 3 ()) (Leaf 2 ()): thm

```

See also

patriciaLib.PTREE_CONV.

PTREE_IS_PTREE_CONV	(patriciaLib)
---------------------	---------------

PTREE_IS_PTREE_CONV : conv

Synopsis

Conversion for evaluating applications of `patricia$IS_PTREE`.

Description

The conversion `PTREE_IS_PTREE_CONV` evaluates terms of the form `IS_PTREE t` where `t` is any tree constructed by `patricia$Empty`, `patricia$Leaf` and `patricia$Branch`. Well-formed trees correspond with those that can be constructed by `patricia$ADD`.

Failure

The conversion will fail if the supplied term is not a suitable application of `patricia$IS_PTREE`.

Example

```

- patriciaLib.PTREE_IS_PTREE_CONV ‘‘IS_PTREE Empty‘‘;
> val it = |- IS_PTREE $= <{}> <=> T: thm

- patriciaLib.PTREE_IS_PTREE_CONV ‘‘IS_PTREE (Branch 0 0 (Leaf 3 2) (Leaf 2 1))‘‘;
> val it = |- IS_PTREE (Branch 0 0 (Leaf 3 2) (Leaf 2 1)) <=> T: thm

- patriciaLib.PTREE_IS_PTREE_CONV ‘‘IS_PTREE (Branch 0 0 (Leaf 3 2) (Leaf 1 1))‘‘;
> val it = |- IS_PTREE (Branch 0 0 (Leaf 3 2) (Leaf 1 1)) <=> F: thm

```

See also

patriciaLib.PTREE_CONV.

PTREE_PEEK_CONV

(patriciaLib)

PTREE_PEEK_CONV : conv

Synopsis

Conversion for evaluating applications of `patricia$PEEK`.

Description

The conversion `PTREE_PEEK_CONV` evaluates terms of the form `t ' m` where `t` is a well-formed Patricia tree (constructed by `patricia$Empty`, `patricia$Leaf` and `patricia$Branch`) and `m` is a natural number literal.

Failure

The conversion will fail if the supplied term is not a suitable application of `patricia$PEEK`.

Example

```
- patriciaLib.PTREE_PEEK_CONV 'Empty ' 3';
> val it = |- <{}> ' 3 = NONE: thm

- patriciaLib.PTREE_PEEK_CONV 'Branch 0 0 (Leaf 3 2) (Leaf 2 1) ' 3';
> val it = |- Branch 0 0 (Leaf 3 2) (Leaf 2 1) ' 3 = SOME 2: thm
```

See also

`patriciaLib.PTREE_CONV`.

PTREE_REMOVE_CONV

(patriciaLib)

PTREE_REMOVE_CONV : conv

Synopsis

Conversion for evaluating applications of `patricia$REMOVE`.

Description

The conversion `PTREE_REMOVE_CONV` evaluates terms of the form `t \ m` where `t` is a well-formed Patricia tree (constructed by `patricia$Empty`, `patricia$Leaf` and `patricia$Branch`) and `m` is a natural number literal.

Failure

The conversion will fail if the supplied term is not a suitable application of `patricia$REMOVE`.

Example

```
- patriciaLib.PTREE_REMOVE_CONV ‘‘Empty \\ 3‘‘;
> val it = |- <{}> \\ 3 = <{}>: thm
```

```
- patriciaLib.PTREE_REMOVE_CONV ‘‘Branch 0 0 (Leaf 3 2) (Leaf 2 1) \\ 3‘‘;
> val it = |- Branch 0 0 (Leaf 3 2) (Leaf 2 1) \\ 3 = Leaf 2 1: thm
```

See also

`patriciaLib.PTREE_CONV`.

PTREE_SIZE_CONV

(patriciaLib)

`PTREE_SIZE_CONV` : conv

Synopsis

Conversion for evaluating applications of `patricia$SIZE`.

Description

The conversion `PTREE_SIZE_CONV` evaluates terms of the form `SIZE t` where `t` is a well-formed Patricia tree (constructed by `patricia$Empty`, `patricia$Leaf` and `patricia$Branch`).

Failure

The conversion will fail if the supplied term is not a suitable application of `patricia$SIZE`.

Example

```
- patriciaLib.PTREE_SIZE_CONV ‘‘SIZE Empty‘‘;
> val it = |- SIZE <{}> = 0: thm
```

```
- patriciaLib.PTREE_SIZE_CONV ‘‘SIZE (Branch 0 0 (Leaf 3 2) (Leaf 2 1))‘‘;
> val it = |- SIZE (Branch 0 0 (Leaf 3 2) (Leaf 2 1)) = 2: thm
```

See also

`patriciaLib.PTREE_CONV`.

PTREE_TRANSFORM_CONV	(patriciaLib)
----------------------	---------------

```
PTREE_TRANSFORM_CONV : conv
```

Synopsis

Conversion for evaluating applications of `patricia$TRANSFORM`.

Description

The conversion `PTREE_TRANSFORM_CONV` evaluates terms of the form `TRANSFORM f t` where `t` is a well-formed Patricia tree (constructed by `patricia$Empty`, `patricia$Leaf` and `patricia$Branch`) and `f` is `map`.

Failure

The conversion will fail if the supplied term is not a suitable application of `patricia$TRANSFORM`.

Example

```
- patriciaLib.PTREE_TRANSFORM_CONV ‘‘TRANSFORM ODD Empty‘‘;
> val it = |- TRANSFORM ODD <{}> = <{}>: thm
```

```
- patriciaLib.PTREE_TRANSFORM_CONV ‘‘TRANSFORM ODD (Branch 0 0 (Leaf 3 2) (Leaf 2 1)) =
> val it =
  |- TRANSFORM ODD (Branch 0 0 (Leaf 3 2) (Leaf 2 1)) =
    Branch 0 0 (Leaf 3 F) (Leaf 2 T):
  thm
```

See also

`patriciaLib.PTREE_CONV`.

PURE_ASM_REWRITE_RULE	(Rewrite)
-----------------------	-----------

```
PURE_ASM_REWRITE_RULE : (thm list -> thm -> thm)
```

Synopsis

Rewrites a theorem including the theorem's assumptions as rewrites.

Description

The list of theorems supplied by the user and the assumptions of the object theorem are used to generate a set of rewrites, without adding implicitly the basic tautologies stored under `basic_rewrites`. The rule searches for matching subterms in a top-down recursive fashion, stopping only when no more rewrites apply. For a general description of rewriting strategies see `GEN_REWRITE_RULE`.

Failure

Rewriting with `PURE_ASM_REWRITE_RULE` does not result in failure. It may diverge, in which case `PURE_ONCE_ASM_REWRITE_RULE` may be used.

See also

`Rewrite.ASM_REWRITE_RULE`, `Rewrite.GEN_REWRITE_RULE`, `Rewrite.ONCE_REWRITE_RULE`, `Rewrite.PURE_REWRITE_RULE`, `Rewrite.PURE_ONCE_ASM_REWRITE_RULE`.

PURE_ASM_REWRITE_TAC

(Rewrite)

`PURE_ASM_REWRITE_TAC` : (thm list -> tactic)

Synopsis

Rewrites a goal including the goal's assumptions as rewrites.

Description

`PURE_ASM_REWRITE_TAC` generates a set of rewrites from the supplied theorems and the assumptions of the goal, and applies these in a top-down recursive manner until no match is found. See `GEN_REWRITE_TAC` for more information on the group of rewriting tactics.

Failure

`PURE_ASM_REWRITE_TAC` does not fail, but it can diverge in certain situations. For limited depth rewriting, see `PURE_ONCE_ASM_REWRITE_TAC`. It can also result in an invalid tactic.

Uses

To advance or solve a goal when the current assumptions are expected to be useful in reducing the goal.

See also

`Rewrite.ASM_REWRITE_TAC`, `Rewrite.GEN_REWRITE_TAC`, `Rewrite.FILTER_ASM_REWRITE_TAC`, `Rewrite.FILTER_ONCE_ASM_REWRITE_TAC`, `Rewrite.ONCE_ASM_REWRITE_TAC`, `Rewrite.ONCE_REWRITE_TAC`, `Rewrite.PURE_ONCE_ASM_REWRITE_TAC`,

Rewrite.PURE_ONCE_REWRITE_TAC, Rewrite.PURE_REWRITE_TAC, Rewrite.REWRITE_TAC,
Tactic.SUBST_TAC.

PURE_CASE_TAC

(BasicProvers)

PURE_CASE_TAC : tactic

Synopsis

Case splits on a term t that features in the goal as `case t of ...`

Description

BasicProvers.PURE_CASE_TAC searches the goal for an instance of `case t of ...`, and performs a `BasicProvers.Cases_on 't'`.

Failure

BasicProvers.PURE_CASE_TAC fails if there is no instance of `case t of ...` in the goal, where the `case` term is a case constant in the typebase and all the free variables of t are free in the goal.

See also

BasicProvers.CASE_TAC.

PURE_LIST_CONV

(listLib)

PURE_LIST_CONV : {{Aux_thms: thm list, Fold_thms: thm list}} -> conv

Synopsis

Proves theorems about list constants applied to `NIL`, `CONS`, `SNOC`, `APPEND`, `FLAT` and `REVERSE`.

Description

PURE_LIST_CONV takes a term of the form:

CONST1 ... (CONST2 ...) ...

where CONST1 and CONST2 are operators on lists and CONST2 returns a list result. It can be one of NIL, CONS, SNOG, APPEND, FLAT or REVERSE. The form of the resulting theorem depends on CONST1 and CONST2. Some auxiliary theorems must be provided about CONST1. PURE_LIST_CONV. These are passed as a record argument. The Fold_thms field of the record should hold a theorem defining the constant in terms of FOLDR or FOLDL. The definition should have the form:

|- CONST1 ...l... = fold f e l

where fold is either FOLDR or FOLDL, f is a function, e a base element and l a list variable. For example, a suitable theorem for SUM is

|- SUM l = FOLDR \$+ 0 l

Given this theorem, no auxiliary theorems and the term --'SUM (CONS x l)'--, a call to PURE_LIST_CONV returns the theorem:

|- SUM (CONS x l) = x + (SUM l)

The Aux_thms field of the record argument to PURE_LIST_CONV provides auxiliary theorems concerning the terms f and e found in the definition with respect to FOLDR or FOLDL. For example, given the theorem:

|- MONOID \$+ 0

and given the term --'SUM (APPEND l1 l2)'--, a call to PURE_LIST_CONV returns the theorem

|- SUM (APPEND l1 l2) = (SUM l1) + (SUM l2)

The following table shows the form of the theorem returned and the auxiliary theorems needed if CONST1 is defined in terms of FOLDR.

CONST2	side conditions	tm2 in result	- tm1 = tm2
=====	=====	=====	=====
[]	NONE	e	
[x]	NONE	f x e	
CONS x l	NONE	f x (CONST1 l)	
SNOG x l	e is a list variable	CONST1 (f x e) l	
APPEND l1 l2	e is a list variable	CONST1 (CONST1 l1) l2	
APPEND l1 l2	- FCOMM g f, - LEFT_ID g e	g (CONST1 l1) (CONST2 l2)	
FLAT l1	- FCOMM g f, - LEFT_ID g e, - CONST3 l = FOLDR g e l		CONST3 (MAP CONST1 l)
REVERSE l	- COMM f, - ASSOC f		CONST1 l
REVERSE l	f == (\x l. h (g x) l) - COMM h, - ASSOC h		CONST1 l

The following table shows the form of the theorem returned and the auxiliary theorems needed if `CONST1` is defined in terms of `FOLDL`.

CONST2	side conditions	tm2 in result	- tm1 = tm2
<code>[]</code>	<code>NONE</code>	<code>e</code>	
<code>[x]</code>	<code>NONE</code>	<code>f x e</code>	
<code>SNOC x l</code>	<code>NONE</code>	<code>f x (CONST1 l)</code>	
<code>CONS x l</code>	<code>e is a list variable</code>	<code>CONST1 (f x e) l</code>	
<code>APPEND l1 l2</code>	<code>e is a list variable</code>	<code>CONST1 (CONST1 l1) l2</code>	
<code>APPEND l1 l2</code>	<code> - FCOMM f g, - RIGHT_ID g e</code>	<code>g (CONST1 l1) (CONST2 l2)</code>	
<code>FLAT l1</code>	<code> - FCOMM f g, - RIGHT_ID g e, - - CONST3 l = FOLDR g e l</code>	<code>CONST3 (MAP CONST1 l)</code>	
<code>REVERSE l</code>	<code> - COMM f, - ASSOC f</code>	<code>CONST1 l</code>	
<code>REVERSE l</code>	<code>f == (\l x. h l (g x)) - COMM h, - ASSOC h</code>		<code>CONST1 l</code>

`|- MONOID f e` can be used instead of `|- FCOMM f f`, `|- LEFT_ID f` or `|- RIGHT_ID f`.
`|- ASSOC f` can also be used in place of `|- FCOMM f f`.

Example

```
- val SUM_FOLDR = theorem "list" "SUM_FOLDR";
val SUM_FOLDR = |- !l. SUM l = FOLDR $+ 0 l
- PURE_LIST_CONV
=   {{Fold_thms = [SUM_FOLDR], Aux_thms = []}} (--'SUM (CONS h t)');
|- SUM (CONS h t) = h + SUM t

- val SUM_FOLDL = theorem "list" "SUM_FOLDL";
val SUM_FOLDL = |- !l. SUM l = FOLDL $+ 0 l
- PURE_LIST_CONV
=   {{Fold_thms = [SUM_FOLDL], Aux_thms = []}} (--'SUM (SNOC h t)');
|- SUM (SNOC h t) = SUM t + h

- val MONOID_ADD_0 = theorem "arithmetic" "MONOID_ADD_0";
val MONOID_ADD_0 = |- MONOID $+ 0
- PURE_LIST_CONV
=   {{Fold_thms = [SUM_FOLDR], Aux_thms = [MONOID_ADD_0]}}
=   (--'SUM (APPEND l1 l2)');
|- SUM (APPEND l1 l2) = SUM l1 + SUM l2

- PURE_LIST_CONV
=   {{Fold_thms = [SUM_FOLDR], Aux_thms = [MONOID_ADD_0]}} (--'SUM (FLAT l)');
|- SUM (FLAT l) = SUM (MAP SUM l)
```


Failure

PURE_LIST_CONV *tm* fails if *tm* is not of the form described above. It also fails if no suitable fold definition for `CONST1` is supplied, or if the required auxiliary theorems as described above are not supplied.

See also

`listLib.LIST_CONV`, `listLib.X_LIST_CONV`.

PURE_ONCE_ASM_REWRITE_RULE	(Rewrite)
----------------------------	-----------

PURE_ONCE_ASM_REWRITE_RULE : (thm list -> thm -> thm)

Synopsis

Rewrites a theorem once, including the theorem's assumptions as rewrites.

Description

PURE_ONCE_ASM_REWRITE_RULE excludes the basic tautologies in `basic_rewrites` from the theorems used for rewriting. It searches for matching subterms once only, without recursing over already rewritten subterms. For a general introduction to rewriting tools see `GEN_REWRITE_RULE`.

Failure

PURE_ONCE_ASM_REWRITE_RULE does not fail and does not diverge.

See also

`Rewrite.ASM_REWRITE_RULE`, `Rewrite.GEN_REWRITE_RULE`,
`Rewrite.ONCE_ASM_REWRITE_RULE`, `Rewrite.ONCE_REWRITE_RULE`,
`Rewrite.PURE_ASM_REWRITE_RULE`, `Rewrite.PURE_REWRITE_RULE`, `Rewrite.REWRITE_RULE`.

PURE_ONCE_ASM_REWRITE_TAC	(Rewrite)
---------------------------	-----------

PURE_ONCE_ASM_REWRITE_TAC : (thm list -> tactic)

Synopsis

Rewrites a goal once, including the goal's assumptions as rewrites.

Description

A set of rewrites generated from the assumptions of the goal and the supplied theorems is used to rewrite the term part of the goal, making only one pass over the goal. The basic tautologies are not included as rewrite theorems. The order in which the given theorems are applied is an implementation matter and the user should not depend on any ordering. See `GEN_REWRITE_TAC` for more information on rewriting tactics in general.

Failure

`PURE_ONCE_ASM_REWRITE_TAC` does not fail and does not diverge.

Uses

Manipulation of the goal by rewriting with its assumptions, in instances where rewriting with tautologies and recursive rewriting is undesirable.

See also

`Rewrite.ASM_REWRITE_TAC`, `Rewrite.GEN_REWRITE_TAC`, `Rewrite.FILTER_ASM_REWRITE_TAC`, `Rewrite.FILTER_ONCE_ASM_REWRITE_TAC`, `Rewrite.ONCE_ASM_REWRITE_TAC`, `Rewrite.ONCE_REWRITE_TAC`, `Rewrite.PURE_ASM_REWRITE_TAC`, `Rewrite.PURE_ONCE_REWRITE_TAC`, `Rewrite.PURE_REWRITE_TAC`, `Rewrite.REWRITE_TAC`, `Tactic.SUBST_TAC`.

<code>PURE_ONCE_REWRITE_CONV</code>	<code>(Rewrite)</code>
-------------------------------------	------------------------

`PURE_ONCE_REWRITE_CONV` : (thm list -> conv)

Synopsis

Rewrites a term once with only the given list of rewrites.

Description

`PURE_ONCE_REWRITE_CONV` generates rewrites from the list of theorems supplied by the user, without including the tautologies given in `basic_rewrites`. The applicable rewrites are employed once, without entailing in a recursive search for matches over the term. See `GEN_REWRITE_CONV` for more details about rewriting strategies in HOL.

Failure

This rule does not fail, and it does not diverge.

See also

`Rewrite.GEN_REWRITE_CONV`, `Conv.ONCE_DEPTH_CONV`, `Rewrite.ONCE_REWRITE_CONV`, `Rewrite.PURE_REWRITE_CONV`, `Rewrite.REWRITE_CONV`.

PURE_ONCE_REWRITE_RULE	(Rewrite)
------------------------	-----------

PURE_ONCE_REWRITE_RULE : (thm list -> thm -> thm)

Synopsis

Rewrites a theorem once with only the given list of rewrites.

Description

PURE_ONCE_REWRITE_RULE generates rewrites from the list of theorems supplied by the user, without including the tautologies given in `basic_rewrites`. The applicable rewrites are employed once, without entailing in a recursive search for matches over the theorem. See `GEN_REWRITE_RULE` for more details about rewriting strategies in HOL.

Failure

This rule does not fail, and it does not diverge.

See also

`Rewrite.ASM_REWRITE_RULE`, `Rewrite.GEN_REWRITE_RULE`, `Conv.ONCE_DEPTH_CONV`, `Rewrite.ONCE_REWRITE_RULE`, `Rewrite.PURE_REWRITE_RULE`, `Rewrite.REWRITE_RULE`.

PURE_ONCE_REWRITE_TAC	(Rewrite)
-----------------------	-----------

PURE_ONCE_REWRITE_TAC : (thm list -> tactic)

Synopsis

Rewrites a goal using a supplied list of theorems, making one rewriting pass over the goal.

Description

PURE_ONCE_REWRITE_TAC generates a set of rewrites from the given list of theorems, and applies them at every match found through searching once over the term part of the goal, without recursing. It does not include the basic tautologies as rewrite theorems. The order in which the rewrites are applied is unspecified. For more information on rewriting tactics see `GEN_REWRITE_TAC`.

Failure

PURE_ONCE_REWRITE_TAC does not fail and does not diverge.

Uses

This tactic is useful when the built-in tautologies are not required as rewrite equations and recursive rewriting is not desired.

See also

Rewrite.ASM_REWRITE_TAC, Rewrite.GEN_REWRITE_TAC, Rewrite.FILTER_ASM_REWRITE_TAC, Rewrite.FILTER_ONCE_ASM_REWRITE_TAC, Rewrite.ONCE_ASM_REWRITE_TAC, Rewrite.ONCE_REWRITE_TAC, Rewrite.PURE_ASM_REWRITE_TAC, Rewrite.PURE_ONCE_ASM_REWRITE_TAC, Rewrite.PURE_REWRITE_TAC, Rewrite.REWRITE_TAC, Tactic.SUBST_TAC.

PURE_REWRITE_CONV	(Rewrite)
-------------------	-----------

PURE_REWRITE_CONV : (thm list -> conv)

Synopsis

Rewrites a term with only the given list of rewrites.

Description

This conversion provides a method for rewriting a term with the theorems given, and excluding simplification with tautologies in `basic_rewrites`. Matching subterms are found recursively, until no more matches are found. For more details on rewriting see `GEN_REWRITE_CONV`.

Uses

PURE_REWRITE_CONV is useful when the simplifications that arise by rewriting a theorem with `basic_rewrites` are not wanted.

Failure

Does not fail. May result in divergence, in which case `PURE_ONCE_REWRITE_CONV` can be used.

See also

Rewrite.GEN_REWRITE_CONV, Rewrite.ONCE_REWRITE_CONV, Rewrite.PURE_ONCE_REWRITE_CONV, Rewrite.REWRITE_CONV.

PURE_REWRITE_RULE	(Rewrite)
-------------------	-----------

PURE_REWRITE_RULE : (thm list -> thm -> thm)

Synopsis

Rewrites a theorem with only the given list of rewrites.

Description

This rule provides a method for rewriting a theorem with the theorems given, and excluding simplification with tautologies in `basic_rewrites`. Matching subterms are found recursively starting from the term in the conclusion part of the theorem, until no more matches are found. For more details on rewriting see `GEN_REWRITE_RULE`.

Uses

`PURE_REWRITE_RULE` is useful when the simplifications that arise by rewriting a theorem with `basic_rewrites` are not wanted.

Failure

Does not fail. May result in divergence, in which case `PURE_ONCE_REWRITE_RULE` can be used.

See also

`Rewrite.ASM_REWRITE_RULE`, `Rewrite.GEN_REWRITE_RULE`, `Rewrite.ONCE_REWRITE_RULE`, `Rewrite.PURE_ASM_REWRITE_RULE`, `Rewrite.PURE_ONCE_ASM_REWRITE_RULE`, `Rewrite.PURE_ONCE_REWRITE_RULE`, `Rewrite.REWRITE_RULE`.

PURE_REWRITE_TAC

(Rewrite)

`PURE_REWRITE_TAC` : (thm list -> tactic)

Synopsis

Rewrites a goal with only the given list of rewrites.

Description

`PURE_REWRITE_TAC` behaves in the same way as `REWRITE_TAC`, but without the effects of the built-in tautologies. The order in which the given theorems are applied is an implementation matter and the user should not depend on any ordering. For more information on rewriting strategies see `GEN_REWRITE_TAC`.

Failure

`PURE_REWRITE_TAC` does not fail, but it can diverge in certain situations; in such cases `PURE_ONCE_REWRITE_TAC` may be used.

Uses

This tactic is useful when the built-in tautologies are not required as rewrite equations. It is sometimes useful in making more time-efficient replacements according to equations for which it is clear that no extra reduction via tautology will be needed. (The difference in efficiency is only apparent, however, in quite large examples.)

PURE_REWRITE_TAC advances goals but solves them less frequently than REWRITE_TAC; to be precise, PURE_REWRITE_TAC only solves goals which are rewritten to "T" (i.e. TRUTH) without recourse to any other tautologies.

Example

It might be necessary, say for subsequent application of an induction hypothesis, to resist reducing a term $b = T$ to b .

```
- PURE_REWRITE_TAC [] ([], Term 'b = T');
> val it = ([([], 'b = T')], fn)
  : (term list * term) list * (thm list -> thm)

- REWRITE_TAC [] ([], Term 'b = T');
> val it = ([([], 'b')], fn)
  : (term list * term) list * (thm list -> thm)
```

See also

Rewrite.ASM_REWRITE_TAC, Rewrite.FILTER_ASM_REWRITE_TAC,
 Rewrite.FILTER_ONCE_ASM_REWRITE_TAC, Rewrite.GEN_REWRITE_TAC,
 Rewrite.ONCE_ASM_REWRITE_TAC, Rewrite.ONCE_REWRITE_TAC,
 Rewrite.PURE_ASM_REWRITE_TAC, Rewrite.PURE_ONCE_ASM_REWRITE_TAC,
 Rewrite.PURE_ONCE_REWRITE_TAC, Rewrite.REWRITE_TAC, Tactic.SUBST_TAC.

pure_ss

(pureSimps)

```
pureSimps.pure_ss : simpset
```

Synopsis

A simpset containing only the conditional rewrite generator and no additional rewrites.

Description

This simpset sits at the root of the simpset hierarchy. It contains no rewrites, congruences, conversions or decision procedures. Instead it contains just the code which converts theorems passed to it as context into (possibly conditional) rewrites.

Simplification with `pure_ss` is analogous to rewriting with `PURE_REWRITE_TAC` and others. The only difference is that the theorems passed to `SIMP_TAC pure_ss` are interpreted as conditional rewrite rules. Though the `pure_ss` can't take advantage of extra contextual information garnered through congruences, it can still discharge side conditions. (This is demonstrated in the examples below.)

Failure

Can't fail, as it is not a functional value.

Example

The theorem `ADD_EQ_SUB` from `arithmeticTheory` states that

$$\vdash !m n p. n \leq p \implies ((m + n = p) = m = p - n)$$

We can use this result to make progress with the following goal in conjunction with `pure_ss` in a way that no form of `REWRITE_TAC` could:

```
- ASM_SIMP_TAC pure_ss [ADD_EQ_SUB] ([--'x <= y'--], --'z + x = y'--);
> val it = ([(['x <= y'], 'z = y - x')], fn) : tactic_result
```

This example illustrates the way in which the simplifier can do conditional rewriting. However, the lack of the congruence for implications means that using `pure_ss` will not be able to discharge the side condition in the goal below:

```
- SIMP_TAC pure_ss [ADD_EQ_SUB] ([], --'x <= y ==> (z + x = y)'--);
> val it = ([([], 'x <= y ==> (z + x = y)')], fn) : tactic_result
```

As `bool_ss` has the relevant congruence included, it does make progress in the same situation:

```
- SIMP_TAC bool_ss [ADD_EQ_SUB] ([], --'x <= y ==> (z + x = y)'--);
> val it = ([([], 'x <= y ==> (z = y - x)')], fn) : tactic_result
```

Uses

The `pure_ss` simpset might be used in the most delicate simplification situations, or, mimicking the way it is used within the distribution itself, as a basis for the construction of other simpsets.

Comments

There is also a `pureSimps.PURE_ss ssfrag` value. Its usefulness is questionable.

See also

`boolSimps.bool_ss`, `Rewrite.PURE_REWRITE_TAC`, `simplib.SIMP_CONV`, `simplib.SIMP_TAC`.

pvariant**(pairSyntax)**

```
pvariant : (term list -> term -> term)
```

Synopsis

Modifies variable and constant names in a paired structure to avoid clashes.

Description

When applied to a list of (possibly paired structures of) variables to avoid clashing with, and a pair to modify, `pvariant` returns a variant of the pair. That is, it changes the names of variables and constants in the pair as intuitively as possible to make them distinct from any variables in the list, or any (non-hidden) constants. This is normally done by adding primes to the names.

The exact form of the altered names should not be relied on, except that the original variables will be unmodified unless they are in the list to avoid clashing with. Also note that if the same variable occurs more than one in the pair, then each instance of the variable will be modified in the same way.

Failure

`pvariant l p` fails if any term in the list `l` is not a paired structure of variables, or if `p` is not a paired structure of variables and constants.

Example

The following shows a case that exhibits most possible behaviours:

```
- pvariant [Term 'b:'a', Term '(c:'a,c':'a)']
           (Term '((a:'a,b:'a),(c:'a,b':'a,T,b:'a))');
val it = '(a,b''),c'',b',T',b'' : term
```

Uses

The function `pvariant` is extremely useful for complicated derived rules which need to rename pairs variable to avoid free variable capture while still making the role of the pair obvious to the user.

See also

`Term.variant`, `Term.genvar`.

Q_TAC

(Tactical)

Q_TAC : (term -> tactic) -> term quotation -> tactic

Synopsis

A tactical that parses in the context of a goal, a la the Q library.

Description

When applied to a term tactic T and a quotation q , the tactic $Q_TAC\ T\ q$ first parses the quotation q in the context of the goal to yield the term t_m , and then applies the tactic $T\ t_m$ to the goal.

Failure

The application of Q_TAC to a term tactic T and a quotation q never fails. The resulting composite tactic $Q_TAC\ T\ q$ fails when applied to a goal if either q cannot be parsed, or $T\ t_m$ fails when applied to the goal.

Comments

Useful for avoiding decorating terms with type abbreviations.

See also

Tactical.EVERY, Tactical.FIRST, Tactical.ORELSE, Tactical.THEN, Tactical.THEN1, Tactical.THENL.

QCHANGED_CONSEQ_CONV

(ConseqConv)

QCHANGED_CONSEQ_CONV : conseq_conv -> conseq_conv

Synopsis

Makes a consequence conversion fail if applying it raises the UNCHANGED exception.

See also

Conv.QCHANGED_CONV, ConseqConv.CHANGED_CONSEQ_CONV.

QCHANGED_CONV

(Conv)

QCHANGED_CONV : conv -> conv

Synopsis

Makes a conversion fail if applying it raises the `UNCHANGED` exception.

Description

If c is a conversion that maps a term t to a theorem $\vdash t = t'$, then so too is `QCHANGED_CONV c`. If c applied to t raises the special `UNCHANGED` exception used by conversions to indicate that they haven't changed an input, then `QCHANGED_CONV c` will fail when applied to t .

This behaviour is similar to that of `CHANGED_CONV`, except that that conversion also fails if the conversion c returns a theorem when applied to t , and if that theorem has alpha-convertible left and right hand sides.

Failure

`QCHANGED_CONV c t` fails if c applied t raises the `UNCHANGED` exception, or if c fails when applied to t .

Uses

`QCHANGED_CONV` can be used in places where `CHANGED_CONV` is appropriate, and where one knows that the conversion argument will not return an instance of reflexivity, or if one does not mind this occurring and not being trapped. Because it is no more than an exception handler, `QCHANGED_CONV` is very efficient.

See also

`Conv.CHANGED_CONV`.

<div data-bbox="236 1406 387 1458" data-label="Text"> <p><code>QCONV</code></p> </div>	<div data-bbox="1230 1406 1409 1458" data-label="Text"> <p><code>(Conv)</code></p> </div>
--	---

`QCONV : conv -> conv`

Synopsis

Stops a conversion raising the `UNCHANGED` exception

Description

If conversion c applied to term t raises the `UNCHANGED` exception, then `QCONV c t` instead returns the theorem $\vdash t = t$.

Failure

`QCONV c t` fails if the application of c to t fails.

See also

Conv.CHANGED_CONV, Conv.QCHANGED_CONV.

quadruple	(Lib)
-----------	-------

quadruple : 'a -> 'b -> 'c -> 'd -> 'a * 'b * 'c * 'd

Synopsis

Makes four values into a quadruple.

Description

quadruple x1 x2 x3 x4 returns (x1, x2, x3, x4).

Failure

Never fails.

See also

Lib.quadruple_of_list, Lib.pair, Lib.triple.

quadruple_of_list	(Lib)
-------------------	-------

quadruple_of_list : 'a list -> 'a * 'a * 'a * 'a

Synopsis

Turns a four-element list into a quadruple.

Description

quadruple_of_list [x1, x2, x3, x4] returns (x1, x2, x3, x4).

Failure

Fails if applied to a list that is not of length 4.

See also

Lib.singleton_of_list, Lib.pair_of_list, Lib.triple_of_list.

QUANT_CONSEQ_CONV

(ConseqConv)

QUANT_CONSEQ_CONV : (conseq_conv -> conseq_conv)

Synopsis

Applies a consequence conversion to the body of a existentially or universally quantified term.

See also

Conv.QUANT_CONV, ConseqConv.FORALL_CONSEQ_CONV, ConseqConv.EXISTS_CONSEQ_CONV.

QUANT_CONV

(Conv)

QUANT_CONV : conv -> conv

Synopsis

Applies a conversion underneath a quantifier.

Description

If `conv N` returns $A \mid - N = P$, then `QUANT_CONV conv (M (\v.N))` returns $A \mid - M (\v.N) = M (\v.P)$.

Failure

If `conv N` fails, or if v is free in A .

Example

```
- QUANT_CONV SYM_CONV (Term '!x. x + 0 = x');
> val it = |- (!x. x + 0 = x) = !x. x = x + 0 : thm
```

Comments

For deeply nested quantifiers, `STRIP_QUANT_CONV` and `STRIP_BINDER_CONV` are more efficient than iterated application of `QUANT_CONV`, `BINDER_CONV`, or `ABS_CONV`.

See also

Conv.BINDER_CONV, Conv.STRIP_QUANT_CONV, Conv.STRIP_BINDER_CONV, Conv.ABS_CONV.

quote

(Lib)

```
quote : string -> string
```

Synopsis

Put quotation marks around a string.

Description

An application `quote s` is equal to `"\" ^ s ^ "\"`. This is often useful when printing messages.

Failure

Never fails

Example

```
- print "foo\n";
foo
> val it = () : unit

- print (quote "foo" ^ "\n");
"foo"
> val it = () : unit
```

See also

`Lib.mlquote`.

r

(proofManagerLib)

```
r : int -> unit
```

Synopsis

Reorders the subgoals on top of the subgoal package goal stack.

Description

The function `r` is part of the subgoal package. The name `rotate` may also be used to access the same function. For a general description of the subgoal package, see `set_goal`.

The `r` function's basic step of operation is to take the first element of the current list of sub-goals and move it to the end of the same list. The numeric argument passed to `r` specifies how many times this operation is to be performed.

Failure

Raises the `NO_PROOFS` exception if there is no current proof manipulated by the subgoal package. Raises a `HOL_ERR` if the current goal state only has one sub-goal, or if the argument passed to `r` is negative.

Uses

Interactively attacking subgoals in a different order to that generated by the subgoal package.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`, `proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`, `proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`, `proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

Raise	(Feedback)
--------------	-------------------

`Raise : exn -> 'a`

Synopsis

Print an exception before re-raising it

Description

The `Raise` function prints out information about its argument exception before re-raising it. It uses the value of `ERR_to_string` to format the message, and prints the information on the outstream held in `ERR_outstream`.

Failure

Never fails, since it always succeeds in raising the supplied exception.

Example

```
- Raise (mk_HOL_ERR "Foo" "bar" "incomprehensible input");
```

```
Exception raised at Foo.bar:
incomprehensible input
! Uncaught exception:
! HOL_ERR
```

See also

Feedback, Feedback.ERR_to_string, Feedback.ERR_outstream, Lib.try, Lib.trye.

rand

(Term)

rand : term -> term

Synopsis

Returns the operand from a combination (function application).

Description

If M is a combination, i.e., has the form $(t_1 t_2)$, then `rand M` returns t_2 .

Failure

Fails if M is not a combination.

See also

Term.rator, Term.dest_comb.

RAND_CONV

(Conv)

RAND_CONV : (conv -> conv)

Synopsis

Applies a conversion to the operand of an application.

Description

If c is a conversion that maps a term " t_2 " to the theorem $\vdash t_2 = t_2'$, then the conversion `RAND_CONV c` maps applications of the form " $t_1 t_2$ " to theorems of the form:

$$\vdash (t_1 t_2) = (t_1 t_2')$$

That is, `RAND_CONV c "t1 t2"` applies c to the operand of the application " $t_1 t_2$ ".

Failure

`RAND_CONV c tm` fails if tm is not an application or if tm has the form " $t_1 t_2$ " but the conversion c fails when applied to the term t_2 . The function returned by `RAND_CONV c` may also fail if the ML function $c:term \rightarrow thm$ is not, in fact, a conversion (i.e. a function that maps a term t to a theorem $\vdash t = t'$).

Example

```
- RAND_CONV numLib.num_CONV (Term 'SUC 2');
> val it = |- SUC 2 = SUC(SUC 1) : thm
```

See also

Conv.ABS_CONV, Conv.BINOP_CONV, Conv.LAND_CONV, Conv.RATOR_CONV, Conv.SUB_CONV.

<div data-bbox="234 658 387 703" data-label="Text"> <p>rator</p> </div>	<div data-bbox="1230 654 1414 705" data-label="Text"> <p>(Term)</p> </div>
---	--

rator : term -> term

Synopsis

Returns the operator from a combination (function application).

Description

If M is a combination, i.e., has the form $(t1\ t2)$, then `rator M` returns $t1$.

Failure

Fails if M is not a combination.

See also

Term.rand, Term.dest_comb.

<div data-bbox="234 1451 531 1503" data-label="Text"> <p>RATOR_CONV</p> </div>	<div data-bbox="1230 1449 1414 1503" data-label="Text"> <p>(Conv)</p> </div>
--	--

RATOR_CONV : (conv -> conv)

Synopsis

Applies a conversion to the operator of an application.

Description

If c is a conversion that maps a term " $t1$ " to the theorem $|- t1 = t1'$, then the conversion `RATOR_CONV c` maps applications of the form " $t1\ t2$ " to theorems of the form:

$$|- (t1\ t2) = (t1'\ t2)$$

That is, `RATOR_CONV c "t1 t2"` applies `c` to the operand of the application `"t1 t2"`.

Failure

`RATOR_CONV c tm` fails if `tm` is not an application or if `tm` has the form `"t1 t2"` but the conversion `c` fails when applied to the term `t1`. The function returned by `RATOR_CONV c` may also fail if the ML function `c:term->thm` is not, in fact, a conversion (i.e. a function that maps a term `t` to a theorem `|- t = t'`).

Example

```
- RATOR_CONV BETA_CONV (Term '(\x y. x + y) 1 2');
> val it = |- (\x y. x + y)1 2 = (\y. 1 + y) 2 : thm
```

See also

`Conv.ABS_CONV`, `Conv.RAND_CONV`, `Conv.SUB_CONV`.

<div data-bbox="159 1019 427 1068" data-label="Text"> <h1 style="margin: 0;">raw_match</h1> </div>	<div data-bbox="1155 1014 1331 1068" data-label="Text"> <h1 style="margin: 0;">(Term)</h1> </div>
--	---

```
raw_match : hol_type list -> term set
  -> term -> term
  -> (term,term) subst *
      ((hol_type,hol_type) subst * hol_type list)
  -> (term,term) subst *
      ((hol_type,hol_type) subst * hol_type list)
```

Synopsis

Primitive term matcher.

Description

The most primitive matching algorithm for HOL terms is `raw_match`. An invocation `raw_match avoid_tys avoid_tms pat ob (tmS,tyS)`, if it succeeds, returns a substitution pair `(S,T)` such that

$$\text{aconv (subst } S' \text{ (inst } T \text{ pat)) ob.}$$

where `S'` is `S` instantiated by `T`. The arguments `avoid_tys` and `avoid_tms` specify type and term variables in `pat` that are not allowed to become redexes in `S` and `T`.

The pair `(tmS,tyS)` is an accumulator argument. This allows `raw_match` to be folded through lists of terms to be matched. `(S,T)` must agree with `(tmS,tyS)`. This means that

if there is a $\{\text{redex}, \text{residue}\}$ in S and also a $\{\text{redex}, \text{residue}\}$ in $\text{tm}S$ so that both redex fields are equal, then the residue fields must be alpha-convertible. Similarly for types: if there is a $\{\text{redex}, \text{residue}\}$ in T and also a $\{\text{redex}, \text{residue}\}$ in $\text{ty}S$ so that both redex fields are equal, then the residue fields must also be equal. If these conditions hold, then the result (S, T) includes $(\text{tm}S, \text{ty}S)$.

Failure

`raw_match` will fail if no S and T meeting the above requirements can be found. If a match (S, T) between `pat` and `ob` can be found, but elements of `avoid_tys` would appear as redexes in T or elements of `avoid_tms` would appear as redexes in S , then `raw_match` will also fail.

Example

We first perform a match that requires type instantiations, and also alpha-convertibility.

```
- val (S,T) = raw_match [] empty_varset
      (Term '\x:'a. x = f (y:'b)')
      (Term '\a.    a = ~p') ([], ([], []));
> val S =
  [{redex = '(f :'b -> 'a)', residue = '$~',
   {redex = '(y :'b)',          residue = '(p :bool)'}] : ...

val T =
  ([{redex = ':'b', residue = ':bool'},
   {redex = ':'a', residue = ':bool'}], []) : ...
```

One of the main differences between `raw_match` and more refined derivatives of it, is that the returned substitutions are un-normalized by `raw_match`. If one naively applied (S, T) to `\x:'a. x = f (y:'b)`, type instantiation with T would be applied first, yielding `\x:bool. x = f (y:bool)`. Then substitution with S would be applied, unsuccessfully, since both f and y in the pattern term have been type instantiated, but the corresponding elements of the substitution haven't. Thus, higher level operations building on `raw_match` typically instantiate S by T to get S' before applying (S', T) to the pattern term. This can be achieved by using `norm_subst`. However, `raw_match` exposes this level of detail to the programmer.

The returned type substitution T has two components $(T1, T2)$. $T1$ is a substitution, and $T2$ is a list of type variables, encountered in the matching process, which have matched to themselves. These identity matches are held in the separate list $T2$ for obscure reasons. Once matching is finished, they can be ignored (which is why they are held on a separate list).

Comments

Higher level matchers are generally preferable, but `raw_match` is occasionally useful when programming inference rules.

See also

`Term.match_term`, `Term.match_term1`, `Term.norm_subst`, `Term.subst`, `Term.inst`, `Type.raw_match_type`, `Type.match_type`, `Type.match_type1`, `Type.type_subst`.

<div data-bbox="159 672 569 725" data-label="Text"> <h1 style="margin: 0;">raw_match_type</h1> </div>	<div data-bbox="1155 667 1331 725" data-label="Text"> <h1 style="margin: 0;">(Type)</h1> </div>
---	---

```
raw_match_type
  : hol_type list
    -> hol_type -> hol_type
    -> (hol_type,hol_type) subst * hol_type list
    -> (hol_type,hol_type) subst * hol_type list
```

Synopsis

Primitive type matching algorithm.

Description

An invocation `raw_match_type away pat ty (S,Id)` performs matching, just as `match_ty1`, except that it takes an extra accumulating parameter `(S,Id)`, which represents a 'raw' substitution that the match `(theta,id)` of `pat` and `ty` must be compatible with. If matching is successful, `(theta,id)` is merged with `(S,Id)` to yield the result.

Failure

A call to `raw_match_type away pat ty (S,Id)` will fail when `match_type1 away pat ty` would. It will also fail when a `{redex,residue}` calculated in the course of matching `pat` and `ty` is such that there is a `{redex_i,residue_i}` in `S` and `redex` equals `redex_i` but `residue` does not equal `residue_i`.

Example

```
- val res1 = raw_match_type [] alpha (alpha --> bool) ([],[]);
> val it = ([{redex = ':'a', residue = ':'a -> bool'}], []) : ...

- raw_match_type [] (alpha --> beta --> gamma)
  ((alpha --> bool) --> beta --> ind) res1;
> val it = ([{redex = ':'c', residue = ':ind'},
  {redex = ':'a', residue = ':'a -> bool'}], [':'b']) : ....
```

Comments

Probably exposes too much internal state of the matching algorithm.

See also

`Type.match_type`, `Type.match_type1`.

<code>read</code>	<code>(Tag)</code>
-------------------	--------------------

```
read : string -> tag
```

Synopsis

Make a tag suitable for use by `mk_oracle_thm`.

Description

In order to construct a tag usable by `mk_oracle_thm`, one uses `read`, which takes a string and makes it into a tag.

Failure

The string must be an alphanumeric, i.e., start with an alphabetic character and thereafter consist only of alphabetic or numeric characters.

Example

```
- Tag.read "Shamboozled";
> val it = Kerneltypes.TAG(["Shamboozled"], []) : tag
```

See also

`Thm.mk_oracle_thm`, `Thm.tag`.

<code>recInduct</code>	<code>(BasicProvers)</code>
------------------------	-----------------------------

```
recInduct : thm -> tactic
```

Synopsis

Induct with supplied recursion induction scheme.

Description

`bossLib.recInduct` is identical to `Induction.recInduct`.

See also

`bossLib.recInduct`.

<code>recInduct</code>

<code>(bossLib)</code>

```
recInduct : thm -> tactic
```

Synopsis

Performs recursion induction.

Description

An invocation `recInduct thm` on a goal `g`, where `thm` is typically an induction scheme returned from an invocation of `Define` or `Hol_defn`, attempts to match the consequent of `thm` to `g` and, if successful, then replaces `g` by the instantiated antecedents of `thm`. The order of quantification of the goal should correspond with the order of quantification in the conclusion of `thm`.

Failure

`recInduct` fails if the goal is not universally quantified in a way corresponding with the quantification of the conclusion of `thm`.

Example

Suppose we had introduced a function for incrementing a number until it no longer can be found in a given list:

```
variant x L = if MEM x L then variant (x + 1) L else x
```

Typically `Hol_defn` would be used to make such a definition, and some subsequent proof would be required to establish termination. Once that work was done, the specified recursion equations would be available as a theorem and, as well, a corresponding induction theorem would also be generated. In the case of `variant`, the induction theorem `variant_ind` is

```
|- !P. (!x L. (MEM x L ==> P (x + 1) L) ==> P x L) ==> !v v1. P v v1
```

Suppose now that we wish to prove that the variant with respect to a list is not in the list:

```
?- !x L. ~MEM (variant x L) L',
```

One could try mathematical induction, but that won't work well, since x gets incremented in recursive calls. Instead, induction with 'variant-induction' works much better. `recInduct` can be used to apply such theorems in tactic proof. For our example, `recInduct variant_ind` yields the goal

```
?- !x L. (MEM x L ==> ~MEM (variant (x + 1) L) L) ==> ~MEM (variant x L) L
```

A few simple tactic applications then prove this goal.

See also

`bossLib.Induct`, `bossLib.Induct_on`, `bossLib.completeInduct_on`,
`bossLib.measureInduct_on`, `Prim_rec.INDUCT_THEN`, `bossLib.Cases`,
`bossLib.Hol_datatype`, `proofManagerLib.g`, `proofManagerLib.e`.

RED_CONV	(reduceLib)
----------	-------------

```
RED_CONV : conv
```

Synopsis

Performs arithmetic or boolean reduction at top level if possible.

Description

The conversion `RED_CONV` attempts to apply, at the top level only, one of the following conversions from the `reduce` library (only one can succeed):

```
ADD_CONV  AND_CONV  BEQ_CONV  COND_CONV
DIV_CONV  EXP_CONV  GE_CONV   GT_CONV
IMP_CONV  LE_CONV   LT_CONV   MOD_CONV
MUL_CONV  NEQ_CONV  NOT_CONV  OR_CONV
PRE_CONV  SBC_CONV  SUC_CONV
```

Failure

Fails if none of the above conversions are applicable at top level.

Example

```
#RED_CONV "(2=3) = F";;
|- ((2 = 3) = F) = ~(2 = 3)
```

```
#RED_CONV "15 DIV 13";;
|- 15 DIV 13 = 1
```

```
#RED_CONV "100 + 100";;
|- 100 + 100 = 200
```

```
#RED_CONV "0 + x";;
evaluation failed      RED_CONV
```

See also

`reduceLib.REDUCE_CONV`, `reduceLib.REDUCE_RULE`, `reduceLib.REDUCE_TAC`.

REDEPTH_CONSEQ_CONV	(ConseqConv)
---------------------	--------------

`REDEPTH_CONSEQ_CONV` : `directed_conseq_conv -> directed_conseq_conv`

Synopsis

Similar to `DEPTH_CONSEQ_CONV`, but revisits modified subterms.

See also

`ConseqConv.DEPTH_CONSEQ_CONV`.

REDEPTH_CONV	(Conv)
--------------	--------

`REDEPTH_CONV` : `(conv -> conv)`

Synopsis

Applies a conversion bottom-up to all subterms, retraversing changed ones.

Description

`REDEPTH_CONV` *c tm* applies the conversion *c* repeatedly to all subterms of the term *tm* and recursively applies `REDEPTH_CONV` *c* to each subterm at which *c* succeeds, until there is no subterm remaining for which application of *c* succeeds.

More precisely, `REDEPTH_CONV c tm` repeatedly applies the conversion `c` to all the subterms of the term `tm`, including the term `tm` itself. The supplied conversion `c` is applied to the subterms of `tm` in bottom-up order and is applied repeatedly (zero or more times, as is done by `REPEATC`) to each subterm until it fails. If `c` is successfully applied at least once to a subterm, `t` say, then the term into which `t` is transformed is retraversed by applying `REDEPTH_CONV c` to it.

Failure

`REDEPTH_CONV c tm` never fails but can diverge if the conversion `c` can be applied repeatedly to some subterm of `tm` without failing.

Example

The following example shows how `REDEPTH_CONV` retraverses subterms:

```
- REDEPTH_CONV BETA_CONV (Term '(\f x. (f x) + 1) (\y.y) 2');
val it = |- (\f x. (f x) + 1)(\y. y)2 = 2 + 1 : thm
```

Here, `BETA_CONV` is first applied successfully to the (beta-redex) subterm:

```
(\f x. (f x) + 1) (\y.y)
```

This application reduces this subterm to:

```
(\x. ((\y.y) x) + 1)
```

`REDEPTH_CONV BETA_CONV` is then recursively applied to this transformed subterm, eventually reducing it to `(\x. x + 1)`. Finally, a beta-reduction of the top-level term, now the simplified beta-redex `(\x. x + 1) 2`, produces `2 + 1`.

Comments

The implementation of this function uses failure to avoid rebuilding unchanged subterms. That is to say, during execution the exception `QConv.UNCHANGED` may be generated and later trapped. The behaviour of the function is dependent on this use of failure. So, if the conversion given as an argument happens to generate the same exception, the operation of `REDEPTH_CONV` will be unpredictable.

See also

`Conv.DEPTH_CONV`, `Conv.ONCE_DEPTH_CONV`, `Conv.TOP_DEPTH_CONV`.

REDUCE_CONV	(numLib)
--------------------	-----------------

`REDUCE_CONV` : `conv`

Synopsis

Evaluate ground expressions involving arithmetic and boolean operations.

Description

An invocation `REDUCE_CONV M`, where `M` is a ground term made up of the standard boolean and numerical operators, uses deductive steps to perform any possible reductions, yielding the result `N`. The theorem $\vdash M = N$ is returned.

Failure

Never fails.

Example

```

- REDUCE_CONV (Term ' !x:num. x = x ');
> val it = |- (!x. x = x) = !x. T : thm

- REDUCE_CONV
  (Term '(y = (((2 + 4 - 1) * 5) ** 3) DIV 2) /\ (p \/ T ==> q)');
> val it =
  |- (y = ((2 + 4 - 1) * 5) ** 3 DIV 2) /\ (p \/ T ==> q) =
    (y = 7812) /\ q : thm

```

See also

`bossLib.EVAL`.

REDUCE_CONV**(reduceLib)**

`REDUCE_CONV` : conv

Synopsis

Performs arithmetic or boolean reduction at all levels possible.

Description

The conversion `REDUCE_CONV` attempts to apply, in bottom-up order to all suitable redexes, one of the following conversions from the `reduce` library (only one can succeed):

```

ADD_CONV  AND_CONV  BEQ_CONV  COND_CONV
DIV_CONV  EXP_CONV  GE_CONV   GT_CONV
IMP_CONV  LE_CONV   LT_CONV   MOD_CONV
MUL_CONV  NEQ_CONV  NOT_CONV  OR_CONV
PRE_CONV  SBC_CONV  SUC_CONV

```

In particular, it will prove the appropriate reduction for an arbitrarily complicated expression constructed from numerals and the boolean constants T and F.

Failure

Never fails, but may give a reflexive equation.

Example

```
#REDUCE_CONV "(2=3) = F";;
|- ((2 = 3) = F) = T
```

```
#REDUCE_CONV "(100 < 200) => (2 EXP (8 DIV 2)) | (3 EXP ((26 EXP 0) * 3))";;
|- (100 < 200 => 2 EXP (8 DIV 2) | 3 EXP ((26 EXP 0) * 3)) = 16
```

```
#REDUCE_CONV "(15 = 16) \\/ (15 < 16)";;
|- (15 = 16) \\/ 15 < 16 = T
```

```
#REDUCE_CONV "0 + x";;
|- 0 + x = 0 + x
```

See also

`reduceLib.RED_CONV`, `reduceLib.REDUCE_RULE`, `reduceLib.REDUCE_TAC`.

REDUCE_RULE	(reduceLib)
--------------------	--------------------

```
REDUCE_RULE : (thm -> thm)
```

Synopsis

Performs arithmetic or boolean reduction on a theorem at all levels possible.

Description

`REDUCE_RULE` attempts to transform a theorem by applying `REDUCE_CONV`.

Failure

Never fails, but may just return the original theorem.

Example

```
#REDUCE_RULE (ASSUME "x = (100 + (60 - 17))");;
. |- x = 143

#REDUCE_RULE (REFL "100 + 12 DIV 6");;
|- T
```

See also

reduceLib.RED_CONV, reduceLib.REDUCE_CONV, reduceLib.REDUCE_TAC.

<div data-bbox="159 745 456 797" data-label="Text"> <p>REDUCE_TAC</p> </div>	<div data-bbox="1011 745 1331 797" data-label="Text"> <p>(reduceLib)</p> </div>
---	---

REDUCE_TAC : tactic

Synopsis

Performs arithmetic or boolean reduction on a goal at all levels possible.

Description

REDUCE_TAC attempts to transform a goal by applying REDUCE_CONV. It will prove any true goal which is constructed from numerals and the boolean constants T and F.

Failure

Never fails, but may not advance the goal.

Example

The following example takes a couple of minutes' CPU time:

```
#g "((1 EXP 3) + (12 EXP 3) = 1729) /\ ((9 EXP 3) + (10 EXP 3) = 1729)";;
"((1 EXP 3) + (12 EXP 3) = 1729) /\ ((9 EXP 3) + (10 EXP 3) = 1729)"
```

```
() : void
```

```
#e REDUCE_TAC;;
```

```
OK..
```

```
goal proved
```

```
|- ((1 EXP 3) + (12 EXP 3) = 1729) /\ ((9 EXP 3) + (10 EXP 3) = 1729)
```

```
Previous subproof:
```

```
goal proved
```

```
() : void
```

See also

reduceLib.RED_CONV, reduceLib.REDUCE_CONV, reduceLib.REDUCE_RULE.

REFINE_EXISTS_TAC**(Q)**

Q.REFINE_EXISTS_TAC : term quotation -> tactic

Synopsis

Attacks existential goals, making the existential variable more concrete.

Description

The tactic Q.REFINE_EXISTS_TAC *q* parses the quotation *q* in the context of the (necessarily existential) goal to which it is applied, and uses the resulting term as the witness for the goal. However, if the witness has any variables not already present in the goal, then these are treated as new existentially quantified variables. If there are no such “free” variables, then the behaviour is the same as EXISTS_TAC.

Failure

Fails if the goal is not existential, or if the quotation can not parse to a term of the same type as the existentially quantified variable.

Example

If the quotation doesn't mention any new variables:

```
- Q.REFINE_EXISTS_TAC 'n' ([['n > x'], '?m. m > x']);
> val it =
  ([(['n > x'], 'n > x'), fn)
  : (term list * term) list * (thm list -> thm)
```

If the quotation does mention any new variables, they are existentially quantified in the new goal:

```
- Q.REFINE_EXISTS_TAC 'n + 2' ([['~P 0'], '?p. P (p - 1)']);
> val it =
  ([(['~P 0'], '?n. P (n + 2 - 1)'), fn)
  : (term list * term) list * (thm list -> thm)
```

Uses

Q.REFINE_EXISTS_TAC is useful if it is clear that a existential goal will be solved by a term of particular form, while it is not yet clear precisely what term this will be. Further

proof activity should be able to exploit the additional structure that has appeared in the place of the existential variable.

See also

`Tactic.EXISTS_TAC`.

REFL	(Thm)
------	-------

`REFL : conv`

Synopsis

Returns theorem expressing reflexivity of equality.

Description

REFL maps any term `t` to the corresponding theorem `|- t = t`.

Failure

Never fails.

See also

`Conv.ALL_CONV`, `Tactic.REFL_TAC`.

REFL_CONSEQ_CONV	(ConseqConv)
------------------	--------------

`REFL_CONSEQ_CONV : conseq_conv`

Synopsis

Given a term `t` of type `bool` this consequence conversion returns the theorem `|- t ==> t`.

See also

`ConseqConv.TRUE_CONSEQ_CONV`, `ConseqConv.FALSE_CONSEQ_CONV`,
`ConseqConv.TRUE_FALSE_REFL_CONSEQ_CONV`.

REFL_TAC	(Tactic)
----------	----------

`REFL_TAC : tactic`

Synopsis

Solves a goal which is an equation between alpha-equivalent terms.

Description

When applied to a goal $A \text{ ?- } t = t'$, where t and t' are alpha-equivalent, `REFL_TAC` completely solves it.

```
A ?- t = t'
===== REFL_TAC
```

Failure

Fails unless the goal is an equation between alpha-equivalent terms.

See also

`Tactic.ACCEPT_TAC`, `Tactic.MATCH_ACCEPT_TAC`, `Rewrite.REWRITE_TAC`.

<code>register_btrace</code>

(Feedback)

```
Feedback.register_btrace : string * bool ref -> unit
```

Synopsis

Registers a trace variable for a boolean reference.

Description

A call to `register_btrace(nm, bref)` registers a trace variable called `nm` that can take on two different values (0 and 1), which correspond to the state of the boolean variable `bref`.

Failure

Fails if the given name is already in use as a trace variable.

Comments

This function uses `register_ftrace` to make a boolean variable appear as an integer value.

See also

`Feedback`, `Feedback.current_trace`, `Feedback.register_trace`, `Feedback.register_ftrace`, `Feedback.set_trace`, `Feedback.trace`, `Feedback.traces`.

register_ftrace**(Feedback)**

```
register_ftrace :  
  (string * ((unit -> int) * (int -> unit)) * int) -> unit
```

Synopsis

Registers a trace that is accessed by a set/get pair of functions.

Description

A call to `register_ftrace(nm, (g,s), m)` registers an integer-valued trace variable that is updated with the `s` function and whose value is read with the `g` function. The variable is given the name `nm` and the variable's maximum allowed value is `m`. The trace's default is the value of `g()`, which is called just once as part of the registration procedure.

Failure

Fails if the given name is already in use as a trace variable, or if the maximum or the default value (returned by `g()`) is less than zero.

Comments

The two functions provide a more general way of accessing something that may not be actually be an integer reference, even though this is the interface that the various trace functions present.

See also

`Feedback`, `Feedback.current_trace`, `Feedback.register_trace`,
`Feedback.register_btrace`, `Feedback.set_trace`, `Feedback.trace`, `Feedback.traces`.

register_trace**(Feedback)**

```
register_trace : (string * int ref * int) -> unit
```

Synopsis

Registers a new tracing variable.

Description

A call to `register_trace(n, r, m)` registers the integer reference variable `r` as a tracing variable associated with name `n`. The integer `m` is its maximum value. Its value at the

time of registration is considered its default value, which will be restored by a call to `reset_trace` n Or `reset_traces`.

Failure

Fails if there is already a tracing variable registered under the name given, or if either the maximum value or the value in the reference is less than zero.

See also

`Feedback`, `Feedback.register_btrace`, `Feedback.register_ftrace`, `Feedback.reset_trace`, `Feedback.reset_traces`, `Feedback.trace`, `Feedback.traces`.

<code>release</code>	<code>(Globals)</code>
----------------------	------------------------

`release` : string

Synopsis

The name of the release series of the HOL system being run.

Example

```
- Globals.release;
> val it = "Kananaskis" : string
```

See also

`Globals.version`.

<code>remove_ovl_mapping</code>	<code>(Parse)</code>
---------------------------------	----------------------

`remove_ovl_mapping`: string -> {Name:string,Thy:string} -> unit

Synopsis

Removes an overloading mapping between the string and constant specified.

Description

Each grammar maintains two maps internally. One is from strings to non-empty lists of terms, and the other is from terms to strings. The first map is used to resolve overloading

when parsing. A string will eventually be turned into one of the terms in the list that it maps to. When printing a constant, the map in the opposite direction is used to turn a term into a string.

A call to `remove_ovl_mapping s {Name,Thy}`, maps the Name-Thy record to a constant `c`, and removes the `c-s` pair from both maps.

Failure

Never fails. If the given pair is not in either map, the function silently does nothing.

Uses

To prune the overloading maps of unwanted possibilities.

Comments

Note that removing a print-mapping for a constant will result in that constant always printing fully qualified as `thy$name`. This situation will persist until that constant is given a name to map to (either with `overload_on` or `update_overload_maps`).

As with other parsing functions, there is a sister function, `temp_remove_ovl_mapping` that does the same thing, but whose effect is not saved to a theory file.

See also

`Parse.clear_overloads_on`, `Parse.overload_on`, `Parse.update_overload_maps`.

<code>remove_rules_for_term</code> (Parse)
--

```
Parse.remove_rules_for_term : string -> unit
```

Synopsis

Removes parsing/pretty-printing rules from the global grammar.

Description

Calling `remove_rules_for_term s` removes all those rules (if any) in the global grammar that are for the term `s`. The string specifies the name of the term that the rule is for, not a token that may happen to be used in concrete syntax for the term.

Failure

Never fails.

Example

The universal quantifier can have its special binder status removed using this function:

```

- val t = Term '!x. P x /\ ~Q x';
<<HOL message: inventing new type variable names: 'a.>>
> val t = '!x. P x /\ ~Q x' : term
- remove_rules_for_term "!";
> val it = () : unit
- t;
> val it = '! (\x. P x /\ ~Q x)' : term

```

Similarly, one can remove the two rules for conditional expressions and see the raw syntax as follows:

```

- val t = Term 'if p then q else r';
<<HOL message: inventing new type variable names: 'a.>>
> val t = 'if p then q else r' : term
- remove_rules_for_term "COND";
> val it = () : unit
- t;
> val it = 'COND p q r' : term

```

Comments

There is a companion `temp_remove_rules_for_term` function, which has the same effect on the global grammar, but which does not cause this effect to persist when the current theory is exported.

See also

`Parse.remove_termtok`.

<div data-bbox="234 1491 644 1545" data-label="Text"> <p><code>remove_ssfrags</code></p> </div>	<div data-bbox="1144 1487 1412 1545" data-label="Text"> <p><code>(simpLib)</code></p> </div>
---	--

`remove_ssfrags : simpset -> string list -> simpset`

Synopsis

Removes named simpset fragments from a simpset.

Description

A call to `remove_ssfrags simpset fragnames` returns a simpset that is the same as `simpset` except that the simpset fragments with names in the list `fragnames` are no longer included.

Failure

Never fails. If a name in the list of fragment names does not occur as a name amongst the simpset fragments in the input simpset, no error is reported.

Example

```
- SIMP_CONV (srw_ss()) [] ‘‘MAP ($+ 1) [3;4;5]‘‘;
<<HOL message: Initialising SRW simpset ... done>>
> val it = |- MAP ($+ 1) [3; 4; 5] = [4; 5; 6] : thm

- val myss = simpLib.remove_ssfrags (srw_ss()) ["REDUCE"]
> val myss = ...output elided...

- SIMP_CONV myss [] ‘‘MAP ($+ 1) [3;4;5]‘‘
> val it = |- MAP ($+ 1) [3; 4; 5] = [1 + 3; 1 + 4; 1 + 5] : thm
```

See also

BasicProvers.diminish_srw_ss.

<div data-bbox="159 1171 571 1220" data-label="Text"> <p>remove_termtok</p> </div>	<div data-bbox="1125 1167 1331 1220" data-label="Text"> <p>(Parse)</p> </div>
--	---

```
remove_termtok : {term_name : string, tok : string} -> unit
```

Synopsis

Removes a rule from the global grammar.

Description

The `remove_termtok` removes parsing/printing rules from the global grammar. Rules to be removed are those that are for the term with the given name (`term_name`) and which include the string `tok` as part of their concrete representation. If multiple rules satisfy this criterion, they are all removed. If none match, the grammar is not changed.

Failure

Never fails.

Example

If one wished to revert to the traditional HOL syntax for conditional expressions, this would be achievable as follows:

```

- remove_termtok {term_name = "COND", tok = "if"};
> val it = () : unit

- Term'if p then q else r';
<<HOL message: inventing new type variable names: 'a, 'b, 'c, 'd, 'e, 'f.>>
> val it = 'if p then q else r' : term

- Term'p => q | r';
<<HOL message: inventing new type variable names: 'a.>>
> val it = 'COND p q r' : term

```

The first invocation of the parser above demonstrates that once the rule for the `if-then-else` syntax has been removed, a string that used to parse as a conditional expression then parses as a big function application (the function `if` applied to five arguments).

The fact that the pretty-printer does not print the term using the old-style syntax, even after the `if-then-else` rule has been removed, is due to the fact that the corresponding rule in the grammar does not have its preferred flag set. This can be accomplished with `prefer_form_with_tok` as follows:

```

- prefer_form_with_tok {term_name = "COND", tok = "=>"};
> val it = () : unit

- Term'p => q | r';
<<HOL message: inventing new type variable names: 'a.>>
> val it = 'p => q | r' : term

```

Uses

Used to modify the global parsing/pretty-printing grammar by removing a rule, possibly as a prelude to adding another rule which would otherwise clash.

Comments

As with other functions in the `Parse` structure, there is a companion `temp_remove_termtok` function, which has the same effect on the global grammar, but which does not cause this effect to persist when the current theory is exported.

The specification of a rule by `term_name` and one of its tokens is not perfect, but seems adequate in practice.

See also

`Parse.remove_rules_for_term`, `Parse.prefer_form_with_tok`.

remove_user_printer	(Parse)
---------------------	---------

```
remove_user_printer :  
  string -> (term * term_grammar.userprinter) option
```

Synopsis

Removes a user-defined pretty-printing function associated with a particular name.

Description

This removes the user-defined pretty-printing function that has been associated with a particular name (the name of the code for the function). If there is such a printer in the global grammar for the specified type, this is returned in the option type. If there is no printer, then `NONE` is returned.

Failure

Never fails.

Comments

As always, there is an accompanying function `temp_remove_user_printer`, which does not affect the grammar exported to disk.

See also

`Parse.add_user_printer`.

remove_word_printer	(wordsLib)
---------------------	------------

```
remove_word_printer : unit -> unit
```

Synopsis

Turns off custom pretty-printing for word literals.

Description

The function `remove_word_printer` calls `Parse.remove_user_printer` to remove pretty-printing for ground instances of “`n2w n`“. This will normally mean that words output in decimal format.

Example

```

- load "wordsLib";
...
- ‘‘0x10000000w‘‘;
<<HOL message: inventing new type variable names: 'a>>
> val it = ‘‘0x10000000w‘‘ : term
- wordsLib.remove_word_printer();
- ‘‘0x10000000w‘‘;
<<HOL message: inventing new type variable names: 'a>>
> val it = ‘‘268435456w‘‘ : term

```

See also

Parse.remove_user_printer, wordsLib.output_words_as,
 wordsLib.output_words_as_dec, wordsLib.output_words_as_bin,
 wordsLib.output_words_as_oct, wordsLib.output_words_as_hex.

rename_bvar	(Term)
--------------------	---------------

rename_bvar : string -> term -> term

Synopsis

Performs one step of alpha conversion.

Description

If M is a lambda abstraction, i.e., has the form $\lambda v. N$, an invocation `rename_bvar s M` performs one step of alpha conversion to obtain $\lambda s. N[s/v]$.

Failure

If M is not a lambda abstraction.

Example

```

- rename_bvar "x" (Term ‘‘\v. v ==> w‘‘);
> val it = ‘‘\x. x ==> w‘‘ : term

- rename_bvar "x" (Term ‘‘\y. y /\ x‘‘);
> val it = ‘‘\x'. x' /\ x‘‘ : term

```

Comments

`rename_bvar` takes constant time in the current implementation.

See also

`Term.aconv`, `Drule.ALPHA_CONV`.

RENAME_VARS_CONV

(Conv)

`Conv.RENAME_VARS_CONV : string list -> term -> thm`

Synopsis

Renames variables underneath a binder.

Description

`RENAME_VARS_CONV` takes a list of strings specifying new names for variables under a binder. More precisely, it will rename variables in abstractions, or bound by universal, existential, unique existence or the select (or Hilbert-choice) “quantifier”.

More than one variable can be renamed at once. If variables occur past the first, then the renaming continues on the appropriate sub-term of the first. (That is, if the term is an abstraction, then renaming will continue on the body of the abstraction. If it is one of the supported quantifiers, then renaming will continue on the body of the abstraction that is the argument of the “binder constant”.)

If `RENAME_VARS_CONV` is passed the empty list, it is equivalent to `ALL_CONV`. The binders do not need to be of the same type all the way into the term.

Failure

Fails if an attempt is made to rename a variable in a term that is not an abstraction, or is not one of the accepted quantifiers. Also fails if all of the names in the list are not distinct.

Example

```
- RENAME_VARS_CONV ["a", "b"] ‘‘\x y. x /\ y‘‘;
> val it = |- (\x y. x /\ y) = (\a b. a /\ b) : thm
- RENAME_VARS_CONV ["a", "b"] ‘‘!x:'a y. P x /\ P y‘‘;
> val it = |- (!x y. P x /\ P y) = !a b. P a /\ P b : thm
- RENAME_VARS_CONV ["a", "b"] ‘‘!x:'a. ?y. P x /\ P y‘‘;
> val it = |- (!x. ?y. P x /\ P y) = !a. ?b. P a /\ P b : thm
```

Uses

Post-processing mangling of names in code implementing derived logical procedures to make names look more appropriate. Changing names can only affect the presentation of terms, not their semantics.

See also

`Term.aconv`, `Thm.ALPHA`.

<code>repeat</code>	<code>(Lib)</code>
---------------------	--------------------

```
repeat : ('a -> 'a) -> 'a -> 'a
```

Synopsis

Iteratively apply a function until it fails.

Description

An invocation `repeat f x` expands to `repeat f (f x)`. Thus it unrolls to `f(...(f x)...)...`, returning the most recent argument to `f` before application fails.

Failure

The evaluation of `repeat f x` fails only if interrupted, or machine resources are exhausted.

Example

The following gives a simple-minded way of calculating the largest integer on the machine.

```
- fun incr x = x+1;
> val incr = fn : int -> int
```

```
val maxint = repeat incr 0; (* takes some time *)
> val maxint = 1073741823 : int
```

(Caution: in some ML implementations, the type `int` is not implemented by machine words, but by ‘bignum’ techniques that allow numbers of arbitrary size, in which case the example above will not return for a very long time.)

See also

`Lib.funpow`.

REPEAT

(Tactical)

```
REPEAT : (tactic -> tactic)
```

Synopsis

Repeatedly applies a tactic until it fails.

Description

The tactic `REPEAT T` is a tactic which applies `T` to a goal, and while it succeeds, continues applying it to all subgoals generated.

Failure

The application of `REPEAT` to a tactic never fails, and neither does the composite tactic, even if the basic tactic fails immediately.

See also

`Tactical.EVERY`, `Tactical.FIRST`, `Tactical.ORELSE`, `Tactical.THEN`, `Tactical.THENL`.

REPEAT_GTCL

(Thm_cont)

```
REPEAT_GTCL : (thm_tactical -> thm_tactical)
```

Synopsis

Applies a theorem-tactical until it fails when applied to a goal.

Description

When applied to a theorem-tactical, a theorem-tactic, a theorem and a goal:

```
REPEAT_GTCL tt1 ttac th goal
```

`REPEAT_GTCL` repeatedly modifies the theorem according to `tt1` till the result of handing it to `ttac` and applying it to the goal fails (this may be no times at all).

Failure

Fails iff the theorem-tactic fails immediately when applied to the theorem and the goal.

Example

The following tactic matches `th`'s antecedents against the assumptions of the goal until it can do so no longer, then puts the resolvents onto the assumption list:

```
REPEAT_GTCL (IMP_RES_THEN ASSUME_TAC) th
```

See also

`Thm_cont.REPEAT_TCL`, `Thm_cont.THEN_TCL`.

REPEAT_TCL	(Thm_cont)
-------------------	-------------------

```
REPEAT_TCL : (thm_tactical -> thm_tactical)
```

Synopsis

Repeatedly applies a theorem-tactical until it fails when applied to the theorem.

Description

When applied to a theorem-tactical, a theorem-tactic and a theorem:

```
REPEAT_TCL ttl ttac th
```

`REPEAT_TCL` repeatedly modifies the theorem according to `ttl` until it fails when given to the theorem-tactic `ttac`.

Failure

Fails iff the theorem-tactic fails immediately when applied to the theorem.

Example

It is often desirable to repeat the action of basic theorem-tactics. For example `CHOOSE_THEN` strips off a single existential quantification, so one might use `REPEAT_TCL CHOOSE_THEN` to get rid of them all.

Alternatively, one might want to repeatedly break apart a theorem which is a nested conjunction and apply the same theorem-tactic to each conjunct. For example the following goal:

$$?- ((0 = w) \wedge (0 = x)) \wedge (0 = y) \wedge (0 = z) ==> (w + x + y + z = 0)$$

might be solved by

```
DISCH_THEN (REPEAT_TCL CONJUNCTS_THEN (SUBST1_TAC o SYM)) THEN
REWRITE_TAC[ADD_CLAUSES]
```

See also

`Thm_cont.REPEAT_GTCL`, `Thm_cont.THEN_TCL`.

REPEATC	(Conv)
----------------	---------------

`REPEATC` : `conv -> conv`

Synopsis

Repeatedly apply a conversion (zero or more times) until it fails.

Description

If c is a conversion effects a transformation of a term t to a term t' , that is if c maps t to the theorem $\vdash t = t'$, then `REPEATC c` is the conversion that repeats this transformation as often as possible. More exactly, if c maps the term t_i to $\vdash t_i = t_{i+1}$ for i from 1 to n , but fails when applied to the $n+1$ th term t_{n+1} , then `REPEATC c t1` returns $\vdash t_1 = t_{n+1}$. And if $c t$ fails, then `REPEATC c t` returns $\vdash t = t$.

Further, if $c t$ raises the `UNCHANGED` exception, then `REPEATC c t` also raises the same exception (rather than go into an infinite loop).

Failure

Never fails, but can diverge if the supplied conversion never fails.

REPLICATE_CONV	(listLib)
-----------------------	------------------

`REPLICATE_CONV` : `conv`

Synopsis

Computes by inference the result of replicating an element a given number of times to form a list.

Description

For an arbitrary expression x and numeral constant n , the result of evaluating

`REPLICATE_CONV (--'REPLICATE n x'--)`

is the theorem

```
|- REPLICATE n x = [x;x;...;x]
```

where the list `[x;x;...;x]` is of length `n`.

Example

Evaluating `REPLICATE_CONV (--'REPLICATE 3 [0;1;2;3]')` will return the following theorem:

```
|- REPLICATE 3 [0;1;2;3] = [[0;1;2;3]; [0;1;2;3]; [0;1;2;3]]
```

Failure

`REPLICATE_CONV tm` fails if `tm` is not of the form described above.

REPLICATE_CONV

(listLib)

```
REPLICATE_CONV : conv
```

Synopsis

Computes by inference the result of replicating an element a given number of times to form a list.

Description

For an arbitrary expression `x` and numeral constant `n`, the result of evaluating

```
REPLICATE_CONV (--'REPLICATE n x')
```

is the theorem

```
|- REPLICATE n x = [x;x;...;x]
```

where the list `[x;x;...;x]` is of length `n`.

Example

Evaluating `REPLICATE_CONV (--'REPLICATE 3 [0;1;2;3]')` will return the following theorem:

```
|- REPLICATE 3 [0;1;2;3] = [[0;1;2;3]; [0;1;2;3]; [0;1;2;3]]
```

Failure

REPLICATE_CONV tm fails if tm is not of the form described above.

RES_CANON

(Drule)

RES_CANON : (thm -> thm list)

Synopsis

Put an implication into canonical form for resolution.

Description

All the HOL resolution tactics (e.g. IMP_RES_TAC) work by using modus ponens to draw consequences from an implicative theorem and the assumptions of the goal. Some of these tactics derive this implication from a theorem supplied explicitly the user (or otherwise from ‘outside’ the goal) and some obtain it from the assumptions of the goal itself. But in either case, the supplied theorem or assumption is first transformed into a list of implications in ‘canonical’ form by the function RES_CANON.

The theorem argument to RES_CANON should be either be an implication (which can be universally quantified) or a theorem from which an implication can be derived using the transformation rules discussed below. Given such a theorem, RES_CANON returns a list of implications in canonical form. It is the implications in this resulting list that are used by the various resolution tactics to infer consequences from the assumptions of a goal.

The transformations done by RES_CANON th to the theorem th are as follows. First, if th is a negation $A \mid\sim t$, this is converted to the implication $A \mid\sim t \implies F$. The following inference rules are then applied repeatedly, until no further rule applies. Conjunctions are split into their components and equivalence (boolean equality) is split into implication in both directions:

$$\frac{A \mid\sim t1 \wedge t2}{A \mid\sim t1 \quad A \mid\sim t2} \qquad \frac{A \mid\sim t1 = t2}{A \mid\sim t1 \implies t2 \quad A \mid\sim t2 \implies t1}$$

Conjunctive antecedents are transformed by:

$$\frac{A \mid\sim (t1 \wedge t2) \implies t}{A \mid\sim t1 \implies (t2 \implies t) \quad A \mid\sim t2 \implies (t1 \implies t)}$$

and disjunctive antecedents by:

$$\frac{A \mid- (t1 \ \vee \ t2) \implies t}{A \mid- t1 \implies t \quad A \mid- t2 \implies t}$$

The scope of universal quantifiers is restricted, if possible:

$$\frac{A \mid- !x. t1 \implies t2}{A \mid- t1 \implies !x. t2} \quad [\text{if } x \text{ is not free in } t1]$$

and existentially-quantified antecedents are eliminated by:

$$\frac{A \mid- (?x. t1) \implies t2}{A \mid- !x'. t1[x'/x] \implies t2} \quad [x' \text{ chosen so as not to be free in } t2]$$

Finally, when no further applications of the above rules are possible, and the theorem is an implication:

$$A \mid- !x1 \dots xn. t1 \implies t2$$

then the theorem $A \cup \{t1\} \mid- t2$ is transformed by a recursive application of `RES_CANON` to get a list of theorems:

$$[A \cup \{t1\} \mid- t21, \dots, A \cup \{t1\} \mid- t2n]$$

and the result of discharging $t1$ from these theorems:

$$[A \mid- !x1 \dots xn. t1 \implies t21, \dots, A \mid- !x1 \dots xn. t1 \implies t2n]$$

is returned. That is, the transformation rules are recursively applied to the conclusions of all implications.

Failure

`RES_CANON th` fails if no implication(s) can be derived from `th` using the transformation rules shown above.

Example

The uniqueness of the remainder $k \text{ MOD } n$ is expressed in HOL by the built-in theorem `MOD_UNIQUE`:

$$\mid- !n \ k \ r. (?q. (k = (q * n) + r) \ \wedge \ r < n) \implies (k \text{ MOD } n = r)$$

For this theorem, the canonical list of implications returned by `RES_CANON` is as follows:

```

- RES_CANON MOD_UNIQUE;
> val it =
  [|- !r n q k. (k = q * n + r) ==> r < n ==> (k MOD n = r),
   |- !n r. r < n ==> !q k. (k = q * n + r) ==> (k MOD n = r)] : thm list

```

The existentially-quantified, conjunctive, antecedent has given rise to two implications, and the scope of universal quantifiers has been restricted to the conclusions of the resulting implications wherever possible.

Uses

The primary use of RES_CANON is for the (internal) pre-processing phase of the built-in resolution tactics IMP_RES_TAC, IMP_RES_THEN, RES_TAC, and RES_THEN. But the function RES_CANON is also made available at top-level so that users can call it to see the actual form of the implications used for resolution in any particular case.

See also

Tactic.IMP_RES_TAC, Thm.cont.IMP_RES_THEN, Tactic.RES_TAC, Thm.cont.RES_THEN.

RES_EXISTS_CONV

(res_quanLib)

RES_EXISTS_CONV : conv

Synopsis

Converts a restricted existential quantification to a conjunction.

Description

When applied to a term of the form $?x::P. Q[x]$, the conversion RES_EXISTS_CONV returns the theorem:

$$|- ?x::P. Q[x] = (?x. x \text{ IN } P \wedge Q[x])$$

which is the underlying semantic representation of the restricted existential quantification.

Failure

Fails if applied to a term not of the form $?x::P. Q$.

See also

res_quanLib.RES_FORALL_CONV, res_quanLib.RESQ_EXISTS_TAC.

RES_EXISTS_CONV

(res_quantools)

RES_EXISTS_CONV : conv

Synopsis

Converts a restricted existential quantification to a conjunction.

Description

When applied to a term of the form $?x::P. Q[x]$, the conversion RES_EXISTS_CONV returns the theorem:

$$\vdash ?x::P. Q[x] = (?x. P x /\ Q[x])$$

which is the underlying semantic representation of the restricted existential quantification.

Failure

Fails if applied to a term not of the form $?x::P. Q$.

See also

res_quantools.RES_FORALL_CONV, res_quantools.RESQ_EXISTS_TAC.

RES_EXISTS_UNIQUE_CONV

(res_quantLib)

RES_EXISTS_UNIQUE_CONV : conv

Synopsis

Converts a restricted unique existential quantification to a conjunction.

Description

When applied to a term of the form $?!x::P. Q[x]$, the conversion RES_EXISTS_UNIQUE_CONV returns the theorem:

$$\vdash ?!x::P. Q[x] = (?x::P. Q[x]) /\ (!x y::P. Q[x] /\ Q[y] ==> (x = y))$$

which is the underlying semantic representation of the restricted unique existential quantification.

Failure

Fails if applied to a term not of the form $?x!::P. Q$.

See also

`res_quanLib.RES_FORALL_CONV`, `res_quanLib.RES_EXISTS_CONV`.

RES_FORALL_AND_CONV	(res_quanLib)
---------------------	---------------

`RES_FORALL_AND_CONV` : `conv`

Synopsis

Splits a restricted universal quantification across a conjunction.

Description

When applied to a term of the form $!x::P. Q \wedge R$, the conversion `RES_FORALL_AND_CONV` returns the theorem:

$$\vdash (!x::P. Q \wedge R) = ((!x::P. Q) \wedge (!x::P. R))$$

Failure

Fails if applied to a term not of the form $!x::P. Q \wedge R$.

RES_FORALL_AND_CONV	(res_quanTools)
---------------------	-----------------

`RES_FORALL_AND_CONV` : `conv`

Synopsis

Splits a restricted universal quantification across a conjunction.

Description

When applied to a term of the form $!x::P. Q \wedge R$, the conversion `RES_FORALL_AND_CONV` returns the theorem:

$$\vdash (\!x::P. Q \wedge R) = ((\!x::P. Q) \wedge (\!x::P. R))$$

Failure

Fails if applied to a term not of the form $\!x::P. Q \wedge R$.

RES_FORALL_CONV	(res_quanLib)
-----------------	---------------

RES_FORALL_CONV : conv

Synopsis

Converts a restricted universal quantification to an implication.

Description

When applied to a term of the form $\!x::P. Q$, the conversion RES_FORALL_CONV returns the theorem:

$$\vdash \!x::P. Q = (\!x. x \text{ IN } P \implies Q)$$

which is the underlying semantic representation of the restricted universal quantification.

Failure

Fails if applied to a term not of the form $\!x::P. Q$.

See also

res_quanLib.IMP_RES_FORALL_CONV.

RES_FORALL_CONV	(res_quanTools)
-----------------	-----------------

RES_FORALL_CONV : conv

Synopsis

Converts a restricted universal quantification to an implication.

Description

When applied to a term of the form $\!x::P. Q$, the conversion RES_FORALL_CONV returns the theorem:

$$\vdash !x::P. Q = (!x. P x ==> Q)$$

which is the underlying semantic representation of the restricted universal quantification.

Failure

Fails if applied to a term not of the form $!x::P. Q$.

See also

`res_quantTools.IMP_RES_FORALL_CONV`.

RES_FORALL_SWAP_CONV	(res_quantLib)
----------------------	----------------

RES_FORALL_SWAP_CONV : conv

Synopsis

Changes the order of two restricted universal quantifications.

Description

When applied to a term of the form $!x::P. !y::Q. R$, the conversion RES_FORALL_SWAP_CONV returns the theorem:

$$\vdash (!x::P. !y::Q. R) = !y::Q. !x::P. R$$

providing that x does not occur free in Q and y does not occur free in P .

Failure

Fails if applied to a term not of the correct form.

See also

`res_quantLib.RES_FORALL_CONV`.

RES_FORALL_SWAP_CONV	(res_quantTools)
----------------------	------------------

RES_FORALL_SWAP_CONV : conv

Synopsis

Changes the order of two restricted universal quantifications.

Description

When applied to a term of the form $\lambda x::P. \lambda y::Q. R$, the conversion `RES_FORALL_SWAP_CONV` returns the theorem:

$$\vdash (\lambda x::P. \lambda y::Q. R) = \lambda y::Q. \lambda x::P. R$$

providing that x does not occur free in Q and y does not occur free in P .

Failure

Fails if applied to a term not of the correct form.

See also

`res_quantools.RES_FORALL_CONV`.

<code>RES_SELECT_CONV</code>	<code>(res_quantLib)</code>
------------------------------	-----------------------------

`RES_SELECT_CONV` : `conv`

Synopsis

Converts a restricted choice quantification to a conjunction.

Description

When applied to a term of the form $\lambda x::P. Q[x]$, the conversion `RES_SELECT_CONV` returns the theorem:

$$\vdash \lambda x::P. Q[x] = (\lambda x. x \text{ IN } P \wedge Q[x])$$

which is the underlying semantic representation of the restricted choice quantification.

Failure

Fails if applied to a term not of the form $\lambda x::P. Q$.

See also

`res_quantLib.RES_FORALL_CONV`, `res_quantLib.RES_EXISTS_CONV`.

<code>RES_TAC</code>	<code>(Tactic)</code>
----------------------	-----------------------

`RES_TAC` : `tactic`

Synopsis

Enriches assumptions by repeatedly resolving them against each other.

Description

RES_TAC searches for pairs of assumed assumptions of a goal (that is, for a candidate implication and a candidate antecedent, respectively) which can be ‘resolved’ to yield new results. The conclusions of all the new results are returned as additional assumptions of the subgoal(s). The effect of RES_TAC on a goal is to enrich the assumptions set with some of its collective consequences.

When applied to a goal $A \text{ ?- } g$, the tactic RES_TAC uses RES_CANON to obtain a set of implicative theorems in canonical form from the assumptions A of the goal. Each of the resulting theorems (if there are any) will have the form:

$$A \text{ |- } u_1 \implies u_2 \implies \dots \implies u_n \implies v$$

RES_TAC then tries to repeatedly ‘resolve’ these theorems against the assumptions of a goal by attempting to match the antecedents u_1, u_2, \dots, u_n (in that order) to some assumption of the goal (i.e. to some candidate antecedents among the assumptions). If all the antecedents can be matched to assumptions of the goal, then an instance of the theorem

$$A \text{ u } \{a_1, \dots, a_n\} \text{ |- } v$$

called a ‘final resolvent’ is obtained by repeated specialization of the variables in the implicative theorem, type instantiation, and applications of modus ponens. If only the first i antecedents u_1, \dots, u_i can be matched to assumptions and then no further matching is possible, then the final resolvent is an instance of the theorem:

$$A \text{ u } \{a_1, \dots, a_i\} \text{ |- } u_{(i+1)} \implies \dots \implies v$$

All the final resolvents obtained in this way (there may be several, since an antecedent u_i may match several assumptions) are added to the assumptions of the goal, in the stripped form produced by using STRIP_ASSUME_TAC. If the conclusion of any final resolvent is a contradiction ‘F’ or is alpha-equivalent to the conclusion of the goal, then RES_TAC solves the goal.

Failure

RES_TAC cannot fail and so should not be unconditionally REPEATED. However, since the final resolvents added to the original assumptions are never used as ‘candidate antecedents’ it is sometimes necessary to apply RES_TAC more than once to derive the desired result.

See also

Tactic.IMP_RES_TAC, Thm_cont.IMP_RES_THEN, DruLe.RES_CANON, Thm_cont.RES_THEN.

RES_THEN

(Thm_cont)

```
RES_THEN : (thm_tactic -> tactic)
```

Synopsis

Resolves all implicative assumptions against the rest.

Description

Like the basic resolution function `IMP_RES_THEN`, the resolution tactic `RES_THEN` performs a single-step resolution of an implication and the assumptions of a goal. `RES_THEN` differs from `IMP_RES_THEN` only in that the implications used for resolution are taken from the assumptions of the goal itself, rather than supplied as an argument.

When applied to a goal $A \text{ ?- } g$, the tactic `RES_THEN ttac` uses `RES_CANON` to obtain a set of implicative theorems in canonical form from the assumptions A of the goal. Each of the resulting theorems (if there are any) will have the form:

$$a_i \text{ |- } !x_1 \dots x_n. u_i \text{ ==> } v_i$$

where a_i is one of the assumptions of the goal. Having obtained these implications, `RES_THEN` then attempts to match each antecedent u_i to each assumption $a_j \text{ |- } a_j$ in the assumptions A . If the antecedent u_i of any implication matches the conclusion a_j of any assumption, then an instance of the theorem $a_i, a_j \text{ |- } v_i$, called a ‘resolvent’, is obtained by specialization of the variables x_1, \dots, x_n and type instantiation, followed by an application of modus ponens. There may be more than one canonical implication derivable from the assumptions of the goal and each such implication is tried against every assumption, so there may be several resolvents (or, indeed, none).

Tactics are produced using the theorem-tactic `ttac` from all these resolvents (failures of `ttac` at this stage are filtered out) and these tactics are then applied in an unspecified sequence to the goal. That is,

```
RES_THEN ttac (A ?- g)
```

has the effect of:

```
MAP EVERY (mapfilter ttac [... ; (a_i, a_j |- v_i) ; ...]) (A ?- g)
```

where the theorems $a_i, a_j \text{ |- } v_i$ are all the consequences that can be drawn by a (single) matching modus-ponens inference from the assumptions A and the implications derived using `RES_CANON` from the assumptions. The sequence in which the theorems $a_i, a_j \text{ |- } v_i$ are generated and the corresponding tactics applied is unspecified.

Failure

Evaluating `RES_THEN ttac th` fails with ‘no implication’ if no implication(s) can be derived from the assumptions of the goal by the transformation process described under the entry for `RES_CANON`. Evaluating `RES_THEN ttac (A ?- g)` fails with ‘no resolvents’ if no assumption of the goal `A ?- g` can be resolved with the derived implication or implications. Evaluation also fails, with ‘no tactics’, if there are resolvents, but for every resolvent `ai,aj |- vi` evaluating the application `ttac (ai,aj |- vi)` fails—that is, if for every resolvent `ttac` fails to produce a tactic. Finally, failure is propagated if any of the tactics that are produced from the resolvents by `ttac` fails when applied in sequence to the goal.

See also

`Tactic.IMP_RES_TAC`, `Thm_cont.IMP_RES_THEN`, `Drule.MATCH_MP`, `Drule.RES_CANON`, `Tactic.RES_TAC`.

<div data-bbox="159 1016 311 1061" data-label="Text"> <p><code>reset</code></p> </div>	<div data-bbox="1182 1010 1331 1064" data-label="Text"> <p>(Lib)</p> </div>
--	---

```
reset : ('a,'b) istream -> ('a,'b) istream
```

Synopsis

Restart an istream.

Description

An application `reset istrm` replaces the current state of `istrm` with the value supplied when `istrm` was constructed.

Failure

Never fails.

Example

```
- reset(next(next
  (mk_istream (fn x => x+1) 0 (concat "gsym" o int_to_string)))));
> val it = <istream> : (int, string) istream

- state it;
> val it = "gsym0" : string
```

Comments

Perhaps the type of `reset` should be `('a,'b) istream -> unit`.

See also

`Lib.mk_istream`, `Lib.next`, `Lib.state`.

<code>reset_trace</code>

(Feedback)

```
reset_trace : string -> unit
```

Synopsis

Resets a tracing variable to its default value.

Description

A call to `reset_trace n` resets the tracing variable associated with the name `n` to its default value, i.e., the value of the expression `!r` when `n` was registered with `register_trace n r`.

Failure

Fails if the name given is not associated with a registered tracing variable, or if a `set` function associated with a "functional" trace (see `register_ftrace`) fails.

See also

`Feedback`, `Feedback.register_trace`, `Feedback.set_trace`, `Feedback.reset_traces`, `Feedback.trace`, `Feedback.traces`.

<code>reset_traces</code>

(Feedback)

```
reset_traces : unit -> unit
```

Synopsis

Resets all registered tracing variables to their default values.

Failure

Fails if a `set` function associated with a "functional" trace (see `register_ftrace`) fails.

See also

Feedback, Feedback.set_trace, Feedback.register_trace, Feedback.reset_trace, Feedback.trace, Feedback.traces.

RESQ_EXISTS_TAC	(res_quantools)
-----------------	-----------------

RESQ_EXISTS_TAC : term -> tactic

Synopsis

Strips the outermost restricted existential quantifier from the conclusion of a goal.

Description

When applied to a goal $A \text{ ?- } ?x::P. t$, the tactic RESQ_EXISTS_TAC reduces it to a new subgoal $A \text{ ?- } P \ x' \ /\ \ t[x'/x]$ where x' is a variant of x chosen to avoid clashing with any variables free in the goal's assumption list. Normally x' is just x .

$$\begin{array}{l} A \text{ ?- } ?x::P. t \\ \text{=====} \text{ RESQ_EXISTS_TAC} \\ A \text{ ?- } P \ x' \ /\ \ t[x'/x] \end{array}$$
Failure

Fails unless the goal's conclusion is a restricted existential quantification.

RESQ_GEN_TAC	(res_quantools)
--------------	-----------------

RESQ_GEN_TAC : tactic

Synopsis

Strips the outermost restricted universal quantifier from the conclusion of a goal.

Description

When applied to a goal $A \text{ ?- } !x::P. t$, the tactic RESQ_GEN_TAC reduces it to a new goal $A, P \ x' \ \text{?-} \ t[x'/x]$ where x' is a variant of x chosen to avoid clashing with any variables free in the goal's assumption list. Normally x' is just x .

$$\frac{A \text{ ?- } !x::P. t}{\text{===== RESQ_GEN_TAC}} A, P \text{ x' ?- } t[x'/x]$$
Failure

Fails unless the goal's conclusion is a restricted universal quantification.

Uses

The tactic `REPEAT RESQ_GEN_TAC` strips away a series of restricted universal quantifiers, and is commonly used before tactics relying on the underlying term structure.

See also

`res_quantTools.RESQ_SPEC`, `res_quantTools.RESQ_SPEC_L`, `Tactic.STRIP_TAC`, `Tactic.GEN_TAC`, `Tactic.X_GEN_TAC`.

RESQ_HALF_SPEC

(res_quantLib)

`RESQ_HALF_SPEC : thm -> thm`

Synopsis

Strip a restricted universal quantification in the conclusion of a theorem.

Description

When applied to a theorem $A \text{ |- } !x::P. t$, the derived inference rule `RESQ_HALF_SPEC` returns the theorem $A \text{ |- } !x. x \text{ IN } P \implies t$, i.e., it transforms the restricted universal quantification to its underlying semantic representation.

$$\frac{A \text{ |- } !x::P. t}{\text{----- RESQ_HALF_SPEC}} A \text{ |- } !x. x \text{ IN } P \implies t$$
Failure

Fails if the theorem's conclusion is not a restricted universal quantification.

See also

`res_quantLib.RESQ_SPEC`.

RESQ_HALF_SPEC

(res_quanTools)

RESQ_HALF_SPEC : (thm -> thm)

Synopsis

Strip a restricted universal quantification in the conclusion of a theorem.

Description

When applied to a theorem $A \vdash !x::P. t$, the derived inference rule RESQ_HALF_SPEC returns the theorem $A \vdash !x. P x ==> t$, i.e., it transforms the restricted universal quantification to its underlying semantic representation.

$$\frac{A \vdash !x::P. t}{A \vdash !x. P x ==> t} \text{ RESQ_HALF_SPEC}$$
Failure

Fails if the theorem's conclusion is not a restricted universal quantification.

See also

res_quanTools.RESQ_SPEC, res_quanTools.RESQ_SPEC_L.

RESQ_IMP_RES_TAC

(res_quanTools)

RESQ_IMP_RES_TAC : thm_tactic

Synopsis

Repeatedly resolves a restricted universally quantified theorem with the assumptions of a goal.

Description

The function RESQ_IMP_RES_TAC performs repeatedly resolution using a restricted quantified theorem. It takes a restricted quantified theorem and transforms it into an implication. This resulting theorem is used in the resolution.

Given a theorem th , the theorem-tactic RESQ_IMP_RES_TAC applies RESQ_IMP_RES_THEN repeatedly to resolve the theorem with the assumptions.

Failure

Never fails

See also

`res_quantTools.RESQ_IMP_RES_THEN`, `res_quantTools.RESQ_RES_THEN`,
`res_quantTools.RESQ_RES_TAC`, `Thm_cont.IMP_RES_THEN`, `Tactic.IMP_RES_TAC`,
`Drule.MATCH_MP`, `Drule.RES_CANON`, `Tactic.RES_TAC`, `Thm_cont.RES_THEN`.

<code>RESQ_IMP_RES_THEN</code>	<code>(res_quantTools)</code>
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`RESQ_IMP_RES_THEN` : `thm_tactical`

Synopsis

Resolves a restricted universally quantified theorem with the assumptions of a goal.

Description

The function `RESQ_IMP_RES_THEN` is the basic building block for resolution using a restricted quantified theorem. It takes a restricted quantified theorem and transforms it into an implication. This resulting theorem is used in the resolution.

Given a theorem-tactic `ttac` and a theorem `th`, the theorem-tactical `RESQ_IMP_RES_THEN` transforms the theorem into an implication `th'`. It then passes `th'` together with `ttac` to `IMP_RES_THEN` to carry out the resolution.

Failure

Evaluating `RESQ_IMP_RES_THEN ttac th` fails if the supplied theorem `th` is not restricted universally quantified, or if the call to `IMP_RES_THEN` fails.

See also

`res_quantTools.RESQ_IMP_RES_TAC`, `res_quantTools.RESQ_RES_THEN`,
`res_quantTools.RESQ_RES_TAC`, `Thm_cont.IMP_RES_THEN`, `Tactic.IMP_RES_TAC`,
`Drule.MATCH_MP`, `Drule.RES_CANON`, `Tactic.RES_TAC`, `Thm_cont.RES_THEN`.

<code>RESQ_MATCH_MP</code>	<code>(res_quantTools)</code>
----------------------------	-------------------------------

`RESQ_MATCH_MP` : `(thm -> thm -> thm)`

Synopsis

Eliminating a restricted universal quantification with automatic matching.

Description

When applied to theorems $A1 \vdash !x::P. Q[x]$ and $A2 \vdash P\ x'$, the derived inference rule `RESQ_MATCH_MP` matches x' to x by instantiating free or universally quantified variables in the first theorem (only), and returns a theorem $A1 \cup A2 \vdash Q[x'/x]$. Polymorphic types are also instantiated if necessary.

$$\frac{A1 \vdash !x::P.Q[x] \quad A2 \vdash P\ x'}{\text{-----} \quad \text{RESQ_MATCH_MP}} \quad A1 \cup A2 \vdash Q[x'/x]$$

Failure

Fails unless the first theorem is a (possibly repeatedly) restricted universal quantification whose quantified variable can be instantiated to match the conclusion of the second theorem, without instantiating any variables which are free in $A1$, the first theorem's assumption list.

See also

`Drule.MATCH_MP`, `res_quantTools.RESQ_HALF_SPEC`.

RESQ_RES_TAC

(res_quantTools)

`RESQ_RES_TAC` : tactic

Synopsis

Enriches assumptions by repeatedly resolving restricted universal quantifications in them against the others.

Description

`RESQ_RES_TAC` uses those assumptions which are restricted universal quantifications in resolution in a way similar to `RES_TAC`. It calls `RESQ_RES_THEN` repeatedly until there is no more resolution can be done. The conclusions of all the new results are returned as additional assumptions of the subgoal(s). The effect of `RESQ_RES_TAC` on a goal is to enrich the assumption set with some of its collective consequences.

Failure

`RESQ_RES_TAC` cannot fail and so should not be unconditionally `REPEATED`.

See also

`res_quantTools.RESQ_IMP_RES_TAC`, `res_quantTools.RESQ_IMP_RES_THEN`,
`res_quantTools.RESQ_RES_THEN`, `Tactic.IMP_RES_TAC`, `Thm_cont.IMP_RES_THEN`,
`Drule.RES_CANON`, `Thm_cont.RES_THEN`, `Tactic.RES_TAC`.

RESQ_RES_THEN	(res_quantTools)
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`RESQ_RES_THEN` : `thm_tactic -> tactic`

Synopsis

Resolves all restricted universally quantified assumptions against other assumptions of a goal.

Description

Like the function `RESQ_IMP_RES_THEN`, the function `RESQ_RES_THEN` performs a single step resolution. The difference is that the restricted universal quantification used in the resolution is taken from the assumptions.

Given a theorem-tactic `ttac`, applying the tactic `RESQ_RES_THEN ttac` to a goal `(asm1,g1)` has the effect of:

```
MAP EVERY (mapfilter ttac [... ; (ai,aj |- vi) ; ...]) (asm1 ?- g)
```

where the theorems `ai,aj |- vi` are all the consequences that can be drawn by a (single) matching modus-ponens inference from the assumptions `asm1` and the implications derived from the restricted universal quantifications in the assumptions.

Failure

Evaluating `RESQ_RES_TAC ttac th` fails if there are no restricted universal quantifications in the assumptions, or if the theorem-tactic `ttac` applied to all the consequences fails.

See also

`res_quantTools.RESQ_IMP_RES_TAC`, `res_quantTools.RESQ_IMP_RES_THEN`,
`res_quantTools.RESQ_RES_TAC`, `Thm_cont.IMP_RES_THEN`, `Tactic.IMP_RES_TAC`,
`Drule.MATCH_MP`, `Drule.RES_CANON`, `Tactic.RES_TAC`, `Thm_cont.RES_THEN`.

RESQ_REWR_CANON	(res_quantLib)
------------------------	-----------------------

`RESQ_REWR_CANON` : `thm -> thm`

Synopsis

Transform a theorem into a form accepted for rewriting.

Description

RESQ_REWR_CANON transforms a theorem into a form accepted by COND_REWR_TAC. The input theorem should be headed by a series of restricted universal quantifications in the following form

$$!x1::P1. \dots !xn::Pn. u[xi] = v[xi])$$

Other variables occurring in u and v may be universally quantified. The output theorem will have all ordinary universal quantifications moved to the outer most level with possible renaming to prevent variable capture, and have all restricted universal quantifications converted to implications. The output theorem will be in the form accepted by COND_REWR_TAC.

Failure

This function fails if the input theorem is not in the correct form.

See also

res_quanLib.RESQ_REWRITE1_TAC, res_quanLib.RESQ_REWRITE1_CONV.

RESQ_REWR_CANON

(res_quanTools)

RESQ_REWR_CANON : thm -> thm

Synopsis

Transform a theorem into a form accepted for rewriting.

Description

RESQ_REWR_CANON transforms a theorem into a form accepted by COND_REWR_TAC. The input theorem should be headed by a series of restricted universal quantifications in the following form

$$!x1::P1. \dots !xn::Pn. u[xi] = v[xi])$$

Other variables occurring in u and v may be universally quantified. The output theorem will have all ordinary universal quantifications moved to the outer most level with possible renaming to prevent variable capture, and have all restricted universal quantifications converted to implications. The output theorem will be in the form accepted by COND_REWR_TAC.

Failure

This function fails if the input theorem is not in the correct form.

See also

`res_quantools.RESQ_REWRITE1_TAC`, `res_quantools.RESQ_REWRITE1_CONV`,
`Cond_rewrite.COND_REWR_CANON`, `Cond_rewrite.COND_REWR_TAC`,
`Cond_rewrite.COND_REWR_CONV`.

<code>RESQ_REWRITE1_CONV</code>	<code>(res_quantLib)</code>
---------------------------------	-----------------------------

```
RESQ_REWRITE1_CONV : thm list -> thm -> conv
```

Synopsis

Rewriting conversion using a restricted universally quantified theorem.

Description

`RESQ_REWRITE1_CONV` is a rewriting conversion similar to `COND_REWRITE1_CONV`. The only difference is the rewriting theorem it takes. This should be an equation with restricted universal quantification at the outer level. It is converted to a theorem in the form accepted by the conditional rewriting conversion.

Suppose that `th` is the following theorem

$$A \vdash !x::P. Q[x] = R[x]$$

evaluating `RESQ_REWRITE1_CONV thms th "t[x']"` will return a theorem

$$A, P\ x' \vdash t[x'] = t'[x']$$

where `t'` is the result of substituting instances of `R[x'/x]` for corresponding instances of `Q[x'/x]` in the original term `t[x]`. All instances of `P x'` which do not appear in the original assumption `asm1` are added to the assumption. The theorems in the list `thms` are used to eliminate the instances `P x'` if it is possible.

Failure

`RESQ_REWRITE1_CONV` fails if `th` cannot be transformed into the required form by the function `RESQ_REWR_CANON`. Otherwise, it fails if no match is found or the theorem cannot be instantiated.

See also

`res_quantLib.RESQ_REWRITE1_TAC`, `res_quantLib.RESQ_REWR_CONV`.

RESQ_REWRITE1_CONV

(res_quanTools)

RESQ_REWRITE1_CONV : thm list -> thm -> conv

Synopsis

Rewriting conversion using a restricted universally quantified theorem.

Description

RESQ_REWRITE1_CONV is a rewriting conversion similar to COND_REWRITE1_CONV. The only difference is the rewriting theorem it takes. This should be an equation with restricted universal quantification at the outer level. It is converted to a theorem in the form accepted by the conditional rewriting conversion.

Suppose that `th` is the following theorem

$$A \vdash !x::P. Q[x] = R[x]$$

evaluating RESQ_REWRITE1_CONV `thms th "t[x']"` will return a theorem

$$A, P\ x' \vdash t[x'] = t'[x']$$

where `t'` is the result of substituting instances of `R[x'/x]` for corresponding instances of `Q[x'/x]` in the original term `t[x]`. All instances of `P x'` which do not appear in the original assumption `asm1` are added to the assumption. The theorems in the list `thms` are used to eliminate the instances `P x'` if it is possible.

Failure

RESQ_REWRITE1_CONV fails if `th` cannot be transformed into the required form by the function RESQ_REWR_CANON. Otherwise, it fails if no match is found or the theorem cannot be instantiated.

See also

`res_quanTools.RESQ_REWRITE1_TAC`, `res_quanTools.RESQ_REWR_CANON`,
`Cond_rewrite.COND_REWR_TAC`, `Cond_rewrite.COND_REWRITE1_CONV`,
`Cond_rewrite.COND_REWR_CONV`, `Cond_rewrite.COND_REWR_CANON`,
`Cond_rewrite.search_top_down`.

RESQ_REWRITE1_TAC

(res_quanLib)

RESQ_REWRITE1_TAC : thm_tactic

Synopsis

Rewriting with a restricted universally quantified theorem.

Description

RESQ_REWRITE1_TAC takes an equational theorem which is restricted universally quantified at the outer level. It calls RESQ_REWR_CANON to convert the theorem to the form accepted by COND_REWR_TAC and passes the resulting theorem to this tactic which carries out conditional rewriting.

Suppose that th is the following theorem

$$A \vdash !x : P. Q[x] = R[x]$$

Applying the tactic RESQ_REWRITE1_TAC th to a goal $(asm1, g1)$ will return a main subgoal $(asm1', g1')$ where $g1'$ is obtained by substituting instances of $R[x'/x]$ for corresponding instances of $Q[x'/x]$ in the original goal $g1$. All instances of $P\ x'$ which do not appear in the original assumption $asm1$ are added to it to form $asm1'$, and they also become new subgoals $(asm1, P\ x')$.

Failure

RESQ_REWRITE1_TAC th fails if th cannot be transformed into the required form by the function RESQ_REWR_CANON. Otherwise, it fails if no match is found or the theorem cannot be instantiated.

See also

`res_quantLib.RESQ_REWRITE1_CONV`, `res_quantLib.RESQ_REWR_CONV`.

RESQ_REWRITE1_TAC	(res_quantTools)
-------------------	------------------

RESQ_REWRITE1_TAC : thm_tactic

Synopsis

Rewriting with a restricted universally quantified theorem.

Description

RESQ_REWRITE1_TAC takes an equational theorem which is restricted universally quantified at the outer level. It calls RESQ_REWR_CANON to convert the theorem to the form accepted by COND_REWR_TAC and passes the resulting theorem to this tactic which carries out conditional rewriting.

Suppose that th is the following theorem

$$A \vdash !x::P. Q[x] = R[x]$$

Applying the tactic `RESQ_REWRITE1_TAC th` to a goal $(asm1, g1)$ will return a main subgoal $(asm1', g1')$ where $g1'$ is obtained by substituting instances of $R[x'/x]$ for corresponding instances of $Q[x'/x]$ in the original goal $g1$. All instances of $P x'$ which do not appear in the original assumption $asm1$ are added to it to form $asm1'$, and they also become new subgoals $(asm1, P x')$.

Failure

`RESQ_REWRITE1_TAC th` fails if `th` cannot be transformed into the required form by the function `RESQ_REWR_CANON`. Otherwise, it fails if no match is found or the theorem cannot be instantiated.

See also

`res_quantools.RESQ_REWRITE1_CONV`, `res_quantools.RESQ_REWR_CANON`,
`Cond_rewrite.COND_REWR_TAC`, `Cond_rewrite.COND_REWRITE1_CONV`,
`Cond_rewrite.COND_REWR_CONV`, `Cond_rewrite.COND_REWR_CANON`,
`Cond_rewrite.search_top_down`.

RESQ_SPEC	(res_quantLib)
-----------	----------------

`RESQ_SPEC : term -> thm -> thm`

Synopsis

Specializes the conclusion of a possibly-restricted universally quantified theorem.

Description

When applied to a term u and a theorem $A \vdash !x::P. t$, `RESQ_SPEC` returns the theorem $A, u \text{ IN } P \vdash t[u/x]$. If necessary, variables will be renamed prior to the specialization to ensure that u is free for x in t , that is, no variables free in u become bound after substitution.

$$\frac{A \vdash !x::P. t}{A, u \text{ IN } P \vdash t[u/x]} \text{ RESQ_SPEC "u"}$$

Additionally, if the input theorem is a standard universal quantification, then `RESQ_SPEC` behaves like `SPEC`.

Failure

Fails if the theorem's conclusion is not restricted universally quantified, or if type instantiation fails.

See also

`res_quanLib.RESQ_HALF_SPEC`.

<div data-bbox="234 656 504 710" data-label="Text"> <p><code>RESQ_SPEC</code></p> </div>	<div data-bbox="973 656 1412 714" data-label="Text"> <p><code>(res_quanTools)</code></p> </div>
--	---

`RESQ_SPEC : (term -> thm -> thm)`

Synopsis

Specializes the conclusion of a restricted universally quantified theorem.

Description

When applied to a term u and a theorem $A \mid- !x::P. t$, `RESQ_SPEC` returns the theorem $A, P u \mid- t[u/x]$. If necessary, variables will be renamed prior to the specialization to ensure that u is free for x in t , that is, no variables free in u become bound after substitution.

$$\frac{A \mid- !x::P. t}{A, P u \mid- t[u/x]} \quad \text{RESQ_SPEC "u"}$$

Failure

Fails if the theorem's conclusion is not restricted universally quantified, or if type instantiation fails.

Example

The following example shows how `RESQ_SPEC` renames bound variables if necessary, prior to substitution: a straightforward substitution would result in the clearly invalid theorem $(\lambda y. 0 < y)y \mid- y = y$.

```
#let th = RESQ_GEN "x:num" "\y.0<y" (REFL "x:num");;
th = |- !x :: \y. 0 < y. x = x

#RESQ_SPEC "y:num" th;;
(\y'. 0 < y')y |- y = y
```

See also

res_quantTools.RESQ_SPECL.

RESQ_SPECL

(res_quantTools)

RESQ_SPECL : (term list -> thm -> thm)

Synopsis

Specializes zero or more variables in the conclusion of a restricted universally quantified theorem.

Description

When applied to a term list $[u_1; \dots; u_n]$ and a theorem $A \mid - !x_1::P_1. \dots !x_n::P_n. \tau$, the inference rule RESQ_SPECL returns the theorem

$$A, P_1 u_1, \dots, P_n u_n \mid - \tau[u_1/x_1] \dots [u_n/x_n]$$

where the substitutions are made sequentially left-to-right in the same way as for RESQ_SPEC, with the same sort of alpha-conversions applied to τ if necessary to ensure that no variables which are free in u_i become bound after substitution.

$$\frac{A \mid - !x_1::P_1. \dots !x_n::P_n. \tau}{A, P_1 u_1, \dots, P_n u_n \mid - \tau[u_1/x_1] \dots [u_n/x_n]} \text{ RESQ_SPECL "[u}_1; \dots; u_n]"$$

It is permissible for the term-list to be empty, in which case the application of RESQ_SPECL has no effect.

Failure

Fails if one of the specialization of the restricted universally quantified variable in the original theorem fails.

See also

res_quantTools.RESQ_GEN_TAC, res_quantTools.RESQ_SPEC.

restart

(proofManagerLib)

restart : unit -> proof

Synopsis

Returns the proof state to the initial goal.

Description

The function `restart` is part of the subgoal package. A call to `restart` clears the proof history and returns to the initial goal. After a call to `restart`, the proof state is the same as it was after the initial call to `set_goal` (or `g`). For a description of the subgoal package, see `set_goal`.

Failure

The function `restart` only fails if no goalstack is being managed.

Uses

Restarting an interactive proof.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`, `proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`, `proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`, `proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

Backup	(proofManagerLib)
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`Backup : unit -> proof`

Synopsis

Restores the proof state of the last save point, undoing the effects of expansions after the save point.

Description

The function `Backup` is part of the subgoal package. A call to `Backup` restores the proof state to the last save point (a proof state saved by `save`). If the current state is a save point then `Backup` clears the current save point and returns to the last save point. If there are no save points in the history, then `Backup` returns to the initial goal and is equivalent to `restart`. For a description of the subgoal package, see `set_goal`.

Failure

The function `Backup` will fail only if no goalstack is being managed.

Uses

Back tracking in a goal-directed proof to a user-defined save point.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`,
`proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`,
`proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`,
`proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

RESTR_EVAL_CONV

(computeLib)

```
RESTR_EVAL_CONV : term list -> conv
```

Synopsis

Symbolically evaluate a term, except for specified constants.

Description

An application `RESTR_EVAL_CONV [c1, ..., cn] M` evaluates the term `M` in the call-by-value style of `EVAL`. When a type instance `c` of any element in `c1,...,cn` is encountered, `c` is not expanded by `RESTR_EVAL_CONV`. The effect is that evaluation stops at `c` (even though any arguments to `c` may be evaluated). This facility can be used to control `EVAL_CONV` to some extent.

Failure

Never fails, but may diverge.

Example

In the following, we first attempt to map the factorial function `FACT` over a list of variables. This attempt goes into a loop, because the conditional statement in the evaluation rule for `FACT` is never determine when the argument is equal to zero. However, if we suppress the evaluation of `FACT`, then we can return a useful answer.

```
- EVAL (Term 'MAP FACT [x; y; z]');    (* loops! *)
> Interrupted.
```

```
- val [FACT] = decls "FACT";    (* find FACT constant *)
> val FACT = 'FACT' : term
```

```
- RESTR_EVAL_CONV [FACT] (Term 'MAP FACT [x; y; z]');
```

```
> val it = |- MAP FACT [x; y; z] = [FACT x; FACT y; FACT z] : thm
```

Uses

Controlling symbolic evaluation when it loops or becomes exponential.

See also

bossLib.EVAL, computeLib.RESTR_EVAL_TAC, computeLib.RESTR_EVAL_RULE, Term.decls.

RESTR_EVAL_RULE	(computeLib)
-----------------	--------------

```
RESTR_EVAL_RULE : term list -> thm -> thm
```

Synopsis

Symbolically evaluate a theorem, except for specified constants.

Description

This is a version of RESTR_EVAL_CONV that works on theorems.

Failure

As for RESTR_EVAL_CONV.

Uses

Controlling symbolic evaluation when it loops or becomes exponential.

See also

bossLib.EVAL, bossLib.EVAL_RULE, computeLib.RESTR_EVAL_CONV, computeLib.RESTR_EVAL_TAC.

RESTR_EVAL_TAC	(computeLib)
----------------	--------------

```
RESTR_EVAL_TAC : term list -> tactic
```

Synopsis

Symbolically evaluate a theorem, except for specified constants.

Description

This is a tactic version of RESTR_EVAL_CONV.

Failure

As for RESTR_EVAL_CONV.

Uses

Controlling symbolic evaluation when it loops or becomes exponential.

See also

bossLib.EVAL, bossLib.EVAL_RULE, bossLib.EVAL_TAC, computeLib.RESTR_EVAL_CONV, computeLib.RESTR_EVAL_RULE.

rev_assoc	(hol88Lib)
-----------	------------

```
rev_assoc : 'a -> ('b * 'a) list -> 'b * 'a
```

Synopsis

Searches a list of pairs for a pair whose second component equals a specified value.

Description

rev_assoc y [(x1,y1), ..., (xn,yn)] returns the first (xi,yi) in the list such that yi equals y. The lookup is done on an eqtype, i.e., the SML implementation must be able to decide equality for the type of y.

Failure

Fails if no matching pair is found. This will always be the case if the list is empty.

Example

```
- rev_assoc 2 [(1,4), (3,2), (2,5), (2,6)];
(3, 2) : (int * int)
```

Comments

Superseded by Lib.rev_assoc and Lib.assoc2.

See also

hol88Lib.assoc, Lib.rev_assoc, Lib.assoc2.

rev_assoc	(Lib)
-----------	-------

```
rev_assoc : 'a -> ('b * 'a) list -> 'b
```

Synopsis

Searches a list of pairs for a pair whose second component equals a specified value.

Description

An invocation `rev_assoc y [(x1,y1), ..., (xn,yn)]` locates the first (x_i, y_i) in a left-to-right scan of the list such that y_i equals y . Then x_i is returned. The lookup is done on an eqtype, i.e., the SML implementation must be able to decide equality for the type of y .

Failure

Fails if no matching pair is found. This will always be the case if the list is empty.

Example

```
- rev_assoc 2 [(1,4), (3,2), (2,5), (2,6)];
> val it = 3 : int
```

See also

`Lib.assoc`, `Lib.assoc1`, `Lib.assoc2`, `Lib.mem`, `Lib.tryfind`, `Lib.exists`, `Lib.all`.

<code>rev_itlist</code>	<code>(Lib)</code>
-------------------------	--------------------

```
rev_itlist : ('a -> 'b -> 'b) -> 'a list -> 'b -> 'b
```

Synopsis

Applies a binary function between adjacent elements of the reverse of a list.

Description

`rev_itlist f [x1, ..., xn] b` returns $f\ x_n\ (\dots\ (f\ x_2\ (f\ x_1\ y))\dots)$. It returns b if the second argument is an empty list.

Failure

Fails if some application of f fails.

Example

```
- rev_itlist (curry op * ) [1,2,3,4] 1;
> val it = 24 : int
```

See also

Lib.itlist, Lib.itlist2, Lib.rev_itlist2, Lib.end_itlist.

<code>rev_itlist2</code>	<code>(Lib)</code>
--------------------------	--------------------

```
rev_itlist2 : ('a -> 'b -> 'c -> 'c) -> 'a list -> 'b list -> 'c -> 'c
```

Synopsis

Applies a function to corresponding elements of 2 lists.

Description

`rev_itlist2 f [x1,...,xn] [y1,...,yn] z` returns

```
f xn yn (f xn-1 yn-1 ... (f x1 y1 z)...) 
```

It returns `z` if both lists are empty.

Failure

Fails if the two lists are of different lengths, or if an application of `f` raises an exception.

Example

```
- rev_itlist2 (fn x => fn y => cons (x,y)) [1,2] [3,4] [];
> val it = [(2, 4), (1, 3)] : (int * int) list
```

See also

Lib.itlist, Lib.rev_itlist, Lib.itlist2, Lib.end_itlist.

<code>reveal</code>	<code>(Parse)</code>
---------------------	----------------------

```
reveal : string -> unit
```

Synopsis

Restores recognition of a constant by the quotation parser.

Description

A call `reveal c`, where `c` the name of a (perhaps) hidden constant, will ‘unhide’ the constant, that is, will make the quotation parser map the identifier `c` to all current

constants with the same name (there may be more than one such as different theories may re-use the same name).

Failure

Never fails, but prints a warning message if the string does not correspond to an actual constant.

Comments

The hiding of a constant only affects the quotation parser; the constant is still there in a theory. If the parameter `c` is already overloaded so as to map to other constants, these overloadings are not altered.

See also

`Parse.hide`, `Parse.hidden`, `Parse.remove_ovl_mapping`, `Parse.update_overload_maps`.

REVERSE	(Tactical)
---------	------------

REVERSE : (tactic -> tactic)

Synopsis

Reverses the order of the generated subgoals.

Description

The tactic `REVERSE T` is a tactic which applies `T` to a goal, and reverses the order of the subgoals generated by `T`.

Failure

The application of `REVERSE` to a tactic `T` never fails. The resulting composite tactic `REVERSE T` fails when applied to a goal if and only if `T` fails.

Comments

Intended for use with `THEN1` to pick the ‘easy’ subgoal.

Example

Given a goal

`G1 /\ G2`

use

```
CONJ_TAC THEN1 TO
THEN ...
```

if the first conjunct is easily dispatched with `TO`, and

```
REVERSE CONJ_TAC THEN1 TO
THEN ...
```

if it is the second conjunct that yields.

See also

`Tactical.EVERY`, `Tactical.FIRST`, `Tactical.ORELSE`, `Tactical.THEN`, `Tactical.THEN1`, `Tactical.THENL`.

REVERSE_CONV	(listLib)
---------------------	------------------

`REVERSE_CONV` : `conv`

Synopsis

Computes by inference the result of reversing a list.

Description

`REVERSE_CONV` takes a term `tm` in the following form:

```
REVERSE [x0; ... xn]
```

It returns the theorem

```
|- REVERSE [x0; ... xn] = [xn; ... x0]
```

where the right-hand side is the list in the reverse order.

Failure

`REVERSE_CONV tm` fails if `tm` is not of the form described above.

Example

Evaluating

```
REVERSE_CONV (--'REVERSE [0;1;2;3;4]'--);
```

returns the following theorem:

```
|- REVERSE [0;1;2;3;4] = [4;3;2;1;0]
```

See also

`listLib.FOLDL_CONV`, `listLib.FOLDR_CONV`, `listLib.list_FOLD_CONV`.

REWR_CONV	(Conv)
------------------	---------------

`REWR_CONV` : (thm -> conv)

Synopsis

Uses an instance of a given equation to rewrite a term.

Description

`REWR_CONV` is one of the basic building blocks for the implementation of rewriting in the HOL system. In particular, the term replacement or rewriting done by all the built-in rewriting rules and tactics is ultimately done by applications of `REWR_CONV` to appropriate subterms. The description given here for `REWR_CONV` may therefore be taken as a specification of the atomic action of replacing equals by equals that is used in all these higher level rewriting tools.

The first argument to `REWR_CONV` is expected to be an equational theorem which is to be used as a left-to-right rewrite rule. The general form of this theorem is:

$$A \vdash t[x_1, \dots, x_n] = u[x_1, \dots, x_n]$$

where x_1, \dots, x_n are all the variables that occur free in the left-hand side of the conclusion of the theorem but do not occur free in the assumptions. Any of these variables may also be universally quantified at the outermost level of the equation, as for example in:

$$A \vdash !x_1 \dots x_n. t[x_1, \dots, x_n] = u[x_1, \dots, x_n]$$

Note that `REWR_CONV` will also work, but will give a generally undesirable result (see below), if the right-hand side of the equation contains free variables that do not also occur free on the left-hand side, as for example in:

$$A \vdash t[x_1, \dots, x_n] = u[x_1, \dots, x_n, y_1, \dots, y_m]$$

where the variables y_1, \dots, y_m do not occur free in $t[x_1, \dots, x_n]$.

If `th` is an equational theorem of the kind shown above, then `REWR_CONV th` returns a conversion that maps terms of the form $t[e_1, \dots, e_n/x_1, \dots, x_n]$, in which the terms e_1, \dots, e_n are free for x_1, \dots, x_n in t , to theorems of the form:

$$A \vdash t[e_1, \dots, e_n/x_1, \dots, x_n] = u[e_1, \dots, e_n/x_1, \dots, x_n]$$

That is, `REWR_CONV th tm` attempts to match the left-hand side of the rewrite rule `th` to the term `tm`. If such a match is possible, then `REWR_CONV` returns the corresponding substitution instance of `th`.

If `REWR_CONV` is given a theorem `th`:

$$A \vdash t[x_1, \dots, x_n] = u[x_1, \dots, x_n, y_1, \dots, y_m]$$

where the variables y_1, \dots, y_m do not occur free in the left-hand side, then the result of applying the conversion `REWR_CONV th` to a term $t[e_1, \dots, e_n/x_1, \dots, x_n]$ will be:

$$A \vdash t[e_1, \dots, e_n/x_1, \dots, x_n] = u[e_1, \dots, e_n, v_1, \dots, v_m/x_1, \dots, x_n, y_1, \dots, y_m]$$

where v_1, \dots, v_m are variables chosen so as to be free nowhere in `th` or in the input term. The user has no control over the choice of the variables v_1, \dots, v_m , and the variables actually chosen may well be inconvenient for other purposes. This situation is, however, relatively rare; in most equations the free variables on the right-hand side are a subset of the free variables on the left-hand side.

In addition to doing substitution for free variables in the supplied equational theorem (or ‘rewrite rule’), `REWR_CONV th tm` also does type instantiation, if this is necessary in order to match the left-hand side of the given rewrite rule `th` to the term argument `tm`. If, for example, `th` is the theorem:

$$A \vdash t[x_1, \dots, x_n] = u[x_1, \dots, x_n]$$

and the input term `tm` is (a substitution instance of) an instance of $t[x_1, \dots, x_n]$ in which the types ty_1, \dots, ty_i are substituted for the type variables vty_1, \dots, vty_i , that is if:

$$tm = t[ty_1, \dots, ty_n/vty_1, \dots, vty_n] [e_1, \dots, e_n/x_1, \dots, x_n]$$

then `REWR_CONV th tm` returns:

$$A \vdash (t = u) [ty_1, \dots, ty_n/vty_1, \dots, vty_n] [e_1, \dots, e_n/x_1, \dots, x_n]$$

Note that, in this case, the type variables vty_1, \dots, vty_i must not occur anywhere in the hypotheses `A`. Otherwise, the conversion will fail.

Failure

`REWR_CONV th` fails if `th` is not an equation or an equation universally quantified at the outermost level. If `th` is such an equation:

$$th = A \vdash !v_1 \dots v_i. t[x_1, \dots, x_n] = u[x_1, \dots, x_n, y_1, \dots, y_n]$$

then `REWR_CONV th tm` fails unless the term `tm` is alpha-equivalent to an instance of the left-hand side `t [x1, ..., xn]` which can be obtained by instantiation of free type variables (i.e. type variables not occurring in the assumptions `A`) and substitution for the free variables `x1, ..., xn`.

Example

The following example illustrates a straightforward use of `REWR_CONV`. The supplied rewrite rule is polymorphic, and both substitution for free variables and type instantiation may take place. `EQ_SYM_EQ` is the theorem:

```
|- !x:'a. !y. (x = y) = (y = x)
```

and `REWR_CONV EQ_SYM_EQ` behaves as follows:

```
- REWR_CONV EQ_SYM_EQ (Term '1 = 2');
> val it = |- (1 = 2) = (2 = 1) : thm
```

```
- REWR_CONV EQ_SYM_EQ (Term '1 < 2');
! Uncaught exception:
! HOL_ERR
```

The second application fails because the left-hand side `x = y` of the rewrite rule does not match the term to be rewritten, namely `1 < 2`.

In the following example, one might expect the result to be the theorem `A |- f 2 = 2`, where `A` is the assumption of the supplied rewrite rule:

```
- REWR_CONV (ASSUME (Term '!x:'a. f x = x')) (Term 'f 2:num');
! Uncaught exception:
! HOL_ERR
```

The application fails, however, because the type variable `'a` appears in the assumption of the theorem returned by `ASSUME (Term '!x:'a. f x = x')`.

Failure will also occur in situations like:

```
- REWR_CONV (ASSUME (Term 'f (n:num) = n')) (Term 'f 2:num');
! Uncaught exception:
! HOL_ERR
```

where the left-hand side of the supplied equation contains a free variable (in this case `n`) which is also free in the assumptions, but which must be instantiated in order to match the input term.

See also

`Rewrite.REWRITE_CONV`.

REWRITE_CONV

(Rewrite)

REWRITE_CONV : (thm list -> conv)

Synopsis

Rewrites a term including built-in tautologies in the list of rewrites.

Description

Rewriting a term using REWRITE_CONV utilizes as rewrites two sets of theorems: the tautologies in the ML list `basic_rewrites` and the ones supplied by the user. The rule searches top-down and recursively for subterms which match the left-hand side of any of the possible rewrites, until none of the transformations are applicable. There is no ordering specified among the set of rewrites.

Variants of this conversion allow changes in the set of equations used: `PURE_REWRITE_CONV` and others in its family do not rewrite with the theorems in `basic_rewrites`.

The top-down recursive search for matches may not be desirable, as this may increase the number of inferences being made or may result in divergence. In this case other rewriting tools such as `ONCE_REWRITE_CONV` and `GEN_REWRITE_CONV` can be used, or the set of theorems given may be reduced.

See `GEN_REWRITE_CONV` for the general strategy for simplifying theorems in HOL using equational theorems.

Failure

Does not fail, but may diverge if the sequence of rewrites is non-terminating.

Uses

Used to manipulate terms by rewriting them with theorems. While resulting in high degree of automation, REWRITE_CONV can spawn a large number of inference steps. Thus, variants such as `PURE_REWRITE_CONV`, or other rules such as `SUBST_CONV`, may be used instead to improve efficiency.

See also

`Rewrite.GEN_REWRITE_CONV`, `Rewrite.ONCE_REWRITE_CONV`, `Rewrite.PURE_REWRITE_CONV`, `Conv.REWR_CONV`, `Drule.SUBST_CONV`.

REWRITE_RULE

(Rewrite)

REWRITE_RULE : (thm list -> thm -> thm)

Synopsis

Rewrites a theorem including built-in tautologies in the list of rewrites.

Description

Rewriting a theorem using `REWRITE_RULE` utilizes as rewrites two sets of theorems: the tautologies in the ML list `basic_rewrites` and the ones supplied by the user. The rule searches top-down and recursively for subterms which match the left-hand side of any of the possible rewrites, until none of the transformations are applicable. There is no ordering specified among the set of rewrites.

Variants of this rule allow changes in the set of equations used: `PURE_REWRITE_RULE` and others in its family do not rewrite with the theorems in `basic_rewrites`. Rules such as `ASM_REWRITE_RULE` add the assumptions of the object theorem (or a specified subset of these assumptions) to the set of possible rewrites.

The top-down recursive search for matches may not be desirable, as this may increase the number of inferences being made or may result in divergence. In this case other rewriting tools such as `ONCE_REWRITE_RULE` and `GEN_REWRITE_RULE` can be used, or the set of theorems given may be reduced.

See `GEN_REWRITE_RULE` for the general strategy for simplifying theorems in HOL using equational theorems.

Failure

Does not fail, but may diverge if the sequence of rewrites is non-terminating.

Uses

Used to manipulate theorems by rewriting them with other theorems. While resulting in high degree of automation, `REWRITE_RULE` can spawn a large number of inference steps. Thus, variants such as `PURE_REWRITE_RULE`, or other rules such as `SUBST`, may be used instead to improve efficiency.

See also

`Rewrite.ASM_REWRITE_RULE`, `Rewrite.GEN_REWRITE_RULE`, `Rewrite.ONCE_REWRITE_RULE`, `Rewrite.PURE_REWRITE_RULE`, `Conv.REWR_CONV`, `Rewrite.REWRITE_CONV`, `Thm.SUBST`.

<code>REWRITE_TAC</code>	<code>(Rewrite)</code>
--------------------------	------------------------

`REWRITE_TAC` : (thm list -> tactic)

Synopsis

Rewrites a goal including built-in tautologies in the list of rewrites.

Description

Rewriting tactics in HOL provide a recursive left-to-right matching and rewriting facility that automatically decomposes subgoals and justifies segments of proof in which equational theorems are used, singly or collectively. These include the unfolding of definitions, and the substitution of equals for equals. Rewriting is used either to advance or to complete the decomposition of subgoals.

REWRITE_TAC transforms (or solves) a goal by using as rewrite rules (i.e. as left-to-right replacement rules) the conclusions of the given list of (equational) theorems, as well as a set of built-in theorems (common tautologies) held in the ML variable `basic_rewrites`. Recognition of a tautology often terminates the subgoaling process (i.e. solves the goal).

The equational rewrites generated are applied recursively and to arbitrary depth, with matching and instantiation of variables and type variables. A list of rewrites can set off an infinite rewriting process, and it is not, of course, decidable in general whether a rewrite set has that property. The order in which the rewrite theorems are applied is unspecified, and the user should not depend on any ordering.

See `GEN_REWRITE_TAC` for more details on the rewriting process. Variants of `REWRITE_TAC` allow the use of a different set of rewrites. Some of them, such as `PURE_REWRITE_TAC`, exclude the basic tautologies from the possible transformations. `ASM_REWRITE_TAC` and others include the assumptions at the goal in the set of possible rewrites.

Still other tactics allow greater control over the search for rewritable subterms. Several of them such as `ONCE_REWRITE_TAC` do not apply rewrites recursively. `GEN_REWRITE_TAC` allows a rewrite to be applied at a particular subterm.

Failure

REWRITE_TAC does not fail. Certain sets of rewriting theorems on certain goals may cause a non-terminating sequence of rewrites. Divergent rewriting behaviour results from a term t being immediately or eventually rewritten to a term containing t as a sub-term. The exact behaviour depends on the HOL implementation.

Example

The arithmetic theorem `GREATER_DEF`, $|- !m n. m > n = n < m$, is used below to advance a goal:

```
- REWRITE_TAC [GREATER_DEF] ([], '5 > 4');
> ([[[]], '4 < 5'], -) : subgoals
```

It is used below with the theorem `LESS_0`, $|- !n. 0 < (SUC n)$, to solve a goal:

```
- val (gl,p) =
  REWRITE_TAC [GREATER_DEF, LESS_0] ([], '(SUC n) > 0');
> val gl = [] : goal list
> val p = fn : proof
```

```
- p[];
> val it = |- (SUC n) > 0 : thm
```

Uses

Rewriting is a powerful and general mechanism in HOL, and an important part of many proofs. It relieves the user of the burden of directing and justifying a large number of minor proof steps. `REWRITE_TAC` fits a forward proof sequence smoothly into the general goal-oriented framework. That is, (within one subgoaling step) it produces and justifies certain forward inferences, none of which are necessarily on a direct path to the desired goal.

`REWRITE_TAC` may be more powerful a tactic than is needed in certain situations; if efficiency is at stake, alternatives might be considered. On the other hand, if more power is required, the simplification functions (`SIMP_TAC` and others) may be appropriate.

See also

`Rewrite.ASM_REWRITE_TAC`, `Rewrite.GEN_REWRITE_TAC`, `Rewrite.FILTER_ASM_REWRITE_TAC`, `Rewrite.FILTER_ONCE_ASM_REWRITE_TAC`, `Rewrite.ONCE_ASM_REWRITE_TAC`, `Rewrite.ONCE_REWRITE_TAC`, `Rewrite.PURE_ASM_REWRITE_TAC`, `Rewrite.PURE_ONCE_ASM_REWRITE_TAC`, `Rewrite.PURE_ONCE_REWRITE_TAC`, `Rewrite.PURE_REWRITE_TAC`, `Conv.REWR_CONV`, `Rewrite.REWRITE_CONV`, `simplib.SIMP_TAC`, `Tactic.SUBST_TAC`.

<code>rewrites</code>	<code>(bossLib)</code>
-----------------------	------------------------

```
rewrites : thm list -> ssfrag
```

Synopsis

Creates an `ssfrag` value consisting of the given theorems as `rewrites`.

Failure

Never fails.

Example

Instead of writing the simpler `SIMP_CONV std_ss thmlist`, one could write

```
SIMP_CONV (std_ss ++ rewrites thmlist) []
```

More plausibly, `rewrites` can be used to create commonly used `ssfrag` values containing a great number of rewrites. This is how the basic system's various `ssfrag` values are constructed where those values consist only of rewrite theorems.

See also

`bossLib.++`, `simplLib.mk_simpset`, `simplLib.SSFRAG`, `bossLib.SIMP_CONV`.

<code>rewrites</code>

<code>(simplLib)</code>

```
rewrites : thm list -> ssfrag
```

Synopsis

Create an `ssfrag` value consisting of the given theorems as rewrites.

Description

`bossLib.rewrites` is identical to `simplLib.rewrites`.

See also

`bossLib.rewrites`.

<code>rhs</code>

<code>(boolSyntax)</code>

```
rhs : term -> term
```

Synopsis

Returns the right-hand side of an equation.

Description

If `M` has the form `t1 = t2` then `rhs M` returns `t2`.

Failure

Fails if term is not an equality.

See also

`boolSyntax.lhs`, `boolSyntax.dest_eq`.

RIGHT_AND_EXISTS_CONV	(Conv)
-----------------------	--------

RIGHT_AND_EXISTS_CONV : conv

Synopsis

Moves an existential quantification of the right conjunct outwards through a conjunction.

Description

When applied to a term of the form $P \wedge (?x.Q)$, the conversion RIGHT_AND_EXISTS_CONV returns the theorem:

$$\vdash P \wedge (?x.Q) = (?x'. P \wedge (Q[x'/x]))$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $P \wedge (?x.Q)$.

See also

Conv.AND_EXISTS_CONV, Conv.EXISTS_AND_CONV, Conv.LEFT_AND_EXISTS_CONV.

RIGHT_AND_FORALL_CONV	(Conv)
-----------------------	--------

RIGHT_AND_FORALL_CONV : conv

Synopsis

Moves a universal quantification of the right conjunct outwards through a conjunction.

Description

When applied to a term of the form $P \wedge (!x.Q)$, the conversion RIGHT_AND_FORALL_CONV returns the theorem:

$$\vdash P \wedge (!x.Q) = (!x'. P \wedge (Q[x'/x]))$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $P \wedge (!x.Q)$.

See also

`Conv.AND_FORALL_CONV`, `Conv.FORALL_AND_CONV`, `Conv.LEFT_AND_FORALL_CONV`.

<code>RIGHT_AND_PEXISTS_CONV</code>	<code>(PairRules)</code>
-------------------------------------	--------------------------

`RIGHT_AND_PEXISTS_CONV` : `conv`

Synopsis

Moves a paired existential quantification of the right conjunct outwards through a conjunction.

Description

When applied to a term of the form $t \wedge (?p. t)$, the conversion `RIGHT_AND_PEXISTS_CONV` returns the theorem:

$$\vdash t \wedge (?p. u) = (?p'. t \wedge (u[p'/p]))$$

where p' is a primed variant of the pair p that does not contain any variables free in the input term.

Failure

Fails if applied to a term not of the form $t \wedge (?p. u)$.

See also

`Conv.RIGHT_AND_EXISTS_CONV`, `PairRules.AND_PEXISTS_CONV`,
`PairRules.PEXISTS_AND_CONV`, `PairRules.LEFT_AND_PEXISTS_CONV`.

<code>RIGHT_AND_PFORALL_CONV</code>	<code>(PairRules)</code>
-------------------------------------	--------------------------

`RIGHT_AND_PFORALL_CONV` : `conv`

Synopsis

Moves a paired universal quantification of the right conjunct outwards through a conjunction.

Description

When applied to a term of the form $t \wedge (!p. u)$, the conversion `RIGHT_AND_PFORALL_CONV` returns the theorem:

$$\vdash t \wedge (!p. u) = (!p'. t \wedge (u[p'/p]))$$

where p' is a primed variant of the pair p that does not contain any variables free in the input term.

Failure

Fails if applied to a term not of the form $t \wedge (!p. u)$.

See also

`Conv.RIGHT_AND_FORALL_CONV`, `PairRules.AND_PFORALL_CONV`,
`PairRules.PFORALL_AND_CONV`, `PairRules.LEFT_AND_PFORALL_CONV`.

RIGHT_BETA	(Drule)
-------------------	----------------

`RIGHT_BETA` : (thm -> thm)

Synopsis

Beta-reduces a top-level beta-redex on the right-hand side of an equation.

Description

When applied to an equational theorem, `RIGHT_BETA` applies beta-reduction at top level to the right-hand side (only). Variables are renamed if necessary to avoid free variable capture.

$$\frac{A \vdash s = (\lambda x. t1) t2}{A \vdash s = t1[t2/x]} \quad \text{RIGHT_BETA}$$

Failure

Fails unless the theorem is equational, with its right-hand side being a top-level beta-redex.

See also

Thm.BETA_CONV, Conv.BETA_RULE, Tactic.BETA_TAC, Drule.RIGHT_LIST_BETA.

RIGHT_CONV_RULE

(Conv)

RIGHT_CONV_RULE : (conv -> thm -> thm)

Synopsis

Applies a conversion to the right-hand side of an equational theorem.

Description

If c is a conversion that maps a term "t2" to the theorem $\vdash t2 = t2'$, then the rule RIGHT_CONV_RULE c infers $\vdash t1 = t2'$ from the theorem $\vdash t1 = t2$. That is, if c "t2" returns $A' \vdash t2 = t2'$, then:

$$\frac{A \vdash t1 = t2}{A \cup A' \vdash t1 = t2'} \text{ RIGHT_CONV_RULE } c$$

Note that if the conversion c returns a theorem with assumptions, then the resulting inference rule adds these to the assumptions of the theorem it returns.

Failure

RIGHT_CONV_RULE c th fails if the conclusion of the theorem th is not an equation, or if th is an equation but c fails when applied its right-hand side. The function returned by RIGHT_CONV_RULE c will also fail if the ML function $c:term \rightarrow thm$ is not, in fact, a conversion (i.e. a function that maps a term t to a theorem $\vdash t = t'$).

See also

Conv.CONV_RULE.

RIGHT_ETA

(Drule)

RIGHT_ETA : thm -> thm

Synopsis

Perform one step of eta-reduction on the right hand side of an equational theorem.

Description

$$\frac{A \vdash M = (\lambda x. (N x))}{A \vdash M = N} \quad x \text{ not free in } N$$
Failure

If the right hand side of the equation is not an eta-redex, or if the theorem is not an equation.

Example

```
- val INC_DEF = new_definition ("INC_DEF", Term `INC = \x. 1 + x`);
> val INC_DEF = |- INC = (\x. 1 + x) : thm

- RIGHT_ETA INC_DEF;
> val it = |- INC = $+ 1 : thm
```

See also

Drule.ETA_CONV, Term.eta_conv.

RIGHT_IMP_EXISTS_CONV

(Conv)

RIGHT_IMP_EXISTS_CONV : conv

Synopsis

Moves an existential quantification of the consequent outwards through an implication.

Description

When applied to a term of the form $P \implies (?x.Q)$, the conversion `RIGHT_IMP_EXISTS_CONV` returns the theorem:

$$\vdash P \implies (?x.Q) = (?x'. P \implies (Q[x'/x]))$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $P \implies (?x.Q)$.

See also

Conv.EXISTS_IMP_CONV, Conv.LEFT_IMP_FORALL_CONV.

RIGHT_IMP_FORALL_CONV

(Conv)

RIGHT_IMP_FORALL_CONV : conv

Synopsis

Moves a universal quantification of the consequent outwards through an implication.

Description

When applied to a term of the form $P \implies (!x.Q)$, the conversion RIGHT_IMP_FORALL_CONV returns the theorem:

$$\vdash P \implies (!x.Q) = (!x'. P \implies (Q[x'/x]))$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $P \implies (!x.Q)$.

See also

Conv.FORALL_IMP_CONV, Conv.LEFT_IMP_EXISTS_CONV.

RIGHT_IMP_PEXISTS_CONV

(PairRules)

RIGHT_IMP_PEXISTS_CONV : conv

Synopsis

Moves a paired existential quantification of the consequent outwards through an implication.

Description

When applied to a term of the form $t \implies (?p. u)$, RIGHT_IMP_PEXISTS_CONV returns the theorem:

$$\vdash t \implies (?p. u) = (?p'. t \implies (u[p'/p]))$$

where p' is a primed variant of the pair p that does not contain any variables that appear free in the input term.

Failure

Fails if applied to a term not of the form $t \implies (?p. u)$.

See also

`Conv.RIGHT_IMP_EXISTS_CONV`, `PairRules.PEXISTS_IMP_CONV`,
`PairRules.LEFT_IMP_PFORALL_CONV`.

<code>RIGHT_IMP_PFORALL_CONV</code>

<code>(PairRules)</code>

`RIGHT_IMP_PFORALL_CONV` : `conv`

Synopsis

Moves a paired universal quantification of the consequent outwards through an implication.

Description

When applied to a term of the form $t \implies (!p. u)$, the conversion `RIGHT_IMP_FORALL_CONV` returns the theorem:

$$\vdash t \implies (!p. u) = (!p'. t \implies (u[p'/p]))$$

where p' is a primed variant of the pair p that does not contain any variables that appear free in the input term.

Failure

Fails if applied to a term not of the form $t \implies (!p. u)$.

See also

`Conv.RIGHT_IMP_FORALL_CONV`, `PairRules.PFORALL_IMP_CONV`,
`PairRules.LEFT_IMP_PEXISTS_CONV`.

<code>RIGHT_LIST_BETA</code>

<code>(Drule)</code>

`RIGHT_LIST_BETA` : `(thm -> thm)`

Synopsis

Iteratively beta-reduces a top-level beta-redex on the right-hand side of an equation.

Description

When applied to an equational theorem, `RIGHT_LIST_BETA` applies beta-reduction over a top-level chain of beta-redexes to the right hand side (only). Variables are renamed if necessary to avoid free variable capture.

$$\frac{A \vdash s = (\lambda x_1 \dots x_n. t) t_1 \dots t_n}{A \vdash s = t[t_1/x_1] \dots [t_n/x_n]} \text{ RIGHT_LIST_BETA}$$

Failure

Fails unless the theorem is equational, with its right-hand side being a top-level beta-redex.

See also

`Thm.BETA_CONV`, `Conv.BETA_RULE`, `Tactic.BETA_TAC`, `Drule.LIST_BETA_CONV`, `Drule.RIGHT_BETA`.

RIGHT_LIST_PBETA	(PairRules)
-------------------------	--------------------

`RIGHT_LIST_PBETA` : (thm -> thm)

Synopsis

Iteratively beta-reduces a top-level paired beta-redex on the right-hand side of an equation.

Description

When applied to an equational theorem, `RIGHT_LIST_PBETA` applies paired beta-reduction over a top-level chain of beta-redexes to the right-hand side (only). Variables are renamed if necessary to avoid free variable capture.

$$\frac{A \vdash s = (\lambda p_1 \dots p_n. t) q_1 \dots q_n}{A \vdash s = t[q_1/p_1] \dots [q_n/p_n]} \text{ RIGHT_LIST_BETA}$$

Failure

Fails unless the theorem is equational, with its right-hand side being a top-level paired beta-redex.

See also

Drule.RIGHT_LIST_BETA, PairRules.PBETA_CONV, PairRules.PBETA_RULE, PairRules.PBETA_TAC, PairRules.LIST_PBETA_CONV, PairRules.RIGHT_PBETA, PairRules.LEFT_PBETA, PairRules.LEFT_LIST_PBETA.

RIGHT_OR_EXISTS_CONV	(Conv)
----------------------	--------

RIGHT_OR_EXISTS_CONV : conv

Synopsis

Moves an existential quantification of the right disjunct outwards through a disjunction.

Description

When applied to a term of the form $P \vee (?x.Q)$, the conversion RIGHT_OR_EXISTS_CONV returns the theorem:

$$\vdash P \vee (?x.Q) = (?x'. P \vee (Q[x'/x]))$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $P \vee (?x.Q)$.

See also

Conv.OR_EXISTS_CONV, Conv.EXISTS_OR_CONV, Conv.LEFT_OR_EXISTS_CONV.

RIGHT_OR_FORALL_CONV	(Conv)
----------------------	--------

RIGHT_OR_FORALL_CONV : conv

Synopsis

Moves a universal quantification of the right disjunct outwards through a disjunction.

Description

When applied to a term of the form $P \vee (!x.Q)$, the conversion RIGHT_OR_FORALL_CONV returns the theorem:

$$\vdash P \vee (!x.Q) = (!x'. P \vee (Q[x'/x]))$$

where x' is a primed variant of x that does not appear free in the input term.

Failure

Fails if applied to a term not of the form $P \vee (!x.Q)$.

See also

`Conv.OR_FORALL_CONV`, `Conv.FORALL_OR_CONV`, `Conv.LEFT_OR_FORALL_CONV`.

RIGHT_OR_PEXISTS_CONV

(PairRules)

`RIGHT_OR_PEXISTS_CONV` : `conv`

Synopsis

Moves a paired existential quantification of the right disjunct outwards through a disjunction.

Description

When applied to a term of the form $t \vee (?p. u)$, the conversion `RIGHT_OR_PEXISTS_CONV` returns the theorem:

$$\vdash t \vee (?p. u) = (?p'. t \vee (u[p'/p]))$$

where p' is a primed variant of the pair p that does not contain any variables free in the input term.

Failure

Fails if applied to a term not of the form $t \vee (?p. u)$.

See also

`Conv.RIGHT_OR_EXISTS_CONV`, `PairRules.OR_PEXISTS_CONV`, `PairRules.PEXISTS_OR_CONV`, `PairRules.LEFT_OR_PEXISTS_CONV`.

RIGHT_OR_PFORALL_CONV

(PairRules)

`RIGHT_OR_PFORALL_CONV` : `conv`

Synopsis

Moves a paired universal quantification of the right disjunct outwards through a disjunction.

Description

When applied to a term of the form $t \vee (!p. u)$, the conversion `RIGHT_OR_FORALL_CONV` returns the theorem:

$$\vdash t \vee (!p. u) = (!p'. t \vee (u[p'/p]))$$

where p' is a primed variant of the pair p that does not contain any variables that appear free in the input term.

Failure

Fails if applied to a term not of the form $t \vee (!p. u)$.

See also

`Conv.RIGHT_OR_FORALL_CONV`, `PairRules.OR_PFORALL_CONV`, `PairRules.PFORALL_OR_CONV`, `PairRules.LEFT_OR_PFORALL_CONV`.

RIGHT_PBETA

(PairRules)

`RIGHT_PBETA : (thm -> thm)`

Synopsis

Beta-reduces a top-level paired beta-redex on the right-hand side of an equation.

Description

When applied to an equational theorem, `RIGHT_PBETA` applies paired beta-reduction at top level to the right-hand side (only). Variables are renamed if necessary to avoid free variable capture.

$$\frac{A \vdash s = (\lambda p. t_1) t_2}{A \vdash s = t_1[t_2/p]} \quad \text{RIGHT_PBETA}$$

Failure

Fails unless the theorem is equational, with its right-hand side being a top-level paired beta-redex.

See also

Drule.RIGHT_BETA, PairRules.PBETA_CONV, PairRules.PBETA_RULE,
PairRules.PBETA_TAC, PairRules.RIGHT_LIST_PBETA, PairRules.LEFT_PBETA,
PairRules.LEFT_LIST_PBETA.

rpair

(Lib)

rpair : 'a -> 'b -> 'b * 'a

Synopsis

Makes two values into a pair, in reverse order.

Description

rpair x y returns (y,x).

Failure

Never fails.

See also

Lib.pair, Lib.swap, Lib.fst, Lib.snd, Lib.curry, Lib.uncurry.

Rsyntax

Rsyntax

Synopsis

A structure that restores a record-style environment for term manipulation.

Description

If one has opened the Psyntax structure, one can open the Rsyntax structure to get record-style functions back.

Each function in the Rsyntax structure has a corresponding function in the Psyntax structure, and vice versa. One can flip-flop between the two structures by opening one and then the other. One can also use long identifiers in order to use both syntaxes at once.

Failure

Never fails.

Example

The following shows how to open the `Rsyntax` structure and the functions that subsequently become available in the top level environment. Documentation for each of these functions is available online.

```

- open Rsyntax;
open Rsyntax
val INST = fn : term subst -> thm -> thm
val INST_TYPE = fn : hol_type subst -> thm -> thm
val INST_TY_TERM = fn : term subst * hol_type subst -> thm -> thm
val SUBST = fn : {thm:thm, var:term} list -> term -> thm -> thm
val SUBST_CONV = fn : {thm:thm, var:term} list -> term -> term -> thm
val define_new_type_bijections = fn
  : {ABS:string, REP:string, name:string, tyax:thm} -> thm
val dest_abs = fn : term -> {Body:term, Bvar:term}
val dest_comb = fn : term -> {Rand:term, Rator:term}
val dest_cond = fn : term -> {cond:term, larm:term, rarm:term}
val dest_conj = fn : term -> {conj1:term, conj2:term}
val dest_cons = fn : term -> {hd:term, tl:term}
val dest_const = fn : term -> {Name:string, Ty:hol_type}
val dest_disj = fn : term -> {disj1:term, disj2:term}
val dest_eq = fn : term -> {lhs:term, rhs:term}
val dest_exists = fn : term -> {Body:term, Bvar:term}
val dest_forall = fn : term -> {Body:term, Bvar:term}
val dest_imp = fn : term -> {ant:term, conseq:term}
val dest_let = fn : term -> {arg:term, func:term}
val dest_list = fn : term -> {els:term list, ty:hol_type}
val dest_pabs = fn : term -> {body:term, varstruct:term}
val dest_pair = fn : term -> {fst:term, snd:term}
val dest_select = fn : term -> {Body:term, Bvar:term}
val dest_type = fn : hol_type -> {Args:hol_type list, Tyop:string}
val dest_var = fn : term -> {Name:string, Ty:hol_type}
val inst = fn : hol_type subst -> term -> term
val match_term = fn : term -> term -> term subst * hol_type subst
val match_type = fn : hol_type -> hol_type -> hol_type subst
val mk_abs = fn : {Body:term, Bvar:term} -> term
val mk_comb = fn : {Rand:term, Rator:term} -> term
val mk_cond = fn : {cond:term, larm:term, rarm:term} -> term

```

```

val mk_conj = fn : {conj1:term, conj2:term} -> term
val mk_cons = fn : {hd:term, tl:term} -> term
val mk_const = fn : {Name:string, Ty:hol_type} -> term
val mk_disj = fn : {disj1:term, disj2:term} -> term
val mk_eq = fn : {lhs:term, rhs:term} -> term
val mk_exists = fn : {Body:term, Bvar:term} -> term
val mk_forall = fn : {Body:term, Bvar:term} -> term
val mk_imp = fn : {ant:term, conseq:term} -> term
val mk_let = fn : {arg:term, func:term} -> term
val mk_list = fn : {els:term list, ty:hol_type} -> term
val mk_pabs = fn : {body:term, varstruct:term} -> term
val mk_pair = fn : {fst:term, snd:term} -> term
val mk_primed_var = fn : {Name:string, Ty:hol_type} -> term
val mk_select = fn : {Body:term, Bvar:term} -> term
val mk_type = fn : {Args:hol_type list, Tyop:string} -> hol_type
val mk_var = fn : {Name:string, Ty:hol_type} -> term
val new_binder = fn : {Name:string, Ty:hol_type} -> unit
val new_constant = fn : {Name:string, Ty:hol_type} -> unit
val new_infix = fn : {Name:string, Prec:int, Ty:hol_type} -> unit
val new_recursive_definition = fn
  : {def:term, fixity:fixity, name:string, rec_axiom:thm} -> thm
val new_specification = fn
  : {consts:{const_name:string, fixity:fixity} list,
     name:string, sat_thm:thm}
  -> thm
val new_type = fn : {Arity:int, Name:string} -> unit
val new_type_definition = fn
  : {inhab_thm:thm, name:string, pred:term} -> thm
val subst = fn : term subst -> term -> term
val subst_occs = fn : int list list -> term subst -> term -> term
val type_subst = fn : hol_type subst -> hol_type -> hol_type

```

See also

Psyntax.

RULE_ASSUM_TAC	(Tactic)
-----------------------	-----------------

RULE_ASSUM_TAC : ((thm -> thm) -> tactic)

Synopsis

Maps an inference rule over the assumptions of a goal.

Description

When applied to an inference rule f and a goal $(\{A_1, \dots, A_n\} \text{ ?- } t)$, the `RULE_ASSUM_TAC` tactical applies the inference rule to each of the `ASSUMED` assumptions to give a new goal.

$$\frac{\{A_1, \dots, A_n\} \text{ ?- } t}{\{f(A_1 \text{ |- } A_1), \dots, f(A_n \text{ |- } A_n)\} \text{ ?- } t} \text{ RULE_ASSUM_TAC } f$$

Failure

The application of `RULE_ASSUM_TAC f` to a goal fails iff f fails when applied to any of the assumptions of the goal.

Comments

It does not matter if the goal has no assumptions, but in this case `RULE_ASSUM_TAC` has no effect.

See also

`Tactical.ASSUM_LIST`, `Tactical.MAP EVERY`, `Tactical.MAP_FIRST`, `Tactical.POP_ASSUM_LIST`.

RW_TAC**(BasicProvers)**

```
RW_TAC : simpset -> thm list -> tactic
```

Synopsis

Simplification with case-splitting and built-in knowledge of declared datatypes.

Description

`bossLib.RW_TAC` is identical to `BasicProvers.RW_TAC`.

See also

`bossLib.RW_TAC`.

RW_TAC**(bossLib)**

```
RW_TAC : simpset -> thm list -> tactic
```

Synopsis

Simplification with case-splitting and built-in knowledge of declared datatypes.

Description

`RW_TAC` is a simplification tactic that provides conditional and contextual rewriting, and automatic invocation of conversions and decision procedures in the course of simplification. An application `RW_TAC ss th1` adds the theorems in `th1` to the simpset `ss` and proceeds to simplify the goal.

The process is based upon the simplification procedures in `simpLib`, but is more persistent in attempting to apply rewrite rules. It automatically incorporates relevant results from datatype declarations (the most important of these are injectivity and distinctness of constructors). It uses the current hypotheses when rewriting the goal. It automatically performs case-splitting on conditional expressions in the goal. It simplifies any equation between constructors occurring in the goal or the hypotheses. It automatically substitutes through the goal any assumption that is an equality $v = M$ or $M = v$, if v is a variable not occurring in M . It eliminates any boolean variable or negated boolean variable occurring as a hypothesis. It breaks down any conjunctions, disjunctions, double negations, or existentials occurring as hypotheses. It keeps the goal in "stripped" format so that the resulting goal will not be an implication or universally quantified.

Failure

Never fails, but may diverge.

Comments

The case splits arising from conditionals and disjunctions can result in many unforeseen subgoals. In that case, `SIMP_TAC` or even `REWRITE_TAC` should be used.

The automatic incorporation of datatype facts can be slow when operating in a context with many datatypes (or a few large datatypes). In such cases, `SRW_TAC` is preferable to `RW_TAC`.

See also

`bossLib.SRW_TAC`, `bossLib.SIMP_TAC`, `Rewrite.REWRITE_TAC`, `bossLib.Hol_datatype`.

S	(Lib)
---	-------

`S : ('a -> 'b -> 'c) -> ('a -> 'b) -> 'a -> 'c`

Synopsis

Generalized function composition: `S f g x equals f x (g x)`.

Failure

$S\ f$ never fails and $S\ f\ g$ never fails, but $S\ f\ g\ x$ fails if $g\ x$ fails or $f\ x\ (g\ x)$ fails.

See also

Lib, Lib.##, Lib.A, Lib.B, Lib.C, Lib.I, Lib.K, Lib.W.

<code>same_const</code>	(Term)
-------------------------	--------

```
same_const : term -> term -> bool
```

Synopsis

Constant time equality check for constants.

Description

In many cases, one needs to check that a constant is an instance of the generic constant originally introduced into the signature, or that two constants are both type instantiations of another. This can be achieved by taking the constants apart with `dest_thy_const` and comparing their name and theory. However, this is relatively inefficient. Instead, one can invoke `same_const`, which takes constant time.

Failure

Never fails.

Example

```
- same_const boolSyntax.universal (rator (concl BOOL_CASES_AX));

> val it = true : bool
```

See also

Term.aconv, Term.dest_thy_const, Term.match_term.

<code>SAT_PROVE</code>	(HolSatLib)
------------------------	-------------

```
val SAT_PROVE : Term.term -> Thm.thm
```

Synopsis

Proves that the supplied term is a tautology, or provides a counterexample.

Description

The supplied term should be purely propositional, i.e., atoms must be Boolean variables or constants, and conditionals must be Boolean-valued. `SAT_PROVE` uses the MiniSat SAT solver's proof logging feature to construct and verify a resolution refutation for the negation of the supplied term.

Failure

Fails if the supplied term is not a tautology. In this case, a theorem providing a satisfying assignment for the negation of the input term is returned, wrapped in an exception.

Example

```
- load "HolSatLib"; open HolSatLib;
(* output omitted *)
> val it = () : unit
- SAT_PROVE `` (a ==> b) /\ (b ==> a) ==> (a=b) ``;
> val it = |- (a ==> b) /\ (b ==> a) ==> (a = b) : thm
- SAT_PROVE `` ~( (a ==> b) /\ (b ==> a) ==> (a=b)) ``
      handle HolSatLib.SAT_cex th => th;
> val it = |- ~b /\ a ==> ~( (a ==> b) /\ (b ==> a) ==> (a = b)) : thm
```

Comments

If MiniSat terminates abnormally, or if the MiniSat binary cannot be located or executed, `SAT_PROVE` falls back to a slower propositional tautology prover implemented in SML. For low-level use of SAT solver facilities and other details, see the section on the HolSat library in the HOL Description.

save	(proofManagerLib)
------	-------------------

save : unit -> proof

Synopsis

Marks the current proof state as a save point, and clears the automatic undo history.

Description

The function `save` is part of the subgoal package. A call to `save` clears the automatic proof history and marks the current state as a save point. A call to `backup` at a save

point will fail. In contrast to `forget_history`, however, `save` does not clear the initial goal or any previous save points. Therefore a call to `restore` or `restart` at a save point will succeed. For a description of the subgoal package, see `set_goal`.

Failure

The function `save` will fail only if no goalstack is being managed.

Uses

Creating save points in an interactive proof, to allow user-directed back tracking. This is in contrast to the automatic back tracking facilitated by `backup`.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`, `proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`, `proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`, `proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

<div data-bbox="236 994 474 1041" data-label="Text"> <p><code>save_thm</code></p> </div>	<div data-bbox="1171 987 1409 1046" data-label="Text"> <p>(Theory)</p> </div>
--	---

```
save_thm : string * thm -> thm
```

Synopsis

Stores a theorem in the current theory segment.

Description

The call `save_thm(name, th)` adds the theorem `th` to the current theory segment under the name `name`. The theorem is also the return value of the call. When the current segment `thy` is exported, things are arranged in such a way that, if `thyTheory` is loaded into a later session, the ML variable `thyTheory.name` will have `th` as its value.

Failure

If `th` is out-of-date, then `save_thm` will fail. If `name` is not a valid ML alphanumeric identifier, `save_thm` will not fail, but `export_theory` will (printing an informative error message first).

Example

```
- val foo = save_thm("foo", REFL (Term 'x:bool'));
> val foo = |- x = x : thm

- current_theorems();
> val it = [("foo", |- x = x)] : (string * thm) list
```


Comments

If a theorem is already saved under `name` in the current theory segment, it will be overwritten.

The results of `new_axiom`, and definition principle (such as `new_definition`, `new_type_definition`, and `new_specification`) are automatically stored in the current theory: one does not have to call `save_thm` on them.

Uses

Saving important theorems for eventual export. Binding the result of `save_thm` to an ML variable makes it easy to access the theorem in the remainder of the current session.

See also

`Theory.new_theory`, `Tactical.store_thm`, `DB.fetch`, `DB.thy`,
`Theory.current_definitions`, `Theory.current_theorems`, `Theory.uptodate_thm`,
`Theory.new_axiom`, `Definition.new_type_definition`, `Definition.new_definition`,
`Definition.new_specification`.

<div data-bbox="161 1048 255 1099" data-label="Text"><code>say</code></div>	<div data-bbox="1182 1041 1331 1093" data-label="Text"><code>(Lib)</code></div>
---	---

```
say : string -> unit
```

Synopsis

Print a string.

Description

An application `say s` prints the string `s` on the standard output.

Failure

Never fails.

Comments

The Standard ML Basis Library structure `TextIO` offers related functions.

<div data-bbox="161 1814 397 1868" data-label="Text"><code>SBC_CONV</code></div>	<div data-bbox="1011 1812 1331 1865" data-label="Text"><code>(reduceLib)</code></div>
--	---

```
SBC_CONV : conv
```

Synopsis

Calculates by inference the difference of two numerals.

Description

If m and n are numerals (e.g. 0, 1, 2, 3,...), then `SBC_CONV "m - n"` returns the theorem:

$$\vdash m - n = s$$

where s is the numeral that denotes the difference of the natural numbers denoted by m and n .

Failure

`SBC_CONV tm` fails unless tm is of the form "m - n", where m and n are numerals.

Example

```
#SBC_CONV "25 - 30";;
|- 25 - 30 = 0
```

```
#SBC_CONV "200 - 200";;
|- 200 - 200 = 0
```

```
#SBC_CONV "60 - 17";;
|- 60 - 17 = 43
```

SCANL_CONV	(listLib)
-------------------	------------------

`SCANL_CONV : conv -> conv`

Synopsis

Computes by inference the result of applying a function to the elements of a list.

Description

`SCANL_CONV` takes a conversion `conv` and a term tm in the following form:

$$\text{SCANL } f \ e0 \ [x1; \dots; xn]$$

It returns the theorem

$$\vdash \text{SCANL } f \ e0 \ [x1; \dots; xn] = [e0; e1; \dots; en]$$

where e_i is the result of applying the function f to the result of the previous iteration and the current element, i.e., $e_i = f\ e_{(i-1)}\ x_i$. The iteration starts from the left-hand side (the head) of the list. The user supplied conversion `conv` is used to derive a theorem

$$\vdash f\ e_{(i-1)}\ x_i = e_i$$

which is used in the next iteration.

Failure

`SCANL_CONV conv tm` fails if `tm` is not of the form described above, or failure occurs when evaluating `conv (--'f e(i-1) xi'--)`.

Example

To sum the elements of a list and save the result at each step, one can use `SCANL_CONV` with `ADD_CONV` from the library `num_lib`.

```
- load_library_in_place num_lib;
- SCANL_CONV Num_lib.ADD_CONV (--'SCANL $+ 0 [1;2;3]'--);
| - SCANL $+ 0 [1;2;3] = [0;1;3;6]
```

In general, if the function f is an explicit lambda abstraction $(\lambda x\ x'.\ t[x,x'])$, the conversion should be in the form

$$((\text{RATOR_CONV BETA_CONV}) \text{ THENC BETA_CONV THENC conv'})$$

where `conv'` applied to $t[x,x']$ returns the theorem

$$\vdash t[x,x'] = e''.$$

See also

`listLib.SCANR_CONV`, `listLib.FOLDL_CONV`, `listLib.FOLDR_CONV`,
`listLib.list_FOLD_CONV`.

<div data-bbox="161 1592 453 1644" data-label="Text"> <h1 style="margin: 0;">SCANR_CONV</h1> </div>	<div data-bbox="1067 1592 1331 1644" data-label="Text"> <h1 style="margin: 0;">(listLib)</h1> </div>
---	--

`SCANR_CONV` : `conv -> conv`

Synopsis

Computes by inference the result of applying a function to the elements of a list.

Description

`SCANR_CONV` takes a conversion `conv` and a term `tm` in the following form:

```
SCANR f e0 [xn;...;x1]
```

It returns the theorem

```
|- SCANR f e0 [xn;...;x1] = [en; ...;e1;e0]
```

where e_i is the result of applying the function f to the result of the previous iteration and the current element, i.e., $e_i = f\ e^{(i-1)}\ x_i$. The iteration starts from the right-hand side (the tail) of the list. The user supplied conversion `conv` is used to derive a theorem

```
|- f e^{(i-1)} x_i = e_i
```

which is used in the next iteration.

Failure

`SCANR_CONV conv tm` fails if `tm` is not of the form described above, or failure occurs when evaluating `conv (--'f e^{(i-1)} xi'--)`.

Example

To sum the elements of a list and save the result at each step, one can use `SCANR_CONV` with `ADD_CONV` from the library `num_lib`.

```
- load_library_in_place num_lib;
- SCANR_CONV Num_lib.ADD_CONV (--'SCANR $+ 0 [1;2;3]'--);
|- SCANR $+ 0 [1;2;3] = [6;5;3;0]
```

In general, if the function f is an explicit lambda abstraction $(\lambda x\ x'.\ t[x,x'])$, the conversion should be in the form

```
((RATOR_CONV BETA_CONV) THENC BETA_CONV THENC conv')
```

where `conv'` applied to $t[x,x']$ returns the theorem

```
|-t[x,x'] = e''.
```

See also

`listLib.SCANL_CONV`, `listLib.FOLDL_CONV`, `listLib.FOLDR_CONV`,
`listLib.list_FOLD_CONV`.

scrub	(Theory)
--------------	-----------------

```
scrub : unit -> unit
```

Synopsis

Remove all out-of-date elements from the current theory segment.

Description

An invocation `scrub()` goes through the current theory segment and removes all out-of-date elements.

Failure

Never fails.

Example

In the following, we define a concrete type and examine the current theory segment to see what consequences of this definition have been stored there. Then we delete the type, which turns all those consequences into garbage. A query, like `current_theorems`, shows that this garbage is not collected automatically. A manual invocation of `scrub` is necessary to show the true state of play.

```
- Hol_datatype 'foo = A | B of 'a';
<<HOL message: Defined type: "foo">>
> val it = () : unit

- current_theorems();
> val it =
  [("foo_induction", |- !P. P A /\ (!a. P (B a)) ==> !f. P f),
   ("foo_Axiom", |- !f0 f1. ?fn. (fn A = f0) /\ !a. fn (B a) = f1 a),
   ("foo_nchotomy", |- !f. (f = A) \\/ ?a. f = B a),
   ("foo_case_cong",
    |- !M M' v f.
      (M = M') /\ ((M' = A) ==> (v = v')) /\
      (!a. (M' = B a) ==> (f a = f' a)) ==>
      (case v f M = case v' f' M')),
   ("foo_distinct", |- !a. ~(A = B a)),
   ("foo_11", |- !a a'. (B a = B a') = (a = a'))] : (string * thm) list

- delete_type "foo";
> val it = () : unit

- current_theorems();
> val it =
  [("foo_induction", |- !P. P A /\ (!a. P (B a)) ==> !f. P f),
   ("foo_Axiom", |- !f0 f1. ?fn. (fn A = f0) /\ !a. fn (B a) = f1 a),
```

```

("foo_nchotomy", |- !f. (f = A) \ / ?a. f = B a),
("foo_case_cong",
 |- !M M' v f.
      (M = M') /\ ((M' = A) ==> (v = v')) /\
      (!a. (M' = B a) ==> (f a = f' a)) ==>
      (case v f M = case v' f' M')),
("foo_distinct", |- !a. ~(A = B a)),
("foo_11", |- !a a'. (B a = B a') = (a = a'))] : (string * thm) list

- scrub();
> val it = () : unit

- current_theorems();
> val it = [] : (string * thm) list

```

Uses

When `export_theory` is called, it uses `scrub` to prepare the current segment for export. Users can also call `scrub` to find out what setting they are really working in.

See also

`Theory.uptodate_type`, `Theory.uptodate_term`, `Theory.uptodate_thm`,
`Theory.delete_type`, `Theory.delete_const`.

<div data-bbox="236 1352 676 1408" data-label="Text"> <p><code>search_top_down</code></p> </div>	<div data-bbox="1002 1352 1412 1406" data-label="Text"> <p><code>(Cond_rewrite)</code></p> </div>
--	---

```

search_top_down
: (term -> term -> ((term # term) list # (type # type) list) list)

```

Synopsis

Search a term in a top-down fashion to find matches to another term.

Description

`search_top_down tm1 tm2` returns a list of instantiations which make the whole or part of `tm2` match `tm1`. The first term should not have a quantifier at the outer most level. `search_top_down` first attempts to match the whole second term to `tm1`. If this fails, it recursively descend into the subterms of `tm2` to find all matches.

The length of the returned list indicates the number of matches found. An empty list means no match can be found between t_{m1} and t_{m2} or any subterms of t_{m2} . The instantiations returned in the list are in the same format as for the function `match`. Each instantiation is a pair of lists: the first is a list of term pairs and the second is a list of type pairs. Either of these lists may be empty. The situation in which both lists are empty indicates that there is an exact match between the two terms, i.e., no instantiation is required to make the entire t_{m2} or a part of t_{m2} the same as t_{m1} .

Failure

Never fails.

Example

```
#search_top_down "x = y:*" "3 = 5";;
[[(["5", "y"); ("3", "x")], [(":num", " :*")]]]
: ((term # term) list # (type # type) list) list
```

```
#search_top_down "x = y:*" "x =y:*";;
[[[]], []] : ((term # term) list # (type # type) list) list
```

```
#search_top_down "x = y:*" "0 < p ==> (x <= p = y <= p)";;
[[(["y <= p", "y"); ("x <= p", "x")], [(":bool", " :*")]]]
: ((term # term) list # (type # type) list) list
```

The first example above shows the entire t_{m2} matching t_{m1} . The second example shows the two terms match exactly. No instantiation is required. The last example shows that a subterm of t_{m2} can be instantiated to match t_{m1} .

See also

`Db.match`.

SEG_CONV	(listLib)
----------	-----------

SEG_CONV : conv

Synopsis

Computes by inference the result of taking a segment of a list.

Description

For any object language list of the form `-- '[x0; ...x(n-1)]' --`, the result of evaluating

```
SEG_CONV (--'SEG m k [x0;...;x(n-1)]'--)
```

is the theorem

$$\vdash \text{SEG } m \ k \ [x_0; \dots; x_{(n-1)}] = [x_k; \dots; x_{(m+k-1)}]$$

Failure

`SEG_CONV tm` fails if `tm` is not in the form described above or the indexes `m` and `k` are not in the correct range, i.e., $m + k \leq n$.

Example

Evaluating the expression

```
SEG_CONV (--'SEG 2 3[0;1;2;3;4;5]'--);
```

returns the following theorem

$$\vdash \text{SEG } 2 \ 3[0;1;2;3;4;5] = [3;4]$$

See also

`listLib.FIRSTN_CONV`, `listLib.LASTN_CONV`, `listLib.BUTFIRSTN_CONV`,
`listLib.BUTLASTN_CONV`, `listLib.LAST_CONV`, `listLib.BUTLAST_CONV`.

<div data-bbox="236 1312 416 1359" data-label="Text"> <p><code>select</code></p> </div>	<div data-bbox="1058 1308 1414 1366" data-label="Text"> <p>(<code>boolSyntax</code>)</p> </div>
---	---

`select` : term

Synopsis

Constant denoting Hilbert's choice operator.

Description

The ML variable `boolSyntax.select` is bound to the term `min$@`.

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.T`, `boolSyntax.F`,
`boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`,
`boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.negation`,
`boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let.tm`,
`boolSyntax.arb`.

SELECT_CONV

(Conv)

SELECT_CONV : conv

Synopsis

Eliminates an epsilon term by introducing an existential quantifier.

Description

The conversion SELECT_CONV expects a boolean term of the form $P[@x.P[x]/x]$, which asserts that the epsilon term $@x.P[x]$ denotes a value, x say, for which $P[x]$ holds. This assertion is equivalent to saying that there exists such a value, and SELECT_CONV applied to a term of this form returns the theorem $\vdash P[@x.P[x]/x] = ?x. P[x]$.

Failure

Fails if applied to a term that is not of the form $P[@x.P[x]/x]$.

Example

```
SELECT_CONV (Term '(@n. n < m) < m');
val it = |- (@n. n < m) < m = (?n. n < m) : thm
```

Uses

Particularly useful in conjunction with CONV_TAC for proving properties of values denoted by epsilon terms. For example, suppose that one wishes to prove the goal

$$([0 < m], (@n. n < m) < \text{SUC } m)$$

Using the built-in arithmetic theorem

$$\text{LESS_SUC} \quad \vdash !m \ n. m < n \implies m < (\text{SUC } n)$$

this goal may be reduced by the tactic MATCH_MP_TAC LESS_SUC to the subgoal

$$([0 < m], (@n. n < m) < m)$$

This is now in the correct form for using CONV_TAC SELECT_CONV to eliminate the epsilon term, resulting in the existentially quantified goal

$$([0 < m], ?n. n < m)$$

which is then straightforward to prove.

See also

`Drule.SELECT_ELIM`, `Drule.SELECT_INTRO`, `Drule.SELECT_RULE`.

SELECT_ELIM	(Drule)
--------------------	----------------

`SELECT_ELIM : thm -> term * thm -> thm`

Synopsis

Eliminates an epsilon term, using deduction from a particular instance.

Description

`SELECT_ELIM` expects two arguments, a theorem `th1`, and a pair `(v,th2) : term * thm`. The conclusion of `th1` should have the form `P($@ P)`, which asserts that the epsilon term `$@ P` denotes some value at which `P` holds. In `th2`, the variable `v` appears only in the assumption `P v`. The conclusion of the resulting theorem matches that of `th2`, and the hypotheses include the union of all hypotheses of the premises excepting `P v`.

$$\frac{A1 \mid- P(\$@ P) \quad A2 \text{ u } \{P \ v\} \mid- t}{A1 \text{ u } A2 \mid- t} \quad \text{SELECT_ELIM } th1 \ (v,th2)$$

where `v` is not free in `A2`. The argument to `P` in the conclusion of `th1` may actually be any term `x`. If `v` appears in the conclusion of `th2`, this argument `x` (usually the epsilon term) will NOT be eliminated, and the conclusion will be `t[x/v]`.

Failure

Fails if the first theorem is not of the form `A1 \mid- P x`, or if the variable `v` occurs free in any other assumption of `th2`.

Example

If a property of functions is defined by:

$$\text{INCR} = \mid- !f. \text{INCR } f = (!t1 \ t2. t1 < t2 ==> (f \ t1) < (f \ t2))$$

The following theorem can be proved.

$$th1 = \mid- \text{INCR}(@f. \text{INCR } f)$$

Additionally, if such a function is assumed to exist, then one can prove that there also exists a function which is injective (one-to-one) but not surjective (onto).

```
th2 = [ INCR g ] |- ?h. ONE_ONE h /\ ~ONTO h
```

These two results may be combined using `SELECT_ELIM` to give a new theorem:

```
- SELECT_ELIM th1 ('g:num->num', th2);
val it = |- ?h. ONE_ONE h /\ ~ONTO h : thm
```

Uses

This rule is rarely used. The equivalence of $P(\$@ P)$ and $\$? P$ makes this rule fundamentally similar to the $?-$ elimination rule `CHOOSE`.

See also

`Thm.CHOOSE`, `Conv.SELECT_CONV`, `Tactic.SELECT_ELIM_TAC`, `Drule.SELECT_INTRO`, `Drule.SELECT_RULE`.

SELECT_ELIM_TAC

(Tactic)

```
SELECT_ELIM_TAC : tactic
```

Synopsis

Eliminates a Hilbert-choice ("selection") term from the goal.

Description

`SELECT_ELIM_TAC` searches the goal it is applied to for terms involving the Hilbert-choice operator, of the form $@x. \dots$. If such a term is found, then the tactic will produce a new goal, where the choice term has disappeared. The resulting goal will require the proof of the non-emptiness of the choice term's predicate, and that any possible choice of value from that predicate will satisfy the original goal.

Thus, `SELECT_ELIM_TAC` can be seen as a higher-order match against the theorem

$$|- !P Q. (?x. P x) /\ (!x. P x ==> Q x) ==> Q ($@ P)$$

where the new goal is the antecedent of the implication. (This theorem is `SELECT_ELIM_THM`, from theory `bool`.)

Example

When applied to this goal,

```
- SELECT_ELIM_TAC ([], '@(x. x < 4) < 5');
> val it = ([([], '@(?x. x < 4) /\ !x. x < 4 ==> x < 5']), fn) :
  (term list * term) list * (thm list -> thm)
```

the resulting goal requires the proof of the existence of a number less than 4, and also that any such number is also less than 5.

Failure

Fails if there are no choice terms in the goal.

Comments

If the choice-term's predicate is everywhere false, goals involving such terms will be true only if the choice of term makes no difference at all. Such situations can be handled with the use of `SPEC_TAC`. Note also that the choice of select term to eliminate is made in an unspecified manner.

See also

`Drule.SELECT_ELIM`, `Drule.SELECT_INTRO`, `Drule.SELECT_RULE`, `Tactic.SPEC_TAC`.

SELECT_EQ	(Drule)
------------------	----------------

`SELECT_EQ : (term -> thm -> thm)`

Synopsis

Applies epsilon abstraction to both terms of an equation.

Description

Effects the extensionality of the epsilon operator @.

$$\frac{A \mid- t1 = t2}{A \mid- (@x.t1) = (@x.t2)} \quad \text{SELECT_EQ "x"} \quad [\text{where } x \text{ is not free in } A]$$

Failure

Fails if the conclusion of the theorem is not an equation, or if the variable `x` is free in `A`.

Example

Given a theorem which shows the equivalence of two distinct forms of defining the property of being an even number:

$$\text{th} = \mid- (x \text{ MOD } 2 = 0) = (?y. x = 2 * y)$$

A theorem giving the equivalence of the epsilon abstraction of each form is obtained:

```
- SELECT_EQ (Term 'x:num') th;
> val it = |- (@x. x MOD 2 = 0) = (@x. ?y. x = 2 * y) : thm
```

See also

Thm.ABS, Thm.AP_TERM, Drule.EXISTS_EQ, Drule.FORALL_EQ, Conv.SELECT_CONV, Drule.SELECT_ELIM, Drule.SELECT_INTRO.

SELECT_INTRO

(Drule)

SELECT_INTRO : (thm -> thm)

Synopsis

Introduces an epsilon term.

Description

SELECT_INTRO takes a theorem with an applicative conclusion, say $P\ x$, and returns a theorem with the epsilon term $\$@ P$ in place of the original operand x .

$$\frac{A \vdash P\ x}{A \vdash P(\$@ P)} \text{ SELECT_INTRO}$$

The returned theorem asserts that $\$@ P$ denotes some value at which P holds.

Failure

Fails if the conclusion of the theorem is not an application.

Example

Given the theorem

```
th1 = |- (\n. m = n)m
```

applying SELECT_INTRO replaces the second occurrence of m with the epsilon abstraction of the operator:

```
- val th2 = SELECT_INTRO th1;
val th2 = |- (\n. m = n)(@$ m = n) : thm
```

This theorem could now be used to derive a further result:

```
- EQ_MP (BETA_CONV(concl th2)) th2;
val it = |- m = (@n. m = n) : thm
```

See also

Thm.EXISTS, Conv.SELECT_CONV, Drule.SELECT_ELIM, Drule.SELECT_RULE.

SELECT_RULE	(Drule)
-------------	---------

SELECT_RULE : thm -> thm

Synopsis

Introduces an epsilon term in place of an existential quantifier.

Description

The inference rule SELECT_RULE expects a theorem asserting the existence of a value x such that P holds. The equivalent assertion that the epsilon term $@x.P$ denotes a value of x for which P holds is returned as a theorem.

$$\frac{A \mid- ?x. P}{A \mid- P[(@x.P)/x]} \quad \text{SELECT_RULE}$$
Failure

Fails if applied to a theorem the conclusion of which is not existentially quantified.

Example

The axiom INFINITY_AX in the theory ind is of the form:

$$\mid- ?f. \text{ONE_ONE } f \wedge \sim\text{ONTO } f$$

Applying SELECT_RULE to this theorem returns the following.

```
- SELECT_RULE INFINITY_AX;
> val it =
  \mid- ONE_ONE (@f. ONE_ONE f /\ ~ONTO f) /\ ~ONTO @f. ONE_ONE f /\ ~ONTO f
  : thm
```

Uses

May be used to introduce an epsilon term to permit rewriting with a constant defined using the epsilon operator.

See also

Thm.CHOOSE, Conv.SELECT_CONV, Drule.SELECT_ELIM, Drule.SELECT_INTRO.

<div style="display: flex; justify-content: space-between;"> set_backup (proofManagerLib) </div>
--

```
proofManagerLib.set_backup : int -> unit
```

Synopsis

Limits the number of proof states saved on the subgoal package backup list.

Description

The assignable variable `set_backup` is initially set to 12. Its value is one less than the maximum number of proof states that may be saved on the backup list. Adding a new proof state (by, for example, a call to `expand`) after the maximum is reached causes the earliest proof state on the list to be discarded. For a description of the subgoal package, see `set_goal`.

Example

```
- set_backup 0;
() unit

- g '(HD[1;2;3] = 1) /\ (TL[1;2;3] = [2;3])';
> val it =
  Proof manager status: 1 proof.
  1. Incomplete:
    Initial goal:
    (HD [1; 2; 3] = 1) /\ (TL [1; 2; 3] = [2; 3])

    : proofs

- e CONJ_TAC;
OK..
2 subgoals:
> val it =
  TL [1; 2; 3] = [2; 3]
```

```

    HD [1; 2; 3] = 1

    :proof

- e (REWRITE_TAC[listTheory.HD]);
OK..

Goal proved.
|- HD [1; 2; 3] = 1

Remaining subgoals:
> val it =
    TL [1; 2; 3] = [2; 3]

    : proof

- b();
> val it =
    TL [1; 2; 3] = [2; 3]

    HD [1; 2; 3] = 1

    : proof

- b();
! Uncaught exception:
! CANT_BACKUP_ANYMORE

```

See also

proofManagerLib.set_goal, proofManagerLib.restart, proofManagerLib.backup,
proofManagerLib.restore, proofManagerLib.save, proofManagerLib.set_backup,
proofManagerLib.expand, proofManagerLib.expandf, proofManagerLib.p,
proofManagerLib.top_thm, proofManagerLib.top_goal.

<code>set_diff</code>	<code>(Lib)</code>
-----------------------	--------------------

`set_diff` : 'a list -> 'a list -> 'a list

Synopsis

Computes the set-theoretic difference of two ‘sets’.

Description

`set_diff l1 l2` returns a list consisting of those elements of `l1` that do not appear in `l2`. It is identical to `Lib.subtract`.

Failure

Never fails.

Example

```
- set_diff [] [1,2];
> val it = [] : int list

- set_diff [1,2,3] [2,1];
> val it = [3] : int list
```

Comments

The order in which the elements occur in the resulting list should not be depended upon.

A high-performance implementation of finite sets may be found in structure `HOLset`.

ML equality types are used in the implementation of `union` and its kin. This limits its applicability to types that allow equality. For other types, typically abstract ones, use the ‘op_’ variants.

See also

`Lib.op_set_diff`, `Lib.subtract`, `Lib.mk_set`, `Lib.set_eq`, `Lib.union`, `Lib.intersect`.

<code>set_eq</code>

<code>(Lib)</code>

```
set_eq : 'a list -> 'a list -> bool
```

Synopsis

Tells whether two lists have the same elements.

Description

An application `set_eq l1 l2` returns `true` just in case `l1` and `l2` are permutations of each other when duplicate elements within each list are ignored.

Failure

Never fails.

Example

```
- set_eq [1,2,1] [1,2,2,1];
> val it = true : bool

- set_eq [1,2,1] [2,1];
> val it = true : bool
```

Comments

A high-performance implementation of finite sets may be found in structure `HOLset`.

ML equality types are used in the implementation of `set_eq` and its kin. This limits its applicability to types that allow equality. For other types, typically abstract ones, use the ‘`op_`’ variants.

See also

`Lib.intersect`, `Lib.union`, `Lib.U`, `Lib.mk_set`, `Lib.mem`, `Lib.insert`, `Lib.set_diff`.

<code>set_fixity</code>	(Parse)
-------------------------	---------

```
set_fixity : string -> fixity -> unit
```

Synopsis

Allows the fixity of tokens to be updated.

Description

The `set_fixity` function is used to change the fixity of single tokens. It implements this functionality rather crudely. When called on to set the fixity of `t` to `f`, it removes all rules mentioning `t` from the global (term) grammar, and then adds a new rule to the grammar. The new rule maps occurrences of `t` with the given fixity to terms of the same name.

Failure

This function fails if the new fixity causes a clash with existing rules, as happens if the precedence level of the specified fixity is already taken by rules using a fixity of a different type. Even if the application of `set_fixity` succeeds, it may cause the next subsequent application of the `Term` parsing function to complain about precedence conflicts

in the operator precedence matrix. These problems may cause the parser to behave oddly on terms involving the token whose fixity was set. Excessive parentheses will usually cure even these problems.

Example

After a new constant is defined, `set_fixity` can be used to give it an appropriate parse status:

```
- val thm = Psyntax.new_recursive_definition
      prim_recTheory.num_Axiom "f"
      (Term'(f 0 n = n) /\ (f (SUC n) m = SUC (SUC (f n m))))');
> val thm =
  |- (!n. f 0 n = n) /\ !n m. f (SUC n) m = SUC (SUC (f n m))
    : thm
- set_fixity "f" (Infixl 500);
> val it = () : unit
- thm;
> val it =
  |- (!n. 0 f n = n) /\ !n m. SUC n f m = SUC (SUC (n f m)) : thm
```

The same function can be used to alter the fixities of existing constants:

```
- val t = Term'2 + 3 + 4 - 6';
> val t = '2 + 3 + 4 - 6' : term
- set_fixity "+" (Infixr 501);
> val it = () : unit
- t;
> val it = '(2 + 3) + 4 - 6' : term
- dest_comb (Term'3 - 1 + 2');
> val it = ('$- 3', '1 + 2') : term * term
```

Comments

This function is of no use if multiple-token rules (such as those for conditional expressions) are desired, or if the token does not correspond to the name of the constant or variable that is to be produced.

As with other functions in the `Parse` structure, there is a companion `temp_set_fixity` function, which has the same effect on the global grammar, but which does not cause this effect to persist when the current theory is exported.

See also

`Parse.add_rule`, `Parse.add_infix`, `Parse.remove_rules_for_term`,
`Parse.remove_termtok`.

`set_flag_abs``(holCheckLib)`

```
set_flag_abs : bool -> model -> model
```

Synopsis

Sets a flag telling HolCheck whether to attempt abstraction.

Description

HolCheck uses a simple heuristic analysis of the model to determine whether it would be worthwhile to do abstraction. This flag can be used to override the default.

Comments

This information is optional when constructing HolCheck models. The default is true.

See also

`holCheckLib.holCheck`, `holCheckLib.empty_model`, `holCheckLib.get_flag_abs`.

`set_flag_ric``(holCheckLib)`

```
set_flag_ric : bool -> model -> model
```

Synopsis

Sets a HolCheck model to be synchronous if the first argument is true, asynchronous otherwise.

Description

ric stands for "relation is conjunctive". This information is used by HolCheck to decide if the transitions of the model occur simultaneously (conjunctive, synchronous) or interleaved (disjunctive, asynchronous).

Comments

This information must be set for a HolCheck model.

See also

`holCheckLib.holCheck`, `holCheckLib.empty_model`, `holCheckLib.get_flag_ric`.

<div data-bbox="161 349 395 405" data-label="Text"><code>set_goal</code></div>	<div data-bbox="842 347 1331 405" data-label="Text"><code>(proofManagerLib)</code></div>
--	--

```
set_goal : term list * term -> unit
```

Synopsis

Initializes the subgoal package with a new goal.

Description

The function `set_goal` initializes the subgoal management package. A proof state of the package consists of either a goal stack and a justification stack if a proof is in progress, or a theorem if a proof has just been completed. `set_goal` sets a new proof state consisting of an empty justification stack and a goal stack with the given goal as its sole goal. The goal is printed.

Failure

Fails unless all terms in the goal are of type `bool`.

Example

```
- set_goal([], Term '(HD[1;2;3] = 1) /\ (TL[1;2;3] = [2;3])');
> val it =
  Proof manager status: 1 proof.
  1. Incomplete:
      Initial goal:
      (HD [1; 2; 3] = 1) /\ (TL [1; 2; 3] = [2; 3])

  : proofs
```

Uses

Starting an interactive proof session with the subgoal package.

The subgoal package implements a simple framework for interactive goal-directed proof. When conducting a proof that involves many subgoals and tactics, the user must keep track of all the justifications and compose them in the correct order. While this is feasible even in large proofs, it is tedious. The subgoal package provides a way of building and traversing the tree of subgoals top-down, stacking the justifications and applying them properly.

The package maintains a proof state consisting of either a goal stack of outstanding goals and a justification stack, or a theorem. Tactics are used to expand the current goal (the one on the top of the goal stack) into subgoals and justifications. These are

pushed onto the goal stack and justification stack, respectively, to form a new proof state. Several preceding proof states are saved and can be returned to if a mistake is made in the proof. The goal stack is divided into levels, a new level being created each time a tactic is successfully applied to give new subgoals. The subgoals of the current level may be considered in any order.

If a tactic solves the current goal (returns an empty subgoal list), then its justification is used to prove a corresponding theorem. This theorem is then incorporated into the justification of the parent goal. If the subgoal was the last subgoal of the level, the level is removed and the parent goal is proved using its (new) justification. This process is repeated until a level with unproven subgoals is reached. The next goal on the goal stack then becomes the current goal. If all the subgoals are proved, the resulting proof state consists of the theorem proved by the justifications. This theorem may be accessed and saved.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`, `proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`, `proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`, `proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

<code>set_implicit_rewrites</code>	<code>(Rewrite)</code>
------------------------------------	------------------------

```
set_implicit_rewrites: rewrites -> unit
```

Synopsis

Allows the user to control the built-in database of simplifications used in rewriting.

Failure

Never fails.

See also

`Rewrite.empty_rewrites`, `Rewrite.add_rewrites`.

<code>SET_INDUCT_TAC</code>	<code>(pred_setLib)</code>
-----------------------------	----------------------------

```
SET_INDUCT_TAC : tactic
```

Synopsis

Tactic for induction on finite sets.

Description

SET_INDUCT_TAC is an induction tactic for proving properties of finite sets. When applied to a goal of the form

$$\text{!s. FINITE s ==> P[s]}$$

SET_INDUCT_TAC reduces this goal to proving that the property $\lambda s.P[s]$ holds of the empty set and is preserved by insertion of an element into an arbitrary finite set. Since every finite set can be built up from the empty set $\{\}$ by repeated insertion of values, these subgoals imply that the property $\lambda s.P[s]$ holds of all finite sets.

The tactic specification of SET_INDUCT_TAC is:

$$\frac{A \text{ ?- !s. FINITE s ==> P}}{\text{===== SET_INDUCT_TAC}} \\ A \text{ |- P[\{\}\}/s] \\ A \text{ u \{FINITE s', P[s'/s], ~e IN s'\} ?- P[e INSERT s'/s]}$$

where e is a variable chosen so as not to appear free in the assumptions A , and s' is a primed variant of s that does not appear free in A (usually, s' is just s).

Failure

SET_INDUCT_TAC (A,g) fails unless g has the form $\text{!s. FINITE s ==> P}$, where the variable s has type $\text{ty} \rightarrow \text{bool}$ for some type ty .

set_init

(holCheckLib)

set_init : term -> model -> model

Synopsis

Sets the initial set of states of a HolCheck model.

Description

The supplied term should be a term of propositional logic over the state variables, with no primed variables.

Failure

Fails if the supplied term is not a quantified boolean formula (QBF).

Example

For a mod-8 counter, we need three boolean variables to encode the state. If the counter starts at 0, the set of initial states of the model would be set as follows (assuming `holCheckLib` has been loaded):

```
- val m = holCheckLib.set_init ‘‘~v0 /\ ~v1 /\ ~v2‘‘ holCheckLib.empty_model;
> val m = <model> : model
```

where `empty_model` can be replaced by whatever model the user is building.

Comments

This information must be set for a `HolCheck` model.

See also

`holCheckLib.holCheck`, `holCheckLib.empty_model`, `holCheckLib.get_init`.

<code>set_known_constants</code>

(Parse)

```
Parse.set_known_constants : string list -> unit
```

Synopsis

Specifies the list of names that should be parsed as constants.

Description

One of the final phases of parsing is the resolution of free names in putative terms as either variables, constants or overloaded constants. If such a free name is not overloaded, then the list of known constants is consulted to determine whether or not to treat it as a constant. If the name is not present in the list, then it will be treated as a free variable.

Failure

Never fails. If a name is specified in the list of constants that is not in fact a constant, a warning message is printed, and that name is ignored.

Example

```
- known_constants();
> val it =
  ["bool_case", "ARB", "TYPE_DEFINITION", "ONTO", "ONE_ONE", "COND",
   "LET", "?!", "~", "F", "\\\/", "\\/", "!", "T", "?", "@",
   "==>", "="]
```



```

      : string list
- Term'p /\ q';
> val it = 'p /\ q' : term
- set_known_constants (Lib.subtract (known_constants()) ["/\"]);
> val it = () : unit
- Term'p /\ q';
<<HOL message: inventing new type variable names: 'a, 'b, 'c.>>
> val it = 'p /\ q' : term
- strip_comb it;
> val it = ('$/\', ['p', 'q']) : term * term list
- dest_var (#1 it);
> val it = ("/\\"", ': 'a -> 'b -> 'c') : string * hol_type

```

Uses

When writing library code that calls the parser, it can be useful to know exactly what constants the parser will "recognise".

Comments

This function does not affect the contents of a theory. A constant made invisible using this call is still really present in the theory; it is just harder to find.

See also

Parse.hidden, Parse.hide, Parse.known_constants, Parse.reveal.

<div style="display: flex; justify-content: space-between;"> set_list_thm_database (listLib) </div>

```
set_list_thm_database: {{Aux_thms: thm list, Fold_thms: thm list}} -> unit
```

Synopsis

Modifies the database of theorems known by LIST_CONV and X_LIST_CONV.

Description

The conversions LIST_CONV and X_LIST_CONV use a database of theorems relating to system list constants. These theorems fall into two categories: definitions of list operators in terms of FOLDR and FOLDL; and auxiliary theorems about the base elements and step functions in those definitions. The database can be modified using set_list_thm_database.

A call `set_list_thm_database{{Fold_thms=fold_thms,Aux_thms=aux_thms}}` replaces the existing database with the theorems given as the arguments. The `Fold_thms` field of the record contains the new fold definitions. The `Aux_thms` field contains the new auxiliary theorems. Theorems which do not have an appropriate form will be ignored.

The following is an example of a fold definition in the database:

```
|- !l. SUM l = FOLDR $+ 0 l
```

Here `$+` is the step function and `0` is the base element of the definition. Definitions are initially held for the following system operators: `APPEND`, `FLAT`, `LENGTH`, `NULL`, `REVERSE`, `MAP`, `FILTER`, `ALL_EL`, `SUM`, `SOME_EL`, `IS_EL`, `AND_EL`, `OR_EL`, `PREFIX`, `SUFFIX`, `SNOC` and `FLAT` combined with `REVERSE`.

The following is an example of an auxiliary theorem:

```
|- MONOID $+ 0
```

Auxiliary theorems stored include monoid, commutativity, associativity, binary function commutativity, left identity and right identity theorems.

Uses

The conversion `LIST_CONV` uses the theorems in the database to prove theorems about list operators. Users are encouraged to define list operators in terms of either `FOLDR` or `FOLDL` rather than recursively. Then if the definition is passed to `LIST_CONV`, it will be able to prove the recursive clauses for the definition. If auxiliary properties are proved about the step function and base element, and they are passed to `LIST_CONV` then it may be able to prove other useful theorems. Theorems can be passed either as arguments to `LIST_CONV` or they can be added to the database using `set_list_thm_database`.

Example

After the following call, `LIST_CONV` will only be able to prove a few theorems about `SUM`.

```
set_list_thm_database
  {{Fold_thms = [theorem "list" "SUM_FOLDR"],
    Aux_thms = [theorem "arithmetic" "MONOID_ADD_0"]}};
```

The following shows a new definition being added which multiplies the elements of a list. `LIST_CONV` is then called to prove the recursive clause.

```
- val MULTL = new_definition("MULTL",(--'MULTL l = FOLDR $* 1 l'--));
val MULTL = |- !l. MULTL l = FOLDR $* 1 l : thm
- let val {{Fold_thms = fold_thms, Aux_thms = aux_thms}} = list_thm_database()
= in
=   set_list_thm_database{{Fold_thms = MULTL::fold_thms,Aux_thms = aux_thms}}
```

```

= end;
val it = () : unit
- LIST_CONV (--'MULTL (CONS x 1)'--);
|- MULTL (CONS x 1) = x * MULTL 1

```

Failure

Never fails.

See also

listLib.LIST_CONV, listLib.list_thm_database, listLib.X_LIST_CONV.

<div data-bbox="161 855 654 911" data-label="Text"> <h1 style="margin: 0;">set_mapped_fixity</h1> </div>	<div data-bbox="1125 855 1329 904" data-label="Text"> <h1 style="margin: 0;">(Parse)</h1> </div>
--	--

```

Parse.set_mapped_fixity :
  {tok : string, term_name : string, fixity : fixity} -> unit

```

Synopsis

Allows the fixity of tokens to be updated.

Description

The `set_mapped_fixity` function is used to change the fixity of a single token, simultaneously mapping forms using that token name to a different name. Apart from the additional `term_name` field, the behaviour is similar to that of `set_fixity`.

Failure

This function fails if the new fixity causes a clash with existing rules, as happens if the precedence level of the specified fixity is already taken by rules using a fixity of a different type. Even if the application of `set_mapped_fixity` succeeds, it may cause the next subsequent application of the Term parsing function to complain about precedence conflicts in the operator precedence matrix. These problems may cause the parser to behave oddly on terms involving the token whose fixity was set. Excessive parentheses will usually cure even these problems.

Comments

This function is of no use if multiple-token rules (such as those for conditional expressions) are desired.

As with other functions in the `Parse` structure, there is a companion `temp_set_mapped_fixity` function, which has the same effect on the global grammar, but which does not cause this effect to persist when the current theory is exported.

See also

`Parse.add_rule`, `Parse.set_fixity`.

<code>set_MLname</code>	(Theory)
-------------------------	----------

```
set_MLname : string -> string -> unit
```

Synopsis

Change the name attached to an element of the current theory.

Description

It can happen that an axiom, definition, or theorem gets stored in the current theory segment under a name that wouldn't be a suitable ML identifier. For example, some advanced definition mechanisms in HOL automatically construct names to bind the results of making a definition. In some cases, particularly when symbolic identifiers are involved, a binding name can be generated that is not a valid ML identifier.

In such cases, we don't want to fail and lose the work done by the definition mechanism. Instead, when `export_theory` is invoked, all names binding axioms, definitions, and theorems are examined to see if they are valid ML identifiers. If not, an informative error message is generated, and it is up to the user to change the names in the offending bindings. The function `set_MLname s1 s2` will replace a binding with name `s1` by one with name `s2`.

Failure

Never fails, although will give a warning if `s1` is not the name of a binding in the current theory segment.

Example

We inductively define a predicate telling if a number is odd in the following. The name is admittedly obscure, however it illustrates our point.

```
- Hol_reln '(%% 1) /\ (!n. %% n ==> %% (n+2))';
> val it =
  (|- %% 1 /\ !n. %% n ==> %% (n + 2),
   |- !%%'. %%' 1 /\ (!n. %%' n ==> %%' (n + 2)) ==> !a0. %% a0 ==> %%' a0,
```

```

|- !a0. %% a0 = (a0 = 1) \ / ?n. (a0 = n + 2) /\ %% n) : thm * thm * thm

- export_theory();
<<HOL message: The following ML binding names in the theory to be exported:
"%%_rules", "%%_ind", "%%_cases"
are not acceptable ML identifiers.
Use 'set_MLname <bad> <good>' to change each name.>>
! Uncaught exception:
! HOL_ERR

- (set_MLname "%%_rules" "odd_rules"; (* OK, do what it says *)
  set_MLname "%%_ind" "odd_ind";
  set_MLname "%%_cases" "odd_cases");
> val it = () : unit

- export_theory();
Exporting theory "scratch" ... done.
> val it = () : unit

```

Comments

The definition principles that currently have the potential to make problematic bindings are `Hol_datatype` and `Hol_reln`.

It is slightly awkward to have to repair the names in a post-hoc fashion. It is probably simpler to proceed by using alphanumeric names when defining constants, and to use overloading to get the desired name.

See also

`bossLib.Hol_reln`, `bossLib.Hol_datatype`, `Theory.export_theory`,
`Theory.current_definitions`, `Theory.current_theorems`, `Theory.current_axioms`,
`DB.thy`, `DB.dest_theory`.

<div data-bbox="161 1693 399 1740" data-label="Text"> <p><code>set_name</code></p> </div>	<div data-bbox="956 1686 1331 1740" data-label="Text"> <p><code>(holCheckLib)</code></p> </div>
---	---

`set_name` : string -> model -> model

Synopsis

Sets the name given to the formal model `HolCheck` constructs internally.

Failure

Fails if the first argument does not follow the naming rules for constants.

Comments

This information is optional when constructing HolCheck models. It should be set if more than one model is being used in the same session, to avoid name clashes.

See also

`holCheckLib.holCheck`, `holCheckLib.empty_model`, `holCheckLib.get_name`.

<div data-bbox="236 745 501 799" data-label="Text"> <p><code>set_props</code></p> </div>	<div data-bbox="1032 741 1410 792" data-label="Text"> <p><code>(holCheckLib)</code></p> </div>
--	--

```
set_props : (string * term) list -> model -> model
```

Synopsis

Sets the properties to be checked for the supplied HolCheck model.

Description

The first argument is a list of (property_name, property) pair, where the name is a string and the property is a well-formed CTL or mu-calculus property. The list must not be empty. Names must be unique.

In the properties, care must be taken to model atomic propositions as functions on the state. At the moment, only boolean variables are allowed as atomic propositions.

Failure

Fails if the property list is empty, or the names violate HOL constant naming rules, or names are unique. Also fails if any atomic proposition is not a paired abstraction of the form `\state. boolvar`.

Example

Specifying a CTL property for a mod-8 counter assuming `holCheckLib` has been loaded (there exists a future in which the most significant bit will go high) :

```
- val m = holCheckLib.set_props [("ef_msb_high", 'C_EF (C_BOOL (B_PROP (\(v0,v1,v2
> val m = <model> : model
```

Comments

This information must be set for a HolCheck model. For more details on how to specify properties, see the examples in the `src/HolCheck/examples` directory; the `mod8` and `amba_apb` examples are good starting points.

See also

holCheckLib.holCheck, holCheckLib.empty_model, holCheckLib.get_props,
holCheckLib.get_results, holCheckLib.set_state, holCheckLib.prove_model.

SET_SPEC_CONV	(pred_setLib)
----------------------	---------------

SET_SPEC_CONV : conv

Synopsis

Axiom-scheme of specification for set abstractions.

Description

The conversion SET_SPEC_CONV expects its term argument to be an assertion of the form $t \text{ IN } \{E \mid P\}$. Given such a term, the conversion returns a theorem that defines the condition under which this membership assertion holds. When E is just a variable v , the conversion returns:

$$\vdash t \text{ IN } \{v \mid P\} = P[t/v]$$

and when E is not a variable but some other expression, the theorem returned is:

$$\vdash t \text{ IN } \{E \mid P\} = \exists x_1 \dots x_n. (t = E) \wedge P$$

where x_1, \dots, x_n are the variables that occur free both in the expression E and in the proposition P .

Example

- SET_SPEC_CONV ‘‘12 IN {n | n > N}‘‘;

|- 12 IN {n | n > N} = 12 > N

- SET_SPEC_CONV ‘‘p IN {(n,m) | n < m}‘‘;

|- p IN {(n,m) | n < m} = (?n m. (p = n,m) /\ n < m)

Failure

Fails if applied to a term that is not of the form $t \text{ IN } \{E \mid P\}$.

set_state	(holCheckLib)
------------------	---------------

set_state : term -> model -> model

Synopsis

Sets the state tuple used internally by the formal model constructed by HolCheck.

Comments

This information is optional when constructing HolCheck models. By default, HolCheck will construct the state tuple itself. In practice however, a user nearly always needs to supply the state tuple, since it is almost always required when specifying properties.

See also

`holCheckLib.holCheck`, `holCheckLib.mk_state`, `holCheckLib.get_state`.

`set_trace`

(Feedback)

```
set_trace : string -> int -> unit
```

Synopsis

Set a tracing level for a registered trace.

Description

Invoking `set_trace n i` sets the level of the tracing mechanism registered under `n` to be `i`. These settings control the verbosity of various tools within the system. This can be useful both when debugging proofs (with the simplifier for example), and also as a guide to how an automatic proof is proceeding (with `mesonLib` for example).

There is no single interpretation of what activity a tracing level should evoke: each tool registered for tracing can treat its trace level in its own way.

Failure

A call to `set_trace n i` fails if `n` has not previously been registered via `register_trace`. It also fails if `i` is less than zero, or if it is greater than the trace's specified maximum value.

Example

```

- set_trace "Rewrite" 1;

- PURE_REWRITE_CONV [AND_CLAUSES] (Term 'x /\ T /\ y');

<<HOL message: Rewrite:
|- T /\ y = y.>>

> val it = |- x /\ T /\ y = x /\ y : thm

```


See also

Feedback, Feedback.register_trace, Feedback.reset_trace, Feedback.reset_traces, Feedback.trace, Feedback.traces.

<div data-bbox="161 535 426 584" data-label="Text">set_trans</div>	<div data-bbox="956 530 1331 582" data-label="Text">(holCheckLib)</div>
---	--

```
set_trans : (string * Term.term) list -> model -> model
```

Synopsis

Sets the transition system for a HolCheck model.

Description

The transition system is supplied as list of (transition label, transition relation) pairs. Each label must be a unique string. Each relation must be a propositional term, in which primed variables represent values in the next state. The transition label "." is internally used as a wildcard that is expected to match all transitions, and is thus not allowed as a transition label, unless there is only one transition.

Failure

Fails if the transition labels are not unique, or the transition list is empty, or the wildcard label is used with a non-singleton transition list, or any of the relation terms is not a quantified boolean formula (QBF).

Example

For a mod-8 counter, we need three boolean variables to encode the state. The single transition relation can then be set as follows (assuming holCheckLib has been loaded):

```
- val m = holCheckLib.set_trans [("v0", "'v0' = ~v0'"), ("v1", "'v1' = (v0 \\/ v1) /\ ~(v0 /\ v1)"),
                                ("v2", "'v2' = (v0 /\ v1 \\/ v2) /\ ~(v0 /\ v1 = v2)')] holCheckLib
> val m = <model> : model
```

where empty_model can be replaced by whatever model the user is building.

Comments

This information must be set for a HolCheck model.

See also

holCheckLib.holCheck, holCheckLib.empty_model, holCheckLib.get_trans, holCheckLib.set_flag_ric.

`set_vord``(holCheckLib)``set_vord : string list -> model -> model`**Synopsis**

Sets the BDD variable ordering used by HolCheck for the given model.

Description

The first argument specifies the ordering of variables. This ordering must contain all current- and next-state variables specified by `set_init` and `set_trans`. In particular, if either `set_init` or `set_trans` use a variable v , then v' must be mentioned in the ordering. Likewise for unprimed versions of primed variables.

Comments

This information is optional when constructing HolCheck models. By default, HolCheck constructs its own heuristic-based variable ordering. The heuristic used is a rather primitive one, at the moment. It just interleaves next- and current-state variables.

See also

`holCheckLib.holCheck`, `holCheckLib.empty_model`, `holCheckLib.get_vord`.

`show_numeral_types``(Parse)``Globals.show_numeral_types : bool ref`**Synopsis**

A flag which causes numerals to be printed with suffix annotation when true.

Description

This flag controls the pretty-printing of numeral forms that have been added to the global grammar with the function `add_numeral_form`. If the flag is true, then all numeric values are printed with the single-letter suffixes that identify which type the value is.

Failure

Never fails, as it is just an SML value.

Example

```

- load "integerTheory";
> val it = () : unit

- Term'~3';
> val it = '~3' : term

- show_numeral_types := true;
> val it = () : unit

- Term'~3';
> val it = '~3i' : term

```

Uses

Can help to disambiguate terms involving numerals.

See also

Parse.add_numeral_form, Globals.show_types.

<div data-bbox="161 1135 426 1191" data-label="Text"> <p>show_tags</p> </div>	<div data-bbox="1069 1131 1331 1187" data-label="Text"> <p>(Globals)</p> </div>
---	---

show_tags : bool ref

Synopsis

Flag for controlling display of tags in theorem prettyprinter.

Description

The flag `show_tags` controls the display of values of type `thm`. When set to `true`, the tag attached to a theorem will be printed when the theorem is printed. When set to `false`, no indication of the presence or absence of a tag will be displayed.

Example

```

- show_tags := false;
> val it = () : unit

- pairTheory.PAIR_MAP_THM;
> val it = |- !f g x y. (f ## g) (x,y) = (f x,g y) : thm

```

```

- mk_thm ([],F);
> val it = |- F : thm

- show_tags := true;
> val it = () : unit

- pairTheory.PAIR_MAP_THM;
> val it = [oracles: ] [axioms: ] [] |- !f g x y. (f ## g) (x,y) = (f x,g y)
      : thm

- mk_thm ([],F);
> val it = [oracles: MK_THM] [axioms: ] [] |- F : thm

```

Comments

The initial value of `show_tags` is `false`.

See also

`Thm.tag`, `Thm.mk_oracle_thm`, `Thm.mk_thm`.

<code>show_types</code>	(Globals)
-------------------------	-----------

`Globals.show_types` : `bool ref`

Synopsis

Flag controlling printing of HOL types (in terms).

Description

Normally HOL types in terms are not printed, since this makes terms hard to read. Type printing is enabled by `show_types := true`, and disabled by `show_types := false`. When printing of types is enabled, not all variables and constants are annotated with a type. The intention is to provide sufficient type information to remove any ambiguities without swamping the term with type information.

Failure

Never fails.

Example

```

- BOOL_CASES_AX;;
> val it = |- !t. (t = T) \ / (t = F) : thm

- show_types := true;
> val it = () : unit

- BOOL_CASES_AX;;
> val it = |- !(t : bool). (t = T) \ / (t = F) : thm

```

Comments

It is possible to construct an abstraction in which the bound variable has the same name but a different type to a variable in the body. In such a case the two variables are considered to be distinct. Without type information such a term can be very misleading, so it might be a good idea to provide type information for the free variable whether or not printing of types is enabled.

See also

`Parse.print_term`.

SIMP_CONV	(bossLib)
-----------	-----------

`SIMP_CONV : simpset -> thm list -> conv`

Synopsis

Applies a `simpset` and a list of rewrite rules to simplify a term.

Description

`SIMP_CONV` is the fundamental engine of the HOL simplification library. It repeatedly applies the transformations included in the provided `simpset` (which is augmented with the given rewrite rules) to a term, ultimately yielding a theorem equating the original term to another.

Values of the `simpset` type embody a suite of different transformations that might be applicable to given terms. These “transformational components” are rewrites, conversions, AC-rules, congruences, decision procedures and a filter, which is used to modify the way in which rewrite rules are added to the `simpset`. The exact types for these components, known as `simpset` fragments, and the way they can be combined to create `simpsets` is given in the reference entry for `SSFRAG`.

Rewrite rules are used similarly to the way in they are used in the rewriting system (`REWRITE_TAC` et al.). These are equational theorems oriented to rewrite from left-hand-side to right-hand-side. Further, `SIMP_CONV` handles obvious problems. If a rewrite rule is of the general form $[...] \vdash x = f\ x$, then it will be discarded, and a message is printed to this effect. On the other hand, if the right-hand-side is a permutation of the pattern on the left, as in $\vdash x + y = y + x$ and $\vdash x \text{ INSERT } (y \text{ INSERT } s) = y \text{ INSERT } (x \text{ INSERT } s)$, then such rules will only be applied if the term to which they are being applied is strictly reduced according to some term ordering.

Rewriting is done using a form of higher-order matching, and also uses conditional rewriting. This latter means that theorems of the form $\vdash P \implies (x = y)$ can be used as rewrites. If a term matching x is found, the simplifier will attempt to satisfy the side-condition P . If it is able to do so, then the rewriting will be performed. In the process of attempting to rewrite P to true, further side conditions may be generated. The simplifier limits the size of the stack of side conditions to be solved (the reference variable `Cond_rewr.stack_limit` holds this limit), so this will not introduce an infinite loop.

Rewrite rules can always be added “on the fly” as all of the simplification functions take a `thm list` argument where these rules can be specified. If a set of rewrite rules is frequently used, then these should probably be made into a `ssfrag` value with the `rewrites` function and then added to an existing simpset with `++`.

The conversions which are part of simpsets are useful for situations where simple rewriting is not enough to transform certain terms. For example, the `BETA_CONV` conversion is not expressible as a standard first order rewrite, but is part of the `bool_ss` simpset and the application of this simpset will thus simplify all occurrences of $(\lambda x. e1)\ e2$.

In fact, conversions in simpsets are not typically applied indiscriminately to all sub-terms. (If a conversion is applied to an inappropriate sub-term and fails, this failure is caught by the simplifier and ignored.) Instead, conversions in simpsets are accompanied by a term-pattern which specifies the sort of situations in which they should be applied. This facility is used in the definition of `bool_ss` to include `ETA_CONV`, but stop it from transforming $\lambda x. P\ x$ into $\$! P$.

AC-rules allow simpsets to be constructed that automatically normalise terms involving associative and commutative operators, again according to some arbitrary term ordering metric.

Congruence rules allow `SIMP_CONV` to assume additional context as a term is rewritten. In a term such as $P \implies Q \wedge f\ x$ the truth of term P may be assumed as an additional piece of context in the rewriting of $Q \wedge f\ x$. The congruence theorem that states this is valid is (`IMP_CONG`):

$$\vdash (P = P') \implies (P' \implies (Q = Q')) \implies ((P \implies Q) = (P' \implies Q'))$$

Other congruence theorems can be part of simpsets. The system provides `IMP_CONG` above and `COND_CONG` as part of the `CONG_ss ssfrag` value. (These `simpset` fragments can be incorporated into simpsets with the `++` function.) Other congruence theorems are already proved for operators such as conjunction and disjunction, but use of these in standard simpsets is not recommended as the computation of all the additional contexts for a simple chain of conjuncts or disjuncts can be very computationally intensive.

Decision procedures in simpsets are similar to conversions. They are arbitrary pieces of code that are applied to sub-terms at low priority. They are given access to the wider context through a list of relevant theorems. The `arith_ss` simpset includes an arithmetic decision procedure implemented in this way.

Failure

`SIMP_CONV` never fails, but may diverge.

Example

```
- SIMP_CONV arith_ss [] “(\x. x + 3) 4“;
> val it = |- (\x. x + 3) 4 = 7 : thm
```

Uses

`SIMP_CONV` is a powerful way of manipulating terms. Other functions in the simplification library provide the same facilities when in the contexts of goals and tactics (`SIMP_TAC`, `ASM_SIMP_TAC` etc.), and theorems (`SIMP_RULE`), but `SIMP_CONV` provides the underlying functionality, and is useful in its own right, just as conversions are generally.

See also

`bossLib.++`, `bossLib.ASM_SIMP_TAC`, `bossLib.FULL_SIMP_TAC`, `simpLib.mk_simpset`, `bossLib.rewrites`, `bossLib.SIMP_RULE`, `bossLib.SIMP_TAC`, `simpLib.SSFRAG`, `bossLib.EVAL`.

<div data-bbox="161 1579 426 1630" data-label="Text"> <h1 style="margin: 0;">SIMP_CONV</h1> </div>	<div data-bbox="1067 1579 1331 1635" data-label="Text"> (simpLib) </div>
--	---

```
SIMP_CONV : simpset -> thm list -> conv
```

Synopsis

Simplify a term with the given simpset and theorems.

Description

`bossLib.SIMP_CONV` is identical to `simpLib.SIMP_CONV`.

See also

bossLib.SIMP_CONV.

<div data-bbox="234 490 533 539" data-label="Text"> <p>SIMP_PROVE</p> </div>	<div data-bbox="1144 488 1414 544" data-label="Text"> <p>(simpLib)</p> </div>
--	---

simpLib.SIMP_PROVE : simpset -> thm list -> term -> thm

Synopsis

Like SIMP_CONV, but converts boolean terms to theorem with same conclusion.

Description

SIMP_PROVE ss thm1 is equivalent to EQT_ELIM o SIMP_CONV ss thm1.

Failure

Fails if the term can not be shown to be equivalent to true. May diverge.

Example

Applying the tactic

```
ASSUME_TAC (SIMP_PROVE arith_ss [] ‘‘x < y ==> x < y + 6‘‘)
```

to the goal $?- x + y = 10$ yields the new goal

```
x < y ==> x < y + 6 ?- x + y = 10
```

Using SIMP_PROVE here allows ASSUME_TAC to add a new fact, where the equality with truth that SIMP_CONV would produce would be less useful.

Uses

SIMP_PROVE is useful when constructing theorems to be passed to other tools, where those other tools would prefer not to have theorems of the form $\vdash P = T$.

See also

simpLib.SIMP_CONV, simpLib.SIMP_RULE, simpLib.SIMP_TAC.

<div data-bbox="234 1816 504 1870" data-label="Text"> <p>SIMP_RULE</p> </div>	<div data-bbox="1144 1816 1414 1870" data-label="Text"> <p>(bossLib)</p> </div>
---	---

SIMP_RULE : simpset -> thm list -> thm -> thm

Synopsis

Simplifies the conclusion of a theorem according to the given simpset and theorem rewrites.

Description

SIMP_RULE simplifies the conclusion of a theorem, adding the given theorems to the simpset parameter as rewrites. The way in which terms are transformed as a part of simplification is described in the entry for SIMP_CONV.

Failure

Never fails, but may diverge.

Example

The following also demonstrates the higher order rewriting possible with simplification (FORALL_AND_THM states $\vdash (\!x. P\ x \wedge Q\ x) = (\!x. P\ x) \wedge (\!x. Q\ x)$):

```
- SIMP_RULE bool_ss [boolTheory.FORALL_AND_THM
    (ASSUME (Term'!x. P (x + 1) /\ R x /\ x < y'))];
> val it = [...] |- (!x. P (x + 1)) /\ (!x. R x) /\ (!x. x < y) : thm
```

Comments

SIMP_RULE ss thmlist is equivalent to CONV_RULE (SIMP_CONV ss thmlist).

See also

simpLib.ASM_SIMP_RULE, bossLib.SIMP_CONV, bossLib.SIMP_TAC, bossLib.bool_ss.

SIMP_RULE	(simpLib)
-----------	-----------

```
SIMP_RULE : simpset -> thm list -> thm -> thm
```

Synopsis

Simplify a term with the given simpset and theorems.

Description

bossLib.SIMP_RULE is identical to simpLib.SIMP_RULE.

See also

bossLib.SIMP_RULE.

SIMP_TAC	(bossLib)
----------	-----------

```
SIMP_TAC : simpset -> thm list -> tactic
```

Synopsis

Simplifies the goal, using the given simpset and the additional theorems listed.

Description

SIMP_TAC adds the theorems of the second argument to the simpset argument as rewrites and then applies the resulting simpset to the conclusion of the goal. The exact behaviour of a simpset when applied to a term is described further in the entry for SIMP_CONV.

With simple simpsets, SIMP_TAC is similar in effect to REWRITE_TAC; it transforms the conclusion of a goal by using the (equational) theorems given and those already in the simpset as rewrite rules over the structure of the conclusion of the goal.

Just as ASM_REWRITE_TAC includes the assumptions of a goal in the rewrite rules that REWRITE_TAC uses, ASM_SIMP_TAC adds the assumptions of a goal to the rewrites and then performs simplification.

Failure

SIMP_TAC never fails, though it may diverge.

Example

SIMP_TAC and the `arith_ss` simpset combine to prove quite difficult seeming goals:

```
- val (_, p) = SIMP_TAC arith_ss []
    ([], Term 'P x /\ (x = y + 3) ==> P x /\ y < x');

> val p = fn : thm list -> thm

- p [];
> val it = |- P x /\ (x = y + 3) ==> P x /\ y < x : thm
```

SIMP_TAC is similar to REWRITE_TAC if used with just the `bool_ss` simpset. Here it is used in conjunction with the arithmetic theorem `GREATER_DEF`, `|- !m n. m > n = n < m`, to advance a goal:

```
- SIMP_TAC bool_ss [GREATER_DEF] ([], Term 'T /\ 5 > 4 \\/ F');
> val it = ([[[]], '4 < 5']), fn : subgoals
```

Comments

The simplification library is described further in other documentation, but its full capabilities are still rather opaque.

Uses

Simplification is one of the most powerful tactics available to the HOL user. It can be used both to solve goals entirely or to make progress with them. However, poor simpsets or a poor choice of rewrites can still result in divergence, or poor performance.

See also

`bossLib.++`, `bossLib.ASM_SIMP_TAC`, `bossLib.std_ss`, `bossLib.bool_ss`,
`bossLib.arith_ss`, `bossLib.list_ss`, `bossLib.FULL_SIMP_TAC`, `simpLib.mk_simpset`,
`Rewrite.REWRITE_TAC`, `bossLib.SIMP_CONV`, `simpLib.SIMP_PROVE`, `bossLib.SIMP_RULE`.

SIMP_TAC	(simpLib)
----------	-----------

```
SIMP_TAC : simpset -> thm list -> tactic
```

Synopsis

Simplify a term with the given simpset and theorems.

Description

`bossLib.SIMP_TAC` is identical to `simpLib.SIMP_TAC`.

See also

`bossLib.SIMP_TAC`.

single	(Lib)
--------	-------

```
single : 'a -> 'a list
```

Synopsis

Turns a value into a single-element list.

Description

`single x` returns `[x]`.

Failure

Never fails.

See also

`Lib.singleton_of_list`.

<code>singleton_of_list</code>	<code>(Lib)</code>
--------------------------------	--------------------

```
singleton_of_list : 'a list -> 'a
```

Synopsis

Turns a single-element list into a singleton.

Description

`singleton_of_list [x]` returns `x`.

Failure

Fails if applied to a list that is not of length 1.

See also

`Lib.single`, `Lib.pair_of_list`, `Lib.triple_of_list`, `Lib.quadruple_of_list`.

<code>SIZES_CONV</code>	<code>(wordsLib)</code>
-------------------------	-------------------------

```
SIZES_CONV : conv
```

Synopsis

Evaluates `dimindex`, `dimword` and `INT_MIN`.

Example

```
- SIZES_CONV ``dimword(:32)``
> val it = |- dimword (:32) = 4294967296 : thm
```

Comments

Evaluations are stored and so will be slightly faster when repeated.

See also

wordsLib.SIZES_{ss}.

SIZES _{ss}	(wordsLib)
---------------------	------------

SIZES_{ss} : ssfrag

Synopsis

Simplification fragment for words.

Description

The fragment SIZES_{ss} evaluates terms ‘‘dimindex(:’a)’’, ‘‘dimword(:’a)’’, ‘‘INT_MIN(:’a)’’, and ‘‘FINITE (UNIV : ’a set)’’ for numeric types.

Example

```
- SIMP_CONV (pure_ss++SIZESss) [] ‘‘dimindex(:32) + INT_MIN(:32) + dimword(:32)’’
> val it =
  |- dimindex (:32) + INT_MIN (:32) + dimword (:32) =
     32 + 2147483648 + 4294967296 : thm
```

See also

wordsLib.SIZES_CONV, wordsLib.WORD_CONV, fcpLib.FCP_{ss}, wordsLib.BIT_{ss}, wordsLib.WORD_ARITH_{ss}, wordsLib.WORD_LOGIC_{ss}, wordsLib.WORD_SHIFT_{ss}, wordsLib.WORD_ARITH_EQ_{ss}, wordsLib.WORD_BIT_EQ_{ss}, wordsLib.WORD_EXTRACT_{ss}, wordsLib.WORD_MUL_LSL_{ss}, wordsLib.WORD_{ss}.

SKOLEM_CONV	(Conv)
-------------	--------

SKOLEM_CONV : conv

Synopsis

Proves the existence of a Skolem function.

Description

When applied to an argument of the form $!x_1 \dots x_n. ?y. P$, the conversion SKOLEM_CONV returns the theorem:

$$\vdash (\lambda x_1 \dots x_n. \lambda y. P) = (\lambda y'. \lambda x_1 \dots x_n. P[y' x_1 \dots x_n/y])$$

where y' is a primed variant of y not free in the input term.

Failure

SKOLEM_CONV tm fails if tm is not a term of the form $\lambda x_1 \dots x_n. \lambda y. P$.

See also

Conv.X.SKOLEM_CONV.

<div data-bbox="236 723 333 770" data-label="Text"> <p>snd</p> </div>	<div data-bbox="1260 719 1414 772" data-label="Text"> <p>(Lib)</p> </div>
---	---

snd : ('a * 'b) -> 'b

Synopsis

Extracts the second component of a pair.

Description

snd (x,y) returns y.

Failure

Never fails. However, notice that snd (x,y,z) fails to typecheck, since (x,y,z) is not a pair.

Example

```

- snd (1, "foo");
> val it = "foo" : string

- snd (1, "foo", []);
! Toplevel input:
! snd (1, "foo", []);
! ~~~~~
! Type clash: expression of type
!   'g * 'h * 'i
! cannot have type
!   'j * 'k
! because the tuple has the wrong number of components

- snd (1, ("foo", ()));
> val it = ("foo", ()) : string * unit

```

See also

Lib, Lib.fst.

SNOC_CONV

(listLib)

SNOC_CONV : conv

Synopsis

Computes by inference the result of adding an element to the tail end of a list.

DescriptionSNOC_CONV takes a term tm in the following form:
$$\text{SNOC } x \ [x_0; \dots; x_n]$$

It returns the theorem

$$\vdash \text{SNOC } x \ [x_0; \dots; x_n] = [x_0; \dots; x_n; x]$$

where the right-hand side is the list in the canonical form, i.e., constructed with only the constructor CONS.

FailureSNOC_CONV tm fails if tm is not of the form described above.**Example**

Evaluating

$$\text{SNOC_CONV } (--' \text{SNOC } 5 \ [0;1;2;3;4] \ '--);$$

returns the following theorem:

$$\vdash \text{SNOC } 5 \ [0;1;2;3;4] = [0;1;2;3;4;5]$$
See also

listLib.FOLDL_CONV, listLib.FOLDR_CONV, listLib.list_FOLD_CONV.

SNOC_INDUCT_TAC

(listLib)

SNOC_INDUCT_TAC : tactic

Synopsis

Performs tactical proof by structural induction on lists.

Description

SNOC_INDUCT_TAC reduces a goal $!l.P[l]$, where l ranges over lists, to two subgoals corresponding to the base and step cases in a proof by structural induction on l from the tail end. The induction hypothesis appears among the assumptions of the subgoal for the step case. The specification of SNOC_INDUCT_TAC is:

$$\frac{A \text{ ?- } !l. P}{\text{===== SNOC_INDUCT_TAC}} \\ A \text{ |- } P[\text{NIL}/l] \quad A \text{ u } \{\{P[l'/l]\}\} \text{ ?- } !x. P[\text{SNOC } x \text{ } l'/l]$$

where l' is a primed variant of l that does not appear free in the assumptions A (usually, l' is just l). When SNOC_INDUCT_TAC is applied to a goal of the form $!l.P$, where l does not appear free in P , the subgoals are just $A \text{ ?- } P$ and $A \text{ u } \{\{P\}\} \text{ ?- } !h.P$.

Failure

SNOC_INDUCT_TAC g fails unless the conclusion of the goal g has the form $!l.t$, where the variable l has type $(ty)list$ for some type ty .

See also

`listLib.EQ_LENGTH_INDUCT_TAC`, `listLib.EQ_LENGTH_SNOC_INDUCT_TAC`,
`listLib.LIST_INDUCT_TAC`.

SOME_EL_CONV

(listLib)

SOME_EL_CONV : conv -> conv

Synopsis

Computes by inference the result of applying a predicate to the elements of a list.

Description

SOME_EL_CONV takes a conversion `conv` and a term `tm` of the following form:

SOME_EL P [x0;...xn]

It returns the theorem

$\text{|- SOME_EL } P \text{ [x0;...xn]} = F$

if for every x_i occurred in the list, `conv (--'P xi'--)` returns a theorem $\text{|- P } x_i = F$, otherwise, if for at least one x_i , evaluating `conv (--'P xi'--)` returns the theorem $\text{|- P } x_i = T$, then it returns the theorem

$$\text{|- SOME_EL P [x0;...xn] = T}$$

Failure

`SOME_EL_CONV conv tm` fails if `tm` is not of the form described above, or failure occurs when evaluating `conv (--'P xi'--)` for some x_i .

Example

Evaluating

```
SOME_EL_CONV bool_EQ_CONV (--'SOME_EL ($= T) [T;F;T]'--);
```

returns the following theorem:

$$\text{|- SOME_EL}(\$= T) [T;F;T] = T$$

In general, if the predicate P is an explicit lambda abstraction $(\lambda x. P x)$, the conversion should be in the form

$$(BETA_CONV \text{ THENC conv'}$$

See also

`listLib.ALL_EL_CONV`, `listLib.IS_EL_CONV`, `listLib.FOLDL_CONV`, `listLib.FOLDR_CONV`, `listLib.list_FOLD_CONV`.

<div data-bbox="162 1462 284 1507" data-label="Text"> <p>sort</p> </div>	<div data-bbox="1182 1456 1331 1507" data-label="Text"> <p>(Lib)</p> </div>
---	---

```
sort : ('a -> 'a -> bool) -> 'a list -> 'a list
```

Synopsis

Sorts a list using a given transitive 'ordering' relation.

Description

The call `sort opr list` where `opr` is a curried transitive relation on the elements of `list`, will sort the list, i.e., will permute `list` such that if $x \text{ opr } y$ but not $y \text{ opr } x$ then x will occur to the left of y in the sorted list. In particular if `opr` is a total order, the result list will be sorted in the usual sense of the word.

Failure

Never fails.

Example

A simple example is:

```
- sort (curry (op<)) [3, 1, 4, 1, 5, 9, 2, 6, 5, 3, 5, 8, 9, 7, 9];
> val it = [1, 1, 2, 3, 3, 4, 5, 5, 5, 6, 7, 8, 9, 9, 9] : int list
```

The following example is a little more complicated. Note that the ‘ordering’ is not antisymmetric.

```
- sort (curry (op< o (fst ## fst)))
      [(1,3), (7,11), (3,2), (3,4), (7,2), (5,1)];
> val it = [(1,3), (3,4), (3,2), (5,1), (7,2), (7,11)] : (int * int) list
```

Comments

The Standard ML Basis Library also provides implementations of sorting.

See also

`Lib.int_sort`, `Lib.topsort`.

SPEC	(Thm)
------	-------

SPEC : term -> thm -> thm

Synopsis

Specializes the conclusion of a theorem.

Description

When applied to a term u and a theorem $A \vdash !x. t$, then SPEC returns the theorem $A \vdash t[u/x]$. If necessary, variables will be renamed prior to the specialization to ensure that u is free for x in t , that is, no variables free in u become bound after substitution.

$$\frac{A \vdash !x. t}{A \vdash t[u/x]} \text{ SPEC } u$$

Failure

Fails if the theorem's conclusion is not universally quantified, or if x and u have different types.

Example

The following example shows how SPEC renames bound variables if necessary, prior to substitution: a straightforward substitution would result in the clearly invalid theorem

```
|- ~y ==> (!y. y ==> ~y).

- let val xv = Term 'x:bool'
      and yv = Term 'y:bool'
  in
    (GEN xv o DISCH xv o GEN yv o DISCH yv) (ASSUME xv)
  end;
> val it = |- !x. x ==> !y. y ==> x : thm

- SPEC (Term '~y') it;
> val it = |- ~y ==> !y'. y' ==> ~y : thm
```

See also

Drule.ISPEC, Drule.SPECL, Drule.SPEC_ALL, Drule.SPEC_VAR, Thm.GEN, Thm.GENL, Drule.GEN_ALL.

SPEC_ALL	(Drule)
----------	---------

SPEC_ALL : thm -> thm

Synopsis

Specializes the conclusion of a theorem with its own quantified variables.

Description

When applied to a theorem $A \vdash !x_1 \dots x_n. t$, the inference rule SPEC_ALL returns the theorem $A \vdash t[x_1'/x_1] \dots [x_n'/x_n]$ where the x_i' are distinct variants of the corresponding x_i , chosen to avoid clashes with any variables free in the assumption list and with the names of constants. Normally x_i' is just x_i , in which case SPEC_ALL simply removes all universal quantifiers.

$$\frac{A \vdash !x_1 \dots x_n. t}{A \vdash t[x_1'/x_1] \dots [x_n'/x_n]} \text{ SPEC_ALL}$$

Failure

Never fails.

Example

```
- SPEC_ALL CONJ_ASSOC;
> val it = |- t1 /\ t2 /\ t3 = (t1 /\ t2) /\ t3 : thm
```

See also

Thm.GEN, Thm.GENL, Drule.GEN_ALL, Tactic.GEN_TAC, Thm.SPEC, Drule.SPECL, Tactic.SPEC_TAC.

<div data-bbox="236 875 474 925" data-label="Text"> <p>SPEC_TAC</p> </div>	<div data-bbox="1173 875 1412 925" data-label="Text"> <p>(Tactic)</p> </div>
--	--

SPEC_TAC : term * term -> tactic

Synopsis

Generalizes a goal.

Description

When applied to a pair of terms (u, x) , where x is just a variable, and a goal $A \text{ ?- } t$, the tactic SPEC_TAC generalizes the goal to $A \text{ ?- } !x. t[x/u]$, that is, all instances of u are turned into x .

$$\begin{array}{l} A \text{ ?- } t \\ \hline \text{SPEC_TAC } (u, x) \\ A \text{ ?- } !x. t[x/u] \end{array}$$
Failure

Fails unless x is a variable with the same type as u .

Uses

Removing unnecessary speciality in a goal, particularly as a prelude to an inductive proof.

See also

Thm.GEN, Thm.GENL, Drule.GEN_ALL, Tactic.GEN_TAC, Thm.SPEC, Drule.SPECL, Drule.SPEC_ALL, Tactic.STRIPE_TAC.

SPEC_VAR

(Drule)

SPEC_VAR : thm -> term * thm

Synopsis

Specializes the conclusion of a theorem, returning the chosen variant.

Description

When applied to a theorem $A \vdash !x. t$, the inference rule SPEC_VAR returns the term x' and the theorem $A \vdash t[x'/x]$, where x' is a variant of x chosen to avoid free variable capture.

$$\frac{A \vdash !x. t}{A \vdash t[x'/x]} \text{ SPEC_VAR}$$
Failure

Fails unless the theorem's conclusion is universally quantified.

Comments

This rule is very similar to plain SPEC, except that it returns the variant chosen, which may be useful information under some circumstances.

See also

Thm.GEN, Thm.GENL, Drule.GEN_ALL, Tactic.GEN_TAC, Thm.SPEC, Drule.SPECL, Drule.SPEC_ALL.

Specialize

(Thm)

Specialize : term -> thm -> thm

Synopsis

Specializes the conclusion of a universal theorem.

Description

When applied to a term u and a theorem $A \vdash !x. t$, Specialize returns the theorem $A \vdash t[u/x]$. Care is taken to ensure that no variables free in u become bound after this operation.

$$\frac{A \vdash !x. t}{A \vdash t[u/x]} \quad \text{Specialize } u$$
Failure

Fails if the theorem's conclusion is not universally quantified, or if x and u have different types.

Comments

`Specialize` behaves identically to `SPEC`, but is faster.

See also

`Thm.SPEC`, `Drule.ISPEC`, `Drule.SPECL`, `Drule.SPEC_ALL`, `Drule.SPEC_VAR`, `Thm.GEN`, `Thm.GENL`, `Drule.GEN_ALL`.

SPECL	(Drule)
-------	---------

`SPECL` : term list -> thm -> thm

Synopsis

Specializes zero or more variables in the conclusion of a theorem.

Description

When applied to a term list $[u_1; \dots; u_n]$ and a theorem $A \vdash !x_1 \dots x_n. t$, the inference rule `SPECL` returns the theorem $A \vdash t[u_1/x_1] \dots [u_n/x_n]$, where the substitutions are made sequentially left-to-right in the same way as for `SPEC`, with the same sort of alpha-conversions applied to t if necessary to ensure that no variables which are free in u_i become bound after substitution.

$$\frac{A \vdash !x_1 \dots x_n. t}{A \vdash t[u_1/x_1] \dots [u_n/x_n]} \quad \text{SPECL } [u_1, \dots, u_n]$$

It is permissible for the term-list to be empty, in which case the application of `SPECL` has no effect.

Failure

Fails unless each of the terms is of the same type as that of the appropriate quantified variable in the original theorem.

Example

The following is a specialization of a theorem from theory `arithmetic`.

```

- arithmeticTheory.LESS_EQ_LESS_EQ_MONO;
> val it = |- !m n p q. m <= p /\ n <= q ==> m + n <= p + q : thm

- SPECL (map Term ['1', '2', '3', '4']) it;
> val it = |- 1 <= 3 /\ 2 <= 4 ==> 1 + 2 <= 3 + 4 : thm

```

See also

Thm.GEN, Thm.GENL, Drule.GEN_ALL, Tactic.GEN_TAC, Thm.SPEC, Drule.SPEC_ALL, Tactic.SPEC_TAC.

spine_pair	(pairSyntax)
------------	--------------

spine_pair : term -> term list

Synopsis

Breaks a paired structure into its constituent pieces.

Example

```

- spine_pair (Term '((1,2),(3,4))');
> val it = ['(1,2)', '3', '4'] : term list

```

Comments

Note that spine_pair is similar, but not identical, to strip_pair which works recursively.

Failure

Never fails.

See also

pairSyntax.strip_pair.

split	(Lib)
-------	-------

split : ('a * 'b) list -> ('a list * 'b list)

Synopsis

Converts a list of pairs into a pair of lists.

Description

`split [(x1,y1), ..., (xn,yn)]` returns `([x1, ..., xn], [y1, ..., yn])`.

Failure

Never fails.

Comments

Identical to the Basis function `ListPair.unzip` and the function `Lib.unzip`.

See also

`Lib.unzip`, `Lib.zip`, `Lib.combine`.

<code>split_after</code>	<code>(Lib)</code>
--------------------------	--------------------

```
split_after : int -> 'a list -> 'a list * 'a list
```

Synopsis

Breaks a list in two at a specified index.

Description

An invocation `split_after k [x1, ..., xk, ..., xn]` returns the pair `([x1, ..., xk], [xk+1, ..., xn])`. If `k` is 0, then `split_after k l` returns `([], l)`. Similarly, `split_after (length l) l` returns `(l, [])`.

Failure

If `k` is negative, or longer than the length of the list.

Example

```
- split_after 2 [1,2,3,4,5]
> val it = ([1, 2], [3, 4, 5]) : int list * int list

- split_after 0 [1,2,3,4,5];
> val it = ([], [1, 2, 3, 4, 5]) : int list * int list

- split_after 5 [1,2,3,4,5];
> val it = ([1, 2, 3, 4, 5], []) : int list * int list
```



```
- split_after 6 [1,2,3,4,5];
! Uncaught exception:
! HOL_ERR

- split_after 0 ([]:int list);
> val it = ([], []) : int list * int list
```

See also

Lib.partition, Lib.pluck.

<div data-bbox="161 837 568 887" data-label="Text"> <p>SPOSE_NOT_THEN</p> </div>	<div data-bbox="1067 837 1329 887" data-label="Text"> <p>(bossLib)</p> </div>
--	---

SPOSE_NOT_THEN : (thm -> tactic) -> tactic

Synopsis

Initiate proof by contradiction.

Description

SPOSE_NOT_THEN provides a flexible way to start a proof by contradiction. Simple tactics for contradiction proofs often simply negate the goal and place it on the assumption list. However, if the goal is quantified, as is often the case, then more processing is required in order to get it into a suitable form for subsequent work. SPOSE_NOT_THEN `ttac` negates the current goal, pushes the negation inwards, and applies `ttac` to it.

Failure

Never fails, unless `ttac` fails.

Example

Suppose we want to prove Euclid's theorem.

```
!m. ?n. prime n /\ m < n
```

The classic proof is by contradiction. However, if we start such a proof with `CCONTR_TAC`, we get the goal

```
{ ~!m. ?n. prime n /\ m < n } ?- F
```

and one would immediately want to simplify the assumption, which is a bit awkward. Instead, an invocation `SPOSE_NOT_THEN ASSUME_TAC` yields

```
{ ?m. !n. ~prime n \\/ ~(m < n) } ?- F
```

and `SPOSE_NOT_THEN STRIP_ASSUME_TAC` results in

```
{ !n. ~prime n \\/ ~(m < n) } ?- F
```

See also

`Tactic.CCONTR_TAC`, `Tactic.CONTR_TAC`, `Tactic.ASSUME_TAC`, `Tactic.STRIP_ASSUME_TAC`.

<code>srw_ss</code>	<code>(BasicProvers)</code>
---------------------	-----------------------------

```
srw_ss : unit -> simpset
```

Synopsis

Implicit `simpset`.

Description

`bossLib.srw_ss` is identical to `BasicProvers.srw_ss`.

See also

`bossLib.srw_ss`.

<code>srw_ss</code>	<code>(bossLib)</code>
---------------------	------------------------

```
srw_ss : unit -> simpset
```

Synopsis

Returns the "stateful rewriting" system's underlying `simpset`.

Description

A call to `srw_ss()` returns a `simpset` value that is internally maintained and updated by the system. Its value changes as new types enter the `TypeBase`, and as theories are loaded. For this reason, it can't be accessed as a simple value, but is instead hidden behind a function.

The value behind `srw_ss()` can change in three ways. First, whenever a type enters the `TypeBase`, the type's associated simplification theorems (accessible directly using

the function `TypeBase.simpls_of`) are all added to the `simpset`. This ensures that the "obvious" rewrite theorems for a type (such as the disjointness of constructors) need never be explicitly specified.

Secondly, users can interactively add `simpset` fragments to the `srw_ss()` value by using the function `augment_srw_ss`. This function might be used after a definition is made to ensure that a particular constant always has its definition expanded. (Whether or not a constant warrants this is something that needs to be determined on a case-by-case basis.)

Thirdly, theories can augment the `srw_ss()` value as they load. This is set up in a theory's script file with the function `export_rewrites`. This causes a list of appropriate theorems to be added when the theory loads. It is up to the author of the theory to ensure that the theorems added to the `simpset` are sensible.

Failure

Never fails.

See also

`bossLib.augment_srw_ss`, `BasicProvers.export_rewrites`, `bossLib.SRW_TAC`.

SRW_TAC	(BasicProvers)
---------	----------------

`SRW_TAC : ssfrag list -> thm list -> tactic`

Synopsis

A version of `RW_TAC` with an implicit `simpset`.

Description

`bossLib.SRW_TAC` is identical to `BasicProvers.SRW_TAC`.

See also

`bossLib.SRW_TAC`.

SRW_TAC	(bossLib)
---------	-----------

`SRW_TAC : ssfrag list -> thm list -> tactic`

Synopsis

A version of `RW_TAC` with an implicit `simpset`.

Description

A call to `SRW_TAC [d1, ..., dn] thlist` produces the same result as

```
RW_TAC (srw_ss() ++ d1 ++ ... ++ dn) thlist
```

Failure

When applied to a goal, the tactic resulting from an application of `SRW_TAC` may diverge.

Comments

There are two reasons why one might prefer `SRW_TAC` to `RW_TAC`. Firstly, when a large number of datatypes are present in the `TypeBase`, the implementation of `RW_TAC` has to merge the attendant simplifications for each type onto its `simpset` argument each time it is called. This can be rather time-consuming. Secondly, the `simpset` returned by `srw_ss()` can be augmented with fragments from other sources than the `TypeBase`, using the functions `augment_srw_ss` and `export_rewrites`. This can make for a tool that is simple to use, and powerful because of all its accumulated `simpset` fragments.

Naturally, the latter advantage can also be a disadvantage: if `SRW_TAC` does too much because there is too much in the `simpset` underneath `srw_ss()`, then there is no way to get around this using `SRW_TAC`.

Typical invocations of `SRW_TAC` will be of the form

```
SRW_TAC [] [th1, th2, ... ]
```

The first argument, for lists of `simpset` fragments is for the inclusion of fragments that are not always appropriate. An example of such a fragment is `numSimps.ARITH_ss`, which embodies an arithmetic decision procedure for the natural numbers.

See also

`bossLib.srw_ss`, `bossLib.augment_srw_ss`, `BasicProvers.export_rewrites`, `simplib.SSFRAG`.

SSFRAG

(simpLib)

```

SSFRAG : { ac      : (thm * thm) list,
          congs    : thm list,
          convs    : {conv  : (term list -> conv) -> term list -> conv,
                    key    : (term list * term) option,
                    name   : string,
                    trace  : int} list,
          dprocs   : Traverse.reducer list,
          filter   : (controlled_thm -> controlled_thm list) option,
          name     : string option,
          rewrs    : thm list } -> ssfrag

```

Synopsis

Constructs `ssfrag` values.

Description

The `ssfrag` type is the way in which simplification components are packaged up and made available to the simplifier (though `ssfrag` values must first be turned into `simpsets`, either by addition to an existing `simpset`, or with the `mk_simpset` function).

The big record type passed to `SSFRAG` as an argument has seven fields. Here we describe each in turn.

The `ac` field is a list of “AC theorem” pairs. Each such pair is the pair of theorems stating that a given binary function is associative and commutative. The theorems can be given in either order, can present the associativity theorem in either direction, and can be generalised to any extent.

The `congs` field is a list of congruence theorems justifying the addition of theorems to simplification contexts. For example, the congruence theorem for implication is

$$\vdash (P = P') \implies (P' \implies (Q = Q')) \implies (P \implies Q = P' \implies Q')$$

This theorem encodes a rewriting strategy. The consequent of the chain of implications is the form of term in question, where the appropriate components have been rewritten. Then, in left-to-right order, the various antecedents of the implication specify the rewriting strategy which gives rise to the consequent. In this example, P is first simplified to P' without any additional context, then, using P' as additional context, simplification of Q proceeds, producing Q' . Another example is a rule for conjunction:

$$\vdash (P \implies (Q = Q')) \implies (Q' \implies (P = P')) \implies ((P \wedge Q) = (P' \wedge Q'))$$

Here P is assumed while Q is simplified to Q' . Then, Q' is assumed while P is simplified to P' . If a antecedent doesn't involve the relation in question (here, equality) then it is treated as a side-condition, and the simplifier will be recursively invoked to try and solve it.

Higher-order congruence rules are also possible. These provide a method for dealing with bound variables. The following is a rule for the restricted universal quantifier, for example:

$$\begin{aligned} &|- (P = Q) ==> (!v. v \text{ IN } Q ==> (f \ v = g \ v)) ==> \\ & \quad (\text{RES_FORALL } P \ f = \text{RES_FORALL } Q \ g) \end{aligned}$$

(If f is an abstraction, $\lambda x. \ t$, then $\text{RES_FORALL } P \ f$ is pretty-printed as $!x: :P. \ t$) Terms in the conclusions of higher-order congruence rules that might be abstractions (such as f above) should be kept as variables, rather than written out as abstractions. In other words, the conclusion of the congruence rule above should not be written as

$$\text{RES_FORALL } P \ (\lambda v. \ f \ v) = \text{RES_FORALL } Q \ (\lambda v. \ g \ v)$$

The `convs` field is a list of conversions that the simplifier will apply. Each conversion added to an `ssfrag` value is done so in a record consisting of four fields.

The `conv` field of this subsidiary record type includes the value of the conversion itself. When the simplifier applies the conversion it is actually passed two extra arguments (as the type indicates). The first is a solver function that can be used to recursively do side-condition solving, and the second is a stack of side-conditions that have been accumulated to date. Many conversions will typically ignore these arguments (as in the example below).

The `key` field of the subsidiary record type is an optional pattern, specifying the places where the conversion should be applied. If the value is `NONE`, then the conversion will be applied to all sub-terms. If the value is `SOME(lcs, t)`, then the term t is used as a pattern specifying those terms to which the conversion should be applied. Further, the list `lcs` (which must be a list of variables), specifies those variables in t which shouldn't be generalised against; they are effectively local constants. Note, however, that the types in the pattern term t will not be used to eliminate possible matches, so that if a match is desired with a particular type instantiation of a term, then the conversion will need to reject the input itself. The `name` and `trace` fields are only relevant to the debugging facilities of the simplifier.

The `dprocs` field of the record passed to `SSFRAG` is where decision procedures can be specified. Documentation describing the construction and use of values of type `reducer` is available in the `DESCRIPTION`.

The `filter` field of the record is an optional function, which, if present, is composed with the standard simplifier's function for generating rewrites from theorems, and replaces that function. The version of this present in `bool_ss` and its descendents will, for


```

                                filter = NONE, rewr = []};
> val ssd2 =
  SSFRAG{ac = [(|- m + n + p = (m + n) + p, |- m + n = n + m)],
          congs = [], convs = [], dprocs = [], filter = NONE,
          rewr = []}
  : ssfrag
- SIMP_CONV (bool_ss ++ ssd2) [] (Term'(y + 3) + x + 4');
  (* note that the printing of + in this example is that of a
     right associative operator.*)
> val it = |- (y + 3) + x + 4 = 3 + 4 + x + y : thm

```

See also

`simpLib.++`, `boolSimps.bool_ss`, `simpLib.Cong`, `simpLib.mk_simpset`,
`simpLib.rewrites`, `simpLib.SIMP_CONV`.

<code>start_time</code>	<code>(Lib)</code>
-------------------------	--------------------

`start_time` : unit -> Timer.cpu_timer

Synopsis

Set a timer running.

Description

An application `start_time ()` creates a timer and starts it. A later invocation `end_time t`, where `t` is a timer, will need to be called to get the elapsed time between the two function calls.

Failure

Never fails.

Example

```

- val clock = start_time ();
> val clock = <cpu_timer> : cpu_timer

```

Comments

Multiple timers may be started without any interfering with the others.

Further operations associated with the type `cpu_timer` may be found in the Standard ML Basis Library structures `Timer` and `Time`.

See also

`Lib.end_time`, `Lib.time`.

<code>state</code>	<code>(Lib)</code>
--------------------	--------------------

```
state : ('a,'b) istream -> 'b
```

Synopsis

Project the state of an istream.

Description

An application `state istrm` yields the value of the current state of `istrm`.

Failure

If the projection function supplied when building the stream fails on the current element of the state.

Example

```
- val istrm = mk_istream (fn x => x+1) 0 (concat "gsym" o int_to_string);  
> val it = <istream> : (int, string) istream
```

```
- state istrm;  
> val it = "gsym0" : string
```

```
- next (next istrm);  
> val it = <istream> : (int, string) istream
```

```
- state istrm;  
> val it = "gsym2" : string
```

See also

`Lib.mk_istream`, `Lib.next`, `Lib.reset`.

<code>std_ss</code>	<code>(bossLib)</code>
---------------------	------------------------

```
std_ss : simpset
```

Synopsis

Basic simplification set.

Description

The simplification set `std_ss` extends `bool_ss` with a useful set of rewrite rules for terms involving options, pairs, and sums. It also performs beta and eta reduction. It applies some standard rewrites to evaluate expressions involving only numerals.

The following rewrites from `pairTheory` are included in `std_ss`:

```

|- !x. (FST x, SND x) = x
|- !x y. FST (x,y) = x
|- !x y. SND (x,y) = y
|- !x y a b. ((x,y) = (a,b)) = (x = a) /\ (y = b)
|- !f. CURRY (UNCURRY f) = f
|- !f. UNCURRY (CURRY f) = f
|- (CURRY f = CURRY g) = (f = g)
|- (UNCURRY f = UNCURRY g) = (f = g)
|- !f x y. CURRY f x y = f (x,y)
|- !f x y. UNCURRY f (x,y) = f x y
|- !f g x y. (f ## g) (x,y) = (f x, g y)

```

The following rewrites from `sumTheory` are included in `std_ss`:

```

|- !x. ISL x ==> (INL (OUTL x) = x)
|- !x. ISR x ==> (INR (OUTR x) = x)
|- (!x. ISL (INL x)) /\ !y. ~ISL (INR y)
|- (!x. ISR (INR x)) /\ !y. ~ISR (INL y)
|- !x. OUTL (INL x) = x
|- !x. OUTR (INR x) = x
|- !x y. ~(INL x = INR y)
|- !x y. ~(INR y = INL x)
|- (!y x. (INL x = INL y) = (x = y)) /\
  (!y x. (INR x = INR y) = (x = y))
|- (!f g x. case f g (INL x) = f x) /\
  (!f g y. case f g (INR y) = g y)

```

The following rewrites from `optionTheory` are included in `std_ss`:

```

|- (!x y. (SOME x = SOME y) = (x = y))
|- (!x. ~(NONE = SOME x))
|- (!x. ~(SOME x = NONE))
|- (!x. THE (SOME x) = x)

```

```

|- (!x. IS_SOME (SOME x) = T)
|- (IS_SOME NONE = F)
|- (!x. IS_NONE x = (x = NONE))
|- (!x. ~IS_SOME x = (x = NONE))
|- (!x. IS_SOME x ==> (SOME (THE x) = x))
|- (!x. case NONE SOME x = x)
|- (!x. case x SOME x = x)
|- (!x. IS_NONE x ==> (case e f x = e))
|- (!x. IS_SOME x ==> (case e f x = f (THE x)))
|- (!x. IS_SOME x ==> (case e SOME x = x))
|- (!u f. case u f NONE = u)
|- (!u f x. case u f (SOME x) = f x)
|- (!f x. OPTION_MAP f (SOME x) = SOME (f x))
|- (!f. OPTION_MAP f NONE = NONE)
|- (OPTION_JOIN NONE = NONE)
|- (!x. OPTION_JOIN (SOME x) = x)
|- !f x y. (OPTION_MAP f x = SOME y) = ?z. (x = SOME z) /\ (y = f z)
|- !f x. (OPTION_MAP f x = NONE) = (x = NONE)

```

Uses

For performing obvious simplification steps on terms, formulas, and goals. Also, sometimes simplification with more powerful simpsets, like `arith_ss`, becomes too slow, in which case one can use `std_ss` supplemented with whatever theorems are needed.

Comments

The simplification sets provided in `BasicProvers` and `bossLib` (currently `bool_ss`, `std_ss`, `arith_ss`, and `list_ss`) do not include useful rewrites stemming from HOL datatype declarations, such as injectivity and distinctness of constructors. However, the simplification routines `RW_TAC` and `SRW_TAC` automatically load these rewrites.

See also

`BasicProvers.RW_TAC`, `BasicProvers.SRW_TAC`, `simpLib.SIMP_TAC`, `simpLib.SIMP_CONV`, `simpLib.SIMP_RULE`, `BasicProvers.bool_ss`, `bossLib.arith_ss`, `bossLib.list_ss`.

<code>store_thm</code>	<code>(Tactical)</code>
------------------------	-------------------------

```
store_thm : string * term * tactic -> thm
```

Synopsis

Proves and then stores a theorem in the current theory segment.

Description

The call `store_thm(name, t, tac)` is equivalent to `save_thm(name, prove(t, tac))`.

Failure

Whenever `prove` fails to prove the given term.

Uses

Saving theorems for retrieval in later sessions. Binding the result of `store_thm` to an ML variable makes it easy to access the theorem in the current terminal session.

See also

`Tactical.prove`, `Theory.save_thm`.

<code>strcat</code>	<code>(Lib)</code>
---------------------	--------------------

```
strcat : string -> string -> string
```

Synopsis

Concatenates two ML strings.

Failure

Never fails.

Example

```
- strcat "1" "";
> val it = "1" : string

- strcat "hello" "world";
> val it = "helloworld" : string

- strcat "hello" (strcat " " "world");
> val it = "hello world" : string
```

STRENGTHEN_CONSEQ_CONV_RULE (ConseqConv)

STRENGTHEN_CONSEQ_CONV_RULE : directed_conseq_conv -> thm -> thm

Synopsis

Tries to strengthen the antecedent of a theorem consisting of an implication.

Description

Given a theorem of the form $\vdash A \implies C$ and a directed consequence conversion c a call of `STRENGTHEN_CONSEQ_CONV_RULE c thm` tries to strengthen A to a predicate sA using c . If it succeeds it returns the theorem $\vdash sA \implies C$.

See also

`ConseqConv.WEAKEN_CONSEQ_CONV_RULE`.

string_to_int (Lib)

string_to_int : string -> int

Synopsis

Translates from a string to an integer.

Description

An application `string_to_int s` returns the integer denoted by s , if such exists.

Failure

If the string cannot be translated to an integer.

Example

```
- string_to_int "123";
> val it = 123 : int

- string_to_int "~123";
> val it = ~123 : int

- string_to_int "foo";
! Uncaught exception:
! HOL_ERR
```

Comments

Similar functionality can be obtained from the Standard ML Basis Library function `Int.fromString`.

See also

`Lib.int_to_string`.

<code>strip_abs</code>	<code>(boolSyntax)</code>
------------------------	---------------------------

`strip_abs : term -> term list * term`

Synopsis

Iteratively breaks apart abstractions.

Description

If M has the form $\lambda x_1 \dots \lambda x_n. t$ then `strip_abs M` returns $([x_1, \dots, x_n], t)$. Note that

$$\text{strip_abs}(\text{list_mk_abs}([x_1, \dots, x_n], t))$$

will not return $([x_1, \dots, x_n], t)$ if t is an abstraction.

Failure

Never fails.

See also

`boolSyntax.list_mk_abs`, `Term.dest_abs`.

<code>strip_abs</code>	<code>(Term)</code>
------------------------	---------------------

`strip_abs : term -> term list * term`

Synopsis

Break apart consecutive lambda abstractions.

Description

If M is a term of the form $\lambda v_1 \dots \lambda v_n. N$, where N is not a lambda abstraction, then `strip_abs M` equals $([v_1, \dots, v_n], N)$. Otherwise, the result is $([], M)$.

Failure

Never fails.

Example

```
- strip_abs (Term '\x y z. x ==> y ==> z');
> val it = (['x', 'y', 'z'], 'x ==> y ==> z') : term list * term

- strip_abs T;
> val it = ([], 'T') : term list * term
```

Comments

In the current implementation of HOL, `strip_abs` is far faster than iterating `dest_abs` for terms with many consecutive binders.

See also

`Term.strip_binder`, `Term.dest_abs`, `boolSyntax.strip_forall`,
`boolSyntax.strip_exists`.

strip_anylet	(pairSyntax)
--------------	--------------

```
strip_anylet : term -> (term * term) list list * term
```

Synopsis

Repeatedly destructs arbitrary let terms.

Description

The invocation `strip_anylet M` where `M` has the form of a let-abstraction, i.e., `LET P Q`, returns a pair `([[[a1,b1],..., [an,bn]], ... [(u1,v1),..., (uk,vk)]], body)`, where the first element of the pair is a list of lists of bindings, and the second is the body of the let. The binding lists are required since let terms can, in general, be of the form (using surface syntax) `let a1 = b1 and ... and an = bn in body`.

Failure

Never fails.

Example

```

- strip_anylet ‘let g x = A in
                let v = g x y in
                let f x y (a,b) = g a
                and foo = M
                in
                f x foo v’;
> val it =
  ([[('g x', 'A')],
   [('v', 'g x y')],
   [('f x y (a,b)', 'g a'), ('foo', 'M')]], 'f x foo v')

```

Uses

Programming that involves manipulation of term syntax.

See also

`boolSyntax.dest_let`, `pairSyntax.mk_anylet`, `pairSyntax.list_mk_anylet`,
`pairSyntax.dest_anylet`.

STRIP_ASSUME_TAC

(Tactic)

`STRIP_ASSUME_TAC : thm_tactic`

Synopsis

Splits a theorem into a list of theorems and then adds them to the assumptions.

Description

Given a theorem `th` and a goal (A, t) , `STRIP_ASSUME_TAC th` splits `th` into a list of theorems. This is done by recursively breaking conjunctions into separate conjuncts, cases-splitting disjunctions, and eliminating existential quantifiers by choosing arbitrary variables. Schematically, the following rules are applied:

$$\begin{array}{l}
 \text{A ?- t} \\
 \hline
 \text{STRIP_ASSUME_TAC (A' |- v1 /\ \dots /\ vn)} \\
 \text{A u \{v1, \dots, vn\} ?- t}
 \end{array}$$

$$\begin{array}{l}
 \text{A ?- t} \\
 \hline
 \text{STRIP_ASSUME_TAC (A' |- v1 \/ \dots \/ vn)} \\
 \text{A u \{v1\} ?- t \dots A u \{vn\} ?- t}
 \end{array}$$

$$\frac{A \text{ ?- } t}{\text{STRIP_ASSUME_TAC } (A' \text{ |- } ?x.v)}$$

$$A \text{ u } \{v[x'/x]\} \text{ ?- } t$$

where x' is a variant of x .

If the conclusion of th is not a conjunction, a disjunction or an existentially quantified term, the whole theorem th is added to the assumptions.

As assumptions are generated, they are examined to see if they solve the goal (either by being alpha-equivalent to the conclusion of the goal or by deriving a contradiction).

The assumptions of the theorem being split are not added to the assumptions of the goal(s), but they are recorded in the proof. This means that if A' is not a subset of the assumptions A of the goal (up to alpha-conversion), $\text{STRIP_ASSUME_TAC } (A' \text{ |- } v)$ results in an invalid tactic.

Failure

Never fails.

Example

When solving the goal

$$\text{?- } m = 0 + m$$

assuming the clauses for addition with $\text{STRIP_ASSUME_TAC ADD_CLAUSES}$ results in the goal

$$\{m + (\text{SUC } n) = \text{SUC}(m + n), (\text{SUC } m) + n = \text{SUC}(m + n), \\ m + 0 = m, 0 + m = m, m = 0 + m\} \text{ ?- } m = 0 + m$$

while the same tactic directly solves the goal

$$\text{?- } 0 + m = m$$

Uses

STRIP_ASSUME_TAC is used when applying a previously proved theorem to solve a goal, or when enriching its assumptions so that resolution, rewriting with assumptions and other operations involving assumptions have more to work with.

See also

Tactic.ASSUME_TAC , Tactic.CHOOSE_TAC , $\text{Thm_cont.CHOOSE_THEN}$,
 $\text{Thm_cont.CONJUNCTS_THEN}$, $\text{Tactic.DISJ_CASES_TAC}$, $\text{Thm_cont.DISJ_CASES_THEN}$.

strip_binder

(Term)

`strip_binder : term option -> term -> term list * term`

Synopsis

Break apart consecutive binders.

Description

An application `strip_binder (SOME c) (c(\v1. ... (c(\vn.M))...))` returns `([v1,...,vn],M)`. The constant `c` should represent a term binding operation.

An application `strip_binder NONE (\v1...vn. M)` returns `([v1,...,vn],M)`.

Failure

Never fails.

Example

`strip_abs` could be defined as follows.

```
- val strip_abs = strip_binder NONE;
> val strip_abs = fn : term -> term list * term

- strip_abs (Term `x y z. x /\ y ==> z`);
> val it = ([`x`, `y`, `z`], `x /\ y ==> z`) : term list * term
```

Defining `strip_forall` is similar.

```
strip_binder (SOME boolSyntax.universal)
```

Comments

Terms with many consecutive binders should be taken apart using `strip_binder` and its instantiations `strip_abs`, `strip_forall`, and `strip_exists`. In the current implementation of HOL, iterating `dest_abs`, `dest_forall`, or `dest_exists` is far slower for terms with many consecutive binders.

See also

`Term.list_mk_binder`, `Term.strip_abs`, `boolSyntax.strip_forall`, `boolSyntax.strip_exists`.

STRIP_BINDER_CONV

(Conv)

```
STRIP_BINDER_CONV : term option -> conv -> conv
```

Synopsis

Applies a conversion underneath a binder prefix.

Description

If the application of `conv` to M yields $\vdash M = N$, then `STRIP_BINDER_CONV (SOME c) conv (c(\v1. ... (c(\v` returns $\vdash c(\v1. ... (c(\vn.M))...) = c(\v1. ... (c(\vn.N))...)$ and `STRIP_BINDER_CONV NONE conv` returns $\vdash (\v1 \dots \vn.M) = (\v1 \dots \vn.N)$.

Failure

If `conv M` fails. Also fails if some of $[v_1, \dots, v_n]$ are free in the hypotheses of `conv M`.

Example

```
- STRIP_BINDER_CONV NONE BETA_CONV (Term `(\u v w. (\a. a + v * w) u`);
> val it = \vdash (\u v w. (\a. a + v * w) u) = (\u v w. u + v * w) : thm

- STRIP_BINDER_CONV (SOME existential) SYM_CONV
      (Term `?u v w x y. u + v = w + x + y`);
> val it = \vdash (?u v w x y. u + v = w + x + y) =
      ?u v w x y. w + x + y = u + v : thm
```

Comments

`STRIP_BINDER_CONV` is more efficient than iterated application of `BINDER_CONV` or `ABS_CONV` or `QUANT_CONV`.

See also

`Conv.BINDER_CONV`, `Conv.ABS_CONV`, `Conv.QUANT_CONV`, `Conv.STRIP_BINDER_CONV`, `Conv.STRIP_QUANT_CONV`.

strip_comb	(boolSyntax)
------------	--------------

```
strip_comb : term -> term * term list
```

Synopsis

Iteratively breaks apart combinations (function applications).

Description

If M has the form $t \ t_1 \ \dots \ t_n$ then `strip_comb M` returns $(t, [t_1, \dots, t_n])$. Note that

```
strip_comb(list_mk_comb(t, [t1, ..., tn]))
```

will not be $(t, [t_1, \dots, t_n])$ if t is a combination.

Failure

Never fails.

Example

```
- strip_comb (Term 'x /\ y');
> val it = ('$/\', ['x', 'y']) : term * term list

- strip_comb T;
> val it = ('T', []) : term * term list
```

See also

`Term.list_mk_comb`, `Term.dest_comb`.

strip_conj	(boolSyntax)
------------	--------------

```
strip_conj : term -> term list
```

Synopsis

Recursively breaks apart conjunctions.

Description

If M is of the form $t_1 \wedge \dots \wedge t_n$, where no t_i is a conjunction, then `strip_conj M` returns $[t_1, \dots, t_n]$. Any t_i that is a conjunction is broken down by `strip_conj`, hence

```
strip_conj(list_mk_conj [t1, ..., tn])
```

will not return $[t_1, \dots, t_n]$ if any t_i is a conjunction.

Failure

Never fails.

Example

```
- strip_conj (Term '(a /\ b) /\ c /\ d');
> val it = ['a', 'b', 'c', 'd'] : term list
```

See also

boolSyntax.dest_conj, boolSyntax.mk_conj, boolSyntax.list_mk_conj.

strip_disj	(boolSyntax)
------------	--------------

```
strip_disj : term -> term list
```

Synopsis

Recursively breaks apart disjunctions.

Description

If M is of the form $t_1 \vee \dots \vee t_n$, where no t_i is a disjunction, then `strip_disj M` returns $[t_1, \dots, t_n]$. Any t_i that is a disjunction is broken down by `strip_disj`, hence

```
strip_disj(list_mk_disj [t1, ..., tn])
```

will not return $[t_1, \dots, t_n]$ if any t_i is a disjunction.

Failure

Never fails.

Example

```
- strip_disj (Term '(a \vee b) \vee c \vee d');
> val it = ['a', 'b', 'c', 'd'] : term list
```

See also

boolSyntax.dest_disj, boolSyntax.mk_disj, boolSyntax.list_mk_disj.

strip_exists	(boolSyntax)
--------------	--------------

```
strip_exists : term -> term list * term
```

Synopsis

Iteratively breaks apart existential quantifications.

Description

If M has the structure $\exists x_1 \dots \exists x_n. t$ then `strip_exists M` returns $([x_1, \dots, x_n], t)$. Note that

```
strip_exists(list_mk_exists(["x1";...;"xn"],"t"))
```

will not return $([x_1, \dots, x_n], t)$ if t is an existential quantification.

Failure

Never fails.

See also

`boolSyntax.list_mk_exists`, `boolSyntax.dest_exists`.

<code>strip_forall</code>	<code>(boolSyntax)</code>
---------------------------	---------------------------

```
strip_forall : term -> term list * term
```

Synopsis

Iteratively breaks apart universal quantifications.

Description

If M has the form $!x_1 \dots x_n. t$ then `strip_forall M` returns $([x_1, \dots, x_n], t)$. Note that

```
strip_forall(list_mk_forall([x1,...,xn],t,))
```

will not return $([x_1, \dots, x_n], t)$ if t is a universal quantification.

Failure

Never fails.

See also

`boolSyntax.list_mk_forall`, `boolSyntax.dest_forall`.

<code>strip_fun</code>	<code>(boolSyntax)</code>
------------------------	---------------------------

```
strip_fun : hol_type -> hol_type list * hol_type
```

Synopsis

Iteratively breaks apart function types.

Description

If fty is of the form $ty_1 \rightarrow (\dots (t_{yn} \rightarrow ty) \dots)$, then `strip_fun fty` returns $([ty_1, \dots, t_{yn}], ty)$. Note that

```
strip_fun(list_mk_fun([ty1,...,tyn],ty))
```

will not return $([ty1, \dots, tyn], ty)$ if ty is a function type.

Failure

Never fails.

Example

```
- strip_fun (Type '(a -> 'bool) -> ('b -> 'c)');
> val it = (['a -> 'bool', ':'b', ':'c') : hol_type list * hol_type
```

See also

`boolSyntax.list_mk_fun`, `Type.dom_rng`, `Type.dest_type`.

STRIP_GOAL_THEN	(Tactic)
-----------------	----------

```
STRIP_GOAL_THEN : thm_tactic -> tactic
```

Synopsis

Splits a goal by eliminating one outermost connective, applying the given theorem-tactic to the antecedents of implications.

Description

Given a theorem-tactic `ttac` and a goal (A, t) , `STRIP_GOAL_THEN` removes one outermost occurrence of one of the connectives `!`, `==>`, `~` or `/\` from the conclusion of the goal t . If t is a universally quantified term, then `STRIP_GOAL_THEN` strips off the quantifier:

$$\begin{array}{l} A \text{ ?- } !x.u \\ \text{===== STRIP_GOAL_THEN ttac} \\ A \text{ ?- } u[x'/x] \end{array}$$

where x' is a primed variant that does not appear free in the assumptions A . If t is a conjunction, then `STRIP_GOAL_THEN` simply splits the conjunction into two subgoals:

$$\begin{array}{l} A \text{ ?- } v /\ w \\ \text{===== STRIP_GOAL_THEN ttac} \\ A \text{ ?- } v \quad A \text{ ?- } w \end{array}$$

If t is an implication $u ==> v$ and if:

```

      A ?- v
===== ttac (u |- u)
      A' ?- v'

```

then:

```

      A ?- u ==> v
===== STRIP_GOAL_THEN ttac
      A' ?- v'

```

Finally, a negation $\sim t$ is treated as the implication $t \implies F$.

Failure

`STRIP_GOAL_THEN ttac (A,t)` fails if t is not a universally quantified term, an implication, a negation or a conjunction. Failure also occurs if the application of `ttac` fails, after stripping the goal.

Example

When solving the goal

```
?- (n = 1) ==> (n * n = n)
```

a possible initial step is to apply

```
STRIP_GOAL_THEN SUBST1_TAC
```

thus obtaining the goal

```
?- 1 * 1 = 1
```

Uses

`STRIP_GOAL_THEN` is used when manipulating intermediate results (obtained by stripping outer connectives from a goal) directly, rather than as assumptions.

See also

`Tactic.CONJ_TAC`, `Thm_cont.DISCH_THEN`, `Thm_cont.FILTER_STRIP_THEN`, `Tactic.GEN_TAC`, `Tactic.STRIP_ASSUME_TAC`, `Tactic.STRIP_TAC`.

<pre>strip_imp</pre>	<pre>(boolSyntax)</pre>
----------------------	-------------------------

```
strip_imp : term -> term list * term
```


Synopsis

Iteratively breaks apart implications.

Description

If M is of the form $t_1 \implies (\dots (t_n \implies t) \dots)$, then `strip_imp M` returns $([t_1, \dots, t_n], t)$. Note that

```
strip_imp(list_mk_imp([t1, ..., tn], t))
```

will not return $([t_1, \dots, t_n], t)$ if t is an implication.

Failure

Never fails.

Example

```
- strip_imp "(T ==> F) ==> (T ==> F)";;
> val it = (["T ==> F"; "T"], "F") : term list * term

- strip_imp (Term `t1 ==> t2 ==> t3 ==> ~t`);
> val it = (['t1', 't2', 't3', 't'], 'F') : term list * term
```

See also

`boolSyntax.list_mk_imp`, `boolSyntax.dest_imp`.

`strip_imp_only`

(`boolSyntax`)

```
strip_imp_only : term -> term list * term
```

Synopsis

Iteratively breaks apart implications.

Description

If M is of the form $t_1 \implies (\dots (t_n \implies t) \dots)$, then `strip_imp_only M` returns $([t_1, \dots, t_n], t)$. Note that

```
strip_imp_only(list_mk_imp([t1, ..., tn], t))
```

will not return $([t_1, \dots, t_n], t)$ if t is an implication.

Failure

Never fails.

Example

```
- strip_imp_only (Term '(T ==> F) ==> (T ==> F)');
> val it = (['T ==> F', 'T'], 'F') : term list * term

- strip_imp_only (Term 't1 ==> t2 ==> t3 ==> ~t');
> val it = (['t1', 't2', 't3'], '~t') : term list * term
```

See also

`boolSyntax.list_mk_imp`, `boolSyntax.dest_imp`.

<div data-bbox="236 1046 504 1102" data-label="Text"> <p><code>strip_neg</code></p> </div>	<div data-bbox="1059 1046 1414 1102" data-label="Text"> <p><code>(boolSyntax)</code></p> </div>
--	---

```
strip_neg : term -> term * int
```

Synopsis

Breaks iterated negations down to an unnegated core.

Description

If M is of the form $\sim \dots \sim t$, then `strip_neg M` returns (t, n) , where n is the number of consecutive negations being applied to t .

Failure

Never fails.

Example

```
- strip_neg (Term '~~~~t');
> val it = ('t', 4) : term * int

- strip_neg (Term 'x');
<<HOL message: inventing new type variable names: 'a>>
> val it = ('x', 0) : term * int
```

Comments

There is no corresponding entrypoint for building iterated negations. If such functionality is desired, `funpow` may be used:

```
- funpow 3 mk_neg T;
> val it = '~~~T' : term
```

See also

`boolSyntax.dest_neg`, `boolSyntax.mk_neg`, `Lib.funpow`.

<code>strip_pabs</code>	<code>(pairSyntax)</code>
-------------------------	---------------------------

```
strip_pabs : term -> term list * term
```

Synopsis

Iteratively breaks apart paired abstractions.

Description

`strip_pabs "\p1 ... pn. t"` returns `([p1,...,pn],t)`. Note that

```
strip_pabs(list_mk_abs([p1,...,pn],t))
```

will not return `([p1,...,pn],t)` if `t` is a paired abstraction.

Failure

Never fails.

See also

`boolSyntax.strip_abs`, `pairSyntax.list_mk_pabs`, `pairSyntax.dest_pabs`.

<code>strip_pair</code>	<code>(pairSyntax)</code>
-------------------------	---------------------------

```
strip_pair : term -> term list
```

Synopsis

Recursively breaks a paired structure into its constituent pieces.

Example

```
- strip_pair (Term '((1,2),(3,4))');
> val it = ['1', '2', '3', '4'] : term list
```

Comments

Note that `strip_pair` is similar, but not identical, to `spine_pair` which does not work recursively.

Failure

Never fails.

See also

`pairSyntax.spine_pair`.

<code>strip_pexists</code>	<code>(pairSyntax)</code>
----------------------------	---------------------------

```
strip_pexists : term -> term list * term
```

Synopsis

Iteratively breaks apart paired existential quantifications.

Description

`strip_pexists "?p1 ... pn. t"` returns $([p_1, \dots, p_n], t)$. Note that

```
strip_pexists(list_mk_pexists([[p1, ..., pn], t]))
```

will not return $([p_1, \dots, p_n], t)$ if t is a paired existential quantification.

Failure

Never fails.

See also

`boolSyntax.strip_exists`, `pairSyntax.dest_pexists`.

<code>strip_pforall</code>	<code>(pairSyntax)</code>
----------------------------	---------------------------

```
strip_pforall : term -> term list * term
```

Synopsis

Iteratively breaks apart paired universal quantifications.

Description

`strip_pforall "!p1 ... pn. t"` returns $([p1, \dots, pn], t)$. Note that

```
strip_pforall(list_mk_pforall([p1, ..., pn], t))
```

will not return $([p1, \dots, pn], t)$ if t is a paired universal quantification.

Failure

Never fails.

See also

`boolSyntax.strip_forall`, `pairSyntax.dest_pforall`.

STRIP_QUANT_CONV

(Conv)

`STRIP_QUANT_CONV : conv -> conv`

Synopsis

Applies a conversion underneath a quantifier prefix.

Description

If tm has the form $Q(\backslash v1. \dots (Q(\backslash vn.M))\dots)$ and the application of `conv` to M yields

$\vdash M = N$, then `STRIP_QUANT_CONV conv tm` returns $\vdash Q(\backslash v1. \dots (Q(\backslash vn.M))\dots) = Q(\backslash v1. \dots (Q(\backslash vn.N))\dots)$ provided Q is Hilbert's choice operator or a universal, existential, or unique-existence quantifier.

Otherwise, `STRIP_QUANT_CONV conv tm` returns `conv tm`.

Failure

If `conv M` fails. Or if `conv tm` fails when tm is not a quantified term. Also fails if some of $[v1, \dots, vn]$ are free in the hypotheses of `conv M`.

Example

```
- STRIP_QUANT_CONV (STRIP_QUANT_CONV SYM_CONV)
  (Term '!x y z. ?!p q r. x + y*z = p*q + r');
```

```
> val it =
  |- (!x y z. ?!p q r. x + y * z = p * q + r) =
    !x y z. ?!p q r. p * q + r = x + y * z : thm
```

Comments

To deal with binders not in the above list, e.g., newly introduced ones, use `STRIP_BINDER_CONV`.

For deeply nested quantifiers, `STRIP_QUANT_CONV` and `STRIP_BINDER_CONV` are more efficient than iterated application of `QUANT_CONV`, `BINDER_CONV`, or `ABS_CONV`.

See also

`Conv.STRIP_BINDER_CONV`, `Conv.QUANT_CONV`, `Conv.BINDER_CONV`, `Conv.ABS_CONV`.

<code>strip_res_exists</code>	<code>(res_quanLib)</code>
-------------------------------	----------------------------

```
strip_res_exists : (term -> ((term # term) list # term))
```

Synopsis

Iteratively breaks apart a restricted existentially quantified term.

Description

`strip_res_exists` is an iterative term destructor for restricted existential quantifications. It iteratively breaks apart a restricted existentially quantified term into a list of pairs which are the restricted quantified variables and predicates and the body.

```
strip_res_exists "?x1::P1. ... ?xn::Pn. t"
```

```
returns ([("x1", "P1"); ...; ("xn", "Pn")], "t").
```

Failure

Never fails.

See also

`res_quanLib.list_mk_res_exists`, `res_quanLib.is_res_exists`,
`res_quanLib.dest_res_exists`.

<code>strip_res_exists</code>	<code>(res_quanTools)</code>
-------------------------------	------------------------------

```
strip_res_exists : (term -> ((term # term) list # term))
```

Synopsis

Iteratively breaks apart a restricted existentially quantified term.

Description

strip_res_exists is an iterative term destructor for restricted existential quantifications. It iteratively breaks apart a restricted existentially quantified term into a list of pairs which are the restricted quantified variables and predicates and the body.

```
strip_res_exists "?x1::P1. ... ?xn::Pn. t"
```

returns ([("x1", "P1"); ...; ("xn", "Pn")], "t").

Failure

Never fails.

See also

res_quantTools.list_mk_res_exists, res_quantTools.is_res_exists,
res_quantTools.dest_res_exists.

strip_res_forall	(res_quantLib)
------------------	----------------

```
strip_res_forall : term -> ((term # term) list # term)
```

Synopsis

Iteratively breaks apart a restricted universally quantified term.

Description

strip_res_forall is an iterative term destructor for restricted universal quantifications. It iteratively breaks apart a restricted universally quantified term into a list of pairs which are the restricted quantified variables and predicates and the body.

```
strip_res_forall "!x1::P1. ... !xn::Pn. t"
```

returns ([("x1", "P1"); ...; ("xn", "Pn")], "t").

Failure

Never fails.

See also

res_quantLib.list_mk_res_forall, res_quantLib.is_res_forall,
res_quantLib.dest_res_forall.

<code>strip_res_forall</code>	<code>(res_quantTools)</code>
-------------------------------	-------------------------------

```
strip_res_forall : (term -> ((term # term) list # term))
```

Synopsis

Iteratively breaks apart a restricted universally quantified term.

Description

`strip_res_forall` is an iterative term destructor for restricted universal quantifications. It iteratively breaks apart a restricted universally quantified term into a list of pairs which are the restricted quantified variables and predicates and the body.

```
strip_res_forall "!x1::P1. ... !xn::Pn. t"
```

```
returns ([("x1", "P1"); ...; ("xn", "Pn")], "t").
```

Failure

Never fails.

See also

`res_quantTools.list_mk_res_forall`, `res_quantTools.is_res_forall`,
`res_quantTools.dest_res_forall`.

<code>STRIP_TAC</code>	<code>(Tactic)</code>
------------------------	-----------------------

```
STRIP_TAC : tactic
```

Synopsis

Splits a goal by eliminating one outermost connective.

Description

Given a goal (A, τ) , `STRIP_TAC` removes one outermost occurrence of one of the connectives `!`, `==>`, `~` or `/\` from the conclusion of the goal τ . If τ is a universally quantified term, then `STRIP_TAC` strips off the quantifier:

```

A ?- !x.u
===== STRIP_TAC
A ?- u[x'/x]
```


where x' is a primed variant that does not appear free in the assumptions A . If t is a conjunction, then STRIP_TAC simply splits the conjunction into two subgoals:

$$\begin{array}{c} A \text{ ?- } v \wedge w \\ \hline \text{STRIP_TAC} \\ A \text{ ?- } v \quad A \text{ ?- } w \end{array}$$

If t is an implication, STRIP_TAC moves the antecedent into the assumptions, stripping conjunctions, disjunctions and existential quantifiers according to the following rules:

$$\begin{array}{c} A \text{ ?- } v_1 \wedge \dots \wedge v_n \implies v \\ \hline A \text{ u } \{v_1, \dots, v_n\} \text{ ?- } v \end{array} \qquad \begin{array}{c} A \text{ ?- } v_1 \vee \dots \vee v_n \implies v \\ \hline A \text{ u } \{v_1\} \text{ ?- } v \dots A \text{ u } \{v_n\} \text{ ?- } v \end{array}$$

$$\begin{array}{c} A \text{ ?- } ?x.w \implies v \\ \hline A \text{ u } \{w[x'/x]\} \text{ ?- } v \end{array}$$

where x' is a primed variant of x that does not appear free in A . Finally, a negation $\sim t$ is treated as the implication $t \implies F$.

Failure

STRIP_TAC (A, t) fails if t is not a universally quantified term, an implication, a negation or a conjunction.

Example

Applying STRIP_TAC twice to the goal:

$$\text{?- !n. } m \leq n \wedge n \leq m \implies (m = n)$$

results in the subgoal:

$$\{n \leq m, m \leq n\} \text{ ?- } m = n$$

Uses

When trying to solve a goal, often the best thing to do first is REPEAT STRIP_TAC to split the goal up into manageable pieces.

See also

Tactic.CONJ_TAC, Tactic.DISCH_TAC, Thm.cont.DISCH_THEN, Tactic.GEN_TAC, Tactic.STRIP_ASSUME_TAC, Tactic.STRIP_GOAL_THEN.

STRIP_THM_THEN	(Thm_cont)
-----------------------	-------------------

STRIP_THM_THEN : thm_tactical

Synopsis

STRIP_THM_THEN applies the given theorem-tactic using the result of stripping off one outer connective from the given theorem.

Description

Given a theorem-tactic *ttac*, a theorem *th* whose conclusion is a conjunction, a disjunction or an existentially quantified term, and a goal (A, t) , STRIP_THM_THEN *ttac th* first strips apart the conclusion of *th*, next applies *ttac* to the theorem(s) resulting from the stripping and then applies the resulting tactic to the goal.

In particular, when stripping a conjunctive theorem $A' \vdash u \wedge v$, the tactic

$$ttac(u|-u) \text{ THEN } ttac(v|-v)$$

resulting from applying *ttac* to the conjuncts, is applied to the goal. When stripping a disjunctive theorem $A' \vdash u \vee v$, the tactics resulting from applying *ttac* to the disjuncts, are applied to split the goal into two cases. That is, if

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t1 \end{array} \quad ttac(u|-u) \quad \text{and} \quad \begin{array}{l} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t2 \end{array} \quad ttac(v|-v)$$

then:

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t1 \quad A \text{ ?- } t2 \end{array} \quad \text{STRIP_THM_THEN } ttac(A' \vdash u \vee v)$$

When stripping an existentially quantified theorem $A' \vdash ?x.u$, the tactic *ttac(u|-u)*, resulting from applying *ttac* to the body of the existential quantification, is applied to the goal. That is, if:

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \\ A \text{ ?- } t1 \end{array} \quad ttac(u|-u)$$

then:

```

      A ?- t
=====  STRIP_THM_THEN ttac (A' |- ?x. u)
      A ?- t1

```

The assumptions of the theorem being split are not added to the assumptions of the goal(s) but are recorded in the proof. If A' is not a subset of the assumptions A of the goal (up to alpha-conversion), `STRIP_THM_THEN ttac th` results in an invalid tactic.

Failure

`STRIP_THM_THEN ttac th` fails if the conclusion of `th` is not a conjunction, a disjunction or an existentially quantified term. Failure also occurs if the application of `ttac` fails, after stripping the outer connective from the conclusion of `th`.

Uses

`STRIP_THM_THEN` is used to enrich the assumptions of a goal with a stripped version of a previously-proved theorem.

See also

`Thm.cont.CHOOSE_THEN`, `Thm.cont.CONJUNCTS_THEN`, `Thm.cont.DISJ_CASES_THEN`, `Tactic.STRIP_ASSUME_TAC`.

STRUCT_CASES_TAC

(Tactic)

`STRUCT_CASES_TAC : thm_tactic`

Synopsis

Performs very general structural case analysis.

Description

When it is applied to a theorem of the form:

$$th = A' \mid - \ ?y_{11} \dots y_{1m}. (x=t_1) \wedge (B_{11} \wedge \dots \wedge B_{1k}) \vee \dots \vee \ ?y_{n1} \dots y_{np}. (x=t_n) \wedge (B_{n1} \wedge \dots \wedge B_{np})$$

in which there may be no existential quantifiers where a ‘vector’ of them is shown above, `STRUCT_CASES_TAC th` splits a goal $A \ ?- \ s$ into n subgoals as follows:

```

      A ?- s
=====
      A u {B11,...,B1k} ?- s[t1/x] ... A u {Bn1,...,Bnp} ?- s[tn/x]

```

that is, performs a case split over the possible constructions (the τ_i) of a term, providing as assumptions the given constraints, having split conjoined constraints into separate assumptions. Note that unless A' is a subset of A , this is an invalid tactic.

Failure

Fails unless the theorem has the above form, namely a conjunction of (possibly multiply existentially quantified) terms which assert the equality of the same variable x and the given terms.

Example

Suppose we have the goal:

```
?- ~(l:(*)list = []) ==> (LENGTH l) > 0
```

then we can get rid of the universal quantifier from the inbuilt list theorem `list_CASES`:

```
list_CASES = !l. (l = []) \\/ (?t h. l = CONS h t)
```

and then use `STRUCT_CASES_TAC`. This amounts to applying the following tactic:

```
STRUCT_CASES_TAC (SPEC_ALL list_CASES)
```

which results in the following two subgoals:

```
?- ~(CONS h t = []) ==> (LENGTH(CONS h t)) > 0
```

```
?- ~([] = []) ==> (LENGTH[]) > 0
```

Note that this is a rather simple case, since there are no constraints, and therefore the resulting subgoals have no assumptions.

Uses

Generating a case split from the axioms specifying a structure.

See also

`Tactic.ASM_CASES_TAC`, `Tactic.BOOL_CASES_TAC`, `Tactic.COND_CASES_TAC`,
`Tactic.DISJ_CASES_TAC`.

<p>SUB_AND_COND_ELIM_CONV</p>	<p>(Arith)</p>
--------------------------------------	-----------------------

`SUB_AND_COND_ELIM_CONV` : conv

Synopsis

Eliminates natural number subtraction, PRE, and conditional statements from a formula.

Description

This function eliminates natural number subtraction and the predecessor function, PRE, from a formula, but in doing so may generate conditional statements, so these are eliminated too. The conditional statements are moved up through the term and if at any point the branches of the conditional become Boolean-valued the conditional is eliminated. Subtraction operators are moved up until a relation (such as less-than) is reached. The subtraction can then be transformed into an addition. Provided the argument term is a formula, only an abstraction can prevent a conditional being moved up far enough to be eliminated. If the term is not a formula it may not be possible to eliminate the subtraction. The function is also incapable of eliminating subtractions that appear in arguments to functions other than the standard operators of arithmetic.

The function is not as delicate as it could be; it tries to eliminate all conditionals in a formula when it need only eliminate those that have to be removed in order to eliminate subtraction.

Failure

Never fails.

Example

```
#SUB_AND_COND_ELIM_CONV
# " $((p + 3) \leq n) \implies (!m. ((m = 0) \implies (n - 1) \mid (n - 2)) > p)$ ";;
|-  $(p + 3) \leq n \implies (!m. ((m = 0) \implies n - 1 \mid n - 2) > p) =$ 
   $(p + 3) \leq n \implies$ 
   $(!m. (\sim(m = 0) \ \backslash / \ n > (1 + p)) \ / \ ((m = 0) \ \backslash / \ n > (2 + p)))$ 

#SUB_AND_COND_ELIM_CONV
# " $!f \ n. f ((SUC \ n = 0) \implies 0 \mid (SUC \ n - 1)) < (f \ n) + 1$ ";;
|-  $(!f \ n. (f((SUC \ n = 0) \implies 0 \mid (SUC \ n) - 1)) < ((f \ n) + 1)) =$ 
   $(!f \ n.$ 
   $(\sim(SUC \ n = 0) \ \backslash / \ (f \ 0) < ((f \ n) + 1)) \ / \$ 
   $((SUC \ n = 0) \ \backslash / \ (f((SUC \ n) - 1)) < ((f \ n) + 1)))$ 

#SUB_AND_COND_ELIM_CONV
# " $!f \ n. (\backslash m. f ((m = 0) \implies 0 \mid (m - 1))) (SUC \ n) < (f \ n) + 1$ ";;
|-  $(!f \ n. ((\backslash m. f((m = 0) \implies 0 \mid m - 1))(SUC \ n)) < ((f \ n) + 1)) =$ 
   $(!f \ n. ((\backslash m. ((m = 0) \implies f \ 0 \mid f(m - 1)))(SUC \ n)) < ((f \ n) + 1))$ 
```

Uses

Useful as a preprocessor to decision procedures which do not allow natural number subtraction in their argument formula.

See also

Arith.COND_ELIM_CONV.

SUB_CONV	(Conv)
----------	--------

SUB_CONV : conv -> conv

Synopsis

Applies a conversion to the top-level subterms of a term.

Description

For any conversion c , the function returned by SUB_CONV c is a conversion that applies c to all the top-level subterms of a term. Its implementation is

```
fun SUB_CONV c = TRY_CONV (COMB_CONV c ORELSEC ABS_CONV c)
```

Example

If the conversion c maps t to $\vdash t = t'$, then SUB_CONV c maps an abstraction " $\lambda x.t$ " to the theorem:

$$\vdash (\lambda x.t) = (\lambda x.t')$$

That is, SUB_CONV c " $\lambda x.t$ " applies c to the body of the abstraction " $\lambda x.t$ ". If c is a conversion that maps " t_1 " to the theorem $\vdash t_1 = t_1'$ and " t_2 " to the theorem $\vdash t_2 = t_2'$, then the conversion SUB_CONV c maps an application " $t_1 t_2$ " to the theorem:

$$\vdash (t_1 t_2) = (t_1' t_2')$$

That is, SUB_CONV c " $t_1 t_2$ " applies c to the both the operator t_1 and the operand t_2 of the application " $t_1 t_2$ ". Finally, for any conversion c , the function returned by SUB_CONV c acts as the identity conversion on variables and constants. That is, if " t " is a variable or constant, then SUB_CONV c " t " returns $\vdash t = t$.

Failure

SUB_CONV c t_m fails if t_m is an abstraction " $\lambda x.t$ " and the conversion c fails when applied to t , or if t_m is an application " $t_1 t_2$ " and the conversion c fails when applied to either t_1

or t_2 . The function returned by `SUB_CONV c` may also fail if the ML function `c:term->thm` is not, in fact, a conversion (i.e. a function that maps a term t to a theorem $|- t = t'$).

See also

`Conv.ABS_CONV`, `Conv.COMB_CONV`, `Conv.RAND_CONV`, `Conv.RATOR_CONV`.

<div data-bbox="161 607 512 660" data-label="Text"> <p>SUBGOAL_THEN</p> </div>	<div data-bbox="1038 607 1331 660" data-label="Text"> <p>(Tactical)</p> </div>
---	---

`SUBGOAL_THEN : term -> thm_tactic -> tactic`

Synopsis

Allows the user to introduce a lemma.

Description

The user proposes a lemma and is then invited to prove it under the current assumptions. The lemma is then used with the `thm_tactic` to simplify the goal. That is, if

$$\begin{array}{l} A1 \text{ ?- } t1 \\ \text{=====} \quad f \text{ (} u \text{ |- } u \text{)} \\ A2 \text{ ?- } t2 \end{array}$$

then

$$\begin{array}{l} A1 \text{ ?- } t1 \\ \text{=====} \quad \text{SUBGOAL_THEN } u \text{ } f \\ A1 \text{ ?- } u \quad A2 \text{ ?- } t2 \end{array}$$

Typically `f (u |- u)` will be an invalid tactic because it would return a validation function which generated the theorem $A1, u \text{ |- } t1$ from the theorem $A2 \text{ |- } t2$. Nonetheless, the tactic `SUBGOAL_THEN u f` is valid because of the extra sub-goal where u must be proved.

Failure

`SUBGOAL_THEN` will fail if an attempt is made to use a nonboolean term as a lemma.

Uses

When combined with `rotate`, `SUBGOAL_THEN` allows the user to defer some part of a proof and to continue with another part. `SUBGOAL_THEN` is most convenient when the tactic solves the original goal, leaving only the subgoal. For example, suppose the user wishes to prove the goal

$$\{n = \text{SUC } m\} \text{ ?- } (0 = n) \implies t$$

Using `SUBGOAL_THEN` to focus on the case in which $\sim(n = 0)$, rewriting establishes its truth, leaving only the proof that $\sim(n = 0)$. That is,

$$\text{SUBGOAL_THEN (Term } \sim(0 = n)\text{) (fn th => REWRITE_TAC [th])}$$

generates the following subgoals:

$$\begin{aligned} \{n = \text{SUC } m\} \text{ ?- } \sim(0 = n) \\ \text{?- T} \end{aligned}$$

Comments

Some users may expect the generated tactic to be $f (A1 \mid - u)$, rather than $f (u \mid - u)$.

SUBS	(Drule)
------	---------

SUBS : (thm list -> thm -> thm)

Synopsis

Makes simple term substitutions in a theorem using a given list of theorems.

Description

Term substitution in HOL is performed by replacing free subterms according to the transformations specified by a list of equational theorems. Given a list of theorems $A1 \mid -t1=v1, \dots, An \mid -tn=vn$ and a theorem $A \mid -t$, `SUBS` simultaneously replaces each free occurrence of t_i in t with v_i :

$$\frac{A1 \mid -t1=v1 \quad \dots \quad An \mid -tn=vn \quad A \mid -t}{A1 \ u \quad \dots \quad u \quad An \ u \quad A \ \mid - \ t[v1, \dots, vn/t1, \dots, tn]} \quad \text{SUBS}[A1 \ \mid -t1=v1; \dots; An \ \mid -tn=vn] \quad (A \ \mid -t)$$

No matching is involved; the occurrence of each t_i being substituted for must be a free in t (see `SUBST_MATCH`). An occurrence which is not free can be substituted by using rewriting rules such as `REWRITE_RULE`, `PURE_REWRITE_RULE` and `ONCE_REWRITE_RULE`.

Failure

`SUBS [th1, ..., thn] (A \mid -t)` fails if the conclusion of each theorem in the list is not an equation. No change is made to the theorem $A \ \mid - \ t$ if no occurrence of any left-hand side of the supplied equations appears in t .

Example

Substitutions are made with the theorems


```

- val thm1 = SPECL [Term'm:num', Term'n:num'] arithmeticTheory.ADD_SYM
  val thm2 = CONJUNCT1 arithmeticTheory.ADD_CLAUSES;
> val thm1 = |- m + n = n + m : thm
  val thm2 = |- 0 + m = m : thm

```

depending on the occurrence of free subterms

```

- SUBS [thm1, thm2] (ASSUME (Term '(n + 0) + (0 + m) = m + n'));
> val it = [...] |- n + 0 + m = n + m : thm

- SUBS [thm1, thm2] (ASSUME (Term '!n. (n + 0) + (0 + m) = m + n'));
> val it = [...] |- !n. n + 0 + m = m + n : thm

```

Uses

SUBS can sometimes be used when rewriting (for example, with REWRITE_RULE) would diverge and term instantiation is not needed. Moreover, applying the substitution rules is often much faster than using the rewriting rules.

See also

Rewrite.ONCE_REWRITE_RULE, Rewrite.PURE_REWRITE_RULE, Rewrite.REWRITE_RULE, Thm.SUBST, Rewrite.SUBST_MATCH, Drule.SUBS_OCCS.

SUBS_OCCS

(Drule)

SUBS_OCCS : (int list * thm) list -> thm -> thm

Synopsis

Makes substitutions in a theorem at specific occurrences of a term, using a list of equational theorems.

Description

Given a list $(l_1, A_1 |- t_1 = v_1), \dots, (l_n, A_n |- t_n = v_n)$ and a theorem $(A |- t)$, SUBS_OCCS simultaneously replaces each t_i in t with v_i , at the occurrences specified by the integers in the list $l_i = [o_1, \dots, o_k]$ for each theorem $A_i |- t_i = v_i$.

$$\frac{(l_1, A_1 |- t_1 = v_1) \dots (l_n, A_n |- t_n = v_n) \quad A |- t}{A_1 \text{ u } \dots \text{ u } A_n \text{ u } A \quad |- \quad t[v_1, \dots, v_n / t_1, \dots, t_n]} \quad \text{SUBS_OCCS}[(l_1, A_1 |- t_1 = v_1), \dots, (l_n, A_n |- t_n = v_n)] \quad (A |- t)$$

Failure

`SUBS_OCCS [(l1,th1), ..., (ln,thn)] (A|-t)` fails if the conclusion of any theorem in the list is not an equation. No change is made to the theorem if the supplied occurrences `li` of the left-hand side of the conclusion of `thi` do not appear in `t`.

Example

The commutative law for addition

```
- val thm = SPECL [Term 'm:num', Term'n:num'] arithmeticTheory.ADD_SYM;
> val thm = |- m + n = n + m : thm
```

can be used for substituting only the second occurrence of the subterm `m + n`

```
- SUBS_OCCS [( [2], thm)]
              (ASSUME (Term '(n + m) + (m + n) = (m + n) + (m + n)'));
> val it = [.] |- n + m + (m + n) = n + m + (m + n) : thm
```

Uses

`SUBS_OCCS` is used when rewriting at specific occurrences of a term, and rules such as `REWRITE_RULE`, `PURE_REWRITE_RULE`, `ONCE_REWRITE_RULE`, and `SUBS` are too extensive or would diverge.

See also

`Rewrite.ONCE_REWRITE_RULE`, `Rewrite.PURE_REWRITE_RULE`, `Rewrite.REWRITE_RULE`, `Drule.SUBS`, `Thm.SUBST`, `Rewrite.SUBST_MATCH`.

subst	(Lib)
--------------	--------------

type ('a,'b) subst

Synopsis

Type abbreviation for substitutions.

Description

The type ('a,'b) `subst` abbreviates the type `{redex,residue} list`, in which `redex` has type 'a and `residue` has type 'b. Usually, a `{redex,residue}` pair in a substitution is interpreted as 'replace occurrences of `redex` by `residue`'.

Comments

The different types of `redex` and `residue` components allows flexibility, as in the rule of inference `SUBST`, which takes a `(term,thm) subst` argument.

See also

Lib.|->, Term.subst, Term.inst, Thm.SUBST.

<div data-bbox="162 492 312 537" data-label="Text">subst</div>	<div data-bbox="1155 488 1331 537" data-label="Text">(Term)</div>
---	--

```
subst : (term,term) subst -> term -> term
```

Synopsis

Substitutes terms in a term.

Description

Given a "(term,term) subst" (a list of {redex, residue} records) and a term `tm`, `subst` attempts to replace each free occurrence of a `redex` in `tm` by its associated `residue`. The substitution is done in parallel, i.e., once a `redex` has been replaced by its `residue`, at some place in the term, that `residue` at that place will not itself be replaced in the current call. When necessary, renaming of bound variables in `tm` is done to avoid capturing the free variables of an incoming `residue`.

Failure

Failure occurs if there exists a {`redex`, `residue`} record in the substitution such that the types of the `redex` and `residue` are not equal.

Example

```
- load "arithmeticTheory";

- subst [Term'SUC 0' |-> Term'1'
        (Term'SUC(SUC 0)');
> val it = 'SUC 1' : term

- subst [Term'SUC 0' |-> Term'1',
        Term'SUC 1' |-> Term'2']
        (Term'SUC(SUC 0)');
> val it = 'SUC 1' : term

- subst [Term'SUC 0' |-> Term'1',
        Term'SUC 1' |-> Term'2']
        (Term'SUC(SUC 0) = SUC 1');
> val it = 'SUC 1 = 2' : term
```

```

- subst [Term'b:num' |-> Term'a:num']
      (Term'\a:num. b:num');
> val it = '\a'. a' : term

- subst [Term'flip:'a' |-> Term'foo:'a']
      (Term'waddle:'a');
> val it = 'waddle' : term

```

See also

Term.inst, Thm.SUBST, Drule.SUBS, Lib.|->.

SUBST

(Thm)

SUBST : (term,thm) subst -> term -> thm -> thm

Synopsis

Makes a set of parallel substitutions in a theorem.

Description

Implements the following rule of simultaneous substitution

$$\begin{array}{c}
 A_1 \vdash t_1 = u_1, \dots, A_n \vdash t_n = u_n, \quad A \vdash t[t_1, \dots, t_n] \\
 \hline
 A \cup A_1 \cup \dots \cup A_n \vdash t[u_1, \dots, u_n]
 \end{array}$$

Evaluating

```

SUBST [x1 |-> (A1 |- t1=u1) , ..., xn |-> (An |- tn=un)]
      t[x1, ..., xn]
      (A |- t[t1, ..., tn])

```

returns the theorem $A_1 \cup \dots \cup A_n \vdash t[u_1, \dots, u_n]$. The term argument $t[x_1, \dots, x_n]$ is a template which should match the conclusion of the theorem being substituted into, with the variables x_1, \dots, x_n marking those places where occurrences of t_1, \dots, t_n are to be replaced by the terms u_1, \dots, u_n , respectively. The occurrence of t_i at the places marked by x_i must be free (i.e. t_i must not contain any bound variables). SUBST automatically renames bound variables to prevent free variables in u_i becoming bound after substitution.

Failure

If the template does not match the conclusion of the hypothesis, or the terms in the conclusion marked by the variables x_1, \dots, x_n in the template are not identical to the left hand sides of the supplied equations (i.e. the terms t_1, \dots, t_n).

Example

```
- val x = --'x:num'--
  and y = --'y:num'--
  and th0 = SPEC (--'0'-- arithmeticTheory.ADD1
  and th1 = SPEC (--'1'-- arithmeticTheory.ADD1;

(*   x = 'x'
   y = 'y'
  th0 = |- SUC 0 = 0 + 1
  th1 = |- SUC 1 = 1 + 1      *)

- SUBST [x |-> th0, y |-> th1]
  (--'(x+y) > SUC 0'--
  (ASSUME (--'(SUC 0 + SUC 1) > SUC 0'--));

> val it = [.] |- (0 + 1) + 1 + 1 > SUC 0 : thm

- SUBST [x |-> th0, y |-> th1]
  (--'(SUC 0 + y) > SUC 0'--
  (ASSUME (--'(SUC 0 + SUC 1) > SUC 0'--));

> val it = [.] |- SUC 0 + 1 + 1 > SUC 0 : thm

- SUBST [x |-> th0, y |-> th1]
  (--'(x+y) > x'--
  (ASSUME (--'(SUC 0 + SUC 1) > SUC 0'--));

> val it = [.] |- (0 + 1) + 1 + 1 > 0 + 1 : thm
```

Comments

SUBST is perhaps overly complex for a primitive rule of inference.

Uses

For substituting at selected occurrences. Often useful for writing special purpose derived inference rules.

See also

Drule.SUBS, Drule.SUBST_CONV, Lib.|->.

<div data-bbox="236 645 531 696" data-label="Text"> <p style="font-size: 1.2em; margin: 0;">SUBST1_TAC</p> </div>	<div data-bbox="1171 645 1410 696" data-label="Text"> <p style="font-size: 1.2em; margin: 0;">(Tactic)</p> </div>
---	---

SUBST1_TAC : thm_tactic

Synopsis

Makes a simple term substitution in a goal using a single equational theorem.

Description

Given a theorem $A' \mid -u=v$ and a goal (A, t) , the tactic `SUBST1_TAC (A' \mid -u=v)` rewrites the term t into $t[v/u]$, by substituting v for each free occurrence of u in t :

$$\begin{array}{l}
 A \text{ ?- } t \\
 \text{=====} \quad \text{SUBST1_TAC } (A' \mid -u=v) \\
 A \text{ ?- } t[v/u]
 \end{array}$$

The assumptions of the theorem used to substitute with are not added to the assumptions of the goal but are recorded in the proof. If A' is not a subset of the assumptions A of the goal (up to alpha-conversion), then `SUBST1_TAC (A' \mid -u=v)` results in an invalid tactic.

`SUBST1_TAC` automatically renames bound variables to prevent free variables in v becoming bound after substitution.

Failure

`SUBST1_TAC th (A, t)` fails if the conclusion of `th` is not an equation. No change is made to the goal if no free occurrence of the left-hand side of `th` appears in t .

Example

When trying to solve the goal

$$\text{?- } m * n = (n * (m - 1)) + n$$

substituting with the commutative law for multiplication

$$\text{SUBST1_TAC (SPECL [\"m:num\"; \"n:num\"] MULT_SYM)}$$

results in the goal

$$?- n * m = (n * (m - 1)) + n$$

Uses

SUBST1_TAC is used when rewriting with a single theorem using tactics such as REWRITE_TAC is too expensive or would diverge. Applying SUBST1_TAC is also much faster than using rewriting tactics.

See also

Rewrite.ONCE_REWRITE_TAC, Rewrite.PURE_REWRITE_TAC, Rewrite.REWRITE_TAC, Tactic.SUBST_ALL_TAC, Tactic.SUBST_TAC.

<div data-bbox="161 860 541 911" data-label="Text"> <p>SUBST_ALL_TAC</p> </div>	<div data-bbox="1096 860 1329 911" data-label="Text"> <p>(Tactic)</p> </div>
--	---

SUBST_ALL_TAC : thm_tactic

Synopsis

Substitutes using a single equation in both the assumptions and conclusion of a goal.

Description

SUBST_ALL_TAC breaches the style of natural deduction, where the assumptions are kept fixed. Given a theorem $A|-u=v$ and a goal $([t_1; \dots; t_n], t)$, SUBST_ALL_TAC $(A|-u=v)$ transforms the assumptions t_1, \dots, t_n and the term t into $t_1[v/u], \dots, t_n[v/u]$ and $t[v/u]$ respectively, by substituting v for each free occurrence of u in both the assumptions and the conclusion of the goal.

$$\begin{array}{l} \{t_1, \dots, t_n\} \text{ ?- } t \\ \hline \text{SUBST_ALL_TAC } (A|-u=v) \\ \{t_1[v/u], \dots, t_n[v/u]\} \text{ ?- } t[v/u] \end{array}$$

The assumptions of the theorem used to substitute with are not added to the assumptions of the goal, but they are recorded in the proof. If A is not a subset of the assumptions of the goal (up to alpha-conversion), then SUBST_ALL_TAC $(A|-u=v)$ results in an invalid tactic.

SUBST_ALL_TAC automatically renames bound variables to prevent free variables in v becoming bound after substitution.

Failure

SUBST_ALL_TAC $th (A, t)$ fails if the conclusion of th is not an equation. No change is made to the goal if no occurrence of the left-hand side of th appears free in (A, t) .

Example

Simplifying both the assumption and the term in the goal

$$\{0 + m = n\} \text{ ?- } 0 + (0 + m) = n$$

by substituting with the theorem $\text{|- } 0 + m = m$ for addition

```
SUBST_ALL_TAC (CONJUNCT1 ADD_CLAUSES)
```

results in the goal

$$\{m = n\} \text{ ?- } 0 + m = n$$
See also

Rewrite.ONCE_REWRITE_TAC, Rewrite.PURE_REWRITE_TAC, Rewrite.REWRITE_TAC, Tactic.SUBST1_TAC, Tactic.SUBST_TAC.

<div data-bbox="236 1099 558 1149" data-label="Text"> <p><code>subst_assoc</code></p> </div>	<div data-bbox="1260 1095 1410 1149" data-label="Text"> <p>(Lib)</p> </div>
--	---

```
subst_assoc : ('a -> bool) -> ('a,'b)subst -> 'b option
```

Synopsis

Treats a substitution as an association list.

Description

An application `subst_assoc P [{redex_1,residue_1},...,{redex_n,residue_n}]` returns `SOME residue_i` if `P` holds of `redex_i`, and did not hold (or fail) for `{redex_j | 1 <= j < i}`. If `P` holds for none of the `redexes` in the substitution, `NONE` is returned.

Failure

If `P redex_i` fails for some `redex` encountered in the left-to-right traversal of the substitution.

Example

```
- subst_assoc is_abs [T |-> F, Term '\x.x' |-> Term 'combin$I'];
> val it = SOME'I' : term option
```


See also

Lib.assoc, Lib.rev_assoc, Lib.assoc1, Lib.assoc2, Lib.|->.

<div data-bbox="161 497 453 546" data-label="Text">SUBST_CONV</div>	<div data-bbox="1125 497 1331 546" data-label="Text">(Drule)</div>
---	--

SUBST_CONV : {redex :term, residue :thm} list -> term -> conv

Synopsis

Makes substitutions in a term at selected occurrences of subterms, using a list of theorems.

Description

SUBST_CONV implements the following rule of simultaneous substitution

$$A1 \mid - t1 = v1 \dots An \mid - tn = vn$$

$$A1 \text{ u } \dots \text{ u } An \mid - t[t1, \dots, tn/x1, \dots, xn] = t[v1, \dots, vn/x1, \dots, xn]$$

The first argument to SUBST_CONV is a list [{redex=x1, residue = A1|-t1=v1}, ..., {redex = xn, residue = An|-tn=vn}]. The second argument is a template term t[x1, ..., xn], in which the variables x1, ..., xn are used to mark those places where occurrences of t1, ..., tn are to be replaced with the terms v1, ..., vn, respectively. Thus, evaluating

```
SUBST_CONV [{redex = x1, residue = A1|-t1=v1}, ...,
            {redex = xn, residue = An|-tn=vn}]
            t[x1, ..., xn]
            t[t1, ..., tn/x1, ..., xn]
```

returns the theorem

$$A1 \text{ u } \dots \text{ u } An \mid - t[t1, \dots, tn/x1, \dots, xn] = t[v1, \dots, vn/x1, \dots, xn]$$

The occurrence of ti at the places marked by the variable xi must be free (i.e. ti must not contain any bound variables). SUBST_CONV automatically renames bound variables to prevent free variables in vi becoming bound after substitution.

Failure

SUBST_CONV [{redex=x1, residue=th1}, ..., {redex=xn, residue=thn}] t[x1, ..., xn] t' fails if the conclusion of any theorem thi in the list is not an equation; or if the template t[x1, ..., xn] does not match the term t'; or if and term ti in t' marked by the variable

`xi` in the template, is not identical to the left-hand side of the conclusion of the theorem `thi`.

Example

The values

```
- val thm0 = SPEC (Term'0') ADD1
  and thm1 = SPEC (Term'1') ADD1
  and x = Term'x:num' and y = Term'y:num';

> val thm0 = |- SUC 0 = 0 + 1 : thm
  val thm1 = |- SUC 1 = 1 + 1 : thm
  val x = 'x' : term
  val y = 'y' : term
```

can be used to substitute selected occurrences of the terms `SUC 0` and `SUC 1`

```
- SUBST_CONV [{redex=x, residue=thm0},{redex=y,residue=thm1}]
  (Term'(x + y) > SUC 1')
  (Term'(SUC 0 + SUC 1) > SUC 1');
> val it = |- SUC 0 + SUC 1 > SUC 1 = (0 + 1) + 1 + 1 > SUC 1 : thm
```

The `|->` syntax can also be used:

```
- SUBST_CONV [x |-> thm0, y |-> thm1]
  (Term'(x + y) > SUC 1')
  (Term'(SUC 0 + SUC 1) > SUC 1');
```

Uses

`SUBST_CONV` is used when substituting at selected occurrences of terms and using rewriting rules/conversions is too extensive.

See also

`Conv.REWR_CONV`, `Drule.SUBS`, `Thm.SUBST`, `Drule.SUBS_OCCS`, `Lib.|->`.

SUBST_MATCH	(Rewrite)
--------------------	------------------

`SUBST_MATCH` : (thm -> thm -> thm)

Synopsis

Substitutes in one theorem using another, equational, theorem.

Description

Given the theorems $A \mid -u=v$ and $A' \mid -t$, `SUBST_MATCH (A|-u=v) (A'|-t)` searches for one free instance of u in t , according to a top-down left-to-right search strategy, and then substitutes the corresponding instance of v .

$$\begin{array}{l} A \mid -u=v \quad A' \mid -t \\ \hline \text{SUBST_MATCH } (A|-u=v) (A'|-t) \\ A \text{ u } A' \mid -t[v/u] \end{array}$$

`SUBST_MATCH` allows only a free instance of u to be substituted for in t . An instance which contain bound variables can be substituted for by using rewriting rules such as `REWRITE_RULE`, `PURE_REWRITE_RULE` and `ONCE_REWRITE_RULE`.

Failure

`SUBST_MATCH th1 th2` fails if the conclusion of the theorem `th1` is not an equation. Moreover, `SUBST_MATCH (A|-u=v) (A'|-t)` fails if no instance of u occurs in t , since the matching algorithm fails. No change is made to the theorem $(A' \mid -t)$ if instances of u occur in t , but they are not free (see `SUBS`).

Example

The commutative law for addition

```
- val thm1 = SPECL [Term 'm:num', Term 'n:num'] arithmeticTheory.ADD_SYM;
> val thm1 = |- m + n = n + m : thm
```

is used to apply substitutions, depending on the occurrence of free instances

```
- SUBST_MATCH thm1 (ASSUME (Term '(n + 1) + (m - 1) = m + n'));
> val it = [...] |- m - 1 + (n + 1) = m + n : thm

- SUBST_MATCH thm1 (ASSUME (Term '!n. (n + 1) + (m - 1) = m + n'));
> val it = [...] |- !n. n + 1 + (m - 1) = m + n : thm
```

Uses

`SUBST_MATCH` is used when rewriting with the rules such as `REWRITE_RULE`, using a single theorem is too extensive or would diverge. Moreover, applying `SUBST_MATCH` can be much faster than using the rewriting rules.

See also

`Rewrite.ONCE_REWRITE_RULE`, `Rewrite.PURE_REWRITE_RULE`, `Rewrite.REWRITE_RULE`, `Drule.SUBS`, `Thm.SUBST`.

subst_occs**(HolKernel)**

```
subst_occs : int list list -> term subst -> term -> term
```

Synopsis

Substitutes for particular occurrences of subterms of a given term.

Description

For each $\{\text{redex}, \text{residue}\}$ in the second argument, there should be a corresponding integer list l_i in the first argument that specifies which free occurrences of redex_i in the third argument should be substituted by residue_i .

Failure

Failure occurs if any substitution fails, or if the length of the first argument is not equal to the length of the substitution. In other words, every substitution pair should be accompanied by a list specifying when the substitution is applicable.

Example

```
- subst_occs [[1,3]] [Term 'SUC 0' |-> Term '1']
                    (Term 'SUC 0 + SUC 0 = SUC(SUC 0)');
> val it = '1 + SUC 0 = SUC 1' : term

- subst_occs [[1],[1]] [Term 'SUC 0' |-> Term '1',
                        Term 'SUC 1' |-> Term '2']
                        (Term 'SUC(SUC 0) = SUC 1');
> val it = 'SUC 1 = 2' : term

- subst_occs [[1],[1]] [Term 'SUC(SUC 0)' |-> Term '2',
                        Term 'SUC 0'      |-> Term '1']
                        (Term 'SUC(SUC 0) = SUC 0');
> val it = '2 = 1' : term
```

See also

Term.subst, Lib.|->.

SUBST_OCCS_TAC**(Tactic)**

```
SUBST_OCCS_TAC : (int list * thm) list -> tactic
```

Synopsis

Makes substitutions in a goal at specific occurrences of a term, using a list of theorems.

Description

Given a list $(l_1, A_1 | -t_1 = u_1), \dots, (l_n, A_n | -t_n = u_n)$ and a goal (A, t) , SUBST_OCCS_TAC replaces each t_i in t with u_i , simultaneously, at the occurrences specified by the integers in the list $l_i = [o_1, \dots, o_k]$ for each theorem $A_i | -t_i = u_i$.

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \text{ SUBST_OCCS_TAC } [(l_1, A_1 | -t_1 = u_1), \dots, \\ A \text{ ?- } t[u_1, \dots, u_n/t_1, \dots, t_n] \qquad (l_n, A_n | -t_n = u_n)] \end{array}$$

The assumptions of the theorems used to substitute with are not added to the assumptions A of the goal, but they are recorded in the proof. If any A_i is not a subset of A (up to alpha-conversion), SUBST_OCCS_TAC $[(l_1, A_1 | -t_1 = u_1), \dots, (l_n, A_n | -t_n = u_n)]$ results in an invalid tactic.

SUBST_OCCS_TAC automatically renames bound variables to prevent free variables in u_i becoming bound after substitution.

Failure

SUBST_OCCS_TAC $[(l_1, th_1), \dots, (l_n, th_n)] (A, t)$ fails if the conclusion of any theorem in the list is not an equation. No change is made to the goal if the supplied occurrences l_i of the left-hand side of the conclusion of th_i do not appear in t .

Example

When trying to solve the goal

$$\text{?- } (m + n) + (n + m) = (m + n) + (m + n)$$

applying the commutative law for addition on the third occurrence of the subterm $m + n$

$$\text{SUBST_OCCS_TAC } [([3], \text{SPECL } [\text{Term 'm:num', Term 'n:num'}] \\ \text{arithmeticTheory.ADD_SYM})]$$

results in the goal

$$\text{?- } (m + n) + (n + m) = (m + n) + (n + m)$$

Uses

SUBST_OCCS_TAC is used when rewriting a goal at specific occurrences of a term, and when rewriting tactics such as REWRITE_TAC, PURE_REWRITE_TAC, ONCE_REWRITE_TAC, SUBST_TAC, etc. are too extensive or would diverge.

See also

Rewrite.ONCE_REWRITE_TAC, Rewrite.PURE_REWRITE_TAC, Rewrite.REWRITE_TAC,
Tactic.SUBST1_TAC, Tactic.SUBST_TAC.

SUBST_TAC	(Tactic)
-----------	----------

SUBST_TAC : (thm list -> tactic)

Synopsis

Makes term substitutions in a goal using a list of theorems.

Description

Given a list of theorems $A_1|-u_1=v_1, \dots, A_n|-u_n=v_n$ and a goal (A, t) , SUBST_TAC rewrites the term t into the term $t[v_1, \dots, v_n/u_1, \dots, u_n]$ by simultaneously substituting v_i for each occurrence of u_i in t with v_i :

$$\frac{A \text{ ?- } t}{\text{===== SUBST_TAC } [A_1|-u_1=v_1, \dots, A_n|-u_n=v_n]} A \text{ ?- } t[v_1, \dots, v_n/u_1, \dots, u_n]$$

The assumptions of the theorems used to substitute with are not added to the assumptions A of the goal, while they are recorded in the proof. If any A_i is not a subset of A (up to alpha-conversion), then SUBST_TAC $[A_1|-u_1=v_1, \dots, A_n|-u_n=v_n]$ results in an invalid tactic.

SUBST_TAC automatically renames bound variables to prevent free variables in v_i becoming bound after substitution.

Failure

SUBST_TAC $[th_1, \dots, th_n]$ (A, t) fails if the conclusion of any theorem in the list is not an equation. No change is made to the goal if no occurrence of the left-hand side of the conclusion of th_i appears in t .

Example

When trying to solve the goal

$$\text{?- } (n + 0) + (0 + m) = m + n$$

by substituting with the theorems

```

- val thm1 = SPEC_ALL arithmeticTheory.ADD_SYM
  val thm2 = CONJUNCT1 arithmeticTheory.ADD_CLAUSES;
thm1 = |- m + n = n + m
thm2 = |- 0 + m = m

```

applying SUBST_TAC [thm1, thm2] results in the goal

```
?- (n + 0) + m = n + m
```

Uses

SUBST_TAC is used when rewriting (for example, with REWRITE_TAC) is extensive or would diverge. Substituting is also much faster than rewriting.

See also

Rewrite.ONCE_REWRITE_TAC, Rewrite.PURE_REWRITE_TAC, Rewrite.REWRITE_TAC, Tactic.SUBST1_TAC, Tactic.SUBST_ALL_TAC.

<div data-bbox="161 1003 397 1050" data-label="Text"> <p>subtract</p> </div>	<div data-bbox="1182 999 1331 1052" data-label="Text"> <p>(Lib)</p> </div>
--	--

subtract : 'a list -> 'a list -> 'a list

Synopsis

Computes the set-theoretic difference of two 'sets'.

Description

Behaves exactly like `set_diff`.

See also

`Lib.set_diff`.

<div data-bbox="161 1603 399 1655" data-label="Text"> <p>SUC_CONV</p> </div>	<div data-bbox="1011 1601 1331 1655" data-label="Text"> <p>(reduceLib)</p> </div>
--	---

SUC_CONV : conv

Synopsis

Calculates by inference the successor of a numeral.

Description

If `n` is a numeral (e.g. 0, 1, 2, 3,...), then `SUC_CONV "SUC n"` returns the theorem:

```
|- SUC n = s
```

where s is the numeral that denotes the successor of the natural number denoted by n .

Failure

SUC_CONV tm fails unless tm is of the form "SUC n ", where n is a numeral.

Example

```
#SUC_CONV "SUC 33";;
|- SUC 33 = 34
```

SUC_TO_NUMERAL_DEFN_CONV (numLib)

```
SUC_TO_NUMERAL_DEFN_CONV : conv
```

Synopsis

Translates equations using SUC n to use numeral constructors instead.

Description

This conversion modifies conjunctions of universally quantified equations so that any argument terms of the form SUC x on the LHS of the equations (with x one of the equation's universally quantified variables), are translated to a form appropriate for rewriting when the argument term is a numeral.

This procedure uses the following theorem:

```
|- !f g. (!n. f (SUC n) = g n (SUC n)) =
  (!n. f (NUMERAL (NUMERAL_BIT1 n)) =
    g (NUMERAL (NUMERAL_BIT1 n))
      (NUMERAL (NUMERAL_BIT1 n) - 1)) /\
  (!n. f (NUMERAL (NUMERAL_BIT2 n)) =
    g (NUMERAL (NUMERAL_BIT2 n))
      (NUMERAL (NUMERAL_BIT1 n)))
```

Example


```

- CONV_RULE SUC_TO_NUMERAL_DEFN_CONV arithmeticTheory.FACT;
> val it =
  |- (FACT 0 = 1) /\
    (!n.
      FACT (NUMERAL (NUMERAL_BIT1 n)) =
        NUMERAL (NUMERAL_BIT1 n) *
        FACT (NUMERAL (NUMERAL_BIT1 n) - 1)) /\
    !n.
      FACT (NUMERAL (NUMERAL_BIT2 n)) =
        NUMERAL (NUMERAL_BIT2 n) *
        FACT (NUMERAL (NUMERAL_BIT1 n)) : thm

```

Failure

Fails if the input term is not the conjunction of universally quantified equations, where there may be just one conjunct, and where equations may have no quantification at all. Those conjuncts which don't involve terms of the form `SUC x` are returned unchanged.

Comments

Useful for translating definitions over numbers (which often involve `SUC` terms), into a form that can be used to work with numerals easily.

See also

`numLib.num_CONV`.

<div data-bbox="161 1352 397 1406" data-label="Text"> <p>SUM_CONV</p> </div>	<div data-bbox="1067 1352 1331 1406" data-label="Text"> <p>(listLib)</p> </div>
---	--

`SUM_CONV` : conv

Synopsis

Computes by inference the result of summing the elements of a list.

Description

For any object language list of the form `--'[x1;x2;...;xn]'`, where `x1`, `x2`, ..., `xn` are numeral constants, the result of evaluating

```
SUM_CONV (--'SUM [x1;x2;...;xn]')
```

is the theorem

```
|- SUM [x1;x2;...;xn] = n
```

where n is the numeral constant that denotes the sum of the elements of the list.

Example

Evaluating `SUM_CONV (--'SUM [0;1;2;3] '--)` will return the following theorem:

$$\vdash \text{SUM } [0;1;2;3] = 6$$

Failure

`SUM_CONV tm` fails if `tm` is not of the form described above.

See also

`listLib.FOLDL_CONV`, `listLib.FOLDR_CONV`, `listLib.list_FOLD_CONV`.

<code>swap</code>	<code>(Lib)</code>
-------------------	--------------------

`swap : 'a * 'b -> 'b * 'a`

Synopsis

Swaps the two components of a pair.

Description

`swap (x,y)` returns `(y,x)`.

Failure

Never fails.

See also

`Lib.fst`, `Lib.snd`, `Lib.pair`, `Lib.rpair`.

<code>SWAP_EXISTS_CONV</code>	<code>(Conv)</code>
-------------------------------	---------------------

`SWAP_EXISTS_CONV : conv`

Synopsis

Interchanges the order of two existentially quantified variables.

Description

When applied to a term argument of the form $?x y. P$, the conversion `SWAP_EXISTS_CONV` returns the theorem:

$$\vdash (\exists x y. P) = (\exists y x. P)$$

Failure

SWAP_PEXISTS_CONV fails if applied to a term that is not of the form $\exists x y. P$.

SWAP_PEXISTS_CONV	(PairRules)
-------------------	-------------

SWAP_PEXISTS_CONV : conv

Synopsis

Interchanges the order of two existentially quantified pairs.

Description

When applied to a term argument of the form $\exists p q. t$, the conversion SWAP_PEXISTS_CONV returns the theorem:

$$\vdash (\exists p q. t) = (\exists q t. t)$$

Failure

SWAP_PEXISTS_CONV fails if applied to a term that is not of the form $\exists p q. t$.

See also

Conv.SWAP_EXISTS_CONV, PairRules.SWAP_PFORALL_CONV.

SWAP_PFORALL_CONV	(PairRules)
-------------------	-------------

SWAP_PFORALL_CONV : conv

Synopsis

Interchanges the order of two universally quantified pairs.

Description

When applied to a term argument of the form $\forall p q. t$, the conversion SWAP_PFORALL_CONV returns the theorem:

$$\vdash (\forall p q. t) = (\forall q p. t)$$

Failure

SWAP_PFORALL_CONV fails if applied to a term that is not of the form $!p \ q. \ t$.

See also

PairRules.SWAP_PEXISTS_CONV.

SYM	(Thm)
-----	-------

SYM : thm -> thm

Synopsis

Swaps left-hand and right-hand sides of an equation.

Description

When applied to a theorem $A \ |- \ t1 = t2$, the inference rule SYM returns $A \ |- \ t2 = t1$.

$$\frac{A \ |- \ t1 = t2}{A \ |- \ t2 = t1} \quad \text{SYM}$$

Failure

Fails unless the theorem is equational.

See also

Conv.GSYM, Drule.NOT_EQ_SYM, Thm.REFL.

SYM_CONV	(Conv)
----------	--------

SYM_CONV : conv

Synopsis

Interchanges the left and right-hand sides of an equation.

Description

When applied to an equational term $t1 = t2$, the conversion SYM_CONV returns the theorem:

$$\vdash (t1 = t2) = (t2 = t1)$$

Failure

Fails if applied to a term that is not an equation.

See also

Thm.SYM.

T

(boolSyntax)

T : term

Synopsis

Constant denoting truth.

Description

The ML variable `boolSyntax.T` is bound to the term `bool$T`.

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`, `boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.negation`, `boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let_tm`, `boolSyntax.arb`.

TAC_PROOF

(Tactical)

TAC_PROOF : goal * tactic -> thm

Synopsis

Attempts to prove a goal using a given tactic.

Description

When applied to a goal-tactic pair $(A \text{ ?- } t, \text{tac})$, the `TAC_PROOF` function attempts to prove the goal $A \text{ ?- } t$, using the tactic `tac`. If it succeeds, it returns the theorem $A' \vdash t$ corresponding to the goal, where the assumption list A' may be a proper superset of A unless the tactic is valid; there is no inbuilt validity checking.

Failure

Fails unless the goal has hypotheses and conclusions all of type `bool`, and the tactic can solve the goal.

See also

`BasicProvers.PROVE`, `Tactical.VALID`.

<code>tag</code>	<code>(Tag)</code>
------------------	--------------------

```
type tag
```

Synopsis

Abstract type of oracle tags.

Description

The type `tag` is used to track the use of oracles in HOL. An ‘oracle’ is a source of theorems that are not proved, but just asserted. In HOL, such unproven ‘theorems’ are used to incorporate the results of external proof tools. Each theorem coming from an oracle has a tag attached to it. This tag gets copied to any theorems hereditarily generated from an oracular theorem by inference.

See also

`Tag.read`, `Thm.mk_oracle_thm`.

<code>tag</code>	<code>(Thm)</code>
------------------	--------------------

```
tag : thm -> tag
```

Synopsis

Extract the tag from a theorem.

Description

An invocation `tag th`, where `th` has type `thm`, returns the tag of the theorem. If derivation of the theorem has appealed at some point to an oracle, the tag of that oracle will be embedded in the result. Otherwise, an empty tag is returned.

Failure

Never fails.

Example

```
- Thm.tag (mk_thm([],F));
> val it = Kerneltypes.TAG(["MK_THM"], []) : tag

- Thm.tag NOT_FORALL_THM;
> val it = Kerneltypes.TAG([], []) : tag
```

See also

Thm.mk_oracle_thm, Tag.read, Tag.merge, Tag.pp_tag.

<div data-bbox="161 945 426 996" data-label="Text"> <p>TAUT_CONV</p> </div>	<div data-bbox="1067 945 1331 996" data-label="Text"> <p>(tautLib)</p> </div>
---	---

TAUT_CONV : conv

Synopsis

Tautology checker. Proves instances of propositional formulae.

Description

Given an instance t of a valid propositional formula, TAUT_CONV proves the theorem $\vdash t = T$. A propositional formula is a term containing only Boolean constants, Boolean-valued variables, Boolean equalities, implications, conjunctions, disjunctions, negations and Boolean-valued conditionals. An instance of a formula is the formula with one or more of the variables replaced by terms of the same type. The conversion accepts terms with or without universal quantifiers for the variables.

Failure

Fails if the term is not an instance of a propositional formula or if the instance is not a valid formula.

Example

```
#TAUT_CONV
# ‘‘!x n y. (((n = 1) \/\ ~x) ==> y) /\ (y ==> ~(n < 0)) /\ (n < 0) ==> x’’;
|- (!x n y. ((n = 1) \/\ ~x ==> y) /\ (y ==> ~n < 0) /\ n < 0 ==> x) = T
```

```
#TAUT_CONV ‘‘(((n = 1) \\/ ~x) ==> y) /\ (y ==> ~(n < 0)) /\ (n < 0) ==> x‘‘;
|- ((n = 1) \\/ ~x ==> y) /\ (y ==> ~n < 0) /\ n < 0 ==> x = T
```

```
#TAUT_CONV ‘‘!n. (n < 0) \\/ (n = 0)‘‘;
```

Uncaught exception:

```
HOL_ERR
```

See also

tautLib.TAUT_PROVE, tautLib.TAUT_TAC, tautLib.PTAUT_CONV.

<div data-bbox="236 808 531 860" data-label="Text"> <p>TAUT_PROVE</p> </div>	<div data-bbox="1144 808 1410 860" data-label="Text"> <p>(tautLib)</p> </div>
---	---

```
TAUT_PROVE : term -> thm
```

Synopsis

Tautology checker. Proves propositional formulae (and instances of them).

Description

Given an instance of a valid propositional formula, TAUT_PROVE returns the instance of the formula as a theorem. A propositional formula is a term containing only Boolean constants, Boolean-valued variables, Boolean equalities, implications, conjunctions, disjunctions, negations and Boolean-valued conditionals. An instance of a formula is the formula with one or more of the variables replaced by terms of the same type. The conversion accepts terms with or without universal quantifiers for the variables.

Failure

Fails if the term is not an instance of a propositional formula or if the instance is not a valid formula.

Example

```
#TAUT_PROVE
```

```
# ‘‘!x n y. (((n = 1) \\/ ~x) ==> y) /\ (y ==> ~(n < 0)) /\ (n < 0) ==> x‘‘;
|- !x n y. ((n = 1) \\/ ~x ==> y) /\ (y ==> ~n < 0) /\ n < 0 ==> x
```

```
#TAUT_PROVE ‘‘(((n = 1) \\/ ~x) ==> y) /\ (y ==> ~(n < 0)) /\ (n < 0) ==> x‘‘;
|- ((n = 1) \\/ ~x ==> y) /\ (y ==> ~n < 0) /\ n < 0 ==> x
```



```
#TAUT_PROVE ‘‘!n. (n < 0) \ / (n = 0)‘‘;  
Uncaught exception:  
HOL_ERR
```

See also

`tautLib.TAUT_CONV`, `tautLib.TAUT_TAC`, `tautLib.PTAUT_PROVE`.

TAUT_TAC

(tautLib)

`TAUT_TAC` : tactic

Synopsis

Tautology checker. Proves propositional goals (and instances of them).

Description

Given a goal that is an instance of a propositional formula, this tactic will prove the goal provided it is valid. A propositional formula is a term containing only Boolean constants, Boolean-valued variables, Boolean equalities, implications, conjunctions, disjunctions, negations and Boolean-valued conditionals. An instance of a formula is the formula with one or more of the variables replaced by terms of the same type. The tactic accepts goals with or without universal quantifiers for the variables.

Failure

Fails if the conclusion of the goal is not an instance of a propositional formula or if the instance is not a valid formula.

See also

`tautLib.TAUT_CONV`, `tautLib.TAUT_PROVE`, `tautLib.PTAUT_TAC`.

tDefine

(bossLib)

`tDefine` : string -> term quotation -> tactic -> thm

Synopsis

General-purpose function definition facility.

Description

`tDefine` is a definition package similar to `Define` except that it has a tactic parameter which is used to perform the termination proof for the specified function. `tDefine` accepts the same syntax used by `Define` for specifying functions.

If the specification is a simple abbreviation, or is primitive recursive (i.e., it exactly follows the recursion pattern of a previously declared HOL datatype) then the invocation of `tDefine` succeeds and stores the derived equations in the current theory segment. Otherwise, the function is not an instance of primitive recursion, and the termination prover may succeed or fail.

When processing the specification of a recursive function, `tDefine` must perform a termination proof. It automatically constructs termination conditions for the function, and invokes the supplied tactic in an attempt to prove the termination conditions. If that attempt fails, then `tDefine` fails.

If it succeeds, then `tDefine` stores the specified equations in the current theory segment, using the string argument as a stem for the name. An induction theorem customized for the defined function is also stored in the current segment. Note, however, that an induction theorem is not stored for primitive recursive functions, since that theorem would be identical to the induction theorem resulting from the declaration of the datatype.

If the tactic application fails, then `tDefine` fails.

Failure

`tDefine` fails if its input fails to parse and typecheck.

`tDefine` fails if it cannot prove the termination of the specified recursive function. In that case, one has to embark on the following multi-step process: (1) construct the function and synthesize its termination conditions with `Hol_defn`; (2) set up a goal to prove the termination conditions with `tgoal`; (3) interactively prove the termination conditions, usually by starting with an invocation of `WF_REL_TAC`; and (4) package everything up with an invocation of `tDefine`.

Example

The following attempt to invoke `Define` fails because the current default termination prover for `Define` is too weak:

```
Hol_datatype 'foo = c1 | c2 | c3';

Define '(f c1 x = x) /\
      (f c2 x = x + 3) /\
      (f c3 x = f c2 (x + 6))';
```

The following invocation of `tDefine` uses the supplied tactic to prove termination.

```

tDefine "f"
  '(f c1 x = x) /\
   (f c2 x = x + 3) /\
   (f c3 x = f c2 (x + 6))'
(WF_REL_TAC 'measure (\p. case FST p of c3 -> 1 || _ -> 0)');

Equations stored under "f_def".
Induction stored under "f_ind".
> val it = |- (f c1 x = x) /\ (f c2 x = x + 3) /\ (f c3 x = f c2 (x + 6)) : thm

```

Comments

tDefine automatically adds the definition it makes into the hidden ‘compset’ accessed by EVAL and EVAL_TAC.

See also

bossLib.Define, bossLib.xDefine, TotalDefn.DefineSchema, bossLib.Hol_defn, Defn.tgoal, Defn.tprove, bossLib.WF_REL_TAC, bossLib.recInduct, bossLib.EVAL, bossLib.EVAL_TAC.

temp_set_grammars	(Parse)
-------------------	---------

```
temp_set_grammars : type_grammar.grammar * term_grammar.grammar -> unit
```

Synopsis

Sets the global type and term grammars.

Description

HOL uses two global grammars to control the parsing and printing of term and type values. These can be adjusted in a controlled way with functions such as `add_rule` and `overload_on`. By using just these standard functions, the system is able to export theories in such a way that changes to grammars persist from session to session.

Nonetheless it is occasionally useful to set grammar values directly. This change can't be made to persist, but will affect the current session.

Failure

Never fails.

See also

Parse.add_rule, Parse.overload_on, Parse.parse_from_grammars, Parse.print_from_grammars, Parse.Term.

Term

(Parse)

```
Parse.Term : term quotation -> term
```

Synopsis

Parses a quotation into a term value.

Description

The parsing process for terms divides into four distinct phases.

The first phase converts the quotation argument into abstract syntax, a relatively simple parse tree datatype, with the following datatype definition (from `Absyn`):

```
datatype vstruct
  = VAQ    of term
  | VIDENT of string
  | VPAIR  of vstruct * vstruct
  | VTYPED of vstruct * pretype
datatype absyn
  = AQ    of term
  | IDENT of string
  | APP   of absyn * absyn
  | LAM   of vstruct * absyn
  | TYPED of absyn * pretype
```

This phase of parsing is concerned with the treatment of the rawest concrete syntax. It has no notion of whether or not a term corresponds to a constant or a variable, so all preterm leaves are ultimately either IDENTs or AQs (anti-quotations).

This first phase converts infixes, mixfixes and all the other categories of syntactic rule from the global grammar into simple structures built up using APP. For example, ‘x op y’ (where op is an infix) will turn into

```
APP(APP(IDENT "op", IDENT "x"), IDENT "y")
```

and ‘tok1 x tok2 y’ (where tok1 _ tok2 has been declared as a `TruePrefix` form for the term f) will turn into

```
APP(APP(IDENT "f", IDENT "x"), IDENT "y")
```

The special syntaxes for “let” and record expressions are also handled at this stage. For more details on how this is done see the reference entry for `Absyn`, which function can be used in isolation to see what is done at this phase.

The second phase of parsing consists of the resolution of names, identifying what were just `VARS` as constants or genuine variables (whether free or bound). This phase also annotates all leaves of the data structure (given in the entry for `Preterm`) with type information.

The third phase of parsing works over the `Preterm` datatype and does type-checking, though ignoring overloaded values. The datatype being operated over uses reference variables to allow for efficiency, and the type-checking is done “in place”. If type-checking is successful, the resulting value has consistent type annotations.

The final phase of parsing resolves overloaded constants. The type-checking done to this point may completely determine which choice of overloaded constant is appropriate, but if not, the choice may still be completely determined by the interaction of the possible types for the overloaded possibilities.

Finally, depending on the value of the global flags `guessing_tyvars` and `guessing_overloads`, the parser will make choices about how to resolve any remaining ambiguities.

The parsing process is entirely driven by the global grammar. This value can be inspected with the `term_grammar` function.

Failure

All over place, and for all sorts of reasons.

Uses

Turns strings into terms.

See also

`Parse.Absyn`, `Parse.overload_on`, `Parse.term_grammar`.

<code>term</code>	<code>(Term)</code>
-------------------	---------------------

`eqtype term`

Synopsis

ML datatype of HOL terms.

Description

The ML abstract type `term` represents the set of HOL terms, which is essentially the simply typed lambda calculus of Church. A term may be a variable, a constant, an application of one term to another, or a lambda abstraction.

Comments

Since `term` is an ML eqtype, any two terms `tm1` and `tm2` can be tested for equality by `tm1 = tm2`. However, the fundamental notion of equality for terms is implemented by `aconv`.

Since `term` is an abstract type, access to its representation is mediated by the interface presented by the `Term` structure.

See also

`Type.hol.type`.

<code>term_grammar</code>	<code>(Parse)</code>
---------------------------	----------------------

`Parse.term_grammar : unit -> term_grammar.grammar`

Synopsis

Returns the current global term grammar.

Failure

Never fails.

Comments

There is a pretty-printer installed in the interactive system so that term grammar values are presented nicely. The global term grammar is passed as a parameter to the `Term` parsing function in the `Parse` structure, and also drives the installed term and theorem pretty-printers.

See also

`Parse.parse_from_grammars`, `Parse.print_from_grammars`, `Parse.temp_set_grammars`, `Parse.Term`.

<code>term_to_string</code>	<code>(Parse)</code>
-----------------------------	----------------------

`Parse.term_to_string : term -> string`

Synopsis

Converts a term to a string.

Description

Uses the global term grammar and pretty-printing flags to turn a term into a string. It assumes that the string should be broken up as if for display on a screen that is as wide as the value stored in the `Globals.linewidth` variable.

Failure

Should never fail.

See also

`Parse.print_term`.

```
term_without_overloads_on_to_backend_string
(Parse)
```

```
Parse.term_without_overloads_on_to_backend_string : string list -> term -> string
```

Synopsis

Returns a string, suitable for the current backend, that represents a term without using overload mappings of certain tokens.

Description

The call `term_without_overloads_on_to_backend_string ls t` returns a current-backend suitable string representation of `t` without using any overloads on tokens in `ls`.

If the current backend is a color-capable terminal, for example, the string will include escape codes for coloring free and bound variables.

Failure

Should never fail.

See also

`Parse.term_without_overloads_on_to_string`,
`Parse.term_without_overloads_to_backend_string`,
`Parse.pp_term_without_overloads_on`, `Parse.clear_overloads_on`,
`Parse.term_to_backend_string`.

```
term_without_overloads_on_to_string
(Parse)
```

```
Parse.term_without_overloads_on_to_string : string list -> term -> string
```

Synopsis

Returns a string representing a term, without using overload mappings of certain tokens.

Description

The call `term_without_overloads_on_to_string ls t` returns a string representation of `t` without using any overloads on tokens in `ls`.

Example

```
> term_without_overloads_on_to_string ["+"] 'x + y';
val it = "arithmetic$+ x y": string
```

Failure

Should never fail.

See also

`Parse.term_without_overloads_on_to_backend_string`,
`Parse.term_without_overloads_to_string`, `Parse.pp_term_without_overloads_on`,
`Parse.clear_overloads_on`, `Parse.term_to_string`.

<code>tex_theory</code>	<code>(EmitTeX)</code>
-------------------------	------------------------

```
tex_theory : string -> unit
```

Synopsis

Emits theory as LaTeX commands and creates a document template.

Description

An invocation of `tex_theory thy` will export the named theory `thy` as a collection of LaTeX commands and it will also generate a document "thy.tex" that presents the theory. The string "-" may be used to denote the current theory segment. The theory is exported with `print_theory_as_tex`.

Failure

Will fail if there is a system error when trying to write the files. It will not overwrite the file `name`, however, "HOLname.tex" may be overwritten.

Example

The invocation


```
- EmitTeX.tex_theory "list";
> val it = () : unit
```

will generate two files "HOLLlist.tex" and "list.tex".

See also

EmitTeX.print_term_as_tex, EmitTeX.print_type_as_tex,
EmitTeX.print_theorem_as_tex, EmitTeX.print_theory_as_tex,
EmitTeX.print_theories_as_tex.doc.

<div data-bbox="161 721 311 779" data-label="Text"> <p>tgoal</p> </div>	<div data-bbox="1155 719 1331 772" data-label="Text"> <p>(Defn)</p> </div>
---	--

tgoal : defn -> proofs

Synopsis

Set up a termination proof

Description

tgoal defn sets up a termination proof for the function represented by defn. It creates a new goalstack and makes it the focus of subsequent goalstack operations.

Failure

tgoal defn fails if defn represents a non-recursive or primitive recursive function.

Example

```
- val qsort_defn =
  Hol_defn "qsort"
  '(qsort ___ [] = []) /\
  (qsort ord (x::rst) =
    APPEND (qsort ord (FILTER ($~ o ord x) rst))
    (x :: qsort ord (FILTER (ord x) rst)))';

- tgoal qsort_defn;
> val it =
  Proof manager status: 1 proof.
  1. Incomplete:
    Initial goal:
    ?R. WF R /\
      (!rst x ord. R (ord,FILTER ($~ o ord x) rst) (ord,x::rst)) /\
      !rst x ord. R (ord,FILTER (ord x) rst) (ord,x::rst)
```

See also

TotalDefn.WF_REL_TAC, Defn.tprove, Defn.Hol_defn.

THEN	(Tactical)
-------------	-------------------

```
op THEN : tactic * tactic -> tactic
```

Synopsis

Applies two tactics in sequence.

Description

If T1 and T2 are tactics, T1 THEN T2 is a tactic which applies T1 to a goal, then applies the tactic T2 to all the subgoals generated. If T1 solves the goal then T2 is never applied.

Failure

The application of THEN to a pair of tactics never fails. The resulting tactic fails if T1 fails when applied to the goal, or if T2 does when applied to any of the resulting subgoals.

Comments

Although normally used to sequence tactics which generate a single subgoal, it is worth remembering that it is sometimes useful to apply the same tactic to multiple subgoals; sequences like the following:

```
EQ_TAC THENL [ASM_REWRITE_TAC[], ASM_REWRITE_TAC[]]
```

can be replaced by the briefer:

```
EQ_TAC THEN ASM_REWRITE_TAC[]
```

See also

Tactical.EVERY, Tactical.ORELSE, Tactical.THENL.

THEN1	(Tactical)
--------------	-------------------

```
op THEN1 : tactic * tactic -> tactic
```

Synopsis

A tactical like THEN that applies the second tactic only to the first subgoal.

Description

If T1 and T2 are tactics, T1 THEN1 T2 is a tactic which applies T1 to a goal, then applies the tactic T2 to the first subgoal generated. T1 must produce at least one subgoal, and T2 must completely solve the first subgoal of T1.

Failure

The application of THEN1 to a pair of tactics never fails. The resulting tactic fails if T1 fails when applied to the goal, if T1 does not produce at least one subgoal (i.e., T1 completely solves the goal), or if T2 does not completely solve the first subgoal generated by T1.

Comments

THEN1 can be applied to make the proof more linear, avoiding unnecessary THENLs. It is especially useful when used with REVERSE.

Example

For example, given the goal

```
simple_goal /\ complicated_goal
```

the tactic

```
(CONJ_TAC THEN1 TO)
THEN T1
THEN T2
THEN ...
THEN Tn
```

avoids the extra indentation of

```
CONJ_TAC THENL
[TO,
 T1
 THEN T2
 THEN ...
 THEN Tn]
```

See also

Tactical.EVERY, Tactical.ORELSE, Tactical.REVERSE, Tactical.THEN, Tactical.THENL.

THEN_CONSEQ_CONV	(ConseqConv)
------------------	--------------

```
THEN_CONSEQ_CONV : (conseq_conv -> conseq_conv -> conseq_conv)
```

Synopsis

Applies two consequence conversions in sequence.

Description

THEN_CONSEQ_CONV *cc1 cc2* corresponds to *c1 THENC c2* for classical conversions. Thus, if *cc1* returns $\vdash t' \implies t$ when applied to *t*, and *cc2* returns $\vdash t'' \implies t'$ when applied to *t'*, then (THEN_CONSEQ_CONV *cc1 cc2*) *t* returns $\vdash t'' \implies t$. THEN_CONSEQ_CONV can handle weakening as well: If *cc1* returns $\vdash t \implies t'$ when applied to *t*, and *cc2* returns $\vdash t' \implies t''$ when applied to *t'*, then (THEN_CONSEQ_CONV *cc1 cc2*) *t* returns $\vdash t \implies t''$. Finally, if *cc1* returns $\vdash t = t'$ when applied to *t*, and *cc2* returns $\vdash t' = t''$ when applied to *t'*, then (THEN_CONSEQ_CONV *cc1 cc2*) *t* returns $\vdash t = t''$. If one of the conversions returns an equation, while the other returns an implication, the needed implication is automatically deduced.

See also

Conv.THENC, ConseqConv.EVERY_CONSEQ_CONV.

THEN_TCL	(Thm_cont)
----------	------------

```
$THEN_TCL : (thm_tactical -> thm_tactical -> thm_tactical)
```

Synopsis

Composes two theorem-tacticals.

Description

If *tt11* and *tt12* are two theorem-tacticals, *tt11 THEN_TCL tt12* is a theorem-tactical which composes their effect; that is, if:

```
tt11 ttac th1 = ttac th2
```

and

```
tt12 ttac th2 = ttac th3
```

then

```
(tt11 THEN_TCL tt12) ttac th1 = ttac th3
```

Failure

The application of THEN_TCL to a pair of theorem-tacticals never fails.

See also

Thm_cont.EVERY_TCL, Thm_cont.FIRST_TCL, Thm_cont.ORELSE_TCL.

<div data-bbox="161 815 314 864" data-label="Text"> <p>THENC</p> </div>	<div data-bbox="1157 815 1331 866" data-label="Text"> <p>(Conv)</p> </div>
--	---

op THENC : (conv -> conv -> conv)

Synopsis

Applies two conversions in sequence.

Description

If the conversion $c1$ returns $\vdash t = t'$ when applied to a term t , and $c2$ returns $\vdash t' = t''$ when applied to t' , then the composite conversion $(c1 \text{ THENC } c2)$ returns $\vdash t = t''$. That is, $(c1 \text{ THENC } c2)$ has the effect of transforming the term t first with the conversion $c1$ and then with the conversion $c2$.

THENC also handles the possibility that either of its arguments might return the UNCHANGED exception. If the first conversion returns UNCHANGED when applied to its argument, THENC just returns the result of the second conversion applied to the same initial term. If the second conversion raises UNCHANGED (and the first did not), then the result will be the theorem returned by the first conversion. In this way, unnecessary calls to TRANS can be avoided.

Failure

$(c1 \text{ THENC } c2)$ fails if either the conversion $c1$ fails when applied to t , or if $c1$ succeeds and returns $\vdash t = t'$ but $c2$ fails when applied to t' . $(c1 \text{ THENC } c2)$ may also fail if either of $c1$ or $c2$ is not, in fact, a conversion (i.e. a function that maps a term t to a theorem $\vdash t = t'$).

See also

Conv.EVERY_CONV.

THENL	(Tactical)
-------	------------

```
op THENL : tactic -> tactic list -> tactic
```

Synopsis

Applies a list of tactics to the corresponding subgoals generated by a tactic.

Description

If T, T_1, \dots, T_n are tactics, $T \text{ THENL } [T_1, \dots, T_n]$ is a tactic which applies T to a goal, and if it does not fail, applies the tactics T_1, \dots, T_n to the corresponding subgoals, unless T completely solves the goal.

Failure

The application of `THENL` to a tactic and tactic list never fails. The resulting tactic fails if T fails when applied to the goal, or if the goal list is not empty and its length is not the same as that of the tactic list, or finally if T_i fails when applied to the i 'th subgoal generated by T .

Uses

Applying different tactics to different subgoals.

See also

`Tactical.EVERY`, `Tactical.ORELSE`, `Tactical.THEN`.

theorems	(DB)
----------	------

```
theorems : string -> (string * thm) list
```

Synopsis

All the theorems stored in the named theory.

Description

An invocation `theorems thy`, where `thy` is the name of a currently loaded theory segment, will return a list of the theorems stored in that theory. Axioms and definitions are excluded. Each theorem is paired with its name in the result. The string `"-"` may be used to denote the current theory segment.

Failure

Never fails. If `thy` is not the name of a currently loaded theory segment, the empty list is returned.

Example

```
- theorems "combin";
> val it =
  [("I_o_ID", |- !f. (I o f = f) /\ (f o I = f)), ("I_THM", |- !x. I x = x),
   ("W_THM", |- !f x. W f x = f x x),
   ("C_THM", |- !f x y. combin$C f x y = f y x),
   ("S_THM", |- !f g x. S f g x = f x (g x)), ("K_THM", |- !x y. K x y = x),
   ("o_ASSOC", |- !f g h. f o g o h = (f o g) o h),
   ("o_THM", |- !f g x. (f o g) x = f (g x))] : (string * thm) list
```

See also

DB.thy, DB.fetch, DB.thms, DB.definitions, DB.axioms, DB.listDB.

<div data-bbox="161 1184 256 1232" data-label="Text"> <p><code>thm</code></p> </div>	<div data-bbox="1182 1180 1329 1232" data-label="Text"> <p>(Thm)</p> </div>
--	---

type thm

Synopsis

Type of theorems of the HOL logic.

Description

The abstract type `thm` represents the theorems derivable by inference in the HOL logic. The type of theorems can be viewed as the inductive closure of the axioms of the HOL logic by the primitive inference rules of HOL. Robin Milner had the brilliant insight to implement this view by encapsulating the primitive rules of inference for a logic as the constructors for an abstract type of theorems. This implementation technique is adopted in HOL.

See also

Thm.dest_thm, Thm.hyp, Thm.concl, Thm.tag, Thm.ASSUME, Thm.REFL, Thm.BETA_CONV, Thm.ABS, Thm.DISCH, Thm.MP, Thm.SUBST, Thm.INST_TYPE.

thm_count**(Count)**

```

thm_count :
  unit ->
  {ASSUME : int, REFL : int, BETA_CONV : int, SUBST : int,
   ABS : int, DISCH : int, MP : int, INST_TYPE : int,
   MK_COMB : int, AP_TERM : int, AP_THM : int, ALPHA : int,
   ETA_CONV : int, SYM : int, TRANS : int, EQ_MP : int,
   EQ_IMP_RULE : int, INST : int, SPEC : int, GEN : int,
   EXISTS : int, CHOOSE : int, CONJ : int, CONJUNCT1 : int,
   CONJUNCT2 : int, DISJ1 : int, DISJ2 : int, DISJ_CASES : int,
   NOT_INTRO : int, NOT_ELIM : int, CCONTR : int, GEN_ABS : int,
   definition : int, axiom : int, from_disk : int, oracle : int,
   total : int }

```

Synopsis

Returns the current value of the theorem counter.

Description

If enabled, HOL maintains a counter which is incremented every time a primitive inference is performed (or an axiom or definition set up). A call to `thm_count()` returns the current value of this counter. Inference counting needs to be enabled with the call `Count.counting_thms true`. Counting can be turned off by calling `counting_thms false`.

The default is for inference counting not to be enabled.

Failure

Never fails.

See also

`Count.apply`.

thms**(DB)**

```

thms : string -> (string * thm) list

```

Synopsis

All the theorems, definitions, and axioms stored in the named theory.

Description

An invocation `thms thy`, where `thy` is the name of a currently loaded theory segment, will return a list of the theorems, definitions, and axioms stored in that theory. Each theorem is paired with its name in the result. The string `"-"` may be used to denote the current theory segment.

Failure

Never fails. If `thy` is not the name of a currently loaded theory segment, the empty list is returned.

Example

```
- thms "combin";
> val it =
  [("C_DEF", |- combin$C = (\f x y. f y x)),
   ("C_THM", |- !f x y. combin$C f x y = f y x), ("I_DEF", |- I = S K K),
   ("I_o_ID", |- !f. (I o f = f) /\ (f o I = f)), ("I_THM", |- !x. I x = x),
   ("K_DEF", |- K = (\x y. x)), ("K_THM", |- !x y. K x y = x),
   ("o_ASSOC", |- !f g h. f o g o h = (f o g) o h),
   ("o_DEF", |- !f g. f o g = (\x. f (g x))),
   ("o_THM", |- !f g x. (f o g) x = f (g x)),
   ("S_DEF", |- S = (\f g x. f x (g x))),
   ("S_THM", |- !f g x. S f g x = f x (g x)),
   ("W_DEF", |- W = (\f x. f x x)), ("W_THM", |- !f x. W f x = f x x)] :
  (string * thm) list
```

See also

`DB.thy`, `DB.theorems`, `DB.axioms`, `DB.definitions`, `DB.fetch`, `DB.listDB`.

<div data-bbox="161 1545 256 1601" data-label="Text"><code>thy</code></div>	<div data-bbox="1212 1541 1331 1597" data-label="Text"><code>(DB)</code></div>
---	--

`thy` : string -> data list

Synopsis

Return the contents of a theory.

Description

An invocation `DB.thy s` returns the contents of the specified theory segment `s` in a list of `(thy,name)`, `(thm,class)` tuples. In a tuple, `(thy,name)` designate the theory and the

name given to the object in the theory. The `thm` element is the named object, and `class` its classification (one of `Thm` (theorem), `Axm` (axiom), or `Def` (definition)).

Case distinctions are ignored when determining the segment. The current segment may be specified, either by the distinguished literal "-", or by the name given when creating the segment with `new_theory`.

Failure

Never fails, but will return an empty list when `s` does not designate a currently loaded theory segment.

Example

```
- DB.thy "pair";
> val it =
  [(("pair", "ABS_PAIR_THM"), (|- !x. ?q r. x = (q,r), Db.Thm)),
   (("pair", "ABS_REP_prod"),
    (|- (!a. ABS_prod (REP_prod a) = a) /\
      !r. IS_PAIR r = (REP_prod (ABS_prod r) = r), Db.Def)),
   (("pair", "CLOSED_PAIR_EQ"),
    (|- !x y a b. ((x,y) = (a,b)) = (x = a) /\ (y = b), Db.Thm)),
   .
   .
   .
```

See also

`DB.class`, `DB.data`, `DB.listDB`, `DB.theorems`, `DB.match`, `Theory.new_theory`.

<code>thy_addon</code>	<code>(Theory)</code>
------------------------	-----------------------

`type thy_addon`

Synopsis

Type of theory additions.

Description

The type abbreviation `thy_addon`, declared as

```
type thy_addon = {sig_ps : (ppstream -> unit) option,
                  struct_ps : (ppstream -> unit) option}
```

packages up the arguments to `adjoin_to_theory`. The `sig_ps` argument is an optional prettyprinter, which will be invoked when the theory signature file is written. The `struct_ps` argument is an optional prettyprinter invoked when the theory structure file is written.

See also

`Theory.adjoin_to_theory`.

<code>time</code>

<code>(Lib)</code>

```
time : ('a -> 'b) -> 'a -> 'b
```

Synopsis

Measure how long a function application takes.

Description

An application `time f x` starts a clock, applies `f` to `x`, and then checks the clock to see how long that took. It prints out the elapsed runtime, garbage collection time, and system time before returning the value of `f x`.

Failure

If `f x` raises `e`, then `time f x` raises `e`, but still reports elapsed time.

Example

```
- time (int_sort) (for 0 999 I);
runtime: 0.771s,    gctime: 0.121s,    systime: 0.771s.
> val it =
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20,
 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38,
 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56,
 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74,
 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92,
 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108,
 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123,
 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138,
 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153,
 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168,
 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183,
```

```

184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198,
199, ...] : int list

- fun f x = f (x + 1);
> val 'a f = fn : int -> 'a

- time f 0;
runtime: 13.787s,    gctime: 0.000s,    systime: 0.035s.
! Uncaught exception:
! Overflow

```

See also

`Lib.end_time`, `Lib.start_time`, `Count.thm_count`.

TOP_DEPTH_CONV

(Conv)

`TOP_DEPTH_CONV` : (`conv` -> `conv`)

Synopsis

Applies a conversion top-down to all subterms, retraversing changed ones.

Description

`TOP_DEPTH_CONV` `c` `tm` repeatedly applies the conversion `c` to all the subterms of the term `tm`, including the term `tm` itself. The supplied conversion `c` is applied to the subterms of `tm` in top-down order and is applied repeatedly (zero or more times, as is done by `REPEATC`) at each subterm until it fails. If a subterm `t` is changed (up to alpha-equivalence) by virtue of the application of `c` to its own subterms, then then the term into which `t` is transformed is retraversed by applying `TOP_DEPTH_CONV` `c` to it.

Failure

`TOP_DEPTH_CONV` `c` `tm` never fails but can diverge.

Comments

The implementation of this function uses failure to avoid rebuilding unchanged subterms. That is to say, during execution the exception `QConv.UNCHANGED` may be generated and later trapped. The behaviour of the function is dependent on this use of failure. So, if the conversion given as an argument happens to generate the same exception, the operation of `TOP_DEPTH_CONV` will be unpredictable.

See also

Conv.DEPTH_CONV, Conv.ONCE_DEPTH_CONV, Conv.REDEPTH_CONV.

top_goal

(proofManagerLib)

```
top_goal : unit -> term list * term
```

Synopsis

Returns the current goal of the subgoal package.

Description

The function `top_goal` is part of the subgoal package. It returns the top goal of the goal stack in the current proof state. For a description of the subgoal package, see `set_goal`.

Failure

A call to `top_goal` will fail if there are no unproven goals. This could be because no goal has been set using `set_goal` or because the last goal set has been completely proved.

Uses

Examining the proof state after a proof fails.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`, `proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`, `proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`, `proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

top_thm

(proofManagerLib)

```
top_thm : unit -> thm
```

Synopsis

Returns the theorem just proved using the subgoal package.

Description

The function `top_thm` is part of the subgoal package. A proof state of the package consists of either goal and justification stacks if a proof is in progress or a theorem if a

proof has just been completed. If the proof state consists of a theorem, `top_thm` returns that theorem. For a description of the subgoal package, see `set_goal`.

Failure

`top_thm` will fail if the proof state does not hold a theorem. This will be so either because no goal has been set or because a proof is in progress with unproven subgoals.

Uses

Accessing the result of an interactive proof session with the subgoal package.

See also

`proofManagerLib.set_goal`, `proofManagerLib.restart`, `proofManagerLib.backup`, `proofManagerLib.restore`, `proofManagerLib.save`, `proofManagerLib.set_backup`, `proofManagerLib.expand`, `proofManagerLib.expandf`, `proofManagerLib.p`, `proofManagerLib.top_thm`, `proofManagerLib.top_goal`.

<code>topsort</code>	<code>(Lib)</code>
----------------------	--------------------

```
topsort : ('a -> 'a -> bool) -> 'a list -> 'a list
```

Synopsis

Topologically sorts a list using a given partial order relation.

Description

The call `topsort opr list` where `opr` is a curried partial order on the elements of `list`, will topologically sort the list, i.e., will permute it such that if `x opr y` then `x` will occur to the left of `y` in the resulting list.

Failure

If `opr` fails when applied to `x` and `y` in `list`. Also, `topsort` will fail if there is a chain of elements `x1, ..., xn`, all in `list`, such that `opr x1 x2`, ..., `opr xn x1`. This displays a cyclic dependency.

Example

The following call arranges a list of terms in subterm order:

```
- fun is_subterm x y = Lib.can (find_term (aconv x)) y;
> val is_subterm = fn : term -> term -> bool

- topsort is_subterm
  ['x+1', 'x:num', 'y + (x + 1)', 'y + x', 'y + x + z', 'y:num'];
> val it = ['y', 'x', 'x + 1', 'y + x', 'y + x + z', 'y + (x + 1)']
```

See also

Lib.sort.

total

(Lib)

```
total : ('a -> 'b) -> 'a -> 'b option
```

Synopsis

Converts a partial function to a total function.

Description

In ML, there are two main ways for a function to signal that it has been called on an element outside of its intended domain of application: exceptions and options. The function `total` maps a function that may raise an exception to one that returns an element in the option type. Thus, if `f x` results in any exception other than `Interrupt` being raised, then `total f x` returns `NONE`. If `f x` raises `Interrupt`, then `total f x` likewise raises `Interrupt`. If `f x` returns `y`, then `total f x` returns `SOME y`.

The function `total` has an inverse `partial`. Generally speaking, `(partial err o total) f` equals `f`, provided that `err` is the only exception that `f` raises. Similarly, `(total o partial err) f` is equal to `f`.

Failure

When application of the first argument to the second argument raises `Interrupt`.

Example

```
- 3 div 0;  
! Uncaught exception:  
! Div  
  
- total (op div) (3,0);  
> val it = NONE : int option  
  
- (partial Div o total) (op div) (3,0);  
! Uncaught exception:  
! Div
```

See also

Lib.partial.

<div data-bbox="236 351 416 405" data-label="Text"><code>tprove</code></div>	<div data-bbox="1230 347 1410 400" data-label="Text"><code>(Defn)</code></div>
--	--

```
tprove : defn * tactic -> thm * thm
```

Synopsis

Prove termination of a `defn`.

Description

`tprove` takes a `defn` and a `tactic`, and uses the `tactic` to prove the termination constraints of the `defn`. A pair of theorems $(eqns, ind)$ is returned: `eqns` is the unconstrained recursion equations of the `defn`, and `ind` is the corresponding induction theorem for the equations, also unconstrained.

`tprove` and `tgoal` can be seen as analogues of `prove` and `set_goal` in the specialized domain of proving termination of recursive functions.

It is up to the user to store the results of `tprove` in the current theory segment.

Failure

`tprove (defn, tac)` fails if `tac` fails to prove the termination conditions of `defn`.

`tprove (defn, tac)` fails if `defn` represents a non-recursive or primitive recursive function.

Example

Suppose that we have defined a version of Quicksort as follows:

```
- val qsort_defn =
  Hol_defn "qsort"
    '(qsort ___ [] = []) /\
      (qsort ord (x::rst) =
        APPEND (qsort ord (FILTER ($~ o ord x) rst))
                (x :: qsort ord (FILTER (ord x) rst)))'
```

Also suppose that a `tactic tac` proves termination of `qsort`. (This `tactic` has probably been built by interactive proof after starting a goalstack with `tgoal qsort_defn`.) Then

```
- val (qsort_eqns, qsort_ind) = tprove(qsort_defn, tac);

> val qsort_eqns =
  |- (qsort v0 [] = []) /\
      (qsort ord (x::rst) =
        APPEND (qsort ord (FILTER ($~ o ord x) rst))
```



```

(x::qsort ord (FILTER (ord x) rst))) : thm

val qsort_ind =
  |- !P.
    (!v0. P v0 []) /\
    (!ord x rst.
      P ord (FILTER ($~ o ord x) rst) /\
      P ord (FILTER (ord x) rst) ==> P ord (x::rst))
    ==>
    !v v1. P v v1 : thm

```

Comments

The recursion equations returned by a successful invocation of `tprove` are automatically added to the global `compset` accessed by `EVAL`.

See also

`Defn.goal`, `Defn.Hol.defn`, `bossLib.EVAL`.

trace	(Feedback)
-------	------------

```
trace : string * int -> ('a -> 'b) -> 'a -> 'b
```

Synopsis

Invoke a function with a specified level of tracing.

Description

The `trace` function is used to set the value of a tracing variable for the duration of one top-level function call.

A call to `trace (nm,i) f x` attempts to set the tracing variable associated with the string `nm` to value `i`. Then it evaluates `f x` and returns the resulting value after restoring the trace level of `nm`.

Failure

Fails if the name given is not associated with a registered tracing variable. Also fails if the function invocation fails.

Example

```

- load "mesonLib";

- trace ("meson",2) prove
  (concl SKOLEM_THM,mesonLib.MESON_TAC []);

0 inferences so far. Searching with maximum size 0.
0 inferences so far. Searching with maximum size 1.
Internal goal solved with 2 MESON inferences.
0 inferences so far. Searching with maximum size 0.
0 inferences so far. Searching with maximum size 1.
Internal goal solved with 2 MESON inferences.
0 inferences so far. Searching with maximum size 0.
0 inferences so far. Searching with maximum size 1.
Internal goal solved with 2 MESON inferences.
0 inferences so far. Searching with maximum size 0.
0 inferences so far. Searching with maximum size 1.
Internal goal solved with 2 MESON inferences.
  solved with 2 MESON inferences.

> val it = |- !P. (!x. ?y. P x y) = ?f. !x. P x (f x) : thm

- traces();

> val it =
  [{default = 1, name = "meson", trace_level = 1},
   {default = 10, name = "Subgoal number", trace_level = 10},
   {default = 0, name = "Rewrite", trace_level = 0},
   {default = 0, name = "Ho_Rewrite", trace_level = 0}]

```

See also

Feedback, Feedback.register_trace, Feedback.reset_trace, Feedback.reset_traces, Feedback.set_trace, Feedback.traces, Lib.with_flag.

traces

(Feedback)

```
traces : unit -> {name : string, current_value : int,
                  default_value : int, maximum : int} list
```

Synopsis

Returns a list of registered tracing variables.

Description

The function `traces` is part of the interface to a collection of variables that control the verbosity of various tools within the system. Tracing can be useful both when debugging proofs (with the simplifier for example), and also as a guide to how an automatic proof is proceeding (with `mesonLib` for example).

Failure

Never fails.

Example

```
- traces();
> val it =
  [{default = 10, name = "Subgoal number", trace_level = 10},
   {default = 0, name = "Rewrite", trace_level = 0},
   {default = 0, name = "Ho_Rewrite", trace_level = 0}]
```

See also

`Feedback.register_trace`, `Feedback.set_trace`, `Feedback.reset_trace`,
`Feedback.reset_traces`, `Feedback.trace`.

TRANS

(Thm)

```
TRANS : (thm -> thm -> thm)
```

Synopsis

Uses transitivity of equality on two equational theorems.

Description

When applied to a theorem $A1 \vdash t1 = t2$ and a theorem $A2 \vdash t2 = t3$, the inference rule `TRANS` returns the theorem $A1 \cup A2 \vdash t1 = t3$.

$$\frac{A1 \mid- t1 = t2 \quad A2 \mid- t2 = t3}{A1 \text{ u } A2 \mid- t1 = t3} \text{ TRANS}$$
Failure

Fails unless the theorems are equational, with the right side of the first being the same as the left side of the second.

Example

```
- val t1 = ASSUME ``a:bool = b`` and t2 = ASSUME ``b:bool = c``;
val t1 = [.] |- a = b : thm
val t2 = [.] |- b = c : thm

- TRANS t1 t2;
val it = [..] |- a = c : thm
```

See also

Thm.EQ_MP, Drule.IMP_TRANS, Thm.REFL, Thm.SYM.

triple

(Lib)

```
triple : 'a -> 'b -> 'c -> 'a * 'b * 'c
```

Synopsis

Makes three values into a triple.

Description

triple x y z returns (x, y, z).

Failure

Never fails.

See also

Lib.triple_of_list, Lib.pair, Lib.quadruple.

triple_of_list

(Lib)

```
triple_of_list : 'a list -> 'a * 'a * 'a
```

Synopsis

Turns a three-element list into a triple.

Description

triple_of_list [x, y, z] returns (x, y, z).

Failure

Fails if applied to a list that is not of length 3.

See also

Lib.singleton_of_list, Lib.pair_of_list, Lib.quadruple_of_list.

TRUE_CONSEQ_CONV

(ConseqConv)

```
TRUE_CONSEQ_CONV : conseq_conv
```

Synopsis

Given a term t of type `bool` this consequence conversion returns the theorem $\vdash t \implies T$.

See also

ConseqConv.FALSE_CONSEQ_CONV, ConseqConv.REFL_CONSEQ_CONV,
ConseqConv.TRUE_FALSE_REFL_CONSEQ_CONV.

TRUE_FALSE_REFL_CONSEQ_CONV

(ConseqConv)

```
TRUE_FALSE_REFL_CONSEQ_CONV : directed_conseq_conv
```

Synopsis

Given a term t of type `bool` this directed consequence conversion returns the theorem $\vdash F \implies t$ for `CONSEQ_CONV_STRENGTHEN_direction`, the theorem $\vdash t \implies T$ for `CONSEQ_CONV_WEAKEN_direction` and $\vdash t = t$ for `CONSEQ_CONV_UNKNOWN_direction`.

See also

ConseqConv.TRUE_CONSEQ_CONV, ConseqConv.FALSE_CONSEQ_CONV,
ConseqConv.REFL_CONSEQ_CONV.

try**(Lib)**

```
try : ('a -> 'b) -> 'a -> 'b
```

Synopsis

Apply a function and print any exceptions

Description

The application `try f x` evaluates `f x`; if this evaluation raises an exception `e`, then `e` is examined and some information about it is printed before `e` is re-raised. If `f x` evaluates to `y`, then `y` is returned.

Often, a `HOL_ERR` exception can propagate all the way to the top level. Unfortunately, the information held in the exception is not then printed. `try` can often display this information.

Failure

When application of the first argument to the second raises an exception.

Example

```
- mk_comb (T,F);
! Uncaught exception:
! HOL_ERR

- try mk_comb (T,F);
```

```
Exception raised at Term.mk_comb:
incompatible types
! Uncaught exception:
! HOL_ERR
```

Evaluation order can be significant. ML evaluates `try M N` by evaluating `M` (yielding `f` say) and `N` (yielding `x` say), and then `f` is applied to `x`. Any exceptions raised in the course of evaluating `M` or `N` will not be detected by `try`. In such cases it is better to use `Raise`. In the following example, the erroneous construction of an abstraction is not detected by `try` and the exception propagates all the way to the top level; however, `Raise` does handle the exception.

```

- try mk_comb (T, mk_abs(T,T));
! Uncaught exception:
! HOL_ERR

- mk_comb (T, mk_abs(T,T)) handle e => Raise e;

Exception raised at Term.mk_abs:
Bvar not a variable
! Uncaught exception:
! HOL_ERR

```

See also

Feedback.Raise, Lib.trye.

TRY	(Tactical)
-----	------------

TRY : (tactic -> tactic)

Synopsis

Makes a tactic have no effect rather than fail.

Description

For any tactic T , the application `TRY T` gives a new tactic which has the same effect as T if that succeeds, and otherwise has no effect.

Failure

The application of `TRY` to a tactic never fails. The resulting tactic never fails.

See also

Tactical.CHANGED_TAC, Tactical.VALID.

TRY_CONV	(Conv)
----------	--------

TRY_CONV : conv -> conv

Synopsis

Attempts to apply a conversion; applies identity conversion in case of failure.

Description

`TRY_CONV c t` attempts to apply the conversion `c` to the term `t`; if this fails, then the identity conversion is applied instead. That is, if `c` is a conversion that maps a term `t` to the theorem `|- t = t'`, then the conversion `TRY_CONV c` also maps `t` to `|- t = t'`. But if `c` fails when applied to `t`, then `TRY_CONV c t` raises the `UNCHANGED` exception (which is understood to mean the instance of reflexivity, `|- t = t`). If `c` applied to `t` raises the `UNCHANGED` exception, then so too does `TRY_CONV c t`.

Failure

Never fails, though the `UNCHANGED` exception can be raised.

See also

`Conv.ALL_CONV`, `Conv.QCONV`.

<code>trye</code>	<code>(Lib)</code>
-------------------	--------------------

`trye : ('a -> 'b) -> 'a -> 'b`

Synopsis

Maps exceptions into `HOL_ERR`

Description

The standard exception for HOL applications to raise is `HOL_ERR`. The use of a single exception simplifies the writing of exception handlers and facilities for decoding and printing error messages. However, ML functions that raise exceptions, such as `hd` and many others, are often used to implement HOL programs. In such cases, `trye` may be used to coerce exceptions into applications of `HOL_ERR`. Note however, that the `Interrupt` exception is not coerced by `trye`.

The application `trye f x` evaluates `f x`; if this evaluates to `y`, then `y` is returned. However, if evaluation raises an exception `e`, there are three cases: if `e` is `Interrupt`, then it is raised; if `e` is `HOL_ERR`, then it is raised; otherwise, `e` is mapped to an application of `HOL_ERR` and then raised.

Failure

Fails if the function application fails.

Example


```
- hd [];  
! Uncaught exception:  
! Empty  
  
- trye hd [];  
! Uncaught exception:  
! HOL_ERR  
  
- trye (fn _ => raise Interrupt) 1;  
> Interrupted
```

See also

Lib, Feedback.Raise, Lib.try.

tryfind

(Lib)

tryfind : ('a -> 'b) -> 'a list -> 'b

Synopsis

Returns the result of the first successful application of a function to the elements of a list.

Description

tryfind f [x1,...,xn] returns (f xi) for the first xi in the list for which application of f does not raise an exception. However, if Interrupt is raised in the course of some application of f xi, then tryfind f [x1,...,xn] raises Interrupt.

Failure

Fails if the application of f fails for all elements in the list. This will always be the case if the list is empty.

See also

Lib.first, Lib.mem, Lib.exists, Lib.all, Lib.assoc, Lib.rev_assoc, Lib.assoc1, Lib.assoc2.

trypluck

(Lib)

trypluck : ('a -> 'b) -> 'a list -> 'b * 'a list

Synopsis

Pull an element out of a list.

Description

An invocation `trypluck f [x1, ..., xk, ..., xn]` returns a pair

$$(f(x_k), [x_1, \dots, x_{k-1}, x_{k+1}, \dots, x_n])$$

where x_k has been lifted out of the list without disturbing the relative positions of the other elements. For this to happen, $f(x_k)$ must hold, and $f(x_i)$ must fail for x_1, \dots, x_{k-1} .

Failure

If the input list is empty. Also fails if f fails on every member of the list.

Example

```
- val (x,rst) = trypluck BETA_CONV [‘1‘, ‘(\x. x+2) 3‘, ‘p + q‘];
> val x = |- (\x. x + 2) 3 = 3 + 2 : thm
   val rst = [‘1‘, ‘p + q‘] : term list
```

See also

`Lib.first`, `Lib.filter`, `Lib.mapfilter`, `Lib.tryfind`.

<code>trypluck'</code>	<code>(Lib)</code>
------------------------	--------------------

`trypluck'` : ('a -> 'b option) -> 'a list -> ('b option * 'a list)

Synopsis

Pull an element out of a list.

Description

An invocation `trypluck' f [x1, ..., xk, ..., xn]` returns either the pair

$$(f(x_k), [x_1, \dots, x_{k-1}, x_{k+1}, \dots, x_n])$$

where x_k has been lifted out of the list without disturbing the relative positions of the other elements, where $f(x_k)$ is `SOME(v)`, and where $f(x_i)$ returns `NONE` for x_1, \dots, x_{k-1} ; or it returns `(NONE, [x1, ... xn])` when f applied to every element of the list returns `NONE`.

This is an 'option' version of the other library function `trypluck`.

Failure

Never fails.

See also

Lib.first, Lib.filter, Lib.mapfilter, Lib.tryfind, Lib.trypluck.

<div data-bbox="161 638 400 694" data-label="Text"> <p>ty_antiq</p> </div>	<div data-bbox="1125 633 1331 689" data-label="Text"> <p>(Parse)</p> </div>
--	---

```
ty_antiq : hol_type -> term
```

Synopsis

Make a variable named ty_antiq.

Description

Given a type ty, the ML invocation ty_antiq ty returns the HOL variable ty_antiq : ty. This provides a way to antiquote types into terms, which is necessary because the HOL term parser only allows terms to be antiquoted. The use of ty_antiq promotes a type to a term variable which can be antiquoted. The HOL parser detects occurrences of ty_antiq ty and inserts ty as a constraint.

Example

Suppose we want to constrain a term to have type num list, which is bound to ML value ty. Attempting to antiquote ty directly into the term won't work:

```
val ty = ':num list';
> val ty = ':num list' : hol_type

- 'x : ^ty';
! Toplevel input:
! Term 'x : ^ty';
!           ^^
! Type clash: expression of type
!   hol_type
! cannot have type
!   term
```

Use of ty_antiq solves the problem:

```

- ‘‘x : ^(ty_antiq ty)’’;
> val it = ‘x’ : term

- type_of it;
> val it = ‘:num list’ : hol_type

```

See also

Parse.Term.

<div data-bbox="234 770 560 826" data-label="Text"> <p>type_abbrev</p> </div>	<div data-bbox="1200 766 1412 819" data-label="Text"> <p>(Parse)</p> </div>
---	---

Parse.type_abbrev : string * hol_type -> unit

Synopsis

Establishes a type abbreviation.

Description

A call to `type_abbrev(s, ty)` sets up a type abbreviation that will cause the parser to treat the string `s` as a synonym for the type `ty`. Moreover, if `ty` includes any type variables, then the abbreviation is treated as a type operator taking as many parameters as appear in `ty`. The order of the parameters will be the alphabetic ordering of the type variables' names.

Abbreviations work at the level of the names of type operators. It is thus possible to link a binary infix to an operator that is in turn an abbreviation.

Failure

Fails if the given type is just a type variable.

Example

This is a simple abbreviation.

```

- type_abbrev ("set", ‘‘:’a -> bool’’);
> val it = () : unit

- ‘‘:num set’’;
> val it = ‘‘:num set’’ : hol_type

```

Here, the abbreviation is set up and provided with its own infix symbol.

```

- type_abbrev ("rfunc", ``:'b -> 'a``);
> val it = () : unit

- add_infix_type {Assoc = RIGHT, Name = "rfunc",
                  ParseName = SOME "<-", Prec = 50};
> val it = () : unit

- ``:'a <- bool``;
> val it = ``:'a <- bool`` : hol_type

- dest_thy_type it;
> val it = {Args = [``:bool``, ``:'a``], Thy = "min", Tyop = "fun"} :
  {Args : hol_type list, Thy : string, Tyop : string}

```

Comments

As is common with most of the parsing and printing functions, there is a companion `temp_type_abbrev` function that does not cause the abbreviation effect to persist when the theory is exported. As the examples show, type abbreviations also affect the pretty-printing of types. The pretty-printer can be instructed not to print particular abbreviations (using `Parse.disable_tyabbrev_printing`), or to not print any (by setting the trace variable `"print_tyabbrevs"`).

See also

`Parse.add_infix_type`, `Parse.disable_tyabbrev_printing`.

<div data-bbox="159 1408 368 1467" data-label="Text"> <p>type_of</p> </div>	<div data-bbox="1155 1406 1331 1460" data-label="Text"> <p>(Term)</p> </div>
---	--

`type_of` : `term` -> `hol_type`

Synopsis

Returns the type of a term.

Failure

Never fails.

Example

```

- type_of boolSyntax.universal;
> val it = `:( 'a -> bool) -> bool` : hol_type

```

<div data-bbox="236 351 474 405" data-label="Text"><code>type_rws</code></div>	<div data-bbox="1145 347 1414 398" data-label="Text"><code>(bossLib)</code></div>
--	---

```
type_rws : string -> thm list
```

Synopsis

List rewrites for a concrete type.

Description

An application `type_rws s`, where `s` is the name of a declared datatype, returns a list of rewrite rules corresponding to the types. The list typically contains theorems about the distinctness and injectivity of constructors, the definition of the 'case' constant introduced at the time the type was defined, and any extra rewrites coming from the use of records.

Failure

If `s` is not the name of a declared datatype.

Example

```
- type_rws "list";

> val it =
  [|- (!v f. case v f [] = v) /\ !v f a0 a1. case v f (a0::a1) = f a0 a1,
    |- !a1 a0. ~([] = a0::a1),
    |- !a1 a0. ~(a0::a1 = []),
    |- !a0 a1 a0' a1'. (a0::a1 = a0'::a1') = (a0 = a0') /\ (a1 = a1')]

- Hol_datatype 'point = <| x:num ; y:num |>';
<<HOL message: Defined type: "point">>

- type_rws "point";
> val it =
  [|- !f a0 a1. case f (point a0 a1) = f a0 a1,
    |- !a0 a1 a0' a1'.
      (point a0 a1 = point a0' a1') = (a0 = a0') /\ (a1 = a1'),
    |- !z x p. p with <|y := x; x := z|> = p with <|x := z; y := x|>,
    |- (!x p. (p with y := x).x = p.x) /\ (!x p. (p with x := x).y = p.y) /\
      (!x p. (p with x := x).x = x) /\ !x p. (p with y := x).y = x,
    |- (!n n0. (point n n0).x = n) /\ !n n0. (point n n0).y = n0,
```

```

|- (!n1 n n0. point n n0 with x := n1 = point n1 n0) /\
    !n1 n n0. point n n0 with y := n1 = point n n1,
|- (!p. p with x := p.x = p) /\ !p. p with y := p.y = p,
|- (!x2 x1 p. p with <|x := x1; x := x2|> = p with x := x1) /\
    !x2 x1 p. p with <|y := x1; y := x2|> = p with y := x1,
|- (!p f. (p with y updated_by f).x = p.x) /\
    (!p f. (p with x updated_by f).y = p.y) /\
    (!p f. (p with x updated_by f).x = f p.x) /\
    !p f. (p with y updated_by f).y = f p.y,
|- !p n0 n. p with <|x := n0; y := n|> = <|x := n0; y := n|>]

```

Comments

RW_TAC and SRW_TAC automatically include these rewrites.

See also

bossLib.rewrites, bossLib.RW_TAC.

<div data-bbox="161 1097 485 1153" data-label="Text"> <p>type_ssfrag</p> </div>	<div data-bbox="1067 1095 1331 1153" data-label="Text"> <p>(simpLib)</p> </div>
---	---

```
simpLib.type_ssfrag : string -> ssfrag
```

Synopsis

Returns a simpset fragment for simplifying types' constructors.

Description

A call to `type_ssfrag(s)` function returns a simpset fragment that embodies simplification routines for the type named by the string `s`. The fragment includes rewrites that express injectivity and disjointness of constructors, and which simplify `case` expressions applied to terms that have constructors at the outermost level.

Failure

Fails if the string argument does not correspond to a type stored in the `TypeBase`.

Example

```

- val ss = simpLib.type_ssfrag "list";
> val ss =
    simpLib.SSFRAG{ac = [], congs = [], convs = [], dprocs = [],

```

```

filter = NONE,
rewrs =
  [|- (!v f. case v f [] = v) /\
    !v f a0 a1. case v f (a0::a1) = f a0 a1,
  |- !a1 a0. ~([] = a0::a1),
  |- !a1 a0. ~(a0::a1 = []),
  |- !a0 a1 a0' a1'. (a0::a1 = a0'::a1') =
    (a0 = a0') /\ (a1 = a1')]]}

: ssfrag

- SIMP_CONV (bool_ss ++ ss) [] ‘‘h::t = []‘‘;
<<HOL message: inventing new type variable names: 'a>>
> val it = |- (h::t = []) = F : thm

```

Comments

RW_TAC and SRW_TAC automatically include these simpset fragments.

See also

BasicProvers.RW_TAC, BasicProvers.srw_ss, bossLib.type_rws, simpLib.SIMP_CONV, TypeBase.

<div data-bbox="237 1270 529 1326" data-label="Text"> <h1 style="margin: 0;">type_subst</h1> </div>	<div data-bbox="1228 1265 1410 1326" data-label="Text"> <h1 style="margin: 0;">(Type)</h1> </div>
---	---

type_subst : (hol_type,hol_type) subst -> hol_type -> hol_type

Synopsis

Instantiates types in a type.

Description

If $\theta = \{redex_1, residue_1\}, \dots, \{redex_n, residue_n\}$ is a (hol_type, hol_type) subst, where the $redex_i$ are the types to be substituted for, and the $residue_i$ the replacements, and ty is a type to instantiate, the call `type_subst theta ty` will replace each occurrence of a $redex_i$ by the corresponding $residue_i$ throughout ty . The replacements will be performed in parallel. If several of the type instantiations are applicable, the choice is undefined. Each $redex_i$ ought to be a type variable, but if it isn't, it will never be replaced in ty . Also, it is not necessary that any or all of the types $redex_1 \dots redex_n$ should in fact appear in ty .

Failure

Never fails.

Example

```
- type_subst [alpha |-> bool] (Type ':a # 'b');
> val it = ':bool # 'b' : hol_type

- type_subst [Type ':a # 'b' |-> Type ':num', alpha |-> bool]
              (Type ':a # 'b');
> val it = ':bool # 'b' : hol_type
```

See also

Term.inst, Thm.INST_TYPE, Lib.|->, Term.subst.

<div data-bbox="161 1050 485 1106" data-label="Text"> <p>type_var_in</p> </div>	<div data-bbox="1155 1048 1331 1106" data-label="Text"> <p>(Type)</p> </div>
---	--

```
type_var_in : hol_type -> hol_type -> bool
```

Synopsis

Checks if a type variable occurs in a type.

Description

An invocation `type_var_in tyv ty` returns true if `tyv` occurs in `ty`. Otherwise, it returns false.

Failure

Fails if `tyv` is not a type variable.

Example

```
- type_var_in alpha (bool --> alpha);
> val it = true : bool

- type_var_in alpha bool;
> val it = false : bool
```

Comments

Can be useful in enforcing side conditions on inference rules.

See also

`Type.type_vars`, `Type.type_varsl`, `Type.exists_tyvar`.

<code>type_vars</code>

<code>(Type)</code>

```
type_vars : hol_type -> hol_type list
```

Synopsis

Returns the set of type variables in a type.

Description

An invocation `type_vars ty` returns a list representing the set of type variables occurring in `ty`.

Failure

Never fails.

Example

```
- type_vars ((alpha --> beta) --> bool --> beta);  
> val it = [':a', ':b'] : hol_type list
```

Comments

Code should not depend on how elements are arranged in the result of `type_vars`.

See also

`Type.type_varsl`, `Type.type_var_in`, `Type.exists_tyvar`, `Type.polymorphic`,
`Term.free_vars`.

<code>type_vars_in_term</code>

<code>(Term)</code>

```
type_vars_in_term : term -> hol_type list
```

Synopsis

Return the type variables occurring in a term.

Description

An invocation `type_vars_in_term M` returns the set of type variables occurring in `M`.

Failure

Never fails.

Example

```
- type_vars_in_term (concl boolTheory.ONE_ONE_DEF);
> val it = [:'b', :'a'] : hol_type list
```

See also

`Term.free_vars`, `Type.type_vars`.

<div data-bbox="159 1070 453 1128" data-label="Text"> <p><code>type_varsl</code></p> </div>	<div data-bbox="1155 1070 1332 1128" data-label="Text"> <p>(Type)</p> </div>
---	--

```
type_varsl : hol_type list -> hol_type list
```

Synopsis

Returns the set of type variables in a list of types.

Description

An invocation `type_varsl [ty1, ..., tyn]` returns a list representing the set-theoretic union of the type variables occurring in `ty1, ..., tyn`.

Failure

Never fails.

Example

```
- type_varsl [alpha, beta, bool, ((alpha --> beta) --> bool --> beta)];
> val it = [:'a', :'b'] : hol_type list
```

Comments

Code should not depend on how elements are arranged in the result of `type_varsl`.

See also

`Type.type_vars`, `Type.type_var_in`, `Type.exists_tyvar`, `Type.polymorphic`,
`Term.free_vars`.

TypeBase

```
structure TypeBase
```

Synopsis

A database of facts stemming from datatype declarations

Description

The structure `TypeBase` provides an interface to a database that is updated when a new datatype is introduced with `Hol_datatype`. When a new datatype is declared, a collection of theorems "about" the type can be automatically derived. These are indeed proved, and are stored in the current theory segment. They are also automatically stored in `TypeBase`.

The interface to `TypeBase` is intended to provide support for writers of high-level tools for reasoning about datatypes.

Example

```
- Hol_datatype `tree = Leaf
                    | Node of 'a => tree => tree`;
<<HOL message: Defined type: "tree">>
> val it = () : unit

- TypeBase.read {Thy = current_theory(), Tyop = "tree"};
> val it =
SOME-----
-----
HOL datatype: "tree"
Primitive recursion:
|- !f0 f1.
    ?fn.
      (!a. fn (Leaf a) = f0 a) /\
      !a0 a1. fn (Node a0 a1) = f1 a0 a1 (fn a0) (fn a1)
Case analysis:
|- (!f f1 a. case f f1 (Leaf a) = f a) /\
```

```

    !f f1 a0 a1. case f f1 (Node a0 a1) = f1 a0 a1
Size:
|- (!a. tree_size (Leaf a) = 1 + a) /\
    !a0 a1. tree_size (Node a0 a1) = 1 + (tree_size a0 + tree_size a1)
Induction:
|- !P.
    (!n. P (Leaf n)) /\ (!t t0. P t /\ P t0 ==> P (Node t t0)) ==>
    !t. P t
Case completeness: |- !t. (?n. t = Leaf n) \/ ?t' t0. t = Node t' t0
One-to-one:
|- (!a a'. (Leaf a = Leaf a') = (a = a')) /\
    !a0 a1 a0' a1'.
    (Node a0 a1 = Node a0' a1') = (a0 = a0') /\ (a1 = a1')
Distinctness: |- !a1 a0 a. ~(Leaf a = Node a0 a1) : tyinfo option

```

See also

bossLib.Hol_datatype.

<div data-bbox="161 1146 312 1200" data-label="Text">types</div>	<div data-bbox="1096 1142 1331 1200" data-label="Text">(Theory)</div>
--	---

```
types : string -> (string * int) list
```

Synopsis

Lists the types in the named theory.

Description

The function `types` should be applied to a string which is the name of an ancestor theory (including the current theory; the special string `"-"` is always interpreted as the current theory). It returns a list of all the type constructors declared in the named theory, in the form of arity-name pairs.

Failure

Fails unless the named theory is an ancestor, or the current theory.

Example

```

- load "bossLib";
> val it = () : unit

```

```
- itlist union (map types (ancestry "-")) [];
> val it =
  [("one", 0), ("option", 1), ("prod", 2), ("sum", 2),
   ("fun", 2), ("ind", 0), ("bool", 0), ("num", 0),
   ("recspace", 1), ("list", 1)] : (string * int) list
```

See also

Theory.constants, Theory.current_axioms, Theory.current_definitions,
Theory.current_theorems, Theory.new_type, Definition.new_type_definition,
Theory.parents, Theory.ancestry.

U	(Lib)
---	-------

```
U : 'a list list -> 'a list
```

Synopsis

Takes the union of a list of sets.

Description

An application $U [l_1, \dots, l_n]$ is equivalent to $\text{union } l_1 (\dots (\text{union } l_{n-1}, l_n)\dots)$. Thus, every element that occurs in one of the lists will appear in the result.

Failure

Never fails.

Example

```
- U [[1,2,3], [4,5,6], [1,2,5]];
> val it = [3, 6, 4, 1, 2, 5] : int list
```

Comments

The order in which the elements occur in the resulting list should not be depended upon.

A high-performance implementation of finite sets may be found in structure `HOLset`.

ML equality types are used in the implementation of `U` and its kin. This limits its applicability to types that allow equality. For other types, typically abstract ones, use the `'op_'` variants.

See also

Lib.op_U, Lib.union, Lib.mk_set, Lib.mem, Lib.insert, Lib.set_eq, Lib.intersect, Lib.set_diff.

UNABBREV_TAC	(Q)
--------------	-----

Q.UNABBREV_TAC : term quotation -> tactic

Synopsis

Removes an abbreviation from a goal's assumptions by substituting it out.

Description

The argument to UNABBREV_TAC must be a quotation containing the name of a variable that is abbreviated in the current goal. In other words, when calling UNABBREV_TAC 'v', there must be an assumption of the form $\text{Abbrev}(v = e)$ in the goal's assumptions. This assumption is removed, and all occurrences of the variable v in the goal are replaced by e . If there are two abbreviation assumptions for v in the goal, the more recent is removed.

Example

The goal

$$\text{Abbrev}(v = 2 * x + 1), v + x < 10 \text{ ?- } P(v)$$

is transformed by Q.UNABBREV_TAC 'v' to

$$2 * x + 1 + x < 10 \text{ ?- } P(2 * x + 1)$$
Failure

Fails if there is no abbreviation of the required form in the goal's assumptions, or if the quotation doesn't parse to a variable.

See also

BasicProvers.Abbr, Q.ABBREV_TAC.

UNBETA_CONV	(Conv)
-------------	--------

UNBETA_CONV : term -> conv

Synopsis

Returns a reversed instance of beta-reduction.

Description

`UNBETA_CONV t1 t2` returns a theorem of the form

$$\vdash t2 = (\lambda v. t') t1$$

The choice of v and the nature of t' depend on whether or $t1$ is a variable. If so, then v will be $t1$ and t' will be $t2$. Otherwise, v will be generated with `genvar` and t' will be the result of substituting v for $t1$, wherever it occurs.

Failure

Never fails.

Comments

Very useful for setting up a higher-order match by hand. The use of `genvar` is predicated on the assumption that it will later be eliminated through the application of the function term to some other argument.

See also

`Thm.BETA_CONV`.

<code>uncurry</code>	<code>(Lib)</code>
----------------------	--------------------

`uncurry` : ('a -> 'b -> 'c) -> ('a * 'b) -> 'c

Synopsis

Converts a function taking two arguments into a function taking a single paired argument.

Description

The application `uncurry f` returns `fn (x,y) => f x y`, so that

$$\text{uncurry } f \text{ (x,y) = f x y}$$

Failure

Never fails.

Example


```
- fun add x y = x + y
> val add = fn : int -> int -> int

- uncurry add (3,4);
> val it = 7 : int
```

See also

Lib, Lib.curry.

UNCURRY_CONV

(PairRules)

UNCURRY_CONV : conv

Synopsis

Uncurrys an application of an abstraction.

Example

```
- UNCURRY_CONV (Term '( $\lambda x y. x + y$ ) 1 2');
> val it = |- ( $\lambda x y. x + y$ ) 1 2 = ( $\lambda(x,y). x + y$ ) (1,2) : thm
```

Failure

UNCURRY_CONV tm fails if tm is not double abstraction applied to two arguments

See also

PairRules.CURRY_CONV.

UNCURRY_EXISTS_CONV

(PairRules)

UNCURRY_EXISTS_CONV : conv

Synopsis

Uncurrys consecutive existential quantifications into a paired existential quantification.

Example

```

- UNCURRY_EXISTS_CONV (Term '?x y. x + y = y + x');
> val it = |- (?x y. x + y = y + x) = ?(x,y). x + y = y + x : thm

- UNCURRY_EXISTS_CONV (Term '?(w,x) (y,z). w+x+y+z = z+y+x+w');
> val it =
  |- (? (w,x) (y,z). w + x + y + z = z + y + x + w) =
    ?((w,x),y,z). w + x + y + z = z + y + x + w : thm

```

Failure

UNCURRY_EXISTS_CONV tm fails if tm is not a consecutive existential quantification.

See also

PairRules.CURRY_CONV, PairRules.UNCURRY_CONV, PairRules.CURRY_EXISTS_CONV, PairRules.CURRY_FORALL_CONV, PairRules.UNCURRY_FORALL_CONV.

UNCURRY_FORALL_CONV (PairRules)

UNCURRY_FORALL_CONV : conv

Synopsis

Uncurries consecutive universal quantifications into a paired universal quantification.

Example

```

- UNCURRY_FORALL_CONV (Term '!x y. x + y = y + x');
> val it = |- (!x y. x + y = y + x) = !(x,y). x + y = y + x : thm

- UNCURRY_FORALL_CONV (Term '! (w,x) (y,z). w+x+y+z = z+y+x+w');
> val it =
  |- (! (w,x) (y,z). w + x + y + z = z + y + x + w) =
    !((w,x),y,z). w + x + y + z = z + y + x + w : thm

```

Failure

UNCURRY_FORALL_CONV tm fails if tm is not a consecutive universal quantification.

See also

PairRules.CURRY_CONV, PairRules.UNCURRY_CONV, PairRules.CURRY_FORALL_CONV, PairRules.CURRY_EXISTS_CONV, PairRules.UNCURRY_EXISTS_CONV.

UNDISCH

(Drule)

UNDISCH : thm -> thm

Synopsis

Undischarges the antecedent of an implicative theorem.

Description

$$\frac{A \mid- t1 ==> t2}{A, t1 \mid- t2} \text{ UNDISCH}$$
Note that UNDISCH treats " $\sim u$ " as " $u ==> F$ ".**Failure**

UNDISCH will fail on theorems which are not implications or negations.

Comments

If the antecedent already appears in (or is alpha-equivalent to one of) the hypotheses, it will not be duplicated.

See also

Thm.DISCH, Drule.DISCH_ALL, Tactic.DISCH_TAC, Thm_cont.DISCH_THEN, Tactic.FILTER_DISCH_TAC, Thm_cont.FILTER_DISCH_THEN, Drule.NEG_DISCH, Tactic.STRIP_TAC, Drule.UNDISCH_ALL, Tactic.UNDISCH_TAC.

UNDISCH_ALL

(Drule)

UNDISCH_ALL : thm -> thm

Synopsis

Iteratively undischarges antecedents in a chain of implications.

Description

$$\frac{A \mid- t1 ==> \dots ==> tn ==> t}{A, t1, \dots, tn \mid- t} \text{ UNDISCH_ALL}$$

Note that `UNDISCH_ALL` treats "`~u`" as "`u ==> F`".

Failure

`UNDISCH_ALL` never fails. When called on something other than an implication or negation, it simply returns its argument unchanged.

Comments

Identical or alpha-equivalent terms which are repeated in `A`, "`t1`", ..., "`tn`" will not be duplicated in the hypotheses of the resulting theorem.

See also

`Thm.DISCH`, `Drule.DISCH_ALL`, `Tactic.DISCH_TAC`, `Thm.cont.DISCH_THEN`,
`Drule.NEG_DISCH`, `Tactic.FILTER_DISCH_TAC`, `Thm.cont.FILTER_DISCH_THEN`,
`Tactic.STRIP_TAC`, `Drule.UNDISCH`, `Tactic.UNDISCH_TAC`.

<code>UNDISCH_TAC</code>	<code>(Tactic)</code>
--------------------------	-----------------------

`UNDISCH_TAC` : `term -> tactic`

Synopsis

Undischarges an assumption.

Description

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \text{ UNDISCH_TAC } v \\ A - \{v\} \text{ ?- } v \text{ ==> } t \end{array}$$

Failure

`UNDISCH_TAC` will fail if "`v`" is not an assumption.

Comments

Undischarging `v` will remove all assumptions which are identical to `v`, but those which are alpha-equivalent will remain.

See also

`Thm.DISCH`, `Drule.DISCH_ALL`, `Tactic.DISCH_TAC`, `Thm.cont.DISCH_THEN`,
`Drule.NEG_DISCH`, `Tactic.FILTER_DISCH_TAC`, `Thm.cont.FILTER_DISCH_THEN`,
`Tactic.STRIP_TAC`, `Drule.UNDISCH`, `Drule.UNDISCH_ALL`.

UNDISCH_THEN

(Thm_cont)

```
Thm_cont.UNDISCH_THEN : term -> thm_tactic -> tactic
```

Synopsis

Discharges the assumption given and passes it to a theorem-tactic.

Description

UNDISCH_THEN finds the first assumption equal to the term given, removes it from the assumption list, ASSUMES it, passes it to the theorem-tactic and then applies the consequent tactic. Thus:

```
UNDISCH_THEN t f ([a1,... ai, t, aj, ... an], goal) =
  f (ASSUME t) ([a1,... ai, aj,... an], goal)
```

For example, if

```
A u {t1} ?- t
===== f (ASSUME t1)
B u {t1} ?- v
```

then

```
A u {t1} ?- t
===== UNDISCH_THEN t1 f
B ?- v
```

Failure

UNDISCH_THEN will fail on goals where the given term is not in the assumption list.

See also

Tactical.PAT_ASSUM, Thm.DISCH, Drule.DISCH_ALL, Tactic.DISCH_TAC,
Thm_cont.DISCH_THEN, Drule.NEG_DISCH, Tactic.FILTER_DISCH_TAC,
Thm_cont.FILTER_DISCH_THEN, Tactic.STRIP_TAC, Drule.UNDISCH, Drule.UNDISCH_ALL,
Tactic.UNDISCH_TAC.

UNFOLD_CONV

(unwindLib)

```
UNFOLD_CONV : (thm list -> conv)
```

Synopsis

Expands sub-components of a hardware description using their definitions.

Description

UNFOLD_CONV th1 "t1 /\ ... /\ tn" returns a theorem of the form:

$$B \mid\text{- } t_1 \wedge \dots \wedge t_n = t_1' \wedge \dots \wedge t_n'$$

where each t_i' is the result of rewriting t_i with the theorems in th1. The set of assumptions B is the union of the instantiated assumptions of the theorems used for rewriting. If none of the rewrites are applicable to a t_i , it is unchanged.

Failure

Never fails.

Example

```
#UNFOLD_CONV [ASSUME "!in out. INV (in,out) = !(t:num). out t = ~(in t)"]
# "INV (11,12) /\ INV (12,13) /\ (!(t:num). 11 t = 12 (t-1) \/ 13 (t-1))";;
. \|- INV(11,12) /\ INV(12,13) /\ (!t. 11 t = 12(t - 1) \/ 13(t - 1)) =
    (!t. 12 t = ~11 t) /\
    (!t. 13 t = ~12 t) /\
    (!t. 11 t = 12(t - 1) \/ 13(t - 1))
```

See also

unwindLib.UNFOLD_RIGHT_RULE.

UNFOLD_RIGHT_RULE**(unwindLib)**

UNFOLD_RIGHT_RULE : (thm list -> thm -> thm)

Synopsis

Expands sub-components of a hardware description using their definitions.

Description

UNFOLD_RIGHT_RULE th1 behaves as follows:

$$\frac{A \mid\text{- } !z_1 \dots z_r. t = ?y_1 \dots y_p. t_1 \wedge \dots \wedge t_n}{B \cup A \mid\text{- } !z_1 \dots z_r. t = ?y_1 \dots y_p. t_1' \wedge \dots \wedge t_n'}$$

where each t_i' is the result of rewriting t_i with the theorems in $th1$. The set of assumptions B is the union of the instantiated assumptions of the theorems used for rewriting. If none of the rewrites are applicable to a t_i , it is unchanged.

Failure

Fails if the second argument is not of the required form, though either or both of r and p may be zero.

Example

```
#UNFOLD_RIGHT_RULE [ASSUME "!in out. INV(in,out) = !(t:num). out t = ~(in t)"]
# (ASSUME "(in:num->bool) out. BUF(in,out) = ?l. INV(in,l) /\ INV(l,out)");;
.. |- !in out.
      BUF(in,out) = (?l. (!t. l t = ~in t) /\ (!t. out t = ~l t))
```

See also

`unwindLib.UNFOLD_CONV.`

<div data-bbox="161 1113 314 1158" data-label="Text"> <p>union</p> </div>	<div data-bbox="1182 1108 1331 1160" data-label="Text"> <p>(Lib)</p> </div>
---	---

`union : 'a list -> 'a list -> 'a list`

Synopsis

Computes the union of two 'sets'.

Description

If $l1$ and $l2$ are both 'sets' (lists with no repeated members), `union l1 l2` returns the set union of $l1$ and $l2$. In the case that $l1$ or $l2$ is not a set, all the user can depend on is that `union l1 l2` returns a list $l3$ such that every unique element of $l1$ and $l2$ is in $l3$ and each element of $l3$ is found in either $l1$ or $l2$.

Failure

Never fails.

Example

```
- union [1,2,3] [1,5,4,3];
val it = [2,1,5,4,3] : int list
```

```
- union [1,1,1] [1,2,3,2];
val it = [1,2,3,2] : int list

- union [1,2,3,2] [1,1,1] ;
val it = [3,2,1,1,1] : int list
```

Comments

Do not make the assumption that the order of items in the list returned by `union` is fixed. Later implementations may use different algorithms, and return a different concrete result while still meeting the specification.

A high-performance implementation of finite sets may be found in structure `HOLset`.

ML equality types are used in the implementation of `union` and its kin. This limits its applicability to types that allow equality. For other types, typically abstract ones, use the ‘`op_`’ variants.

See also

`Lib.op_union`, `Lib.U`, `Lib.mk_set`, `Lib.mem`, `Lib.insert`, `Lib.set_eq`, `Lib.intersect`, `Lib.set_diff`, `Lib.subtract`.

<div data-bbox="234 1191 531 1243" data-label="Text"> <p><code>UNION_CONV</code></p> </div>	<div data-bbox="1032 1191 1412 1247" data-label="Text"> <p><code>(pred_setLib)</code></p> </div>
---	--

`UNION_CONV` : `conv -> conv`

Synopsis

Reduce $\{t_1; \dots; t_n\}$ UNION s to t_1 INSERT $(\dots (t_n$ INSERT $s))$.

Description

The function `UNION_CONV` is a parameterized conversion for reducing sets of the form $\{t_1; \dots; t_n\}$ UNION s , where $\{t_1; \dots; t_n\}$ and s are sets of type $ty \rightarrow bool$. The first argument to `UNION_CONV` is expected to be a conversion that decides equality between values of the base type ty . Given an equation $e_1 = e_2$, where e_1 and e_2 are terms of type ty , this conversion should return the theorem $\vdash (e_1 = e_2) = T$ or the theorem $\vdash (e_1 = e_2) = F$, as appropriate.

Given such a conversion, the function `UNION_CONV` returns a conversion that maps a term of the form $\{t_1; \dots; t_n\}$ UNION s to the theorem

$$\vdash \{t_1; \dots; t_n\} \text{ UNION } s = t_i \text{ INSERT } \dots (t_j \text{ INSERT } s)$$

where $\{t_i; \dots; t_j\}$ is the set of all terms t that occur as elements of $\{t_1; \dots; t_n\}$ for which the conversion `IN_CONV conv` fails to prove that $\vdash (t \text{ IN } s) = T$ (that is, either by proving $\vdash (t \text{ IN } s) = F$ instead, or by failing outright).

Example

In the following example, `REDUCE_CONV` is supplied as a parameter to `UNION_CONV` and used to test for membership of each element of the first finite set $\{1;2;3\}$ of the union in the second finite set $\{\text{SUC } 0;3;4\}$.

```
- UNION_CONV REDUCE_CONV (Term '{1;2;3} UNION {SUC 0;3;4}');
> val it = |- {1; 2; 3} UNION {SUC 0; 3; 4} = {2; SUC 0; 3; 4} : thm
```

The result is $\{2; \text{SUC } 0; 3; 4\}$, rather than $\{1; 2; \text{SUC } 0; 3; 4\}$, because `UNION_CONV` is able by means of a call to

```
- IN_CONV REDUCE_CONV (Term '1 IN {SUC 0;3;4}');
```

to prove that 1 is already an element of the set $\{\text{SUC } 0; 3; 4\}$.

The conversion supplied to `UNION_CONV` need not actually prove equality of elements, if simplification of the resulting set is not desired. For example:

```
- UNION_CONV NO_CONV '{1;2;3} UNION {SUC 0;3;4}';
> val it = |- {1;2;3} UNION {SUC 0;3;4} = {1;2;SUC 0;3;4} : thm
```

In this case, the resulting set is just left unsimplified. Moreover, the second set argument to `UNION` need not be a finite set:

```
- UNION_CONV NO_CONV '{1;2;3} UNION s';
> val it = |- {1;2;3} UNION s = 1 INSERT (2 INSERT (3 INSERT s)) : thm
```

And, of course, in this case the conversion argument to `UNION_CONV` is irrelevant.

Failure

`UNION_CONV conv` fails if applied to a term not of the form $\{t_1; \dots; t_n\} \text{ UNION } s$.

See also

`pred_setLib.IN_CONV`, `numLib.REDUCE_CONV`.

universal

(boolSyntax)

universal : term

Synopsis

Constant denoting universal quantification.

Description

The ML variable `boolSyntax.universal` is bound to the term `bool$!`.

See also

`boolSyntax.equality`, `boolSyntax.implication`, `boolSyntax.select`, `boolSyntax.T`, `boolSyntax.F`, `boolSyntax.universal`, `boolSyntax.existential`, `boolSyntax.exists1`, `boolSyntax.conjunction`, `boolSyntax.disjunction`, `boolSyntax.negation`, `boolSyntax.conditional`, `boolSyntax.bool_case`, `boolSyntax.let_tm`, `boolSyntax.arb`.

UNPBETA_CONV	(PairRules)
---------------------	--------------------

`UNPBETA_CONV` : (term -> conv)

Synopsis

Creates an application of a paired abstraction from a term.

Description

The user nominates some pair structure of variables `p` and a term `t`, and `UNPBETA_CONV` turns `t` into an abstraction on `p` applied to `p`.

```
----- UNPBETA_CONV "p" "t"
|- t = (\p. t) p
```

Failure

Fails if `p` is not a paired structure of variables.

See also

`PairRules.PBETA_CONV`, `PairedLambda.PAIRED_BETA_CONV`.

UNWIND_ALL_BUT_CONV	(unwindLib)
----------------------------	--------------------

`UNWIND_ALL_BUT_CONV` : (string list -> conv)

Synopsis

Unwinds all lines of a device (except those in the argument list) as much as possible.

Description

UNWIND_ALL_BUT_CONV 1 when applied to the following term:

```
"t1 /\ ... /\ eqn1 /\ ... /\ eqnm /\ ... /\ tn"
```

returns a theorem of the form:

```
|- t1 /\ ... /\ eqn1 /\ ... /\ eqnm /\ ... /\ tn =
   t1' /\ ... /\ eqn1 /\ ... /\ eqnm /\ ... /\ tn'
```

where t_i' (for $1 \leq i \leq n$) is t_i rewritten with the equations eqn_i ($1 \leq i \leq m$). These equations are those conjuncts with line name not in 1 (and which are equations).

Failure

Never fails but may loop indefinitely.

Example

```
#UNWIND_ALL_BUT_CONV ['12']
# "(!(x:num). l1 x = (l2 x) - 1) /\
# ( !x. f x = (l2 (x+1)) + (l1 (x+2))) /\
# ( !x. l2 x = 7)";;
|- ( !x. l1 x = (l2 x) - 1) /\
   ( !x. f x = (l2(x + 1)) + (l1(x + 2))) /\
   ( !x. l2 x = 7) =
   ( !x. l1 x = (l2 x) - 1) /\
   ( !x. f x = (l2(x + 1)) + ((l2(x + 2)) - 1)) /\
   ( !x. l2 x = 7)
```

See also

unwindLib.UNWIND_ONCE_CONV, unwindLib.UNWIND_CONV, unwindLib.UNWIND_AUTO_CONV, unwindLib.UNWIND_ALL_BUT_RIGHT_RULE, unwindLib.UNWIND_AUTO_RIGHT_RULE.

UNWIND_ALL_BUT_RIGHT_RULE	(unwindLib)
---------------------------	-------------

UNWIND_ALL_BUT_RIGHT_RULE : (string list -> thm -> thm)

Synopsis

Unwinds all lines of a device (except those in the argument list) as much as possible.

Description

UNWIND_ALL_BUT_RIGHT_RULE *l* behaves as follows:

```

A |- !z1 ... zr.
    t =
      (?l1 ... lp. t1 /\ ... /\ eqn1 /\ ... /\ eqnm /\ ... /\ tn)
-----
A |- !z1 ... zr.
    t =
      (?l1 ... lp. t1' /\ ... /\ eqn1 /\ ... /\ eqnm /\ ... /\ tn')

```

where t_i' (for $1 \leq i \leq n$) is t_i rewritten with the equations eqn_i ($1 \leq i \leq m$). These equations are those conjuncts with line name not in *l* (and which are equations).

Failure

Fails if the argument theorem is not of the required form, though either or both of *p* and *r* may be zero. May loop indefinitely.

Example

```

#UNWIND_ALL_BUT_RIGHT_RULE ['12']
# (ASSUME
#   "!f. IMP(f) =
#     ?12 l1.
#     (!x:num). l1 x = (12 x) - 1) /\
#     (!x. f x = (12 (x+1)) + (l1 (x+2))) /\
#     (!x. 12 x = 7)");;
. |- !f.
  IMP f =
    (?12 l1.
      (!x. l1 x = (12 x) - 1) /\
      (!x. f x = (12(x + 1)) + ((12(x + 2)) - 1)) /\
      (!x. 12 x = 7))

```

See also

unwindLib.UNWIND_AUTO_RIGHT_RULE, unwindLib.UNWIND_ALL_BUT_CONV,
 unwindLib.UNWIND_AUTO_CONV, unwindLib.UNWIND_ONCE_CONV, unwindLib.UNWIND_CONV.

UNWIND_AUTO_CONV

(unwindLib)

UNWIND_AUTO_CONV : conv

Synopsis

Automatic unwinding of equations defining wire values in a standard device specification.

Description

UNWIND_AUTO_CONV "?l1 ... lm. t1 /\ ... /\ tn" returns a theorem of the form:

$$|- (?l1 ... lm. t1 /\ ... /\ tn) = (?l1 ... lm. t1' /\ ... /\ tn')$$

where t_j' is t_j rewritten with equations selected from the t_i 's.

The function decides which equations to use for rewriting by performing a loop analysis on the graph representing the dependencies of the lines. By this means the term can be unwound as much as possible without the risk of looping. The user is left to deal with the recursive equations.

Failure

Fails if there is more than one equation for any line variable.

Example

```
#UNWIND_AUTO_CONV
# "(!(x:num). l1 x = (l2 x) - 1) /\
#  (!x. f x = (l2 (x+1)) + (l1 (x+2))) /\
#  (!x. l2 x = 7)";;
|- (!x. l1 x = (l2 x) - 1) /\
   (!x. f x = (l2(x + 1)) + (l1(x + 2))) /\
   (!x. l2 x = 7) =
   (!x. l1 x = 7 - 1) /\ (!x. f x = 7 + (7 - 1)) /\ (!x. l2 x = 7)
```

See also

unwindLib.UNWIND_ONCE_CONV, unwindLib.UNWIND_CONV,
 unwindLib.UNWIND_ALL_BUT_CONV, unwindLib.UNWIND_ALL_BUT_RIGHT_RULE,
 unwindLib.UNWIND_AUTO_RIGHT_RULE.

UNWIND_AUTO_RIGHT_RULE

(unwindLib)

UNWIND_AUTO_RIGHT_RULE : (thm -> thm)

Synopsis

Automatic unwinding of equations defining wire values in a standard device specification.

Description

UNWIND_AUTO_RIGHT_RULE behaves as follows:

$$A \mid - !z_1 \dots z_r. t = ?l_1 \dots l_m. t_1 \wedge \dots \wedge t_n$$

$$A \mid - !z_1 \dots z_r. t = ?l_1 \dots l_m. t_1' \wedge \dots \wedge t_n'$$

where t_j' is t_j rewritten with equations selected from the t_i 's.

The function decides which equations to use for rewriting by performing a loop analysis on the graph representing the dependencies of the lines. By this means the term can be unwound as much as possible without the risk of looping. The user is left to deal with the recursive equations.

Failure

Fails if there is more than one equation for any line variable, or if the argument theorem is not of the required form, though either or both of m and r may be zero.

Example

```
#UNWIND_AUTO_RIGHT_RULE
# (ASSUME
#   "!f. IMP(f) =
#     ?l2 l1.
#     (!x:num). l1 x = (l2 x) - 1) /\
#     (!x. f x = (l2 (x+1)) + (l1 (x+2))) /\
#     (!x. l2 x = 7)");;
. |- !f.
  IMP f =
    (?l2 l1.
      (!x. l1 x = 7 - 1) /\ (!x. f x = 7 + (7 - 1)) /\ (!x. l2 x = 7))
```

See also

unwindLib.UNWIND_ALL_BUT_RIGHT_RULE, unwindLib.UNWIND_AUTO_CONV,
 unwindLib.UNWIND_ALL_BUT_CONV, unwindLib.UNWIND_ONCE_CONV,
 unwindLib.UNWIND_CONV.

UNWIND_CONV

(unwindLib)

UNWIND_CONV : ((term -> bool) -> conv)

Synopsis

Unwinds device behaviour using selected line equations until no change.

Description

UNWIND_CONV p "t1 /\ ... /\ eqn1 /\ ... /\ eqnm /\ ... /\ tn" returns a theorem of the form:

$$\begin{array}{l} |- t1 \ \wedge \ \dots \ \wedge \ eqn1 \ \wedge \ \dots \ \wedge \ eqnm \ \wedge \ \dots \ \wedge \ tn = \\ \quad t1' \ \wedge \ \dots \ \wedge \ eqn1 \ \wedge \ \dots \ \wedge \ eqnm \ \wedge \ \dots \ \wedge \ tn' \end{array}$$

where t_i' (for $1 \leq i \leq n$) is t_i rewritten with the equations eqn_i ($1 \leq i \leq m$). These equations are the conjuncts for which the predicate p is true. The t_i terms are the conjuncts for which p is false. The rewriting is repeated until no changes take place.

Failure

Never fails but may loop indefinitely.

Example

```
#UNWIND_CONV (\tm. mem (line_name tm) ['l1';'l2'])
# "(!(x:num). l1 x = (l2 x) - 1) /\
# (!x. f x = (l2 (x+1)) + (l1 (x+2))) /\
# (!x. l2 x = 7)";;
|- (!x. l1 x = (l2 x) - 1) /\
   (!x. f x = (l2(x + 1)) + (l1(x + 2))) /\
   (!x. l2 x = 7) =
   (!x. l1 x = (l2 x) - 1) /\ (!x. f x = 7 + (7 - 1)) /\ (!x. l2 x = 7)
```

See also

unwindLib.UNWIND_ONCE_CONV, unwindLib.UNWIND_ALL_BUT_CONV,
 unwindLib.UNWIND_AUTO_CONV, unwindLib.UNWIND_ALL_BUT_RIGHT_RULE,
 unwindLib.UNWIND_AUTO_RIGHT_RULE.

UNWIND_ONCE_CONV

(unwindLib)

```
UNWIND_ONCE_CONV : ((term -> bool) -> conv)
```

Synopsis

Basic conversion for parallel unwinding of equations defining wire values in a standard device specification.

Description

UNWIND_ONCE_CONV p tm unwinds the conjunction tm using the equations selected by the predicate p . tm should be a conjunction, equivalent under associative-commutative re-ordering to:

$$t_1 \wedge t_2 \wedge \dots \wedge t_n$$

p is used to partition the terms t_i for $1 \leq i \leq n$ into two disjoint sets:

$$\begin{aligned} \text{REW} &= \{t_i \mid p \ t_i\} \\ \text{OBJ} &= \{t_i \mid \sim p \ t_i\} \end{aligned}$$

The terms t_i for which p is true are then used as a set of rewrite rules (thus they should be equations) to do a single top-down parallel rewrite of the remaining terms. The rewritten terms take the place of the original terms in the input conjunction. For example, if tm is:

$$t_1 \wedge t_2 \wedge t_3 \wedge t_4$$

and $\text{REW} = \{t_1, t_3\}$ then the result is:

$$\vdash t_1 \wedge t_2 \wedge t_3 \wedge t_4 = t_1 \wedge t_2' \wedge t_3 \wedge t_4'$$

where t_i' is t_i rewritten with the equations REW .

Failure

Never fails.

Example

```
#UNWIND_ONCE_CONV (\tm. mem (line_name tm) ['11';'12'])
# "(!(x:num). 11 x = (12 x) - 1) /\
# (!x. f x = (12 (x+1)) + (11 (x+2))) /\
# (!x. 12 x = 7)";;
```



```
|- (!x. 11 x = (12 x) - 1) /\
    (!x. f x = (12(x + 1)) + (11(x + 2))) /\
    (!x. 12 x = 7) =
    (!x. 11 x = (12 x) - 1) /\
    (!x. f x = 7 + ((12(x + 2)) - 1)) /\
    (!x. 12 x = 7)
```

See also

unwindLib.UNWIND_CONV, unwindLib.UNWIND_ALL_BUT_CONV,
 unwindLib.UNWIND_AUTO_CONV, unwindLib.UNWIND_ALL_BUT_RIGHT_RULE,
 unwindLib.UNWIND_AUTO_RIGHT_RULE.

unzip	(Lib)
-------	-------

unzip : ('a * 'b) list -> ('a list * 'b list)

Synopsis

Converts a list of pairs into a pair of lists.

Description

unzip [(x1,y1), ..., (xn,yn)] returns ([x1, ..., xn], [y1, ..., yn]).

Failure

Never fails.

Comments

Identical to Lib.split.

See also

Lib.split, Lib.zip, Lib.combine.

update_overload_maps	(Parse)
----------------------	---------

```
update_overload_maps :
  string -> ({Name : string, Thy : string} list *
            {Name : string, Thy : string} list) -> unit
```

Synopsis

Adds to the parser's overloading maps.

Description

The parser/pretty-printer for terms maintains two maps between constants and strings. From strings to terms, the map is from one string to a set of terms. Each term represents a possible overloading for the string. In the other direction, a term maps to just one string, its preferred representation.

The function `update_overload_maps` adds to (potentially overriding old mappings in) both of these maps. Its first parameter, a string, is the string involved in both directions. The two lists of `Name-Thy` records specify terms for the two maps. The first component of the tuple, specifies terms that the string will be overloaded to. (Note that it is perfectly reasonable to "overload" to just one term, and that this is the default situation for newly defined constants.)

The second component of the tuple sets the given string as the preferred identifier for the given terms.

Failure

Fails if any of the `Name-Thy` pairs doesn't correspond to an actual constant.

See also

`Parse.clear_overloads_on`, `Parse.hide`, `Parse.overload_on`,
`Parse.remove_ovl_mapping`, `Parse.reveal`.

<code>upto</code>	<code>(Lib)</code>
-------------------	--------------------

```
upto : int -> int -> int list
```

Synopsis

Builds a list of integers

Description

An invocation `upto b t` returns the list `[b, b+1, ..., t]`, if `b <= t`. Otherwise, the empty list is returned.

Failure

Never fails.

Example

```
- upto 2 10;
> val it = [2,3,4,5,6,7,8,9,10]
```

<div data-bbox="161 351 542 405" data-label="Text">uptodate_term</div>	<div data-bbox="1096 347 1331 405" data-label="Text">(Theory)</div>
--	---

```
uptodate_term : term -> bool
```

Synopsis

Tells if a term is out of date.

Description

Operations in the current theory segment of HOL allow one to redefine types and constants. This can cause theorems to become invalid. As a result, HOL has a rudimentary consistency maintenance system built around the notion of whether type operators and term constants are “up-to-date”.

An invocation `uptodate_term M` checks `M` to see if it has been built from any out-of-date components. The definition of `out-of-date` is mutually recursive among types, terms, and theorems. If `M` is a variable, it is out-of-date if its type is out-of-date. If `M` is a constant, it is out-of-date if it has been redeclared, or if its type is out-of-date, or if the witness theorem used to justify its existence is out-of-date. If `M` is a combination, it is out-of-date if either of its components are out-of-date. If `M` is an abstraction, it is out-of-date if either the bound variable or the body is out-of-date.

All items from ancestor theories are fixed, and unable to be overwritten, thus are always up-to-date.

Failure

Never fails.

Example

```
- Define 'fact x = if x=0 then 1 else x * fact (x-1)';
Equations stored under "fact_def".
Induction stored under "fact_ind".
> val it = |- fact x = (if x = 0 then 1 else x * fact (x - 1)) : thm

- val M = Term '!x. 0 < fact x';
> val M = '!x. 0 < fact x' : term

- uptodate_term M;
> val it = true : bool

- delete_const "fact";
```

```
> val it = () : unit

- uptodate_term M;
> val it = false : bool
```

See also

Theory.uptodate_type, Theory.uptodate_thm.

uptodate_thm

(Theory)

```
uptodate_thm : thm -> bool
```

Synopsis

Tells if a theorem is out of date.

Description

Operations in the current theory segment of HOL allow one to redefine types and constants. This can cause theorems to become invalid. As a result, HOL has a rudimentary consistency maintenance system built around the notion of whether type operators and term constants are "up-to-date".

An invocation `uptodate_thm th` should check `th` to see if it has been proved from any out-of-date components. However, HOL does not currently keep the proofs of theorems, so a simpler approach is taken. Instead, `th` is checked to see if its hypotheses and conclusions are up-to-date.

All items from ancestor theories are fixed, and unable to be overwritten, thus are always up-to-date.

Failure

Never fails.

Example

```
- Define 'fact x = if x=0 then 1 else x * fact (x-1)';
Equations stored under "fact_def".
Induction stored under "fact_ind".
> val it = |- fact x = (if x = 0 then 1 else x * fact (x - 1)) : thm

- val th = EVAL (Term 'fact 3');
```

```

> val th = |- fact 3 = 6 : thm

- uptodate_thm th;
> val it = true : bool

- delete_const "fact";
> val it = () : unit

- uptodate_thm th;
> val it = false : bool

```

Comments

It may happen that a theorem `th` is proved with the use of another theorem `th1` that subsequently becomes garbage because a constant `c` was deleted. If `c` does not occur in `th`, then `th` does not become garbage, which may be contrary to expectation. The conservative extension property of HOL says that `th` is still provable, even in the absence of `c`.

See also

`Theory.uptodate_type`, `Theory.uptodate_term`, `Theory.delete_const`, `Theory.delete_type`.

uptodate_type
--

(Theory)

```
uptodate_type : hol_type -> bool
```

Synopsis

Tells if a type is out of date.

Description

Operations in the current theory segment of HOL allow one to redefine types and constants. This can cause theorems to become invalid. As a result, HOL has a rudimentary consistency maintenance system built around the notion of whether type operators and term constants are "up-to-date".

An invocation `uptodate_type ty`, checks `ty` to see if it has been built from any out of date components, returning `false` just in case it has. The definition of out-of-date is mutually recursive among types, terms, and theorems. A type variable never out-of-date. A compound type is out-of-date if either (a) its type operator is out-of-date,

or (b) any of its argument types are out-of-date. A type operator is out-of-date if it has been re-declared or if the witness theorem used to justify the type in the call to `new_type_definition` is out-of-date. Only a component of the current theory segment may be out-of-date. All items from ancestor theories are fixed, and unable to be overwritten, thus are always up-to-date.

Failure

Never fails.

Example

```
- Hol_datatype 'foo = A | B of 'a';
<<HOL message: Defined type: "foo">>
> val it = () : unit

- val ty = Type ':'a foo list';
> val ty = ':'a foo list' : hol_type

- uptodate_type ty;
> val it = true : bool

- delete_type "foo";
> val it = () : unit

- uptodate_type ty;
> val it = false : bool
```

See also

`Theory.uptodate_term`, `Theory.uptodate_thm`.

VALID	(Tactical)
--------------	-------------------

`VALID : tactic -> tactic`

Synopsis

Makes a tactic fail if it would otherwise return an invalid proof.

Description

If `tac` applied to the goal $(as1, g)$ produces a justification that does not create a theorem $A \vdash g$, with A a subset of $as1$, then `VALID tac (as1, g)` fails (raises an exception). If `tac` produces a valid proof on the goal, then the behaviour of `VALID tac (as1, g)` is the same

Failure

Fails by design if its argument produces an invalid proof when applied to a goal. Also fails if its argument fails when applied to the given proof.

See also

`proofManagerLib.expand`.

<code>var_compare</code>	<code>(Term)</code>
--------------------------	---------------------

```
var_compare : term * term -> order
```

Synopsis

Total ordering on variables.

Description

An invocation `var_compare (v1, v2)` will return one of `{LESS, EQUAL, GREATER}`, according to an ordering on term variables. The ordering is transitive and total.

Failure

If `v1` and `v2` are not both variables.

Example

```
- var_compare (mk_var("x", bool), mk_var("x", bool --> bool));
> val it = LESS : order
```

Comments

Used to build high performance datastructures for dealing with sets having many variables.

See also

`Term.empty_varset`, `Term.compare`.

var_occurs**(Term)**

```
var_occurs : term -> term -> bool
```

Synopsis

Check if a variable occurs in free in a term.

Description

An invocation `var_occurs v M` returns `true` just in case `v` occurs free in `M`.

Failure

If the first argument is not a variable.

Example

```
- var_occurs (Term'x:bool') (Term 'a /\ b ==> x');
> val it = true : bool
```

```
- var_occurs (Term'x:bool') (Term '!x. a /\ b ==> x');
> val it = false : bool
```

Comments

Identical to `free_in`, except for the requirement that the first argument be a variable.

See also

`Term.free_vars`, `Term.free_in`.

variant**(Term)**

```
variant : term list -> term -> term
```

Synopsis

Modifies a variable name to avoid clashes.

Description

When applied to a list of variables to avoid clashing with, and a variable to modify, `variant` returns a variant of the variable to modify, that is, it changes the name as

intuitively as possible to make it distinct from any variables in the list, or any constants. This is normally done by adding primes to the name.

The exact form of the variable name should not be relied on, except that the original variable will be returned unmodified unless it is itself in the list to avoid clashing with, or if it is the name of a constant.

Failure

`variant l t` fails if any term in the list `l` is not a variable or if `t` is not a variable.

Example

The following shows a couple of typical cases:

```
- variant [Term'y:bool', Term'z:bool'] (Term'x:bool');
> val it = 'x' : term

- variant [Term'x:bool', Term'x':num', Term'x'':num'] (Term 'x:bool');
> val it = 'x'''' : term
```

while the following shows that clashes with the names of constants are also avoided:

```
- variant [] (mk_var("T",bool));
> val it = 'T' : term
```

The style of renaming can be altered by modifying the reference variable `Globals.priming`:

```
- with_flag (priming,SOME "_")
  (uncurry variant)
  ([Term'x:bool', Term'x':num', Term'x'':num'], Term 'x:bool');

> val it = 'x_1' : term
```

Uses

The function `variant` is extremely useful for complicated derived rules which need to rename variables to avoid free variable capture while still making the role of the variable obvious to the user.

See also

`Term.genvar`, `Term.prim_variant`, `Globals.priming`.

<div data-bbox="161 1827 370 1877" data-label="Text"> <p><code>version</code></p> </div>	<div data-bbox="1069 1823 1332 1879" data-label="Text"> <p>(Globals)</p> </div>
--	---

`Globals.version` : int

Synopsis

The version number of the HOL system being run.

Example

```
- Globals.version;
> val it = 2 : int
```

See also

Globals.release.

W	(Lib)
---	-------

$W : ('a \rightarrow 'a \rightarrow 'b) \rightarrow 'a \rightarrow 'b$

Synopsis

Duplicates function argument : $W f x$ equals $f x x$.

Description

The W combinator can be understood as a planner: in the application $f x x$, the function f can scrutinize x and generate a function that then gets applied to x .

Failure

$W f$ never fails. $W f x$ fails if $f x$ fails or if $f x x$ fails.

Example

```
- load "tautLib";
- tautLib.TAUT_PROVE (Term '(a = b) = (~a = ~b)');
> val it = |- (a = b) = (~a = ~b) : thm

- W (GENL o free_vars o concl) it;
> val it = |- !b a. (a = b) = (~a = ~b) : thm
```

See also

Lib.##, Lib.A, Lib.B, Lib.C, Lib.I, Lib.K, Lib.S.

WARNING_outstream**(Feedback)**

WARNING_outstream : TextIO.outstream ref

Synopsis

Controlling output stream used when printing HOL_WARNING

Description

The value of reference cell WARNING_outstream controls where HOL_WARNING prints its argument.

The default value of WARNING_outstream is TextIO.stdOut.

Example

```
- val ostrm = TextIO.openOut "foo";
> val ostrm = <ostream> : ostream

- WARNING_outstream := ostrm;
> val it = () : unit

- HOL_WARNING "Module" "Function" "Sufferin' Succotash!";
> val it = () : unit

- TextIO.closeOut ostrm;
> val it = () : unit

- val istrm = TextIO.openIn "foo";
> val istrm = <instream> : instream

- print (TextIO.inputAll istrm);
<<HOL warning: Module.Function: Sufferin' Succotash!>>
```

See also

Feedback, Feedback.HOL_WARNING, Feedback.ERR_outstream, Feedback.MESG_outstream, Feedback.emit_WARNING.

WARNING_to_string

(Feedback)

WARNING_to_string : (string -> string -> string -> string) ref

Synopsis

Alterable function for formatting HOL_WARNING

Description

WARNING_to_string is a reference to a function for formatting the argument to HOL_WARNING.

The default value of WARNING_to_string is format_WARNING.

Example

```
- fun alt_WARNING_report s t u =
    String.concat["WARNING---", s, ".", t, ": ", u, "----END WARNING\n"];

- WARNING_to_string := alt_WARNING_report;

- HOL_WARNING "Foo" "bar" "Look out";
WARNING---Foo.bar: Look out---END WARNING
> val it = () : unit
```

See also

Feedback, Feedback.HOL_WARNING, Feedback.format_WARNING, Feedback.ERR_to_string, Feedback.MESG_to_string.

WEAKEN_CONSEQ_CONV_RULE

(ConseqConv)

WEAKEN_CONSEQ_CONV_RULE : (directed_conseq_conv -> thm -> thm)

Synopsis

Tries to weaken the conclusion of a theorem consisting of an implication.

Description

Given a theorem of the form $| - A ==> C$ and a directed consequence conversion c a call of WEAKEN_CONSEQ_CONV_RULE c thm tries to weaken C to a predicate wC using c . If it succeeds it returns the theorem $| - A ==> wC$.

See also

ConseqConv . STRENGTHEN_CONSEQ_CONV_RULE.

WEAKEN_TAC	(Tactic)
------------	----------

WEAKEN_TAC : (term -> bool) -> tactic

Synopsis

Deletes assumption from goal.

Description

Given an ML predicate P mapping terms to true or false and a goal $(as1, g)$, an invocation `WEAKEN_TAC P (as1, g)` removes the first element (call it tm) that P holds of from $as1$, returning the goal $(as1 - tm, g)$.

Failure

Fails if the assumption list of the goal is empty, or if P holds of no element in $as1$.

Example

Suppose we want to dispose of the equality assumption in the following goal:

```
C x
-----
0.  A = B
1.  B x
```

The following application of `WEAKEN_TAC` does the job.

```
- e (WEAKEN_TAC is_eq);
OK.
1 subgoal:
> val it =
  C x
  -----
  B x
```

Uses

Occasionally useful for getting rid of superfluous assumptions.

See also

Tactical.PAT_ASSUM, Tactical.POP_ASSUM.

WF_REL_TAC**(bossLib)**

WF_REL_TAC : term quotation -> tactic

Synopsis

Start termination proof.

Description

WF_REL_TAC builds a tactic that starts a termination proof. An invocation WF_REL_TAC *q*, where *q* should parse into a term that denotes a wellfounded relation, builds a tactic *tac* that is intended to be applied to a goal arising from an application of *tgoal* or *tprove*. Such a goal has the form

$$?R. \text{WF } R \wedge \dots$$

The tactic *tac* will instantiate *R* with the relation denoted by *q* and will attempt various simplifications of the goal. For example, it will try to automatically prove the well-foundedness of the relation denoted by *q*, and will also attempt to simplify the goal using some basic facts about well-founded relations. Often this can result in a much simpler goal.

Failure

WF_REL_TAC *q* fails if *q* does not parse into a term whose type is an instance of `'a -> 'a -> bool`.

Example

Suppose that a version of Quicksort had been defined as follows:

```
val qsort_defn =
  Hol_defn "qsort"
    '(qsort ___ [] = []) /\
    (qsort ord (x::rst) =
      APPEND (qsort ord (FILTER ($~ o ord x) rst))
              (x :: qsort ord (FILTER (ord x) rst)))';
```

Then one can start a termination proof as follows: set up a goalstack with *tgoal* and then apply WF_REL_TAC with a quotation denoting a suitable wellfounded relation.

```

- tgoal qsort_defn;
> val it =
  Proof manager status: 1 proof.
  1. Incomplete:
    Initial goal:
      ?R. WF R /\
        (!rst x ord. R (ord,FILTER ($~ o ord x) rst) (ord,x::rst)) /\
          !rst x ord. R (ord,FILTER (ord x) rst) (ord,x::rst)

- e (WF_REL_TAC 'measure (LENGTH o SND)');

```

OK..

2 subgoals:

```

> val it =
  !rst x ord. LENGTH (FILTER (ord x) rst) < LENGTH (x::rst)

  !rst x ord. LENGTH (FILTER (\x'. ~ord x x') rst) < LENGTH (x::rst)

```

Execution of WF_REL_TAC has automatically proved the wellfoundedness of

measure (LENGTH o SND)

and the remainder of the goal has been simplified into a pair of easy goals.

Comments

There are two problems to deal with when trying to prove termination. First, one has to understand, intuitively and then mathematically, why the function under consideration terminates. Second, one must be able to phrase this in HOL. In the following, we shall give a few examples of how this is done.

There are a number of basic and advanced means of specifying wellfounded relations. The most common starting point for dealing with termination problems for recursive functions is to find some function, known as a 'measure' under which the arguments of a function call are larger than the arguments to any recursive calls that result.

For a very simple starter example, consider the following definition of a function that computes the greatest common divisor of two numbers:

```

- val gcd_defn = Hol_defn "gcd"
  '(gcd (0,n) = n) /\
    (gcd (m,n) = gcd (n MOD m, m))';

- Defn.tgoal gcd_defn;

```

```

> val it =
  Proof manager status: 1 proof.
  1. Incomplete:
    Initial goal:
    ?R. WF R /\ !v2 n. R (n MOD SUC v2,SUC v2) (SUC v2,n)

```

The recursion happens in the first argument, and the recursive call in that position is a smaller number. The way to phrase the termination of `gcd` in HOL is to use a ‘measure’ function to map from the domain of `gcd`—a pair of numbers—to a number. The definition of `measure` is equivalent to

```
measure f x y = (f x < f y).
```

(The actual definition of `measure` in `prim_recTheory` is more primitive.) Now we must pick out the argument position to measure and invoke `WF_REL_TAC`:

```

- e (WF_REL_TAC 'measure FST');
OK..

```

```

1 subgoal:
> val it =
  !v2 n. n MOD SUC v2 < SUC v2

```

This goal is easy to prove with a few simple arithmetic facts:

```

- e (PROVE_TAC [arithmeticTheory.DIVISION, prim_recTheory.LESS_0]);
OK..

```

```
Goal proved. ...
```

Sometimes one needs a measure function that is itself recursive. For example, consider a type of binary trees and a function that ‘unbalances’ trees. The algorithm works by rotating the tree until it gets a `Leaf` in the left branch, then it recurses into the right branch. At the end of execution the tree has been linearized.

```

- Hol_datatype
  'btree = Leaf
    | Brh of btree => btree';

- val Unbal_defn =
  Hol_defn "Unbal"
  '(Unbal Leaf = Leaf)
  /\ (Unbal (Brh Leaf bt) = Brh Leaf (Unbal bt))

```



```

/\ (Unbal (Brh (Brh bt1 bt2) bt) = Unbal (Brh bt1 (Brh bt2 bt)))';

- Defn.tgoal Unbal_defn;

> val it =
  Proof manager status: 1 proof.
  1. Incomplete:
    Initial goal:
      ?R. WF R /\
          (!bt. R bt (Brh Leaf bt)) /\
          !bt bt2 bt1. R (Brh bt1 (Brh bt2 bt)) (Brh (Brh bt1 bt2) bt)

```

Since the size of the tree is unchanged in the last clause in the definition of `Unbal`, a simple size measure will not work. Instead, we can assign weights to nodes in the tree such that the recursive calls of `Unbal` decrease the total weight in every case. One such assignment is

```

Weight (Leaf) = 0
Weight (Brh x y) = (2 * Weight x) + (Weight y) + 1

```

It is easiest to use `Define` to define `Weight`, but if one is worried about "polluting" the signature, one can also use `prove_rec_fn_exists` from the `Prim_rec` structure:

```

val Weight =
  Prim_rec.prove_rec_fn_exists (TypeBase.axiom_of ("", "btree"))
  (Term'(Weight (Leaf) = 0) /\
    (Weight (Brh x y) = (2 * Weight x) + (Weight y) + 1)');

> val Weight =
  |- ?Weight.
    (Weight Leaf = 0) /\
    !x y. Weight (Brh x y) = 2 * Weight x + Weight y + 1 : thm

- e (STRIP_ASSUME_TAC Weight);
OK..

```

```

1 subgoal:
> val it =
  ?R.
    WF R /\ (!bt. R bt (Brh Leaf bt)) /\
    !bt bt2 bt1. R (Brh bt1 (Brh bt2 bt)) (Brh (Brh bt1 bt2) bt)
-----

```

0. Weight Leaf = 0
1. !x y. Weight (Brh x y) = 2 * Weight x + Weight y + 1

Now we can invoke WF_REL_TAC:

```
e (WF_REL_TAC 'measure Weight');
OK..

2 subgoals:
> val it =
!bt bt2 bt1.
  Weight (Brh bt1 (Brh bt2 bt)) < Weight (Brh (Brh bt1 bt2) bt)
-----
0. Weight Leaf = 0
1. !x y. Weight (Brh x y) = 2 * Weight x + Weight y + 1

!bt. Weight bt < Weight (Brh Leaf bt)
-----
0. Weight Leaf = 0
1. !x y. Weight (Brh x y) = 2 * Weight x + Weight y + 1
```

Both of these subgoals are quite easy to prove.

The technique of ‘weighting’ nodes in a tree in order to prove termination also goes by the name of ‘polynomial interpretation’. It must be admitted that finding the correct weighting for a termination proof is more an art than a science. Typically, one makes a guess and then tries the termination proof to see if it works.

Occasionally, there’s a combination of factors that complicate the termination argument. For example, the following specification describes a naive pattern matching algorithm on strings (represented as lists here). The function takes four arguments: the first is the remainder of the pattern being matched. The second is the remainder of the string being searched. The third argument holds the original pattern to be matched. The fourth argument is the string being searched. If the pattern (first argument) becomes exhausted, then a match has been found and the function returns T. Otherwise, if the string being searched becomes exhausted, the function returns F.

```
val match0_defn =
  Hol_defn "match0"
    '(match0 [] _ _ _ = T)
  /\ (match0 _ [] _ _ = F)
  /\ (match0 (p::pp) (s::ss) p0 rs =
      if p=s then match0 pp ss p0 rs else
      if NULL rs then F
```

```
else match0 p0 (TL rs) p0 (TL rs))';
```

```
- val match = Define 'match pat str = match0 pat str pat str';
```

The remaining case is when there's more searching to do; the function checks if the head of the pattern is the same as the head of the string being searched. If yes, then we recursively search, using the tail of the pattern and the tail of the string being searched. If no, that means that we have failed to match the pattern, so we should move one character ahead in the string being searched and try again. If the string being searched is empty, however, then we return `F`. The second and third arguments both represent the string being searched. The second argument is a kind of 'local' version of the string being searched; we recurse into it as long as there are matches with the pattern. However, if the search eventually fails, then the fourth argument, which 'remembers' where the search started from, is used to restart the search.

So much for the behaviour of the function. Why does it terminate? There are two recursive calls. The first call reduces the size of the first and second arguments, and leaves the other arguments unchanged. The second call can increase the size of the first and second arguments, but reduces the size of the fourth.

This is a classic situation in which to use a lexicographic ordering: some arguments to the function are reduced in some recursive calls, and some others are reduced in other recursive calls. Recall that `LEX` is an infix operator, defined in `pairTheory` as follows:

$$\text{LEX } R1 \ R2 = \lambda(x,y) (p,q). R1 \ x \ p \ \wedge \ ((x=p) \ /\ R2 \ y \ q)$$

In the second recursive call, the length of `rs` is reduced, and in the first it stays the same. This motivates having the length of the fourth argument be the first component of the lexicographic combination, and the length of the second argument as the second component.

What we need now is to formalize this. We want to map from the four-tuple of arguments into a lexicographic combination of relations. This is enabled by `inv_image` from `relationTheory`:

$$\text{inv_image } R \ f = \lambda x \ y. R \ (f \ x) \ (f \ y)$$

The actual relation maps from the four-tuple of arguments into a pair of numbers (m,n) , where m is the length of the fourth argument, and n is the length of the second argument. These lengths are then compared lexicographically with respect to less-than (`<`).

```
- Defn.tgoal match0_defn;
```

```
- e (WF_REL_TAC 'inv_image ($< LEX $<)
      (\(w,x,y,z). (LENGTH z, LENGTH x))');
```

```

OK..
2 subgoals:
> val it =
!rs ss s p.
  (p=s) ==> LENGTH rs < LENGTH rs \ / LENGTH ss < LENGTH (s::ss)

!ss rs s p.
  ~(p = s) /\ ~NULL rs ==>
  LENGTH (TL rs) < LENGTH rs \ /
  (LENGTH (TL rs) = LENGTH rs) /\ LENGTH (TL rs) < LENGTH (s::ss)

```

The first subgoal needs a case-split on `rs` before it is proved by rewriting, and the second is also easy to prove by rewriting.

As a final example, one occasionally needs to recurse over non-concrete data, such as finite sets or multisets. We can define a ‘fold’ function (of questionable utility) for finite sets as follows:

```

load "pred_setTheory"; open pred_setTheory;

val FOLD_SET_defn =
  Defn.Hol_defn "FOLD_SET"
  'FOLD_SET (s:'a->bool) (b:'b) =
    if FINITE s then
      if s={} then b
      else FOLD_SET (REST s) (f (CHOICE s) b)
    else ARB';

```

Typically, such functions terminate because the cardinality of the set (or multiset) is reduced in the recursive call, and this is another application of `measure`:

```

val (FOLD_SET_0, FOLD_SET_IND) =
  Defn.tprove (FOLD_SET_defn,
    WF_REL_TAC 'measure (CARD o FST)'
    THEN PROVE_TAC [CARD_PSUBSET, REST_PSUBSET]);

```

The desired recursion equation

```

|- FINITE s ==> (FOLD_SET f s b =
  if s = {} then b
  else FOLD_SET f (REST s) (f (CHOICE s) b))

```

is easy to obtain from FOLD_SET_0.

See also

Defn.tgoal, Defn.tprove, bossLib.Hol_defn.

WF_REL_TAC

(TotalDefn)

WF_REL_TAC : term quotation -> tactic

Synopsis

Initiate a termination proof.

Description

bossLib.WF_REL_TAC is identical to TotalDefn.WF_REL_TAC.

See also

bossLib.WF_REL_TAC.

with_exn

(Lib)

with_exn : ('a -> 'b) -> 'a -> exn -> 'b

Synopsis

Apply a function to an argument, raising supplied exception on failure.

Description

An evaluation of `with_exn f x e` applies function `f` to argument `x`. If that computation finishes with `y`, then `y` is the result. Otherwise, `f x` raised an exception, and the exception `e` is raised instead. However, if `f x` raises the `Interrupt` exception, then `with_exn f x e` results in the `Interrupt` exception being raised.

Failure

When `f x` fails or is interrupted.

Example

```
- with_exn dest_comb (Term'\x. x /\ y') (Fail "My kingdom for a horse");
! Uncaught exception:
! Fail "My kingdom for a horse"

- with_exn (fn _ => raise Interrupt) 1 (Fail "My kingdom for a horse");
> Interrupted.
```

Comments

Often `with_exn` can be used to clean up programming where lots of exceptions may be handled. For example, taking apart a compound term of a certain desired form may fail at several places, but a uniform error message is desired.

```
local val expected = mk_HOL_ERR "" "dest_quant" "expected !v.M or ?v.M"
in
fun dest_quant tm =
  let val (q,body) = with_exn dest_comb tm expected
      val (p as (v,M)) = with_exn dest_abs body expected
  in
    if q = universal orelse q = existential
    then p
    else raise expected
  end
end
```

See also

`Feedback.wrap_exn`, `Lib.assert_exn`, `Lib.assert`.

<div data-bbox="234 1532 504 1585" data-label="Text"> <p><code>with_flag</code></p> </div>	<div data-bbox="1260 1532 1412 1581" data-label="Text"> <p>(Lib)</p> </div>
--	---

```
with_flag : 'a ref * 'a -> ('b -> 'c) -> 'b -> 'c
```

Synopsis

Apply a function under a particular flag setting.

Description

An invocation `with_flag (r,v) f x` sets the reference variable `r` to the value `v`, then evaluates `f x`, then resets `r` to its original value, and returns the value of `f x`.

Failure

Fails if $f\ x$ fails. In that case, r is reset to its original value before raising the exception from $f\ x$.

Example

```
- fun print_term_nl tm = (print_term tm; print "\n");
> val print_term_nl = fn : term -> unit

- with_flag (show_types, true) print_term_nl (concl T_DEF);
T = ((\x :bool). x) = (\x :bool). x))
> val it = () : unit

- print_term_nl (concl T_DEF);
T = ((\x. x) = (\x. x))
> val it = () : unit
```

See also

`Feedback.traces`, `Feedback.register_btrace`, `Feedback.trace`, `Lib.time`.

WORD_ARITH_CONV	(wordsLib)
-----------------	------------

WORD_ARITH_CONV : conv

Synopsis

Conversion based on `WORD_ARITH_ss` and `WORD_ARITH_EQ_ss`.

Description

The conversion `WORD_ARITH_CONV` converts word arithmetic expressions into a canonical form.

Example

`WORD_ARITH_CONV` fixes the sign of equalities.

```
- SIMP_CONV (std_ss++WORD_ARITH_ss++WORD_ARITH_EQ_ss) [] ‘‘$- a = b : 'a word‘‘
> val it = |- ($- a = b) = ($- 1w * a + $- 1w * b = 0w) : thm

- WORD_ARITH_CONV ‘‘$- a = b : 'a word‘‘
> val it = |- ($- a = b) = (a + b = 0w) : thm
```

Comments

The fragment `WORD_ARITH_EQ_ss` and conversion `WORD_CONV` do not adjust the sign of equalities.

See also

`wordsLib.WORD_ARITH_ss`, `wordsLib.WORD_ARITH_EQ_ss`, `wordsLib.WORD_LOGIC_CONV`, `wordsLib.WORD_MUL_LSL_CONV`, `wordsLib.WORD_CONV`, `wordsLib.WORD_BIT_EQ_CONV`, `wordsLib.WORD_EVAL_CONV`.

<code>WORD_ARITH_EQ_ss</code>	<code>(wordsLib)</code>
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`WORD_ARITH_EQ_ss` : `ssfrag`

Synopsis

Simplification fragment for words.

Description

The fragment `WORD_ARITH_EQ_ss` simplifies ‘‘`a = b : 'a word`’’ to ‘‘`a - b = 0w`’’. It also simplifies using the theorems `WORD_LEFT_ADD_DISTRIB`, `WORD_RIGHT_ADD_DISTRIB`, `WORD_MUL_LSL` and `WORD_NOT`. When combined with `wordsLib.WORD_ARITH_ss` this fragment can be used to test for the arithmetic equality of words.

Example

```
- SIMP_CONV (std_ss++WORD_ARITH_ss++WORD_ARITH_EQ_ss) [] ‘‘3w * (a + b) = b + 3w *
<<HOL message: inventing new type variable names: 'a>>
> val it = |- (3w * (a + b) = b + 3w * a) = (2w * b = 0w) : thm
```

Comments

This fragment is not included in `WORDS_ss`.

See also

`wordsLib.WORD_ARITH_CONV`, `fcplib.FCP_ss`, `wordsLib.BIT_ss`, `wordsLib.SIZES_ss`, `wordsLib.WORD_ARITH_ss`, `wordsLib.WORD_LOGIC_ss`, `wordsLib.WORD_SHIFT_ss`, `wordsLib.WORD_BIT_EQ_ss`, `wordsLib.WORD_EXTRACT_ss`, `wordsLib.WORD_MUL_LSL_ss`, `wordsLib.WORD_ss`.

<code>WORD_ARITH_ss</code>	<code>(wordsLib)</code>
----------------------------	-------------------------

`WORD_ARITH_ss` : `ssfrag`

Synopsis

Simplification fragment for words.

Description

The fragment `WORD_ARITH_ss` does AC simplification for word multiplication, addition and subtraction. It also simplifies `INT_MINw`, `INT_MAXw` and `UINT_MAXw`. If the word length is known then further simplification may occur, in particular for $\$- (n2w\ n)$ and $w2n (n2w\ n)$.

Example

```
- SIMP_CONV (pure_ss++WORD_ARITH_ss) [] ‘‘3w * b + a + 2w * b - a * 4w‘‘
<<HOL message: inventing new type variable names: 'a'>>
> val it = |- 3w * b + a + 2w * b - a * 4w = $- 3w * a + 5w * b : thm
```

```
- SIMP_CONV (pure_ss++WORD_ARITH_ss) [] ‘‘INT_MINw + INT_MAXw + UINT_MAXw‘‘
<<HOL message: inventing new type variable names: 'a'>>
> val it = |- INT_MINw + INT_MAXw + UINT_MAXw = $- 2w : thm
```

More simplification occurs when the word length is known.

```
- SIMP_CONV (pure_ss++WORD_ARITH_ss) [] ‘‘3w * b + a + 2w * b - a * 4w:word2‘‘
> val it = |- 3w * b + a + 2w * b - a * 4w = a + b : thm
```

```
- SIMP_CONV (pure_ss++WORD_ARITH_ss) [] ‘‘w2n (33w:word4)‘‘;
> val it = |- w2n 33w = 1 : thm
```

Comments

Any term of value `UINT_MAXw` simplifies to $\$- 1w$ even when the word length is known - this helps when simplifying bitwise operations. If the word length is not known then `INT_MAXw` becomes `INT_MINw + $- 1w`.

See also

`wordsLib.WORD_ARITH_CONV`, `wordsLib.WORD_CONV`, `fcplib.FCP_ss`, `wordsLib.BIT_ss`, `wordsLib.SIZES_ss`, `wordsLib.WORD_LOGIC_ss`, `wordsLib.WORD_SHIFT_ss`, `wordsLib.WORD_ARITH_EQ_ss`, `wordsLib.WORD_BIT_EQ_ss`, `wordsLib.WORD_EXTRACT_ss`, `wordsLib.WORD_MUL_LSL_ss`, `wordsLib.WORD_ss`.

WORD_BIT_EQ_CONV

(wordsLib)

`WORD_BIT_EQ_CONV` : conv

Synopsis

Conversion based on `WORD_BIT_EQ_ss`.

Description

The conversion `WORD_BIT_EQ_CONV` performs simplification using `fcplib.FCP_ss`.

Example

```
- WORD_BIT_EQ_CONV ‘a << 2 >>> 1 = ((5 -- 0) a << 1) :word8‘
> val it = |- (a << 2 >>> 1 = (5 -- 0) a << 1) = T : thm
```

See also

`wordsLib.WORD_BIT_EQ_ss`, `wordsLib.WORD_ARITH_CONV`, `wordsLib.WORD_LOGIC_CONV`, `wordsLib.WORD_MUL_LSL_CONV`, `wordsLib.WORD_CONV`, `wordsLib.WORD_EVAL_CONV`.

`WORD_BIT_EQ_ss`

(`wordsLib`)

`WORD_BIT_EQ_ss` : `ssfrag`

Synopsis

Simplification fragment for words.

Description

The fragment `WORD_BIT_EQ_ss` simplifies using `fcplib.FCP_ss` and the definitions of "bitwise" operations, e.g., conjunction, disjunction, 1's complement, shifts, concatenation and sub-word extraction. Can be used in combination with decision procedures to test for the bitwise equality of words.

Example

```
- SIMP_CONV (std_ss++WORD_BIT_EQ_ss) [] ‘a = b : 'a word‘
> val it = |- (a = b) = !i. i < dimindex (:'a) ==> (a ' i = b ' i) : thm
```

Further simplification occurs when the word length is known.

```
- SIMP_CONV (std_ss++WORD_BIT_EQ_ss) [] ‘a = b : word2‘
> val it = |- (a = b) = (a ' 1 = b ' 1) /\ (a ' 0 = b ' 0) : thm
```

Best used in combination with decision procedures.

```
- (SIMP_CONV (std_ss++WORD_BIT_EQ_ss) [] THENC tautLib.TAUT_CONV) ‘‘a && b && a = a && b
<<HOL message: inventing new type variable names: 'a>>
> val it = |- (a && b && a = a && b) = T : thm
```

Comments

This fragment is not included in WORDS_{ss}.

See also

wordsLib.WORD_BIT_EQ_CONV, fcpLib.FCP_{ss}, wordsLib.BIT_{ss}, wordsLib.SIZES_{ss}, wordsLib.WORD_ARITH_{ss}, wordsLib.WORD_LOGIC_{ss}, wordsLib.WORD_SHIFT_{ss}, wordsLib.WORD_ARITH_EQ_{ss}, wordsLib.WORD_EXTRACT_{ss}, wordsLib.WORD_MUL_LSL_{ss}, wordsLib.WORD_{ss}.

WORD_CONV	(wordsLib)
-----------	------------

WORD_CONV : conv

Synopsis

Conversion for words.

Description

The conversion WORD_CONV applies the simpset fragment WORD_{ss}.

Example

```
- WORD_CONV ‘‘c * (a + b) !! (b + a) * c‘‘
<<HOL message: inventing new type variable names: 'a>>
> val it = |- c * (a + b) !! (b + a) * c = a * c + b * c : thm
```

See also

wordsLib.WORD_{ss}, wordsLib.WORD_ARITH_CONV, wordsLib.WORD_LOGIC_CONV, wordsLib.WORD_MUL_LSL_CONV, wordsLib.WORD_BIT_EQ_CONV, wordsLib.WORD_EVAL_CONV.

WORD_DECIDE	(wordsLib)
-------------	------------

WORD_DECIDE : conv

Synopsis

A decision procedure for words.

Description

The conversion `WORD_DECIDE` is the same as `WORD_DP WORD_CONV bossLib.DECIDE`.

Example

```

- WORD_DECIDE ‘‘a && (b !! a) = a !! a && b’’
<<HOL message: inventing new type variable names: 'a>>
> val it = |- a && (b !! a) = a !! a && b : thm

- WORD_DECIDE ‘‘a + 2w <+ 4w = a <+ 2w \ / 13w <+ a :word4’’
> val it = |- a + 2w <+ 4w = a <+ 2w \ / 13w <+ a : thm

- WORD_DECIDE ‘‘a < 0w = 1w <+ a : word2’’
> val it = |- a < 0w = 1w <+ a : thm

- WORD_DECIDE ‘‘(?w:word4. 14w <+ w) /\ ~(?w:word4. 15w <+ w)’’
> val it = |- (?w. 14w <+ w) /\ ~ ?w. 15w <+ w : thm

```

See also

`wordsLib.WORD_DP`.

WORD_DECIDE_TAC

(wordsLib)

`WORD_DECIDE_TAC : tactic`

Synopsis

A decision procedure tactic for words.

Description

`WORD_DECIDE_TAC` is a tactical version of `WORD_DECIDE`.

Failure

As for `WORD_DECIDE`.

See also

`wordsLib.WORD_DECIDE`.

WORD_DP

(wordsLib)

```
WORD_DP : conv -> conv -> conv
```

Synopsis

Constructs a decision procedure for words.

Description

The conversion `WORD_DP conv dp` is a decision procedure for words that makes use of the supplied conversion `conv` and decision procedure `dp`. Suitable decision procedures include `tautLib.TAUT_PROVE`, `bossLib.DECIDE`, `intLib.ARITH_PROVE` and `intLib.COOPER_PROVE`. The procedure will first apply `conv` and then `WORD_BIT_EQ_CONV`. If this is not sufficient then an attempt is made to solve the problem by applying an arithmetic decision procedure `dp`, e.g. `“(a = 0w) \\/ (a = 1w :1 word)”` is mapped to the goal `“(w2n a < 2 ==> (w2n a = 0) \\/ (w2n a = 1)”`.

Failure

The invocation will fail when the decision procedure `dp` fails.

Example

```
- wordsLib.WORD_DP ALL_CONV tautLib.TAUT_PROVE ‘‘a && b && a = a && b’’
<<HOL message: inventing new type variable names: 'a>>
> val it = |- a && b && a = a && b : thm
```

```
- wordsLib.WORD_DP ALL_CONV DECIDE ‘‘a < b /\ b < c ==> a < c : 'a word’’
> val it = |- a < b /\ b < c ==> a < c : thm
```

```
- wordsLib.WORD_DP ALL_CONV intLib.ARITH_PROVE ‘‘a <+ 3w:word16 ==> (a = 0w) \\/ (a = 1w)
> val it = |- a <+ 3w ==> (a = 0w) \\/ (a = 1w) \\/ (a = 2w) : thm
```

Comments

On large problems `intLib.ARITH_PROVE` will perform much better than `bossLib.DECIDE`.

See also

`wordsLib.WORD_BIT_EQ_CONV`, `wordsLib.WORD_DECIDE`.

<code>WORD_EVAL_CONV</code>	<code>(wordsLib)</code>
-----------------------------	-------------------------

`WORD_EVAL_CONV : conv`**Synopsis**

Evaluation for words.

Description

The conversion `WORD_EVAL_CONV` provides efficient evaluation for word operations. It uses `wordsLib.words_compset`.

Example

```
- WORD_EVAL_CONV ‘‘word_log2 (word_reverse (3w * (33w #<< 4))) : word32‘‘
> val it = |- word_log2 (word_reverse (3w * 33w #<< 4)) = 27w : thm
```

Comments

This conversion is best suited to evaluating ground terms with known word lengths. The conversion `wordsLib.WORD_CONV` is a suitable alternative.

See also

`bossLib.EVAL`, `computeLib.CBV_CONV`, `wordsLib.WORD_LOGIC_CONV`, `wordsLib.WORD_MUL_LSL_CONV`, `wordsLib.WORD_CONV`, `wordsLib.WORD_BIT_EQ_CONV`, `wordsLib.WORD_EVAL_CONV`.

<code>WORD_EXTRACT_SS</code>	<code>(wordsLib)</code>
------------------------------	-------------------------

`WORD_EXTRACT_SS : ssfrag`**Synopsis**

Simplification fragment for words.

Description

The fragment `WORD_EXTRACT_SS` simplifies the operations `w2w`, `sw2sw` (signed word-to-word conversion), `word_lsb`, `word_msb`, `word_bit`, `>>` (arithmetic right shift), `>>>` (logical right shift), `#>>` (rotate right), `#<<` (rotate left), `@@` (concatenation), `--` (word bits) and `''` (word slice). The result is expressed in terms of `!!` (disjunction), `<<` (left shift) and `><` (word extract).

Example

```

- SIMP_CONV (std_ss++WORD_ss++WORD_EXTRACT_ss) [] ‘‘(((7 >< 5) (a:word8)):3 word @@ ((4
> val it = |- (7 >< 5) a @@ (4 >< 0) a = a : thm

- SIMP_CONV (std_ss++WORD_ss++WORD_EXTRACT_ss) [] ‘‘(4 -- 2) ((a:word8) #>> 4)‘‘
> val it = |- (4 -- 2) (a #>> 4) = (7 >< 6) a !! (0 >< 0) a << 2 : thm

- SIMP_CONV (std_ss++WORD_ss++WORD_EXTRACT_ss) [] ‘‘w2w (sw2sw (a:word4):word8):word4‘‘
> val it = |- w2w (sw2sw a) = a : thm

```

Comments

Best used in combination with `WORD_ss`.

See also

`fcplib.FCP_ss`, `wordsLib.BIT_ss`, `wordsLib.SIZES_ss`, `wordsLib.WORD_ARITH_ss`,
`wordsLib.WORD_LOGIC_ss`, `wordsLib.WORD_ARITH_EQ_ss`, `wordsLib.WORD_BIT_EQ_ss`,
`wordsLib.WORD_SHIFT_ss`, `wordsLib.WORD_MUL_LSL_ss`, `wordsLib.WORD_ss`.

WORD_LOGIC_CONV	(wordsLib)
-----------------	------------

`WORD_LOGIC_CONV` : conv

Synopsis

Conversion based on `WORD_LOGIC_ss`.

Description

The conversion `WORD_LOGIC_CONV` converts word logic expressions into a canonical form.

Example

```

- WORD_LOGIC_CONV ‘‘a && (b !! ~a !! c)‘‘
<<HOL message: inventing new type variable names: 'a>>
> val it = |- a && (b !! ~a !! c) = a && b !! a && c : thm

```

See also

`wordsLib.WORD_LOGIC_ss`, `wordsLib.WORD_ARITH_CONV`, `wordsLib.WORD_MUL_LSL_CONV`,
`wordsLib.WORD_CONV`, `wordsLib.WORD_BIT_EQ_CONV`, `wordsLib.WORD_EVAL_CONV`.

WORD_LOGIC_ss	(wordsLib)
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WORD_LOGIC_ss : ssfrag

Synopsis

Simplification fragment for words.

Description

The fragment WORD_LOGIC_ss does AC simplification for word conjunction, disjunction and 1's complement (negation). If the word length is known then further simplification occurs, in particular for $\sim(n2w\ n)$.

Example

```
- SIMP_CONV (pure_ss++WORD_LOGIC_ss) [] ‘‘3w !! 12w && a !! ~4w !! a && 16w’’
<<HOL message: inventing new type variable names: 'a>>
> val it = |- 3w !! 12w && a !! ~4w !! a && 16w = 28w && a !! $- 5w : thm
```

More simplification occurs when the word length is known.

```
- SIMP_CONV (pure_ss++WORD_LOGIC_ss) [] ‘‘~12w !! ~14w : word8’’
> val it = |- ~12w !! ~14w = 243w : thm
```

Comments

The term $\$- 1w$ represents `UINT_MAXw`, which is the supremum in bitwise operations.

See also

wordsLib.WORD_LOGIC_CONV, wordsLib.WORD_CONV, fcpLib.FCP_ss, wordsLib.BIT_ss, wordsLib.SIZES_ss, wordsLib.WORD_ARITH_ss, wordsLib.WORD_SHIFT_ss, wordsLib.WORD_ARITH_EQ_ss, wordsLib.WORD_BIT_EQ_ss, wordsLib.WORD_EXTRACT_ss, wordsLib.WORD_MUL_LSL_ss, wordsLib.WORD_ss.

WORD_MUL_LSL_CONV	(wordsLib)
-------------------	------------

WORD_MUL_LSL_CONV : conv

Synopsis

Conversion based on WORD_MUL_LSL_ss.

Description

The conversion WORD_MUL_LSL_CONV converts a multiplication by a word literal into a sum of left shifts.

Example

```
- WORD_MUL_LSL_CONV ``49w * a``
> val it = |- 49w * a = a << 5 + a << 4 + a : thm
```

See also

wordsLib.WORD_MUL_LSL_ss, wordsLib.WORD_ARITH_CONV, wordsLib.WORD_LOGIC_CONV, wordsLib.WORD_CONV, wordsLib.WORD_BIT_EQ_CONV, wordsLib.WORD_EVAL_CONV.

WORD_MUL_LSL_ss	(wordsLib)
-----------------	------------

WORD_MUL_LSL_ss : ssfrag

Synopsis

Simplification fragment for words.

Description

The fragment WORD_MUL_LSL_ss simplifies a multiplication by a word literal into a sum of left shifts.

Example

```
- SIMP_CONV (std_ss++WORD_MUL_LSL_ss) [] ``49w * a``
> val it = |- 49w * a = a << 5 + a << 4 + a : thm

- SIMP_CONV (std_ss++WORD_ss++WORD_MUL_LSL_ss) [] ``2w * a + a << 1``
<<HOL message: inventing new type variable names: 'a>>
> val it = |- 2w * a + a << 1 = a << 2 : thm
```

Comments

This fragment is not included in WORDS_ss. It should not be used in combination with WORD_ARITH_EQ_ss or wordsLib.WORD_ARITH_CONV, since these convert left shifts into multiplications.

See also

wordsLib.WORD_MUL_LSL_CONV, fcpLib.FCP_ss, wordsLib.BIT_ss, wordsLib.SIZES_ss, wordsLib.WORD_ARITH_ss, wordsLib.WORD_LOGIC_ss, wordsLib.WORD_ARITH_EQ_ss, wordsLib.WORD_BIT_EQ_ss, wordsLib.WORD_SHIFT_ss, wordsLib.WORD_EXTRACT_ss, wordsLib.WORD_ss.

WORD_SHIFT_ss	(wordsLib)
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WORD_SHIFT_ss : ssfrag

Synopsis

Simplification fragment for words.

Description

The fragment WORD_SHIFT_ss does some basic simplifications for the operations: << (left shift), >> (arithmetic right shift), >>> (logical right shift), #>> (rotate right) and #<< (rotate left). More simplification is possible when used in combination with wordsLib.SIZES_ss.

Example

```
- SIMP_CONV (std_ss++WORD_SHIFT_ss) [] ‘‘a << 2 << 3 + a >> 3 >> 2 + a >>> 1 >>> 2
<<HOL message: inventing new type variable names: ‘a>>
> val it =
  |- a << 2 << 3 + a >> 3 >> 2 + a >>> 1 >>> 2 + a #<< 1 #<< 2 =
    a << 5 + a >> 5 + a >>> 3 + a #<< 3 : thm
```

```
- SIMP_CONV (std_ss++WORD_SHIFT_ss) [] ‘‘a >> 0 + 0w << n + a #<< 2 #>> 2‘‘
<<HOL message: inventing new type variable names: ‘a>>
> val it = |- a >> 0 + 0w << n + a #<< 2 #>> 2 = a + 0w + a : thm
```

More simplification is possible when the word length is known.

```
- SIMP_CONV (std_ss++SIZES_ss++WORD_SHIFT_ss) [] ‘‘a << 4 + (a #<< 6) : word4‘‘
> val it = |- a << 4 = 0w + a #<< 2 : thm
```

Comments

When the word length is known the fragment WORD_ss simplifies #<< to #>>.

See also

fcplib.FCP_ss, wordsLib.BIT_ss, wordsLib.SIZES_ss, wordsLib.WORD_ARITH_ss, wordsLib.WORD_LOGIC_ss, wordsLib.WORD_ARITH_EQ_ss, wordsLib.WORD_BIT_EQ_ss, wordsLib.WORD_EXTRACT_ss, wordsLib.WORD_MUL_LSL_ss, wordsLib.WORD_ss.

WORD_ss

(wordsLib)

WORD_ss : ssfrag

Synopsis

Simplification fragment for words.

Description

The fragment WORD_ss contains BIT_ss, SIZES_ss, WORD_LOGIC_ss, WORD_ARITH_ss and WORD_SHIFT_ss. It also performs ground term evaluation.

Example

```
- SIMP_CONV (pure_ss++WORD_ss) [] ``BIT i 42``
> val it = |- BIT i 42 = i IN {1; 3; 5} : thm

- SIMP_CONV (pure_ss++WORD_ss) [] ``dimword(:42)``
> val it = |- dimword (:42) = 4398046511104 : thm

- SIMP_CONV (pure_ss++WORD_ss) [] ``((a #<< 2 #>> 2 + a) && $- 1w) - a``
<<HOL message: inventing new type variable names: 'a>>
> val it = |- (a #<< 2 #>> 2 + a && $- 1w) - a = a : thm

- SIMP_CONV (pure_ss++WORD_ss) [] ``(4 -- 2) ($- 1w : word8)``
> val it = |- (4 -- 2) ($- 1w) = 7w : thm
```

Comments

The WORD_ss fragment does not include WORD_ARITH_EQ_ss, WORD_BIT_EQ_ss, WORD_EXTRACT_ss or WORD_MUL_LSL_ss. These extra fragments have more specialised applications.

See also

wordsLib.WORD_CONV, fcplib.FCP_ss, wordsLib.BIT_ss, wordsLib.SIZES_ss, wordsLib.WORD_ARITH_ss, wordsLib.WORD_LOGIC_ss, wordsLib.WORD_ARITH_EQ_ss, wordsLib.WORD_BIT_EQ_ss, wordsLib.WORD_SHIFT_ss, wordsLib.WORD_EXTRACT_ss, wordsLib.WORD_MUL_LSL_ss.

words2	(Lib)
--------	-------

```
words2 : string -> string -> string list
```

Synopsis

Splits a string into a list of substrings, breaking at occurrences of a specified character.

Description

`words2 char s` splits the string `s` into a list of substrings. Splitting occurs at each occurrence of a sequence of the character `char`. The `char` characters do not appear in the list of substrings. Leading and trailing occurrences of `char` are also thrown away. If `char` is not a single-character string (its length is not 1), then `s` will not be split and so the result will be the list `[s]`.

Failure

Never fails.

Example

```
- words2 "/" "/the/cat//sat/on//the/mat/";
> val it = ["the", "cat", "sat", "on", "the", "mat"] : string list

- words2 "/" "/the/cat//sat/on//the/mat/";
> val it = ["/the/cat//sat/on//the/mat/"] : string list
```

Comments

The SML Library functions `String.tokens` and `String.fields` offer similar functionality.

WORDS_EMIT_RULE	(wordsLib)
-----------------	------------

```
WORDS_EMIT_RULE : rule
```

Synopsis

For use with `EmitML.emitML`.

Description

When using `EmitML.emitML` the rule `WORDS_EMIT_RULE` should be applied to all definitions containing word operations. The rule introduces type annotated word operations and it also handles word equality and case statements.

Example

```
- val example_def = Define `example (w:1 word) = case w of 0w -> 1w:word8 || _ -> sw2sw
Definition has been stored under "example_def".
> val example_def = |- !w. example w = case w of 0w -> 1w || v -> sw2sw w : thm
- WORDS_EMIT_RULE example_def
> val it =
  |- !w.
    example w =
      case word_eq w (n2w_itself (0,(:unit))) of
        T -> n2w_itself (1,(:8))
      || F -> sw2sw_itself (:8) w : thm
```

Comments

Before using `EmitML.emitML` the references `type_pp.pp_num_types` and `type_pp.pp_array_types` should both be set to `false`. In addition type abbreviations can be disabled with `disable_tyabbrev_printing` or alternatively they must be handled by adding an appropriate signature entry. For example:

```
- ``:word8``
> val it = ``:bool[8]`` : hol_type
- type_pp.pp_array_types := false;
> val it = () : unit
- type_pp.pp_num_types := false;
> val it = () : unit
- disable_tyabbrev_printing "word8";
> val it = () : unit
- ``:word8``;
> val it = ``:unit bit0 bit0 bit0 word`` : hol_type
```

If the type abbreviation is not disabled then add the entry

```
EmitML.MLSIG "type word8 = wordsML.word8"
```

wrap_exn

(Feedback)

```
wrap_exn : string -> string -> exn -> exn
```

Synopsis

Adds supplementary information to an application of `HOL_ERR`.

Description

`wrap_exn s1 s2 (HOL_ERR{origin_structure,origin_function,message})` where `s1` typically denotes a structure and `s2` typically denotes a function, returns

```
HOL_ERR{origin_structure=s1,origin_function=s2,message}
```

where `origin_structure` and `origin_function` have been added to the `message` field. This can be used to achieve a kind of backtrace when an error occurs.

In MoscowML, the interrupt signal in Unix is mapped into the `Interrupt` exception. If `wrap_exn` were to translate an interrupt into a `HOL_ERR` exception, crucial information might be lost. For this reason, `wrap_exn s1 s2 Interrupt` raises the `Interrupt` exception.

Every other exception is mapped into an application of `HOL_ERR` by `wrap_exn`.

Failure

Never fails.

Example

In the following example, the original `HOL_ERR` is from `Foo.bar`. After `wrap_exn` is called, the `HOL_ERR` is from `Fred.barney` and its `message` field has been augmented to reflect the original source of the exception.

```
- val test_exn = mk_HOL_ERR "Foo" "bar" "incomprehensible input";
> val test_exn = HOL_ERR : exn
```

```
- wrap_exn "Fred" "barney" test_exn;
> val it = HOL_ERR : exn
```

```
- print(exn_to_string it);
```

```
Exception raised at Fred.barney:
Foo.bar - incomprehensible input
```

The following example shows how `wrap_exn` treats the `Interrupt` exception.

```
- wrap_exn "Fred" "barney" Interrupt;
> Interrupted.
```

The following example shows how `wrap_exn` translates all exceptions that aren't either `HOL_ERR` or `Interrupt` into applications of `HOL_ERR`.

```
- wrap_exn "Fred" "barney" Div;
> val it = HOL_ERR : exn

- print(exn_to_string it);
```

```
Exception raised at Fred.barney:
Div
```

See also

`Feedback`, `Feedback.HOL_ERR`.

<div data-bbox="159 956 512 1008" data-label="Text"> <h1 style="margin: 0;">X_CASES_THEN</h1> </div>	<div data-bbox="1038 956 1331 1008" data-label="Text"> <h1 style="margin: 0;">(Thm_cont)</h1> </div>
--	--

`X_CASES_THEN` : term list list -> thm_tactical

Synopsis

Applies a theorem-tactic to all disjuncts of a theorem, choosing witnesses.

Description

Let $[y_{11}, \dots, y_{1n}]$ represent a list of variable lists, each of length zero or more, and x_{11}, \dots, x_{1n} each represent a vector of zero or more variables, so that the variables in each of $y_{11} \dots y_{1n}$ have the same types as the corresponding x_{1i} . `X_CASES_THEN` expects such a list of variable lists, $[y_{11}, \dots, y_{1n}]$, a tactic generating function $f: \text{thm} \rightarrow \text{tactic}$, and a disjunctive theorem, where each disjunct may be existentially quantified:

$$\text{th} = \lambda \text{.} \lambda \text{.} (\exists x_{11}. B_1) \ \backslash / \dots \backslash / \ (\exists x_{1n}. B_n)$$

each disjunct having the form $(\exists x_{i1} \dots x_{im}. B_i)$. If applying f to the theorem obtained by introducing witness variables y_{li} for the objects x_{li} whose existence is asserted by each disjunct, typically $(\{B_i[y_{li}/x_{li}]\} \lambda \text{.} B_i[y_{li}/x_{li}])$, produce the following results when applied to a goal $(A \text{ ?- } t)$:

$$\begin{array}{l} A \text{ ?- } t \\ \text{===== } f \ (\{B_1[y_{11}/x_{11}]\} \lambda \text{.} B_1[y_{11}/x_{11}]) \\ A \text{ ?- } t_1 \end{array}$$

...

```
A ?- t
===== f ({Bn[yln/xln]} |- Bn[yln/xln])
A ?- tn
```

then applying (`X_CHOOSE_THEN [y11,...,yln] f th`) to the goal (`A ?- t`) produces n subgoals.

```
A ?- t
===== X_CHOOSE_THEN [y11,...,yln] f th
A ?- t1 ... A ?- tn
```

Failure

Fails (with `X_CHOOSE_THEN`) if any y_{1i} has more variables than the corresponding x_{1i} , or (with `SUBST`) if corresponding variables have different types. Failures may arise in the tactic-generating function. An invalid tactic is produced if any variable in any of the y_{1i} is free in the corresponding B_i or in t , or if the theorem has any hypothesis which is not alpha-convertible to an assumption of the goal.

Example

Given the goal `?- (x MOD 2) <= 1`, the following theorem may be used to split into 2 cases:

```
th = |- (?m. x = 2 * m) \/ (?m. x = (2 * m) + 1)
```

by the tactic

```
X_CASES_THEN [[Term'n:num'], [Term'n:num']] ASSUME_TAC th
```

to produce the subgoals:

```
{x = (2 * n) + 1} ?- (x MOD 2) <= 1
```

```
{x = 2 * n} ?- (x MOD 2) <= 1
```

See also

`Thm_cont.DISJ_CASES_THENL`, `Thm_cont.X_CASES_THENL`, `Thm_cont.X_CHOOSE_THEN`.

<div data-bbox="234 1823 617 1877" data-label="Text"> <p><code>X_CASES_THENL</code></p> </div>	<div data-bbox="1114 1823 1410 1877" data-label="Text"> <p><code>(Thm_cont)</code></p> </div>
--	---

`X_CASES_THENL : term list list -> thm_tactic list -> thm_tactic`

Synopsis

Applies theorem-tactics to corresponding disjuncts of a theorem, choosing witnesses.

Description

Let $[y_{11}, \dots, y_{1n}]$ represent a list of variable lists, each of length zero or more, and x_{11}, \dots, x_{1n} each represent a vector of zero or more variables, so that the variables in each of $y_{11} \dots y_{1n}$ have the same types as the corresponding x_{1i} . The function `X_CASES_THENL` expects a list of variable lists, $[y_{11}, \dots, y_{1n}]$, a list of tactic-generating functions $[f_1, \dots, f_n] : (\text{thm} \rightarrow \text{tactic}) \text{list}$, and a disjunctive theorem, where each disjunct may be existentially quantified:

$$\text{th} = \lambda \text{.} \lambda \text{.} (\exists x_{11}. B_1) \ \backslash / \dots \backslash / \ (\exists x_{1n}. B_n)$$

each disjunct having the form $(\exists x_{i1} \dots x_{im}. B_i)$. If applying each f_i to the theorem obtained by introducing witness variables y_{li} for the objects x_{li} whose existence is asserted by the i th disjunct, $(\{B_i[y_{li}/x_{li}]\} \vdash B_i[y_{li}/x_{li}])$, produces the following results when applied to a goal $(A \text{ ?- } t)$:

```

A ?- t
===== f1 ({B1[y11/x11]} |- B1[y11/x11])
A ?- t1

...

A ?- t
===== fn ({Bn[y1n/x1n]} |- Bn[y1n/x1n])
A ?- tn

```

then applying `X_CASES_THENL [y11, ..., y1n] [f1, ..., fn] th` to the goal $(A \text{ ?- } t)$ produces n subgoals.

```

A ?- t
===== X_CASES_THENL [y11, ..., y1n] [f1, ..., fn] th
A ?- t1 ... A ?- tn

```

Failure

Fails (with `X_CASES_THENL`) if any y_{li} has more variables than the corresponding x_{li} , or (with `SUBST`) if corresponding variables have different types, or (with `combine`) if the number of theorem tactics differs from the number of disjuncts. Failures may arise in the tactic-generating function. An invalid tactic is produced if any variable in any of the y_{li} is free in the corresponding B_i or in t , or if the theorem has any hypothesis which is not alpha-convertible to an assumption of the goal.

Example

Given the goal $?- (x \text{ MOD } 2) \leq 1$, the following theorem may be used to split into 2 cases:

$$\text{th} = |- (?m. x = 2 * m) \vee (?m. x = (2 * m) + 1)$$

by the tactic

$$\text{X_CASES_THENL} \text{ [[Term'n:num'], [Term'n:num']] [ASSUME_TAC, SUBST1_TAC] \text{ th}}$$

to produce the subgoals:

$$?- (((2 * n) + 1) \text{ MOD } 2) \leq 1$$

$$\{x = 2 * n\} ?- (x \text{ MOD } 2) \leq 1$$
See also

`Thm.cont.DISJ_CASES_THEN`, `Thm.cont.X_CASES_THEN`, `Thm.cont.X_CHOOSE_THEN`.

X_CHOOSE_TAC	(Tactic)
---------------------	-----------------

`X_CHOOSE_TAC` : `term -> thm_tactic`

Synopsis

Assumes a theorem, with existentially quantified variable replaced by a given witness.

Description

`X_CHOOSE_TAC` expects a variable y and theorem with an existentially quantified conclusion. When applied to a goal, it adds a new assumption obtained by introducing the variable y as a witness for the object x whose existence is asserted in the theorem.

$$\begin{array}{l} A \text{ ?- } \tau \\ \hline \text{X_CHOOSE_TAC } y \text{ (A1 } |- \text{ ?x. } w) \\ A \text{ u } \{w[y/x]\} \text{ ?- } \tau \quad \quad \quad (y \text{ not free anywhere}) \end{array}$$
Failure

Fails if the theorem's conclusion is not existentially quantified, or if the first argument is not a variable. Failures may arise in the tactic-generating function. An invalid tactic is produced if the introduced variable is free in w or τ , or if the theorem has any hypothesis which is not alpha-convertible to an assumption of the goal.

Example

Given a goal of the form

$$\{n < m\} \text{ ?- } ?x. m = n + (x + 1)$$

the following theorem may be applied:

$$\text{th} = [n < m] \text{ |- } ?p. m = n + p$$

by the tactic (X_CHOOSE_TAC (Term'q:num') th) giving the subgoal:

$$\{n < m, m = n + q\} \text{ ?- } ?x. m = n + (x + 1)$$

See also

Thm.CHOOSE, Thm.cont.CHOOSE_THEN, Thm.cont.X_CHOOSE_THEN.

<div data-bbox="159 913 539 967" data-label="Text"> <p>X_CHOOSE_THEN</p> </div>	<div data-bbox="1038 913 1331 967" data-label="Text"> <p>(Thm_cont)</p> </div>
---	--

X_CHOOSE_THEN : (term -> thm_tactical)

Synopsis

Replaces existentially quantified variable with given witness, and passes it to a theorem-tactic.

Description

X_CHOOSE_THEN expects a variable y , a tactic-generating function $f: \text{thm} \rightarrow \text{tactic}$, and a theorem of the form $(A1 \text{ |- } ?x. w)$ as arguments. A new theorem is created by introducing the given variable y as a witness for the object x whose existence is asserted in the original theorem, $(w[y/x] \text{ |- } w[y/x])$. If the tactic-generating function f applied to this theorem produces results as follows when applied to a goal $(A \text{ ?- } t)$:

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \quad f (\{w[y/x]\} \text{ |- } w[y/x]) \\ A \text{ ?- } t1 \end{array}$$

then applying (X_CHOOSE_THEN "y" f (A1 |- ?x. w)) to the goal (A ?- t) produces the subgoal:

$$\begin{array}{l} A \text{ ?- } t \\ \text{=====} \quad \text{X_CHOOSE_THEN } y \text{ f (A1 |- ?x. w)} \\ A \text{ ?- } t1 \quad \quad \quad (y \text{ not free anywhere}) \end{array}$$

Failure

Fails if the theorem's conclusion is not existentially quantified, or if the first argument is not a variable. Failures may arise in the tactic-generating function. An invalid tactic is produced if the introduced variable is free in w or t , or if the theorem has any hypothesis which is not alpha-convertible to an assumption of the goal.

Example

Given a goal of the form

$$\{n < m\} \text{ ?- } ?x. m = n + (x + 1)$$

the following theorem may be applied:

$$\text{th} = [n < m] \text{ |- } ?p. m = n + p$$

by the tactic `(X_CHOOSE_THEN (Term'q:num') SUBST1_TAC th)` giving the subgoal:

$$\{n < m\} \text{ ?- } ?x. n + q = n + (x + 1)$$

See also

`Thm.CHOOSE`, `Thm_cont.CHOOSE_THEN`, `Thm_cont.CONJUNCTS_THEN`,
`Thm_cont.CONJUNCTS_THEN2`, `Thm_cont.DISJ_CASES_THEN`, `Thm_cont.DISJ_CASES_THEN2`,
`Thm_cont.DISJ_CASES_THENL`, `Thm_cont.STRIP_THM_THEN`, `Tactic.X_CHOOSE_TAC`.

X_FUN_EQ_CONV	(Conv)
----------------------	---------------

`X_FUN_EQ_CONV` : (term -> conv)

Synopsis

Performs extensionality conversion for functions (function equality).

Description

The conversion `X_FUN_EQ_CONV` embodies the fact that two functions are equal precisely when they give the same results for all values to which they can be applied. For any variable "x" and equation "f = g", where x is of type `ty1` and f and g are functions of type `ty1->ty2`, a call to `X_FUN_EQ_CONV "x" "f = g"` returns the theorem:

$$\text{|- } (f = g) = (!x. f x = g x)$$

Failure

`X_FUN_EQ_CONV x tm` fails if `x` is not a variable or if `tm` is not an equation `f = g` where `f` and `g` are functions. Furthermore, if `f` and `g` are functions of type `ty1->ty2`, then the variable `x` must have type `ty1`; otherwise the conversion fails. Finally, failure also occurs if `x` is free in either `f` or `g`.

See also

`Drule.EXT`, `Conv.FUN_EQ_CONV`.

<div data-bbox="159 728 427 781" data-label="Text">X_GEN_TAC</div>	<div data-bbox="1096 728 1331 781" data-label="Text">(Tactic)</div>
---	--

`X_GEN_TAC : (term -> tactic)`

Synopsis

Specializes a goal with the given variable.

Description

When applied to a term `x'`, which should be a variable, and a goal `A ?- !x. t`, the tactic `X_GEN_TAC` returns the goal `A ?- t[x'/x]`.

```

      A ?- !x. t
===== X_GEN_TAC "x'"
      A ?- t[x'/x]

```

Failure

Fails unless the goal's conclusion is universally quantified and the term a variable of the appropriate type. It also fails if the variable given is free in either the assumptions or (initial) conclusion of the goal.

See also

`Tactic.FILTER_GEN_TAC`, `Thm.GEN`, `Thm.GENL`, `Drule.GEN_ALL`, `Thm.SPEC`, `Drule.SPECL`, `Drule.SPEC_ALL`, `Tactic.SPEC_TAC`, `Tactic.STRIP_TAC`.

<div data-bbox="159 1814 485 1868" data-label="Text">X_LIST_CONV</div>	<div data-bbox="1067 1814 1331 1868" data-label="Text">(listLib)</div>
---	---

`X_LIST_CONV: {{Aux_thms: thm list, Fold_thms: thm list}} -> conv`

Synopsis

Proves theorems about list constants applied to NIL, CONS, SNOC, APPEND, FLAT and REVERSE. Auxiliary information can be passed as an argument.

Description

X_LIST_CONV is a version of LIST_CONV which can be passed auxiliary theorems about user-defined constants as an argument. It takes a term of the form:

$$\text{CONST1 } \dots (\text{CONST2 } \dots) \dots$$

where CONST1 and CONST2 are operators on lists and CONST2 returns a list result. It can be one of NIL, CONS, SNOC, APPEND, FLAT or REVERSE. The form of the resulting theorem depends on CONST1 and CONST2. Some auxiliary information must be provided about CONST1. X_LIST_CONV maintains a database of such auxiliary information. It initially holds information about the constants in the system. However, additional information can be supplied by the user as new constants are defined. The main information that is needed is a theorem defining the constant in terms of FOLDR or FOLDL. The definition should have the form:

$$|- \text{CONST1 } \dots.l\dots = \text{fold } f \ e \ l$$

where fold is either FOLDR or FOLDL, f is a function, e a base element and l a list variable. For example, a suitable theorem for SUM is

$$|- \text{SUM } l = \text{FOLDR } \$+ \ 0 \ l$$

Knowing this theorem and given the term --'SUM (CONS x l)'--, X_LIST_CONV returns the theorem:

$$|- \text{SUM } (\text{CONS } x \ l) = x + (\text{SUM } l)$$

Other auxiliary theorems that are needed concern the terms f and e found in the definition with respect to FOLDR or FOLDL. For example, knowing the theorem:

$$|- \text{MONOID } \$+ \ 0$$

and given the term --'SUM (APPEND l1 l2)'--, X_LIST_CONV returns the theorem

$$|- \text{SUM } (\text{APPEND } l1 \ l2) = (\text{SUM } l1) + (\text{SUM } l2)$$

The following table shows the form of the theorem returned and the auxiliary theorems needed if CONST1 is defined in terms of FOLDR.

CONST2	side conditions	tm2 in result - tm1 = tm2
=====	=====	=====
[]	NONE	e
[x]	NONE	f x e
CONS x l	NONE	f x (CONST1 l)
SNOC x l	e is a list variable	CONST1 (f x e) l
APPEND l1 l2	e is a list variable	CONST1 (CONST1 l1) l2
APPEND l1 l2	- FCOMM g f, - LEFT_ID g e	g (CONST1 l1) (CONST2 l2)
FLAT l1	- FCOMM g f, - LEFT_ID g e, - CONST3 l = FOLDR g e l	CONST3 (MAP CONST1 l)
REVERSE l	- COMM f, - ASSOC f	CONST1 l
REVERSE l	f == (\x l. h (g x) l) - COMM h, - ASSOC h	CONST1 l

The following table shows the form of the theorem returned and the auxiliary theorems needed if CONST1 is defined in terms of FOLDL.

CONST2	side conditions	tm2 in result - tm1 = tm2
=====	=====	=====
[]	NONE	e
[x]	NONE	f x e
SNOC x l	NONE	f x (CONST1 l)
CONS x l	e is a list variable	CONST1 (f x e) l
APPEND l1 l2	e is a list variable	CONST1 (CONST1 l1) l2
APPEND l1 l2	- FCOMM f g, - RIGHT_ID g e	g (CONST1 l1) (CONST2 l2)
FLAT l1	- FCOMM f g, - RIGHT_ID g e, - CONST3 l = FOLDR g e l	CONST3 (MAP CONST1 l)
REVERSE l	- COMM f, - ASSOC f	CONST1 l
REVERSE l	f == (\l x. h l (g x)) - COMM h, - ASSOC h	CONST1 l

|- MONOID f e can be used instead of |- FCOMM f f, |- LEFT_ID f or |- RIGHT_ID f.
|- ASSOC f can also be used in place of |- FCOMM f f.

Auxiliary theorems are held in a user-updatable database. In particular, definitions of constants in terms of FOLDR and FOLDL, and monoid, commutativity, associativity, left identity, right identity and binary function commutativity theorems are stored. The database can be updated by the user to allow LIST_CONV to prove theorems about new constants. This is done by calling `set_list_thm_database`. The database can be inspected by calling `list_thm_database`. The database initially holds FOLDR/L theorems for the following system constants: APPEND, FLAT, LENGTH, NULL, REVERSE, MAP, FILTER, ALL_EL, SUM, SOME_EL, IS_EL, AND_EL, OR_EL, PREFIX, SUFFIX, SNOC and FLAT combined with

REVERSE. It also holds auxiliary theorems about their step functions and base elements. Rather than updating the database, additional theorems can be passed to `X_LIST_CONV` as an argument. It takes a record with one field, `Fold_thms`, for fold definitions, and one, `Aux_thms`, for theorems about step functions and base elements.

Example

```
- val MULTL = new_definition("MULTL",(--'MULTL l = FOLDR $* 1 l'--));
val MULTL = |- !l. MULTL l = FOLDR $* 1 l : thm

- X_LIST_CONV {{Fold_thms = MULTL, Aux_thms = []}} (--'MULTL (CONS x l)'--);
|- MULTL (CONS x l) = x * MULTL l
```

Failure

`X_LIST_CONV tm` fails if `tm` is not of the form described above. It fails if no fold definition for `CONST1` are either in the database or passed as an argument. It also fails if the required auxiliary theorems, as described above, are not held in the databases or passed as an argument.

See also

`listLib.LIST_CONV`, `listLib.PURE_LIST_CONV`.

X_SKOLEM_CONV	(Conv)
----------------------	---------------

`X_SKOLEM_CONV` : (term -> conv)

Synopsis

Introduces a user-supplied Skolem function.

Description

`X_SKOLEM_CONV` takes two arguments. The first is a variable `f`, which must range over functions of the appropriate type, and the second is a term of the form `!x1...xn. ?y. P`. Given these arguments, `X_SKOLEM_CONV` returns the theorem:

$$|- (!x1...xn. ?y. P) = (?f. !x1...xn. tm[f x1 ... xn/y])$$

which expresses the fact that a skolem function `f` of the universally quantified variables `x1...xn` may be introduced in place of the the existentially quantified value `y`.

Failure

`X_SKOLEM_CONV f tm` fails if `f` is not a variable, or if the input term `tm` is not a term of the form `!x1...xn. ?y. P`, or if the variable `f` is free in `tm`, or if the type of `f` does not match its intended use as an `n`-place curried function from the variables `x1...xn` to a value having the same type as `y`.

See also

`Conv.SKOLEM_CONV`.

<div data-bbox="159 732 368 781" data-label="Text"> <p>xDefine</p> </div>	<div data-bbox="1067 728 1331 784" data-label="Text"> <p>(bossLib)</p> </div>
---	---

```
xDefine : string -> term quotation -> thm
```

Synopsis

General-purpose function definition facility.

Description

`xDefine` behaves exactly like `Define`, except that it takes an alphanumeric string which is used as a stem for building names with which to store the definition, associated induction theorem (if there is one), and any auxiliary definitions used to construct the specified function (if there are any) in the current theory segment.

Failure

`xDefine` allows the definition of symbolic identifiers, but `Define` doesn't. In all other respects, `xDefine` and `Define` succeed and fail in the same way.

Example

The following example shows how `Define` fails when asked to define a symbolic identifier.

```
- set_fixity ("/", Infixl 600);    (* tell the parser about "/" *)
> val it = () : unit

- Define
  'x/y = if y=0 then NONE else
        if x<y then SOME 0
        else OPTION_MAP SUC ((x-y)/y)';
```

```
Definition failed! Can't make name for storing definition
```

because there is no alphanumeric identifier in:

```
"/".
```

Try "xDefine <alphanumeric-stem> <eqns-quotation>" instead.

Next the same definition is attempted with `xDefine`, supplying the name for binding the definition and the induction theorem with in the current theory.

```
- xDefine "div"
  'x/y = if y=0 then NONE else
    if x<y then SOME 0
    else OPTION_MAP SUC ((x-y)/y)';
```

Equations stored under "div_def".

Induction stored under "div_ind".

```
> val it =
  |- x / y =
    (if y = 0 then NONE
     else
      (if x < y then SOME 0
       else OPTION_MAP SUC ((x - y) / y))) : thm
```

Comments

`Define` can be thought of as an application of `xDefine`, in which the stem is taken to be the name of the function being defined.

`bossLib.xDefine` is most commonly used. `TotalDefn.xDefine` is identical to `bossLib.xDefine`, except that the `TotalDefn` structure comes with less baggage—it depends only on `numLib` and `pairLib`.

See also

`bossLib.Define`.

<code>xDefine</code>	<code>(TotalDefn)</code>
----------------------	--------------------------

`xDefine : string -> term quotation -> thm`

Synopsis

General purpose function definition facility.

Description

`bossLib.xDefine` is identical to `TotalDefn.xDefine`.

See also

`bossLib.xDefine`.

zDefine	(bossLib)
---------	-----------

`zDefine : term quotation -> thm`

Synopsis

General-purpose function definition facility.

Description

`zDefine` behaves exactly like `Define`, except that it does not add the definition to `computeLib.the_compset`. Consequently the definition is not used by `bossLib.EVAL` when evaluating expressions.

Failure

`zDefine` and `Define` succeed and fail in the same way.

Example

```
- zDefine 'foo = 10 ** 10 ** 10'  
- EVAL 'foo';  
> val it = |- foo = foo: thm
```

Comments

`zDefine` is helpful when users wish to derive and use their own efficient evaluation theorems, which can be added using `computeLib.add_funs` OR `computeLib.add_persistent_funs`.

See also

`bossLib.Define`.

`zip``(Lib)`

```
zip : 'a list -> 'b list -> ('a * 'b) list
```

Synopsis

Transforms a pair of lists into a list of pairs.

Description

`zip [x1,...,xn] [y1,...,yn]` returns `[(x1,y1),..., (xn,yn)]`.

Failure

Fails if the two lists are of different lengths.

Comments

Has much the same effect as the SML Basis function `ListPair.zip` except that it fails if the arguments are not of equal length. `zip` is a curried version of `combine`

See also

`Lib.combine`, `Lib.unzip`, `Lib.split`.

`|->``(Lib)`

```
op |-> : 'a * 'b -> {redex : 'a, residue : 'b}
```

Synopsis

Infix operator for building a component of a substitution.

Description

An application `x |-> y` is equal to `{redex = x, residue = y}`. Since HOL substitutions are lists of `{redex,residue}` records, the `|->` operator is merely sugar used to create substitutions.

Failure

Never fails.

Example

```
- type_subst [alpha |-> beta, beta |-> gamma]
              (alpha --> beta);
> val it = ':'b -> 'c' : hol_type
```

See also

Lib.subst, Type.type_subst, Term.subst, Term.inst, Thm.SUBST.

>	(Lib)
---	-------

op |> : 'a -> ('a -> 'b) -> 'b

Synopsis

Infix operator for writing function application

Description

The expression $x \mid> f$ is equal to $f\ x$. This way of writing application has two advantages, both apparent when multiple functions are being applied. Without using $\mid>$, one might write $f\ (g\ (h\ x))$. With it, one writes $x \mid> h \mid> g \mid> f$. The latter form needs fewer parentheses, and also makes the order in which functions will operate correspond to a left-to-right reading.

Failure

Never fails.

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